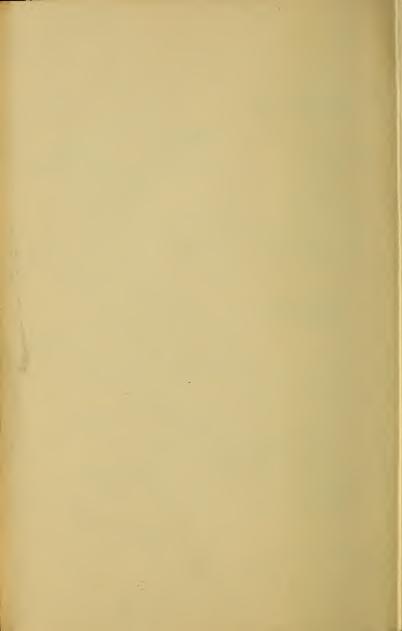
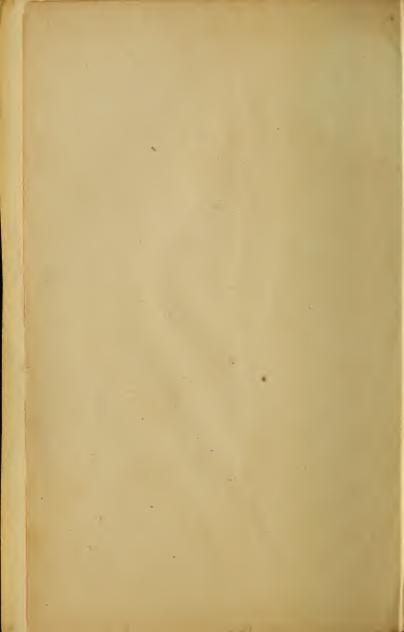
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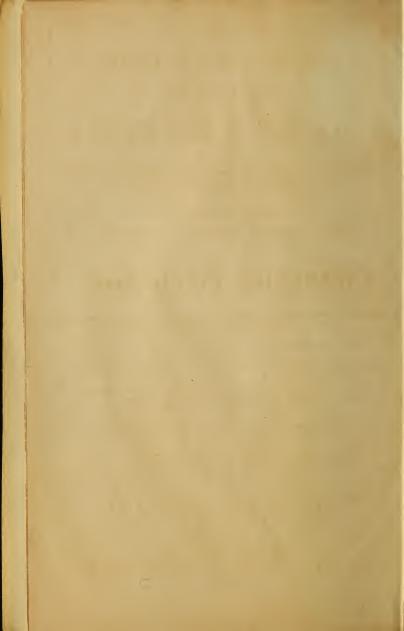




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#### MECHANIC'S, MACHINIST'S, AND ENGINEER'S

#### PRACTICAL

# BOOK OF REFERENCE:

CCNTAINING TABLES AND FORMULÆ FOR USE IN SUPERFICIAL AND SOLID MENSURATION; STRENGTH AND WEIGHT OF MATERIALS; MECHANICS; MACHINERY; HYDRAULICS, HYDRODYNAMICS; MARINE ENGINES, CHEMISTIK; AND MISCELLANEOUS RECIPES,

ADAPTED TO AND FOR THE USE OF

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TOGETHER WITH THE

## ENGINEER'S FIELD BOOK:

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TABLES OF RADII AND THEIR LOGARITHMS,

NATURAL AND LOGARITHMIC VERSED SINES AND EXTERNAL SECANTS,

NATURAL SINES AND TANGENTS TO EVERY DEGREE AND MINUTE OF THE QUADRANT,

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LOGARITHMS OF NATURAL NUMBERS FROM 1 TO 10,000.

BY CHARLES HASLETT,
Civil Engineer.

EDITED BY CHARLES W. HACKLEY, Professor of Matherfatics in Columbia College, N. Y.

NEW YORK:

STRINGER & TOWNSEND, 222 BROADWAY.

1856.

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# PREFACE.

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No more useful little works have ever been presented to the public than the various pocket companions of a character analogous to that here offered. These have been a good deal, though not yet too much, multiplied of late; and where the formulas, rules, and tables which they contain have been skilfully framed under the guidance of scientific men, they have afforded to the Practical Engineer, Architect, and Mechanic, the most welcome aid in the constructions and computations which make part of their daily occupation, and which, without the ever-at-hand suggestions and directions of these unpretending little servants, might consume hours and days in the turning over of large volumes, or in painful investigations based on general principles of science where the individual happened to be competent to conduct them.

The wants to be supplied in such a work are discovered by experience and observation in the different callings for which they are more especially intended. That these wants have not all been met in the works of a similar kind which have already appeared will be made evident by a simple inspection of the amount and variety of new matter contained in the present volume.

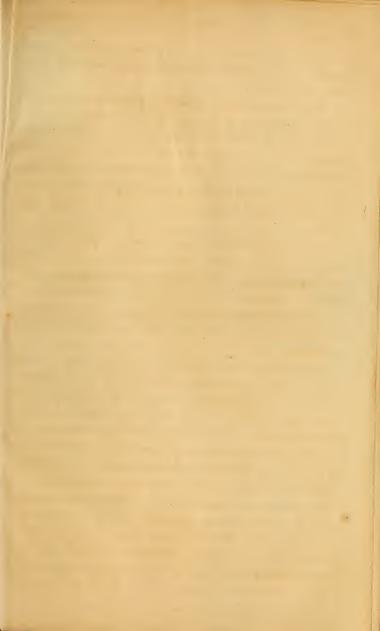
It is not every one, however practically expert he may be in his own pursuit, that is capable of arranging and digesting in the best manner the knowledge necessary for his own use which he may have been years in acquiring, so as to render it available for the use of others. Such a task, to be well performed, requires a combination of mental qualities not always, perhaps not often, found in the same individual.

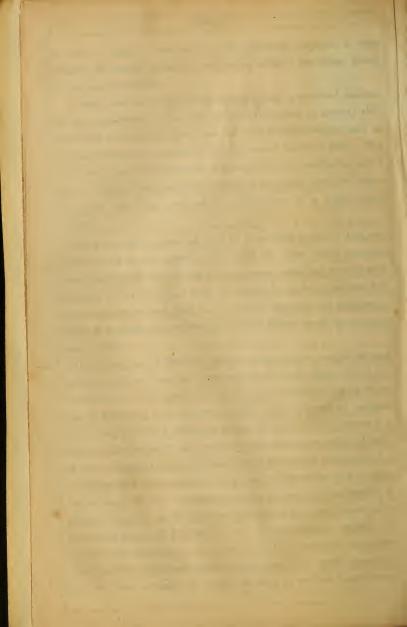
A happy concurrence of circumstances has by accident secured for the composition of the present work the labors of several skilful hands, both as compilers from the best foreign sources, and as original producers of valuable material never before in print. The result of so much well directed industry is the rich collection, not a line of which is not invaluable, which, in the aptest form for immediate use, has been crowded into the space of a single small volume.

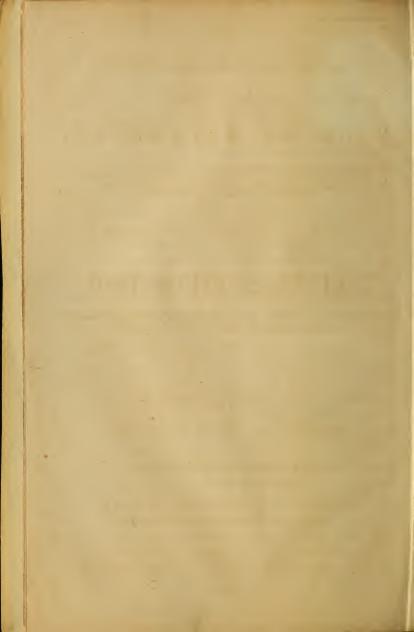
Steam and its application play so important a part in the economy of life at the present day, that the most useful practical rules and formulas for all the ordinary cases occurring, cannot with propriety be omitted in a work of this kind. A due attention will be found to have been paid to the matter, and some of the newest modes of managing in steam supplied with the means of the requisite computation.

The laying out of Railroad curves is one of the most important and at the same time laborious and troublesome duties which the Civil Engineer has to perform. So much of this occurring on every line of Railroad, any, however slight, improvement of method which may serve to facilitate or lessen the labor of this process is a real boon to that large and eminently useful and accomplished body of men to whom the supervision of such operations is committed.

The use of the more common trigonometric functions, to wit, sines, cosines, tangents, and cotangents, which ordinary tables furnish, is not well adapted to the peculiar problems which are presented in the construction of Railroad curves. The additional columns of secants and cosecants in the tables of Dr. Bowditch sometimes afford a slight additional facility, which would be much increased had we also columns of natural secants as well as logarithmic.







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Still there would be much labor of computation which may be saved by the use of tables of external secants and versed sines, which have been employed with great success recently by the Engineers on the Ohio and Mississippi Railroad, and which, with the formulas and rules necessary for their application to the laying down of curves, drawn up by Mr. Haslett, one of the Engineers of that Road, are now for the first time given to the public. This portion of the volume alone, by the great abridgment of labor for which it provides the means, and the simplicity and convenience of the matter which it furnishes, will give it an extensive circulation among Practical Engineers.

But besides this, the Architect, the Shipbuilder, the Mason, the Carpenter, the Joiner, the Manufacturer and Artisan in iron and every species of material, will find rules and recipes for all kinds of estimates, computations, constructions, compositions, mixtures, et cetera, which will excite surprise at their number, novelty, and value to every one.

The contents of this volume are of so varied a nature that it was not deemed necessary to make any strenuous efforts to arrange them systematically. Being solely intended for a book of reference, the relative order of the subjects is immaterial; and the copious Table of Contents and Index afford all the assistance that can be desired by those who wish to consult its pages.

THE EDITOR.

Columbia College, Sept. 1855 and the state of t

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#### THE

MECHANIC'S, MACHINIST'S, AND ENGINEER'S

#### PRACTICAL

## BOOK OF REFERENCE:

CONTAINING

#### TABLES AND FORMULÆ

FOR USE IN

SUPERFICIAL AND SOLID MENSURATION; STRENGTH AND WEIGHT OF MATERIALS; MECHANICS; MACHINERY: HYDRAULICS; HYDRODYNAMICS; MARINE ENGINES; CHEMISTRY; AND MISCELLANEOUS RECIPES.

ADAPTED TO AND FOR THE USE OF

ALL CLASSES OF PRACTICAL MECHANICS.

EDITED BY

CHARLES W. HACKLEY, Professor of Mathematics in Columbia College, N. Y.

MINIMARINE WATERWAYS, AND CHORESTEEN

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### PRACTICAL BOOK OF REFERENCE.

#### ARITHMETICAL SIGNS.

THE following definitions of arithmetical signs which are employed in mechanical calculations, will be found of great value to those who do not yet understand them, and of some interest to those who are already familiar with their meanings.

- = This is the sign of equality, and signifies equal to. For example: 12 inches = 1 foot (12 inches is equal to 1 foot).
- + This is the sign of addition, and signifies plus, or more. For example: 5 + 3 = 8 (5 added to 3 is equal to 8).
- This is the sign of subtraction, and signifies minus, or less. For example: 10-8=2 (10 minus 8 leaves or is equal to 2).
- $\times$  This is the sign of *multiplication*, and signifies *multiplied by*, or *into*. For example:  $10 \times 3 = 30$  (10 *multiplied by 3 is equal to 30*).
- $\div$  This is the sign of division, and signifies divided by. For example:  $156 \div 6 = 26$  (156 divided by 6 is equal to 26); or  $24 \div 4 = 6$  (24 divided by 4 is equal to 6); or  $\frac{24}{4} = 6$  (24 fourths are equal to 6 wholes).
- : :: This is the sign of proportion, and signifies proportion. For example: 4:6::8:12 (as 4 is to 6, so is 8 to 12); or 3:5::9:15 (that is, as 3 is to 5, so is 9 to 15);  $\frac{3}{5} = \frac{9}{15}$ .
- $\sqrt{1}$  This is the sign of the SQUARE root. When it is placed before a number (as thus,  $\sqrt{5} = 25$ ), it means that the square root of that number is required. For example:  $\sqrt{25} = 5$ , because  $5 \times 5 = 25$ ; or,  $\sqrt{9} = 3$ , because  $3 \times 3 = 9$ ; or,  $\sqrt{64} = 8$ , because  $8 \times 8 = 64$ .
- \*\formula This is the sign of the CUBE root. When it is placed before a number, it means that the cube root of that number is required. For example:  $\sqrt[3]{64} = 4$  (that is,  $4 \times 4 = 16$ , and  $4 \times 16 = 64$ ); or,  $\sqrt[3]{216} = 6$  (that is,  $6 \times 6 = 36$ , and  $6 \times 36 = 216$ ).

- <sup>2</sup> When this mark is added to a number (thus,  $6^2$ ), it means that that number is to be *squared*. For example:  $5^2 = 25$  (that is,  $5 \times 5 = 25$ ); or  $6^2 = 36$  (that is,  $6 \times 6 = 36$ ).
- <sup>3</sup> When this mark is added to a number, it means that that number is to be *cubed*. For example;  $5^3 = 5 \times 5 \times 5 = 125$  (that is,  $5 \times 5 = 25$ , and  $5 \times 25 = 125$ ; or,  $7^3 = 343$  (that is,  $7 \times 7 = 49$ , and  $7 \times 49 = 243$ ). The *index* or *power* (as the small figure annexed is called) shows how many times a number is to be multiplied by itself.
- This is called the bar. It signifies that all the numbers or quantities under it are to be taken together. For example:  $3+5 \times 4=32$  (3 plus 5 are equal to 8, and that, multiplied by 4, is equal to 32); or, 7-3+8=12 (7 less 3 is equal to 4, and that, if added to 8, is equal to 12); or,  $5\times 4+3=35$  (that is, 4 and 3 are 7, which, if multiplied by 5, is equal to 35); or,  $5\times 6+4=50$  (that is, 6 and 4 are 10, and ten times 5 are 50). The parenthesis () is sometimes used in place of the bar, thus:  $(6+4)\times 5=50$ .
  - ... The meaning of this sign is therefore.
    - .. This sign signifies because.
    - 1 The meaning of this sign is perpendicular.
    - ∠ This sign signifies an angle.
- $\sim$  This sign denotes difference, and is placed between two quantities (as  $x\sim y$ ) when it is not known which of them is the greater.

> or  $\sqsupset$  The meaning of these signs is greater than. For example: A B > C D (that is, A B is greater than C D).

< or  $\sqsubset$  The meaning of these signs is less than. For example: A B < C D (that is, A B is less than C D).

- This is a decimal point. When placed before a number (thus, .1), it means that that number has a unit (1) for its denominator. For example: .1 is the same as  $\frac{1}{10}$ ; .125 is the same as  $\frac{125}{1000}$ ; .01 is the same as  $\frac{1}{1000}$ ; .001 is the same as  $\frac{1}{1000}$ ; .217 is the same as  $\frac{1}{1000}$ ; .42.85 is the same as  $42\frac{85}{100}$ ; .57.217 is the same as  $57\frac{217}{1000}$ .
- ° This is a degree mark. It is written and printed as follows: 25° (that is, 25 degrees).
  - ' This is a minute sign.
  - "These two accents signify seconds.
- "These three accents signify thirds. They read thus: 57° 17' 43" 39" (that is, 57 degrees, 17 minutes, 43 seconds, and 39 thirds).

#### ALGEBRAIC SYMBOLS.

The advantage of these, in a work like the present, may be thus illustrated:

Let l denote the length, b the breadth, and d the depth of an iron beam. If it be desired to express the product of the length and breadth, divided by the depth, it is done as follows:

 $\frac{l\,b}{d}$ 

That is to say, multiplication is expressed by simply writing the letters which represent numbers one after the other; division, by drawing a line under the dividend, and writing the divisor below.

The sum of the length and breadth, divided by the depth, would be expressed briefly thus:

 $\frac{l+b}{d}$ 

The square of the length, multiplied by the cube of the breadth, thus:

 $l^2 \, b^3$ 

The square root of the length, divided by the fourth root of the breadth, thus:

 $\frac{\sqrt{l}}{\sqrt[4]{b}}$ 

The square root of the difference of the length and breadth, divided by the depth, thus:

$$\frac{\sqrt{l-b}}{d}$$

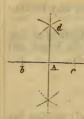
The square root of the quotient of the sum and difference of the length and breadth, thus:

$$\sqrt{\frac{l+b}{l-b}}$$

Any other letters—as a, b, c, &c.—may stand for the given dimensions.

These explanations will serve to give the sense of the symbols which will be met with throughout the work.

#### PRACTICAL GEOMETRY.



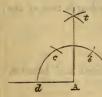
1. From any given point, in a straight line, to erect a perpendicular; or, to make a line at right angles with a given line.

On each side of the point A, from which the line is to be made, take equal distances, as A b, A c; and from b and c as centres, with any distance greater than b A or c A, describe arcs cutting each other at d; then will the line A d be the perpendicular required.



2. When a perpendicular is to be made at or near the end of a given line.

With any convenient radius, and with any distance from the given line Ab, describe a portion of a circle, as bAc, cutting the given point in A; draw, through the centre of the circle n, the line bnc; and a line from the point A, cutting the intersections at c, is the perpendicular required.



#### 3. To do the same otherwise.

From the given point A, with any convenient radius, describe the arc d c b; from d cut the arc in c, and from c cut the arc in b; also from c and b as centres, describe arcs cutting each other in t; then will the line A t be the perpendicular as required.

Note.—When the three sides of a triangle are in the proportion of 3.4 and 5 equal parts, respectively, two of the sides form a right angle; and observe that in each of these or the preceding problems, the perpendiculars may be continued below the given lines, if necessarily required.

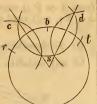


#### 4. To bisect any given angle.

From the point A as a centre, with any radius less than the extent of the angle, describe an arc, as c d; and from c and d as centres, describe arcs cutting each other at b; then will the line A b bisect the angle as required.

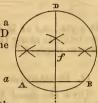
5. To find the centre of a circle, or radius, that shall cut any three given points, not in a direct line.

From the middle point b as a centre, with any radius, as b c, b d, describe a portion of a circle, r as c s d; and from r and t as centres, with an equal radius, cut the portion of the circle in c s and d s; draw lines through where the arcs cut each other; and the intersection of the lines at s is the centre of the circle as required.



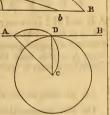
6. To find the centre of a given circle.

Bisect any chord in the circle, as AB, by a perpendicular, CD; bisect also the diameter ED in f; and the intersection of the lines at f is the centre of the circle required.



7. To find the length of any given arc of a circle.

With the radius AC, equal to  $\frac{1}{4}$ th the length of the chord of the arc AB, and from A as a centre, cut the arc in c; also from B as a centre, with equal radius, cut the chord in b; draw the line Cb; and twice the length of the cline is the length of the arc nearly.

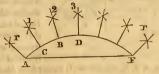


8. Through any given point, to draw a tangent to a circle.

Let the given point be at A; draw the line AC, on which describe the semicircle ADC; draw the line ADB, cutting the circumference in D, which is the tangent as required.

9. To draw from or to the circumference of a circle lines tending towards the centre, when the centre is inaccessible.

Divide the whole or any given portion of the circumference into the desired number of equal parts; then, with any radius less than the distance of two divisions, describe arcs cutting each other, as A 1, B 1, C 2, D 2, &c.; draw the lines C 1, B 2, D 3, &c., which lead



lines C 1, B 2, D 3, &c., which lead to the centre, as required.

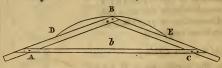
To draw the end lines.

As Ar, Fr, from C describe the arc r, and with the radius C1,

from A or F as centres, cut the former arcs at r, or r, and the lines A r, F r, will tend to the centre as required.

10. To describe an arc, or segment of a circle, of large radii.

Of any suitable material, construct a triangle, as A B C; make



A B, B C, each equal in length to the chord of the arc D E, and height, twice that of the arc B b. At each end of the chord D E

fix a pin, and at B, in the triangle. fix a tracer (as a pencil), move the triangle along the pins as guides; and the tracer will describe the arc required.

#### 11. Or otherwise.

Draw the chord ACB; also draw the line HDI, parallel with the chord, and equal to the height of the segment; bisect the chord

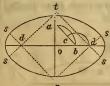
H 2 3 D 3 2 n 1 3 2 n 1 3 2 n 1 8

in C, and erect the perpendicular CD; join AD, DB; draw AH perpendicular to AD, and BI perpendicular to BD; erect also the perpendiculars An, Bn; divide

A B and H I into any number of equal parts; draw the lines 1 1, 2 2, 3 3, &c.; likewise divide the lines A n, B n, each into half the number of equal parts; draw lines to D from each division in the lines A n, B n, and, through where they intersect the former lines, describe a curve, which will be the arc or segment required.

12. To describe an ellipse, having the two diameters given.

On the intersection of the two diameters as a centre, with a



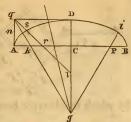
radius equal to the difference of the semidiameters, describe the arc ab; and from b as a centre, with half the chord bca, describe the arc cd; from c, as a centre, with the distance cd, cut the diameters in dr, dt; draw the lines r, s, s, and t, s, s; then from r and t describe the arcs s, s, s, s, also from d and d, describe the smaller arcs

s, s, s, s, which will complete the ellipse as required.

13. To describe an elliptic arch, the width and rise of span being given.

Bisect with a line at right angles the chord or span AB; erect

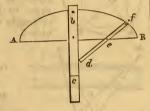
the perpendicular A q, and draw the line q D equal and parallel to A C; bisect A C and A q in r and n; make C l equal to C D, and draw the line l r q; draw also the line n s D; bisect s D with a line at right angles, and meeting the line C D in g; draw the line g q, make C P equal to C k, and draw the line g P i; then from g as a centre, with the radius g D, describe the arc s D i; and from k and P as centres, with the radius



dius A k, describe the arcs A s and B i, which completes the arch as required. Or,

14. Bisect the chord AB, and fix at right angles any straight

guide, as bc; prepare, of any suitable material, a rod or staff, equal to half the chord's length, as dcf; from the end of the staff, equal to the height of the arch, fix a pin e, and at the extremity a tracer f; move the staff, keeping its end to the guide and the fixed pin to the chord, and the tracer will describe one half the arc required.



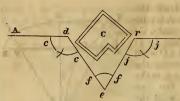
# 15. To describe a parabola, the dimensions being given.

Let AB equal the length, and CD the breadth of the required parabola; divide CA, CB into any number of equal parts; also divide the perpendiculars Aa and Bb into the same number of equal parts; then from a and b

draw lines meeting each division on the line ACB; and a curve line drawn through each intersection will form the parabola required.

16. To obtain by measurement the length of any direct line, though intercepted by some material object.

Suppose the distance between A and B is required, but the right line is intercepted by the object C. On the point d, with any convenient radius, describe the arc c, make the arc twice the radius in length, through which draw the line d e e; and on e describe another



are equal in length to once the radius, as eff; draw the line efr equal to efd; on r describe the arc jj, in length twice the radius; continue the line through rj, which will be a right line, and de, or er, equal the distance between dr,

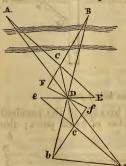
by which the distance between A and B is obtained as required.

17. A round piece of timber being given, out of which to cut a beam

Decopies of strongest section.

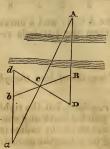


Divide into three equal parts any diameter in the circle, as Ad, eC; from d or e, erect a perpendicular meeting the circumference of the circle, as dB; draw AB and BC, also AD equal to BC, and DC equal to AB, and the rectangle will be a section of the beam as required.



18. To measure the distance between two objects, both being inaccessible.

From any point C draw any line C c, and bisect it in D; take any point E in the prolongation of A C, and draw the line E c, making D c equal to D E; in like manner take any point F in the prolongation of B C, and make D f equal to F D. Produce A D and c c till they meet in d, and also B D and f c till they meet in b; then a b equal A B, or the distance between the objects as required.

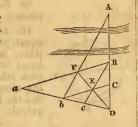


19. To ascertain the distance, geometrically, of any inaccessible object on an equal plane.

Let it be required to find the distance between A and B, A being inaccessible; produce the line in the direction of A B to any point, as D; draw the line D d at any angle to the line A B; bisect the line D d, through which draw the line B b, making cb equal to B c; draw the line db a; also through c, in the direction cA, draw the line acA, intersecting the line db a; then b a equal B A, the distance required.

20. Otherwise.

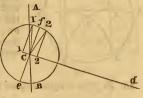
Prolong A B to any point D, making B C equal to C D; draw the line D a at any angle with D A, and the line C b similar to B c; draw also the line D E F, which intersects the line B a; then a b equal B A, or the distance required.



21. To find the proper position for an eccentric, in relation to the crank in a steam engine, the angle of eccentric rod, and travel of the valve, being given.

Draw the right line AB, as the situation of the crank at commencement of the stroke; draw also the line Cd, as the proper given angle of eccentric rod with the crank; then from C as centre,

describe a circle equal to the travel of the valve; draw the line ef at right angles to the line Ca, draw also the lines 11, and 22, parallel to the line ef; and at a distance from ef on each side, equal to the lap and lead of the valve, draw the angular lines C1, C2, which are the angles of eccentric with the crank,

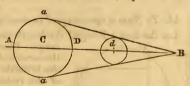


for forward or backward motion, as may be required.

22. The throw of an eccentric, and the travel of the valve in a steamengine, also the length of one lever for communicating motion to the valve, being given, to determine the proper length for the other.

On any right line, as AB, describe a circle AD, equal to the

of any right line, as Arthrow of eccentric and travel of valve; then from C as a centre, with a radius equal to the length of lever given, cut the line A B, as at d, on which describe a circle, equal to the throw of eccentric or travel of valve, as may be

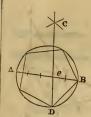


required; draw the tangents Ba, Ba, cutting each other in the line AB, and AB is the length of the lever as required.

Note.—The throw of an eccentric is equal to the sum of twice the distance between the centres of formation and revolution, as **ab**, or to the degree of eccentricity it is made to describe, as cd. And

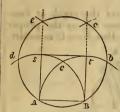
The travel of a valve is equal to the sum of the widths of the two steam openings, and the valve's excess of length more than just sufficient to cover the openings.





23. To inscribe any regular polygon in a given circle.

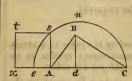
Divide any diameter, as AB, into so many equal parts as the polygon is required to have sides; from A and B as centres, with a radius equal to the diameter, describe arcs cutting each other in C; draw the line CD through the second point of division on the diameter e, and the line DB is one side of the polygon required.



24. To construct a square upon a given right line.

From A and B as centres, with the radius AB, describe the arcs Acb, Bcd, and from c, with an equal radius, describe the circle or portion of a circle ed, AB, bc; from bd cut the circle at e and c; draw the lines A e, B c, also the line st, which completes the square as required.

25. To form a square equal in area to a given triangle.



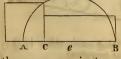
Let ABC be the given triangle; let fall the perpendicular Bd, and make Ae half the height dB; bisect eC, and describe the semicircle en C: erect the perpendicular As, or side of the square, then A stx is the square of equal area as required.

and erect the perpendicular CD, meeting

the curve at D, and CD equal a side of

26. To form a square equal in area to a given rectangle.

Let the line AB equal the length and breadth of the given rectangle; bisect the line in e, and describe the semicircle ADB; then from A with the breadth, or from B with the length, of the rectangle, cut the line AB at C,

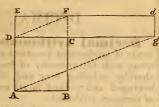


the square required.

27. To find the length for a rectangle whose area shall be equal to that of a given square, the breadth of the rectangle being also given.

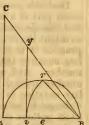
Let ABCD be the given square and DE the given breadth of

rectangle; continue the line B C to F, and draw the line D F; also continue the line D C to g, and draw the line A g parallel to D F; from the intersection of the lines at g, draw the line g d parallel to D E, and E d parallel to D g; then ED d g is the rectangle as required.



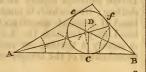
28. To bisect any given triangle.

Suppose ABC the given triangle; bisect one of its sides, as AB in e, from which describe the semicircle ArB; bisect the same in r, and from B, with the distance Br, cut the diameter AB in v; draw the line v y parallel to AC, which will bisect the triangle as required.



29. To describe a circle of greatest diameter in a given triangle.

Bisect the angles A and B, and draw the intersecting lines A D, B D, cutting each other in D; then from D as centre, with the distance or radius D C, describe the circle C e f, as required.



30. To form a rectangle of greatest surface, in a given triangle.

Let A B C be the given triangle; bisect any two of its sides, as A B, B C, in e and d; draw the line ed; also, at right angles with the line ed, draw the lines ep, dp, and eppd is the rectangle required.



#### RATIO OF THE HARDNESS OF METALS.

1. Iron,

4. Silver, 5. Gold. 6. Tin, 7. Lead.

Platina,
 Copper.

#### STRENGTH OF WOOD,

All woods are from 7 to 20 times stronger transversely than longitudinally. They become stronger both ways when dry.

# DECIMAL ARITHMETIC.

Decimal Arithmetic is the most simple and explicit mode of performing practical calculations, on account of its doing away with the necessity of fractional parts in the fractional form, thereby reducing long and tedious operations to a few figures arranged and worked in all respects according to the usual rules of common arithmetic.

Decimals simply signify tenths; thus, the decimal of a foot is the tenth part of a foot, the decimal of that tenth is the hundredth of a foot, the decimal of that hundredth is the thousandth of a foot, and so might the divisions be carried on and lessened to infinity: but in practice it is seldom necessary to take into account any degree of less measure than a one-hundredth part of the integer or whole number. And, as the entire system consists in supposing the whole number divided into tenths, hundredths, thousandths, &c., no peculiar notation is required, otherwise than placing a mark or dot to distinguish between the whole and any part of the whole, thus: 34.25 gallons signify 34 gallons, 2 tenths, and 5 hundredths of a gallon; 11.04 yards signify 11 yards and 4 hundredths of a yard; 16.008 shillings signify 16 shillings and 8 thousandth parts of a shilling; from which it must appear plain that ciphers on the right hand of decimals are of no value whatever, but placed on the left hand they diminish the decimal value in a tenfold proportion: for .6 signify 6 tenths; .06 signify 6 hundredths; and .006 signify 6 thousandths of the integer or whole number.

# Reduction.

Reduction means the converting or changing of vulgar fractions to decimals of equal value; also finding the fractional value of any decimal given.

Rule 1. Add to the numerator of the fraction any number of ciphers at pleasure, divide the sum by the denominator, and the

quotient is the decimal of equivalent value.

Rule 2. Multiply the given decimal by the various fractional denominations of the integer, or whole number, cutting off from the right hand of each product, for decimals, a number of figures equal to the given number of decimals, and thus proceed until the lowest degree, or required value, is obtained.

Ex. 1. Required the decimal equivalent, or decimal of equal

value, to  $\frac{3}{12}$  of a foot.

 $\frac{3.00}{12}$  = .25, the decimal required.

Ex. 2. Reduce the fraction  $\frac{1}{8}$  of an inch to a decimal of equal value.  $\frac{1.000}{2} = 125$ , the decimal required.

Ex. 3. What is the decimal equivalent to  $\frac{7}{8}$  of a gallon?  $\frac{7.000}{9} = .875$ , the decimal equivalent.

Ex. 4. Required the fractional value of the decimal .40625 of an inch.

Multiply by 
$$\frac{1}{8} = \frac{8}{3 \cdot 25000}$$
  
 $\times \frac{2}{16} = \frac{1}{8} = \frac{2}{50000}$   
 $\times \frac{2}{32} = \frac{1}{16} = \frac{2}{100000} = \frac{2}{8}$  and  $\frac{1}{32}$  of an inch, the value required.

Ex. 5. What is the fractional value of .625 of a cwt.?

Multiply by 4 qrs 
$$\frac{4}{2.500}$$

× 28 lbs.  $\frac{28}{14.000}$  = 2 quarters and 14 lbs., the value required.

Ex. 6. Ascertain the fractional value of 875 of an imperial gallon.

Multiply by 4 quarts 
$$\frac{.875}{4}$$
 $\times 2 \text{ pints} \quad \frac{2}{1.000} = 3 \text{ quarts and 1 pint, the value re-required.}$ 

Ex. 7. What is the fractional value of 525 of a £. sterling?

Independent of the mark or dot which distinguishes between integers and decimals, the fundamental rules—viz. Addition, Subtraction, Multiplication, and Division—are in all respects the same as in Simple Arithmetic; and an example in each, illustrative of placing the separating point, will no doubt render the whole system sufficiently intelligible, even to the dullest capacity.

Ex. 1. Add into one sum the following integers and decimals:

16.625; 11.4; 20.7831; 12.125; 8.04; and 7.002.

16.625 11.4 20.7831 12.125 8.04

 $\frac{7.002}{75.9751} =$ the sum required.

Ex. 2. Subtract 119.80764 from 234.98276.

234·98276 119·80764

115:17512 = the remainder required.

Ex. 3. Multiply 62:10372 by 16:732.

 $\begin{array}{r} 62\cdot 10872 \\ 16\cdot 732 \\ \hline 12420744 \\ 18631116 \\ 43472604 \\ 37262232 \\ 6210872 \end{array}$ 

1039·11944304 = the product required.

Observe that the number of figures in the product from the right hand, accounted as decimals, are equal to the number of decimals in the multiplier and multiplicand taken together.

Ex. 4. Divide 39.375 by 9.25.

9.25) 39.375 (4.256 = the quotient required.

 $\begin{array}{r}
3700 \\
\hline
2375 \\
1850 \\
\hline
6250 \\
4625 \\
\hline
6250 \\
5550 \\
\hline
700
\end{array}$ 

Observe that the number of decimals, in the divisor and quotient together, must be equal to the number in the dividend.

Note.—The operation might be still continued, so as to reduce the quotient to a degree of greater exactitude; but in practice it is quite unnecessary, being even now reduced to a measure of greater nicety than is commonly required.

# MENSURATION.

Mensuration is the method of calculating the comparative magnitudes of figures, and it is divided into two parts—Mensuration of Superficies or Surfaces, and Mensuration of Solids.

The magnitude of a surface is called its area, and is the space

inclosed between its boundary lines,

The magnitude of a body is called its solid contents, and is expressed in cubic feet, inches, &c.

### Mensuration of Superficies.



A Square is a quadrilateral figure, which has all its sides equal, and all its angles right angles.

A RECTANGLE is a four-sided figure, which has its angles, right angles, and its opposite sides parallel.

Rhombus.
B

D

B Rhomboid.

A Ruombus is a parallelogram, whose sides are equal, but whose angles are not right angles.

A Ruomboid is a parallelogram, whose adjacent sides are unequal,

and whose angles are not right angles.

A Trapezon is a four-sided figure, which has but two of its sides parallel.

A Circle is a figure bounded by one line, called the circumference, and is such that all lines drawn to the circumference from a certain point within the figure, called the centre, are equal to each other. Any of these lines is called a radius; and a line drawn through the centre, terminating both ways in the circumference, is called a diameter. The portion of circle cut off by a diameter is called a semicircle.

An Arc of a circle is any portion of the circumference.

A SEGMENT of a circle is a figure contained by an arc and its chord.

A VERSED SINE is a line drawn from the middle of a chord per-

pendicular to the circumference.

A Sector of a circle is a figure contained by two radii and an arc, as A C B E.

#### PROBLEM I.

### To find the area of any parallelogram.

RULE. Multiply the length by the perpendicular height, and the product will be the area.

EXAMPLE. Required the area of a rhomboid whose length AB=20.5, and perpendicular height aA=11.75.

$$20.5 \times 11.75 = 240.875$$
, the area.

Note.—In a square, or rectangle, the perpendicular height is the breadth: therefore, to find the areas of a square and rectangle, multiply the length by the breadth.

#### PROBLEM II.

#### To find the area of a trapezoid.

RULE. Add together the two parallel sides, multiply their sum by the breadth or height, and half the product is the area.

EXAMPLE. Required the area of a trapezoid whose sides A B and C D are 14.5 and 10.25, and breadth, aA = 7.25.

$$\frac{14.5 + 10.25 \times 7.25}{2} = 89.71875,$$

the area.

### PROBLEM III.

### To find the area of a triangle.

RULE. Multiply one of its sides as a base by a perpendicular let fall from the opposite angle, and take half the product for the area.

Or, from half the sum of the three sides subtract each side separately, and multiply the three remainders so obtained and the half sum together, and the square root of the product will be the area.

EXAMPLE 1. Required the area of a triangle ABC, whose base AB = 16.5, and perpendicular DC = 10.25.

$$\frac{16.5 \times 10.25}{2} = 84.5625,$$

the area.

EXAMPLE 2. What is the area of that triangle whose three sides are 8, 12, and 16 respectively?

then, 18 18 18 
$$\frac{8+12+16}{2}=18$$
, the half sum of the sides;  $\frac{8}{12}=\frac{16}{10}=\frac{16}{6}=\frac{12}{2}$  and  $\frac{4}{18}\times10\times6\times2=46.47$ , the area.

#### PROBLEM IV.

If any two sides of a right-angled triangle be given, the third side may be found by the following rules.

1.—To the square of the base add the square of the perpendicular; and the square root of the sum will be the hypothenuse or longest side.

2.—Multiply the sum of the hypothenuse, and one side by their difference; and the square root of the product will be the other

side.

EXAMPLE 1. Given the base AB = 16, and perpendicular BC = 12; required the length of the hypothenuse AC.

$$\sqrt{16^2 + 12^2} = 20$$
, the length of the hypothenuse A C.



Example 2. Given the base AB = 16, and hypothenuse AC = 20; required the length of the perpendicular BC.

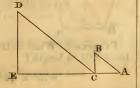
$$\sqrt{20 + 16 \times 4} = 12$$
, length of the perpendicular BC.

Note.—The diagonal line, or hypothenuse in a square, is equal to the square root of twiee the square of the side. And the side of a square is equal to the square root of half the square of its diagonal.

Thus suppose each side of a square equal 12 feet:

$$12^2 \times 2 = \sqrt{288} = 16^{\circ}9705$$
 feet, the diagonal. Or,  $\frac{16^{\circ}9705^2}{9} = \sqrt{144} = 12$  feet, the length of each side.

Similar triangles, or those which are equi-angular to each other, have the sides about their equal angles proportional; thus, in the annexed figure the triangles A B C and CDE are similar, and therefore have the sides about the equal angles proportional;



AC:BC::CE:DE; AB:BC::CD:DE &c.

The utility, then, of the above triangles for practical purposes, as, for instance, ascertaining the heights of buildings, &c., will be seen from the following:

Suppose D E to be an eminence, of which it is required to find the height, and E C the length of the shadow cast by the sun; then, in order to find D E, we may erect perpendicularly at C a pole of any known length, as B C, and after measuring the length of its shadow A C, state—as the length of the pole's shadow is to the height of the pole itself, so is the length of the shadow of D E to the height of D E; or,

As A C: CB:: CE: ED;

and supposing A C = 6 feet, B C = 4 feet, and C E = 30 feet, then E D would be 20 feet.

B C D

Again, supposing we wished to find the distance between two objects A and B; draw D B of any length at right angles to A B, and in D B take any point C, through which draw A E; also, at D, at right angles to D B, draw D E, making the triangle D E C, and state,

As D C: D E:: B C: B A.

### PROBLEM V.

To find the area of any regular polygon.

Rule. Multiply the sum of its sides by a perpendicular drawn from its centre to one of its sides, and take half the product for the area.

Or, multiply the square of the side of a polygon (from three to twelve sides) by the numbers in the fourth column of the table for polygons, opposite the number of sides required, and the product will be the area nearly.



Example 1. Required the area of the regular pentagon A B C D E, each side being 7.5, and perpendicular F G=6.4.

$$\frac{7.5 \times 5 \times 6.4}{2} = 120, \text{ the area.}$$

EXAMPLE 2. What is the area of a regular hexagon, each side being 8.75 in length?

 $8.75^2 \times 2.598 = 199.009375$ , the area.

# Table of multipliers for polygons from three to twelve sides.

	Names.	Sides.	Multipliers.	Multipliers.	Multipliers.	Areas.
	Trigon	3	2	1.73	.579	433
-	Tetragon	4	1.41	1.412	.705	1.000
i	Pentagon	5	1.238	1.174	*852	1.72
.	Hexagon	6	1.156	= Radius.	= Length	2.598
	amprovide say	ato will	of the said	-01 = N -11	of side.	1 4
	Heptagon	7	1.11	.867	1.16	3.634
1	Octagon	8	1.08	.765	1.307	4.828
	Nonagon	9	1.062	·681	1.47	6.1818
	Decagon	10	1.05	·616	1.625	7.694
	Undecagon.	. 11	1.04	.561	1.777	9.365
-	Dodecagon	12	1.037	.515625	1.94	11.196

1. The breadth of a polygon given, to find the radius of a circle to contain that polygon.

Rule. Multiply half the breadth of the polygon by the numbers in the first column opposite to its name, or number of sides, and the product will be the radius of a circle to contain that polygon.

And if the polygon have an unequal number of sides, the half

breadth is accounted from its centre to one of its sides.

2. The radius of a circle given, to find the length of side.

Rule. Multiply the radius of any circle by the numbers in the second column opposite the polygon required, and the product will be the length of side nearly that will divide that circle into the proposed number of sides. And,

3. The length of side given, to find the radius.

Rule. Multiply the given length of side by the numbers in the third column opposite the polygon required, and the product will be the radius of a circle to contain that polygon.

Example 1. Required the radius of a circle to contain an octagon, whose breadth AB=18.5 inches.

Half of 18.5 = 9.25, and  $9.25 \times 1.08 = 9.99$  or ten inches nearly, the radius of the circle O D.

Example 2. Given the radius O D = 9.99 inches, required the length of side D C.

 $9.99 \times .765 = 7.64235$ , the length of side.

EXAMPLE 3. Given the length of side D C = 7.64235; required the radius D O.

 $7.64235 \times 1.307 = 9.98855145$ , or 9.99 in. nearly.

#### PROBLEM VI.

Having the diameter of a circle given, to find the circumference; or the circumference given, to find the diameter.

Rule 1. As 7 is to 22, so is the diameter to the circumference. Or, as 22 is to 7, so is the circumference to the diameter.

2. As 1 is to 3 1416, so is the diameter to the circumference. Or, as 3 1416 is to 1, so is the circumference to the diameter.

EXAMPLE 1. Required the circumference of a circle when the diameter is 23 5.

$$\frac{23.5 \times 22}{7} = 73\frac{6}{7}$$
, the circumference.

EXAMPLE 2. The circumference of a circle is  $73\frac{6}{7}$ , required the diameter.

$$\frac{73\frac{6}{7}\times7}{22}\times23.5$$
, the diameter.

EXAMPLE 3. Required the circumference of a circle whose diameter is 30.

 $3.1416 \times 30 = 94.248$ , the circumference.

Example 4. What is the diameter of a circle when the circumference is 94.248?

 $94.248 \div 3.1416 = 30$ , the diameter.

# PROBLEM VII.

To find the length of any arc of a circle.

RULE. Subtract the chord of the whole arc from eight times the chord of half the arc; and ; of the remainder is the length of the arc nearly.

EXAMPLE. Required the length of the arc ABC; the chord of half the arc AB=19.8, and chord of the whole arc AC=34.4.

B 
$$19.8 \times 8 = 158.4$$
, and  $158.4 - 34.4 = 41.33$ , the length of the arc.

#### PROBLEM VIIL

To find the diameter of a circle, by having the chord and versed sine given.

Rule. Divide the square of half the chord by the versed sine, to

the quotient of which add the versed sine, and the sum will be the diameter.

Or, if the sum of the squares of the semichord and versed sine be divided by the versed sine, the quotient will be the diameter of the circle to which that segment corresponds.

EXAMPLE. Given the chord AB = 24, and versed sine CD = 8; required the diameter of the circle CE.

Half the chord = 12, and  $12^2 \div 8 = 18 + 8 =$ 

26, the diameter.

Or, 
$$\frac{12^2 + 8^2}{8} = 26$$
, as before.



#### PROBLEM IX.

To find the area of an ellipsis, or oval.

Rule. Multiply the longest diameter by the shortest, and the product by '7854; the result is the area.

An oval is 25 inches by 16.5: what are its superficial contents?

$$25 \times 16.0 = 412.5 \times .7854 = 323.9775$$
 inches, the area.

Note.—Multiply half the sum of the two diameters by 3 1416, and the product is the circumference of the oval or ellipsis.

#### PROBLEM X.

To find the area of a parabola, or its segment.

Rule. Multiply the base by the perpendicular height, and two-thirds of the product is the area.

What is the area of a parabola whose base is 20 feet and height

123

$$20 \times 12 = \frac{240 \times 2}{3} = 160$$
 feet, the area.

# Some of the properties of a circle.

1. It is the most capacious of all plane figures, or contains the greatest area within the same perimeter or outline.

2. The areas of circles are to each other as the squares of their diameters, or of their radii.

3. Any circle whose diameter is double that of another, contains four times the area of the other.

4. The area of a circle is equal to the area of a triangle whose base is equal to the circumference, and perpendicular equal to the radius.

5. The area of a circle is equal to the rectangle of its radius

and a right line equal to half its circumference.

6. The area of a circle is found by squaring the diameter, and multiplying by the decimal '7854; or by multiplying the circumference by the radius, and dividing the product by 2?

EXAMPLE 1. Required the area of a circle, the diameter being 30.5.

 $30.5^2 \times .7854 = 730.618350$ , the area required.

Example 2. What is the area of a circle when the diameter is 1? In this case the circumference is 3.1416, half of which is 1.5708. and half of 1 = .5; then  $1.5708 \times .5 = .7854$ , the area.

Having the area of a circle given, to find the diameter.

RULE. As 355 is to 452, so is the area to the square of the diameter.

Or, multiply the square root of the area by 1'12837, and the product will be the diameter.

Or, divide the area by the decimal '7854, and extract the square

root.

Example. Required the diameter of that circle whose area is 122.71875.

$$\frac{\sqrt{122.71875 \times 452}}{355}$$
 = 12.5, diameter.

Or,  $\sqrt{122.71875} = 11.077$ ; and  $11.077 \times 1.12837 = 12.49895$ , or 12.5, diameter.

#### PROBLEM XI.

To find the area of a sector of a circle.

RULE. Multiply the length of the are by the radius of the circle, and half the product will be the area.



Example. Required the area of a sector of a circle whose arc ABC = 26.666, and radius B O = 16.9.

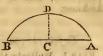
$$\frac{26.666 \times 16.9}{2} = 225.3277$$
, the area.

# PROBLEM XII.

To find the area of a segment of a circle.

RULE. Multiply the versed sine by the decimal 626, to the square of the product add the square of half the chord; multiply twice the square root of the sum by 3 of the versed sine, and the product will be the area. EXAMPLE. Required the area of a segment of a circle whose chord AB=48, and versed sine CD=18.

 $18 \times 626 = 11.268^2 = 126.967824$ ; which add to 576, being the square of half the chord = 702967824, twice the square root of which is 53.026  $\times$  12; being  $\frac{2}{3}$  of the versed sine = 636.312, the area.



The following is a near approximate to the preceding rule:

To the cube of the versed sine, divided by twice the length of the chord, add § of the product of the chord, multiplied by the versed sine; and the sum will be the area of the segment nearly. Take the last example:

Versed sine = 18, and chord 48, then,  $\frac{18^3}{48 \times 2} = 60.7$ ; and  $\frac{18 \times 18 \times 2}{2} = 576 + 60.7 = 636.7$ , the area nearly.

Or, the area of a segment may be found by finding the area of a sector having the same radius as the segment; then deducting the area of the triangle, leaves the area of the segment.

## PROBLEM XIII.

To find the area of a circular ring or space included between two concentric circles.

RULE. Add the inside and outside diameters together, multiply the sum by their difference, and by 7854, and the product will be the area.

EXAMPLE. The diameters of two concentric circles, AB and CD, are 10 and 6; required the area of the ring or space contained between them.

 $10 + 6 \times 4 \times 7854 = 50.2656$ , the area.



#### PROBLEM XIV.

To find the area of an ellipsis.

Rule. Multiply the transverse or longer diameter by the conjugate or shorter diameter, and by 7854, and the product will be the area.

Example. Required the area of an ellipsis whose longer diameter A B=12, and shorter diameter C D=9.

 $13 \times 9 \times .7854 = 84.8232$ , the area.

Note.—If half the sum of the two diameters be multiplied by 3 1416, the product will be the circumference of the ellipsis.

Thus 
$$12 + 9 = 21$$
, and  $\frac{3.1416 \times 21}{2} = 36.1384$ , the circumference.

#### Mensuration of Solids.

By solids are meant all bodies, whether solid, fluid, or bounded space, that can be comprehended within length, breadth, and thickness.

#### PROBLEM I.

To find the convex surface and solid content of a cylinder.

RULE 1. Multiply the circumference of the base by the height of the cylinder, and the product is the convex surface.

RULE 2. Multiply the area of the base by the height of the cylin-

der, and the product is the solid content.

EXAMPLE 1. Required the convex surface of the cylinder ABCD, whose base AB = 32 inches, and perpendicular height BC = 6



 $3\cdot1416\times32\times72$  inches =  $7238\cdot2464$  square or superficial inches, and  $7238\cdot2464\div144=50\cdot2658$  superficial feet.

EXAMPLE 2. Required the solid content, in cubic inches and cubic feet, of the cylinder as above.

 $32^2 \times .7854 \times 72 = 57905.9712$  cubic inches, and  $57905.9712 \div 1728 = 33.5104$  cubic feet.

EXAMPLE 3. Suppose the cylinder ABCD be intended to contain a fluid, and that the sides and bottom are each one inch in thickness, how many imperial gallons would it contain?

32-2=30 inches diameter; and 72-1=71 inches deep;

then  $\frac{30^2 \times .7854 \times .71}{277 \cdot 274} = 181$  gallons.

Or,  $50187.06 \times .003607 = 181$ , as before.

#### PROBLEM II.

To determine the dimensions of any cylindrical vessel, whereby to contain the greatest cubical contents, bounded by the least superficial surface.

RULE. Multiply the given cubical contents by 2.56, and the cube root of the product equal the diameter, and half the diameter equal

the depth.

Example. Suppose a cylindrical vessel is to be made so as to contain 600 cubic feet, and of such dimensions as to require the least possible materials by which it is constructed, what must be its depth and diameter?

 $600 \times 2.56 = \sqrt[3]{1536} = 11.5379$  feet diameter, and  $11.5379 \div 2 = 5.76895$  feet in depth.

Note.—If the vessel is to be constructed with two ends, then the cube root of four times the solidity divided by 3'1416 equal both the length and diameter, so as to expose the least possible surface, or be composed of the least possible materials, of which to be constructed.

#### PROBLEM III.

To find the surface and solid content of a cone or pyramid.

RULE 1. Multiply the circumference of the base by the slant height, and half the product will be the slant surface; to which add the area of the base, and the product will be the whole surface.

RULE 2. Multiply the area of the base by the perpendicular height, and \( \frac{1}{2} \) of the product will be the solid content.

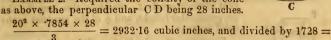
Example 1. Required the convex surface of a cone whose base AB=20 inches, and slant height  $BD=29^{\circ}5$ .

 $\frac{3.1416 \times 20 \times 29.5}{2} = 926772$  square inches,

and divided by 144 = 6.435 superficial feet.

Example 2. Required the solidity of the cone

1.697 cubic feet.

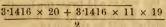


#### PROBLEM IV.

To find the surface of the frustum of a cone or pyramid.

RULE. Multiply the sum of the perimeters of the two ends by the slant height, and half the product will be the slant surface; to which add the areas of the two ends, and the product will be the whole surface.

Example. Required the convex surface of the frustum of a cone ABCD, whose base AB=20 inches, the slant height BC=19, and top end CD=11.



= 925.2012 square inches, and divided by 144 = 6.425 feet nearly.



#### PROBLEM V.

To find the solid content of the frustum of a cone.

Rule. To the product of the diameters of the two ends add the sum of their squares; multiply this sum by the perpendicular height and by 2618; the product is the solid content.

EXAMPLE 1. Required the solid content of the frustum in Problem IV., whose perpendicular E F = 18 inches.

 $20 \times 11 = 220$ , and  $220 + 20^2 + 11^2 \times 18 \times 2618 = 3491.8884$  cubic inches, and divided by 1728 = 2.0208 cubic feet nearly.

EXAMPLE 2. Required the content, in imperial gallons, of the inverted frustum of a cone ABCD, whose inner dimensions are 3½ feet deep, 18 inches diameter at bottom, and 22 inches diameter at top.



$$22 \times 18 = 396$$
, and  $396 + 22^2 + 18^2 \times 42$   
  $\times \cdot 2618 = \frac{13238 \cdot 7024}{277 \cdot 274} = 47 \cdot 745$  galls, nearly.

Or,  $13238.7024 \times 0.00360654 = 47.75$  gallons nearly, as before.

#### PROBLEM VI.

To find the solid content of the frustum of a pyramid.

RULE. To the sum of the areas of the two ends add the square root of their product; multiply this sum by the perpendicular height, and ½ of the product is the

solid content.



EXAMPLE. Required the solid content of the frustum of a pyramid ABCD, whose perpendicular height = 24 inches, the area of the base = 144 inches, and area of the top end = 64.

 $\frac{144 + 64 = 208, \text{ and } \sqrt{144 \times 64} = 96; \text{ then } \frac{208 + 96 \times 24}{3} = 2432 \text{ cubic inches, and } \div 1728$ = 1.4074 cubic feet nearly.

# PROBLEM VII.

To find the solidity of a wedge.

RULE. To the length of the wedge add twice the length of the base; multiply that sum by the height, and by the breadth of the base, and one-sixth of the product will be the solidity.



EXAMPLE. Required the content in cubic inches of the wedge ABCDE, whose base ABC=12 inches long and 4 inches broad, the length of the edge DE=10 inches, and perpendicular height rE=20 inches.

$$\frac{\overline{10+24}\times20\times4}{6} = 452.33 \text{ cubic inches.}$$

### PROBLEM VIII.

To find the convex surface and solid content of a sphere or globe.

RULE 1. Multiply the square of the diameter by 3.1416; the product will be the convex superficies.

RULE 2. Multiply the cube of the diameter by 5236, and the product is the solid content.

Example 1. Required the convex surface of a sphere, whose diameter  $AB = 25\frac{1}{2}$  inches.

 $25 \cdot 5^2 \times 3 \cdot 1416 = 2042 \cdot 8254$  square inches, ÷ 144 = 14 \cdot 1862 square or superficial feet.

Example 2. Required the solid content of a sphere whose diameter  $AB = 25\frac{1}{2}$  inches.

 $25.5^3 \times .5236 = 8682.00795$  eubic inches;  $\div 1728 = 5.0243$  eubic feet.



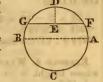
### PROBLEM IX.

To find the convex surface and solid content of the segment of a sphere.

Rule 1. Multiply the height of the segment by the whole circumference of the sphere, and the product is the curved surface,

RULE 2. Add the square of the height to three times the square of the radius of the base; multiply that sum by the height, and by 5236, and the product is the solid content.

EXAMPLE 1. The diameter A B of the sphere A B C D = 20 inches; what is the convex surface of that segment of it whose height E D = 8 inches?



 $3.1416 \times 20 \times 8 = 502.656$  square inches;  $\div 144 = 3.49$  superficial feet.

EXAMPLE 2. The base F G of the segment F D G = 18 inches, and perpendicular E D = 8; what is the solid content?

 $8^2 = 64$ , and  $9^2 \times 3 = 243$ ; then  $243 + 64 \times 8 \times 5236 = 1285.9616$  cubic inches,  $\div 1728 = .7441$  cubic feet.

EXAMPLE 3. Suppose ABCD to be a sugar-pan, and that the diameter of the mouth AB is 4 feet, the depth DC being 25 inches, how many imperial gallons will it contain?

 $\frac{25^2 = 625, \text{ and } 24^2 \times 3 = 1728; \text{ then }}{1728 + 625 \times 25 \times .5236 = \frac{30800.77}{277.274} =}$ 111.084 gallons.

### PROBLEM X.

To find the solidity of a spheroid.

RULE. Multiply the square of the revolving axis by the fixed axis, and by 5236, and the product will be the solidity.



EXAMPLE 1. Required the solid content of the prolate spheroid ABCD, whose fixed axis AC is 50, and revolving axis BD 30.

 $30^2 \times 50 \times .5236 = 23562$ , the solidity.

EXAMPLE 2. What is the solid content of an oblate spheroid, the fixed axis being 30, and revolving axis 50?

 $50^2 \times 30 \times .5236 = 39270$ , the solid content.

#### PROBLEM XI.

To find the solidity of the segment of a spheroid when the base is circular or parallel to the revolving axis.

RULE. From triple the fixed axis take double the height of the segment; multiply the difference by the square of the height, and by 5236; then say, as the square of the fixed axis is to the square of the revolving axis, so is the former product to the solidity.

EXAMPLE 1. Required the solid content of the segment ABC, whose height Br is 10; the revolving axis EF being 40, and fixed axis BD 25.

 $\overline{25 \times 3} - \overline{10 \times 2} = 55$ , and  $55 \times 10^2 \times 5236 = 2879.8$ . Then, as  $25^2 : 40^2 :: 2879.8 : 7372.3$  nearly.



EXAMPLE 2. What is the solid content of the segment of a spheroid whose height = 20 inches, the revolving axis being 25, and fixed axis 50?

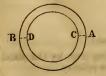
 $50 \times 3 - 20 \times 2 = 110$ , and  $110 \times 20^2 \times 5236 = 23038.4$ ; then, as  $50^2 : 25^2 :: 23038.4 : 5759.6$  inches, the solid content.

#### PROBLEM XII.

To find the convex surface and solid content of a cylindric ring.

RULE 1. Multiply the thickness of the ring added to the inner diameter by the thickness and by 9.8698, and the product will be the convex surface.

RULE 2. To the thickness of the ring add the inner diameter; multiply that sum by the square of the thickness and by 2:4674, and the product will be the solid content.



EXAMPLE 1. The thickness of a cylindric ring A C or D B = 2 inches, and inner diameter = 18, required the convex superficies.

 $\overline{18+2} \times 2 \times 9.8698 = 394.792$  square inches, and  $\div 144 = 2.741$  superficial feet nearly.

### Example 2. Required the solid content of the ring as above.

 $18 + 2 \times 2^2 \times 2 \cdot 4674 = 197 \cdot 392$  cubic inches, and  $\div 1728 = \cdot 114$  cubic feet.

Note.—A cubic foot is equal to 1728 cubic inches, or 2200 cylindrical inches, or 3300 spherical inches, or 6600 conical inches.

# Decimal Approximations,

FOR FACILITATING CALCULATIONS IN MENSURATION.

Lineal feet multiplied by	.00019	= miles.
" yards, "	.000568	= "
Square inches, "	.007	= square feet.
" yards, "	.0002067	= acres.
Circular inches, "	*00546	= square feet.
Cylindrical inches, "	.0004546	
feet, "	.02909	= cubic yards.
Cubic inches, ""	'00058	= cubic feet.
" feet, "	03704	= cubic yards.
	6.232	= imperial gallons.
" inches, "	.003607	= " "
	4.895	= " "
inches, "	002832	= " "
Cubic inches, "	.263	= lbs. avs. of east iron.
and see many seed and an arranged and	281	= " wrought do.
mac la contraction and contrac	283	= " steel. = " copper.
" " " " " " " " " " " " " " " " " " "	3225	= " copper.
46 46 46	3037	= " brass. = " zinc.
	.26	= "zinc.
66 66 66	<b>.41</b> 03	= " lead. = " tin.
and the same of th	2636	
	4908	= " mercury.
Cylindrical inches, "	2065	= " cast iron.
and the same than the same	2168	= " wrought iron.
66 . 65 - 1111	2223	= " wrought iron. = " steel. = " copper.
	.2533	= " copper.
Assessment from proper property of the	.2385	= "brass.
	2042	= " zinc.
P. C.	3223	
" "	207	= " tin.
	·3854	= " mercury.
Avoirdupois lbs., "	.009	= cwts.
66	.00045	= tons.

# INSTRUMENTAL ARITHMETIC;

OR, UTILITY OF THE SLIDE RULE.

The slide rule is an instrument by which the greater portion of operations in arithmetic and mensuration may be advantageously performed, provided the lines of division and gauge points be made properly correct, and their several values familiarly understood.

The lines of division are distinguished by the letters ABCD, AB and C being each divided alike, and containing what is termed a double radius, or double series of logarithmic numbers, each series being supposed to be divided into 1000 equal parts, and distributed along the radius in the following manner:

From	1	to	2	contains	301	of	those	parts,	being	the	log. o	f 2.
44			3	44	477				44			3.
6.6			4	44	602				44			4.
**			5	- 66 (1	699				54			5.
4.6			6	44	778				44			6.
4.6			7	**	845				44			7.
			8	4.	903				44			8.
			9	44 .	954				4.6			9.
					1000	be	ing the	e whol	e num	ber.		

The line D, on the improved rules, consists of only a single radius; and although of larger radius, the logarithmic series is the same, and disposed of along the line in a similar proportion, forming exactly a line of square roots to the numbers on the lines B C.

#### Numeration.

Numeration teaches us to estimate or properly value the num-

bers and divisions on the rule in an arithmetical form.

Their values are all entirely governed by the value set upon the first figure, and, being decimally reckoned, advance tenfold from the commencement to the termination of each radius: thus, suppose 1 at the joint be one, the 1 in the middle of the rule is ten, and 1 at the end one hundred. Again, suppose 1 at the joint ten, 1 in the middle is 100, and 1 or 10 at the end is 1000, &c., the intermediate divisions on which complete the whole system of its notation.

# To Multiply Numbers by the Rule.

Set 1 on B opposite to the multiplier on A; and against the number to be multiplied on B is the product on A.

Multiply 6 by 4.

Set 1 on B to 4 on A: and against 6 on B is 24 on A. The slide thus set, against

1300	011 0	3 21 OI	44.	-
7 (	on B i	s 28 o		
8		32		
9	66	36	44	
10	= 44	40	44	
11	- 46	44	66	
12	4.6	48	=	
15	66	60	"	
25	44	100, 8	Ec. , &	cc.

### To divide Numbers upon the Rule.

Set the divisor on B to 1 on A, and against the number to be divided on B is the quotient on A.

Divide 63 by 3.

Set 3 on B to 1 on A, and against 63 on B is 21 on A.

# Proportion, or Rule of Three Direct.

Rule. Set the first term on B to the second on A, and against the third upon B is the fourth upon A.

1. If 4 yards of cloth cost 38 shillings, what will 30 yards cost at

the same rate?

Set 4 on B to 38 on A, and against 30 on B is 285 shillings on A.

2. Suppose I pay 31s. 6d. for 3 cwt. of iron, at what rate is that per ton? 1 ton = 20 cwt.

Set 3 upon B to 31'5 upon A, and against 20 upon B is 210 upon A.

### Rule of Three Inverse.

Rule. Invert the slide, and the operation is the same as direct

proportion.

1. I know that six men are capable of performing a certain given portion of work in eight days, but I want the same performed in three: how many men must there be employed?

Set 6 upon C to 8 upon A, and against 3 upon C is 16 upon A.

2. The lever of a safety valve is 20 inches in length, and 5 inches between the fixed end and centre of the valve: what weight must there be placed on the end of the lever to equipoise a force or pressure of 40 lbs. tending to raise the valve?

Set 5 upon C to 40 upon A, and against 20 on C is 10 on A.

3. If  $8\frac{3}{4}$  yards of cloth,  $1\frac{1}{2}$  yards in width, be a sufficient quantity, how much will be required of that which is only  $\frac{7}{4}$ ths in width, to effect the same purpose?

Set 1'5 on C to 8'75 on A, and against 8'75 upon C is 15 yards upon A.

### Square and Cube Roots of Numbers.

On the engineer's rule, when the lines C and D are equal at both ends, C is a table of squares, and D a table of roots, as—

Squares, 1 4 9 16 25 36 49 64 81 on C. Roots, 1 2 3 4 5 6 7 8 9 on D.

To find the geometrical mean proportion between two numbers.

Set one of the numbers upon C to the same number upon D, and against the other number upon C is the mean number or side of an equal square upon D.

Required the mean proportion between 20 and 45.

Set 20 upon C to 20 upon D, and against 45 upon C is 30 on D.

To cube any number, set the number upon C to 1 or 10 upon D, and against the same number upon D is the cube number upon C.

Required the cube of 4.

Set 4 upon C to 1 or 10 upon D, and against 4 upon D is 64 upon C.

To extract the cube root of any number, invert the slide, and set the number upon B to 1 or 10 upon D, and where two numbers of equal value coincide, on the lines B D, is the root of the given number.

Required the cube root of 64.

Set 64 upon B to 1 or 10 upon D, and against 4 upon B is 64 upon D, or root of the given number.

On the common rule, when 1 in the middle of the line C is set opposite to 10 on D, then C is a table of squares, and D a table of roots.

To cube any number by this rule, set the number upon C to 10 upon D, and against the same number upon D is the cube upon C.

#### Mensuration of Surface.

#### 1. Squares, Rectangles, &c.

Rule. When the length is given in feet, and the breadth in inches, set the breadth on B to 12 on A; and against the length on A is the content in square feet on B.

If the dimensions are all inches, set the breadth on B to 144 upon A; and against the length upon A is the number of square feet on B. Required the content of a board 15 inches broad and 14 feet long. Set 15 upon B to 12 upon A; and against 14 upon A is 175 square feet on B.

### 2. Circles, Polygons, &c.

Rule. Set 7854 upon C to 1 or 10 upon D  $\cdot$  then will the lines C and D be a table of areas and diameters.

Areas, 3:14 7:06 12:56 19:63 28:27 38:48 50:26 63:61 upon C. Diameters, 2 3 4 5 6 7 8 9 upon D.

In the common rule, set 7854 on C to 10 on D; then C is a line or table of areas, and D of diameters, as before.

Set 7 upon B to 22 upon A; then B and A form or become a table of diameters and circumferences of circles.

Circumferences, 3'14 6'28 9'42 12'56 15'7 18'85 22 25'13 28'27 upon A. Diameters, 1 2 3 4 5 6 7 8 9 upon B.

Polygons from 3 to 12 sides. Set the gauge-point upon C to 1 or 10 upon D; and against the length of one side upon D is the area upon C.

Sides, 3 5 6 7 8 9 10 11 12. Gauge-points, 433 1.7 2.6 3.63 4.82 6.18 7.69 9.37 11.17.

Required the area of an equilateral triangle, each side 12 inches in length.

Set '433 upon C to 1 upon D; and against 12 upon D are 62'5 square inches upon C.

TABLE OF GAUGE-POINTS FOR THE ENGINEER'S RULE.

Names.	F, F, F.	F, I, I.	I, I, I.	F, 1.	I, I.	F.	1.
Cubic inches,	578	83	1728	106	1273	105	121
Cubic feet,	1	144	1	1833	22	121	33
Imperial gallons, .	163	231	277	294	353	306	529
Water in lbs.,	16	23	276	293	352	305	528
Gold "	814	1175	141	149	178	155	269
Silver "	15	216	261	276	334	286	5
Mercury "	118	169	203	216	258	225	389
Brass "	193	177	333	354	424	369	637
Copper "	18	26	319	331	397	345	596
Lead "	141	203	243	258	31	27	465
Wro't iron "	207	297	357	338	453	394	682
Cast " "	222	32	384	407	489	424	733
Tin "	219	315	378	401	481	419	728
Steel "	202	292	352	372	448	385	671
Coal "	127	183	22	33	28	242	42
Marble "	591	85	102	116	13	113	195
Freestone "	632	915	11	1162	14	141	21
3-3-1-0		AL 10	10	0.000		100	

#### FOR THE COMMON SLIDE RULE.

Names.	F, F, F	F, I, I.	I, I, I.	F, I.	I, I.	F.	I.	
Cubic inches,	36	518	624	660	799	625	113	
Cubic feet,	625	9	108	114	138	119	206	
Water in lbs.,	10	144	174	184	22	191	329	
Gold "	507	735	88	96	118	939	180	
Silver "	938	136	157	173	208	173	354	
Mercury "	738	122	127	132	162	141	242	
Brass "	12	174	207	221	265	23	397	
Copper "	112	163	196	207	247	214	371	
Lead "	880	126	152	162	194	169	289	
Wro't iron "	129	186	222	235	283	247	423	
Cast " "	139	2	241	254	304	265	458	
Tin "	137	135	235	25	300	261	454	
Steel "	136	183	22	233	278	239	418	
Coal "	795	114	138	146	176	151	262	
Marble "	370	53	637	725	81	72	121	
Freestone "	394	57	69	728	873	755	132	
The second second		122	11. 19			- 1		

# Mensuration of Solidity and Capacity.

General Rule. Set the length upon B to the gauge-point upon A; and against the side of the square, or diameter on D, are the cubic contents, or weight in lbs. on C.

1. Required the cubic contents of a tree 30 feet in length, and 10

inches quarter girt.

Set 20 upon B to 144 (the gauge-point) upon  ${\bf A}_{\, 1}$  and against 10 upon D is 2075 feet upon C.

2. In a cylinder 9 inches in length and 7 inches diameter, how many cubic inches?

Set 9 upon B to 1273 (the gauge-point) upon A; and against 7 on D is 346 inches on C.

3. What is the weight of a bar of cast iron 3 inches square, and 6 feet long?

Set 6 upon B to 32 (the gauge-point) upon A; and against 3 upon D is 168 lbs. upon C.

By the common rule.

4. Required the weight of a cylinder of wrought iron 10 inches long, and 5½ diameter.

Set 10 upon B to 233 (the gauge-point) upon A; and against 5½ upon D is 66.65 lbs. on C.

5. What is the weight of a dry rope 25 yards long, and 4 inches circumference?

Set 25 upon B to 47 (the gauge-point) upon A; and against 4 on D is 53'16 lbs. on C.

6. What is the weight of a short linked chain 30 yards in length, and  $\frac{6}{16}$ ths of an inch in diameter?

Set 30 upon B to 52 (the gauge-point) upon A; and against 6 on D is 129 5 lbs. on C.

### Land Surveying.

If the dimensions taken are in chains, the gauge-point is 1 or 10; if in perches, 160; and if in yards, 4840.

Rule. Set the length upon B to the gauge-point on A; and

against the breadth upon A is the content in acres upon B.

1. Required the number of acres or contents of a field 20 chains 50 links in length, and 4 chains 40 links in breadth.

Set 20.5 on B to 1 on A; and against 4.4 on A is 9 acres on B.

2. In a piece of ground 440 yards long, and 44 broad, how many acres?

Set 440 upon B to 4340 on A; and against 44 on A is 4 acres on B.

# Power of Steam-Engines.

Condensing Engines—Rule. Set 3.5 on C to 10 on D; then D is a line of diameters for cylinders, and C the corresponding number of horse power; thus,

Horse power, .  $3\frac{1}{4}$  4 5 6 8 10 12 16 20 25 30 40 50 on C. C. D. . . . . 10 in.  $10\frac{1}{4}$  12  $13\frac{1}{4}$  15 $\frac{1}{2}$  17  $18\frac{3}{4}$  21 $\frac{1}{4}$  24  $26\frac{3}{4}$  29 $\frac{1}{2}$  33 $\frac{3}{4}$  37 $\frac{3}{4}$  on D.

The same is effected on the common rule by setting 5 on C to 12 on D.

Non-condensing Engines.—Rule. Set the pressure of steam in lbs. per square inch on B to 4 upon A; and against the cylinder's diameter on D is the number of horse power upon C.

Required the power of an engine, when the cylinder is 20 inches

diameter, and steam 30 lbs. per square inch.

Set 30 on B to 4 on A; and against 20 on D is 30 horse power on C.

The same is effected on the common rule by setting the force of the steam on B to 250 on A.

# Of Engine Boilers.

How many superficial feet are contained in a boiler 23 feet in length and  $5\frac{1}{2}$  in width?

Set 1 upon B to 23 upon A; and against 5.5 upon B is 126.5 square feet upon A.

If 5 square feet of boiler surface be sufficient for each horse power, how many horse power of engine is the boiler equal to?

Set 5 upon B to 126'5 upon A; and against 1 upon B is 25'5 upon A.

### The Laws of Motion.

If M = mass of a material body, And W = the weight of it.

$$W = M \times 32.19$$
;

Or the mass of a body is equal to its weight divided by 32·19. EXAMPLE. Find the weight of a body whose mass is 3½:

$$W = 3.5 \times 32.19 = 112.66$$
 lbs.

The gravity of a material body is its weight. Falling bodies fall through the same space in the same time, whatever may be their weight. A body one ton will fall to the ground no faster than a body one pound.

The velocity of a body is the number of feet passed over in one

second.

Put v = the velocity of a falling body, at the end of t seconds,

$$v = 32.19 \times t$$

The quantity 32:19 is the velocity of a falling body at the end of one second.

Rule, to find the Velocity of a Falling Body at the end of any Number of Seconds.

Multiply the number of seconds by 32·19, the product will be the velocity.

EXAMPLE. Find the velocity of a body falling from a height in nine seconds:

Velocity =  $32.19 \times 9 = 289.71$ .

Put s for the number of feet a falling body falls through in t seconds:

$$\therefore s = \frac{32 \cdot 19 \ t^2}{2}.$$

Rule to find the Space passed over by a Falling Body in any Number of Seconds.

Square the number of seconds, and multiply the result by 16.09, the product will be the distance passed over in feet.

EXAMPLE. A stone fell from the top of a chimney to the bottom in four seconds; find the height of the chimney:

Height of chimney =  $16.09 \times 16 = 257.44$  feet.

$$s = \frac{v^2}{64.39}$$
, where  $v$  is the velocity.

Rule to find the Space passed over by a Falling Body when the Velocity is given.

Square the velocity, and divide by 64.39; the quotient will be

the number of feet passed over.

The quantity 32.19 is frequently called the accelerating force of gravity, and is denoted by f. The following formulæ include all cases that can occur in falling bodies.

$$s = \text{space passed over} = \frac{ft^2}{2} = \frac{t}{2} \frac{v}{2} = \frac{v^2}{2f};$$

$$v = \text{velocity at the end of } (t) \text{ seconds } = ft = \frac{2s}{t} = \sqrt{2fs};$$

$$t = \text{time} = \frac{v}{f} = \frac{2 s}{v} = \sqrt{\frac{2 s}{f}};$$

$$f = \frac{v}{t} = \frac{v^2}{2 \, s} = \frac{2 \, s}{t^2}.$$

The above formulæ and rules are applicable only to the case when the body is acted upon by the force of gravity.

Rules and Formulæ when a body is acted on by any force.

Put M = mass acted on by a force of F pounds.

a = velocity at the end of a second, which is called accelerating force.

s =space passed over in (t) seconds, producing a velocity (v).

$$\therefore \alpha = \frac{F}{M} = \frac{v}{t};$$
And  $2 s = \frac{Ft^2}{M} = \frac{Mv^2}{F}$ 

Rule for finding the accelerating force of a body.

Divide the force by the mass (remembering that mass is equal to weight divided by 32·19) or the velocity by the time, either quotient will give the accelerating force.

EXAMPLE. A force of 25 lbs. acts on a body whose weight is 84 lbs.

Find the accelerating force.

The mass = 
$$\frac{84}{32 \cdot 19}$$
 = 2.6 nearly;  
 $\therefore a = \frac{25}{2.6}$  = 9.62 nearly.

The velocity at the end of 10 seconds =  $9.62 \times 10 = 96.2$ .

Time of a Body falling down an Inclined Plane.

Let ABC be an inclined plane, BC perpendicular, and AB parallel to the horizon.

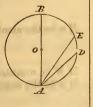
The velocity at A in falling down A C is the same as it would be in falling perpendicularly down the height B C.



Put t = time in falling from C to A. l = A C the length of the inclined plane. h = B C the height of ditto.

$$\therefore t = \sqrt{\frac{2 l^2}{f h}}.$$

Let  $A\ D\ E\ B$  be a circle whose diameter  $A\ B$  is perpendicular to the horizon. The times of a body falling down any chords  $A\ D$ ,  $A\ E$  are equal, and equal to the time in falling vertically through  $A\ B$ .



The Time of Oscillation of a Simple Pendulum.

Let A B the length of the pendulum = l, And  $\pi = 3.14159$ , &c.; q = 32.19

T = time in seconds oscillating from the point B to D.

The arc  $\widehat{BC} = \widehat{CD}$  is small.

$$\therefore \mathbf{T} = \pi \left(\frac{l}{g}\right)^{\frac{1}{2}}$$



Rule to find the Time of one Oscillation of a Simple Pendulum.

Divide the length of the pendulum by 32.19; extract the square root of this quotient, and multiply the result by 3.1416, and the product will be the time of oscillation in seconds.

If L be the length of a pendulum which oscillates in one second,

$$\therefore T = \left(\frac{l}{L}\right)^{\frac{1}{2}}.$$

The value of L for the latitude of London is 39:1386 inches. A pendulum  $9\frac{25}{30}$ ,  $4\frac{25}{70}$ ,  $2\frac{57}{108}$  inches long, will oscillate in a half, a third, a quarter seconds respectively.

If n be the number of oscillations made by a pendulum in one

hour, then

$$l = 3600^2 \times \frac{L}{n^2}$$

The time of oscillation is not dependent on the weight of the bob.

### Centrifugal Force.



Let the weight W, placed at B, be connected with a cord, or wire, with the fixed point A round which it revolves with a uniform velocity.

Put V = velocity of rotation.

r = A B, the length of the cord in feet.

F = centrifugal force, or the force which is exerted to break the cord in the direction of its length.

$$\therefore F = \frac{W V^2}{32 \cdot 19 \times r}.$$

If n be the number of revolutions in one minute,

$$\therefore F = \frac{331}{1000000} \times Wr n^2.$$

If W be measured in tons, then F will be in tons also. If w be the angular velocity,  $\therefore F = \frac{W r w^2}{q}$ 

$$: F = \frac{W r w^2}{q}$$

If T be the time of the weight making a complete revolution,

$$v = \text{angular velocity} = \frac{2\pi}{T} = \frac{V}{r}$$
.



If there be several bodies at B, C, D, and revolving round the axis passing through A, and perpendicular to the plane A D B C,

$$\therefore F = \frac{w^2}{g} \left\{ r^1 W^1 + W^2 + r^3 W^3 + \&c. \right\}$$

Where w = angular velocity,  $W^3$ ;  $W^2$ ;  $W^3$ , &c.: the weights at  $B \ C \ D$ , &c., and  $r^1$ ,  $r^2$ ,  $r^3$ , &c, the distances  $A \ B$ ,  $A \ C$ ,  $A \ D$ , &c.

EXAMPLE. Let the weights at B and C be 80 and 90 lbs. respectively, revolving at a distance A B = 8 feet, A C = 12 feet, with a velocity making 40 revolutions per minute. Find the centrifugal force, or the pressure on the axis passing through A.

$$w = \frac{2\pi \times 40}{60} = \frac{4\pi}{3};$$

$$\therefore F = \frac{16 \pi^2}{9} \left\{ 8 \times 80 + 12 \times 90 \right\} = 30178 \text{ lbs.}$$

The moment of inertia.

If 
$$(W_1 + W_2 + W_3 + \&c.) k^2 = W_1 r_1 + W_2 r_2^2 + W_3 r_3^2 + \&c.$$

Each side of this equation is called the moment of inertia, and the distance k is called the radius of gyration of the revolving system.

Let a constant force F act at a distance Af = a from the axis

of motion.

The angular velocity at the end of a second

$$= \frac{g F a}{(W_1 + W_2 + W_3 + \text{de.}) k^2}.$$

The angular velocity at the end of one revolution

$$= \frac{2 \ V_{g} \ F a \pi}{V W_{1} + W_{2} + W_{3} + \&c. \times k}$$

If a point O be determined from the equation

$$A O = \frac{k^2}{A G},$$

where G is the centre of gravity of the system, then O is called the centre of oscillation.

The values of k in Geometrical Solids.

A rectangular parallelopipedon revolving about an axis passing through its centre of gravity, and parallel to either of its edges.

$$k^2 = \frac{b^2 + c^2}{12},$$

where b c are the length and breadth at right angles to the axis of revolution.

An upright triangular prism about a vertical axis passing through its centre of gravity.

$$k^2 = \frac{a^2}{48} + \frac{c^2}{36}.$$

The section of the prism perpendicular to the revolving axis is an isosceles triangle, the base being denoted by (a), and the perpendicular upon it from the angle contained by the equal sides by (c).

In a cylinder, whose radius is (r), revolving about its axis,

$$k^2 = \frac{r^2}{2}.$$

In a hollow cylinder, whose internal and external radii are a and b respectively, revolving about its axis,

$$k^2 = \frac{a^2 + b^2}{2}$$

In a cylinder, whose radius is r and length l, revolving round a line at right angles to its axis, and passing through its middle,

$$k^2 = \frac{l^2}{12} + \frac{r^2}{4}.$$

In a sphere, whose radius is r, revolving about its diameter,

$$k^2 = \frac{2 r^2}{5}.$$

In a hollow sphere, whose internal and external radii are (a) and (b) respectively, revolving about its diameter,

$$k^2 = \frac{2(b^5 - a^5)}{5(b^3 - a^3)}.$$

In a cone, whose base is a circle, radius r,

$$k^2 = \frac{3 r^2}{10}.$$

In a cone, whose radius of base is r and height h, revolving about a line at right angles to its axis, and passing through its centre of gravity,

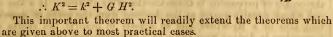
$$k^2 = \frac{3 (4 r^2 + h^2)}{80}.$$

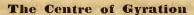
The square of the radius of gyration about any line in a revolving system, is equal to the square of the radius of gyration about a line parallel to it passing through the centre of gravity and the square of the distance from the centre of gravity to the line about which the system revolves.

Let G be the centre of gravity of any body; draw AB any line about which the system revolves. Let CD be parallel to AB, and draw G H perpendicular to A B.

Let K = radius of gyration when revolving about A B.

> k = radius of gyration when revolving about CD.





is that part of a body revolving about an axis, into which, if the whole quantity of matter were collected, the same moving force would generate the same angular velocity.

To find the centre of Gyration, multiply the weight of the several particles by the squares of their distances from the centre of motion, and divide the sum of the products by the weight of the whole mass; the square root of the quotient will be the distance of the centre of gyration, from the centre of motion.

The distances of the centre of gyration from the centre of

motion, of different revolving bodies, are as follows:

In a straight rod revolving about one end, the length  $\times$  :5773. In a circular plate, revolving on its centre, the radius × .7071.

In a circular plate, revolving about one diameter, the radius  $\times$  5. In a thin circular ring, revolving about one diameter, radius × .7071.

In a solid sphere, revolving about one diameter, the radius

In a thin hollow sphere, revolving about one diameter, the radius × '8164.

In a cone, revolving about its axis, the radius of the base x .5477.

In a right-angled cone, revolving about its vertex, the height

In a paraboloid, revolving about its axis, the radius of the base × ·5773.

#### The Centre of Percussion

is that point in a body revolving about a fixed axis, into which the whole of the force or motion is collected.

It is, therefore, that point of a revolving body which would strike any obstacle with the greatest effect; and, from this property, it has received the name of the centre of percussion.

The centres of oscillation and percussion are in the same point.

If a heavy straight bar, of uniform density, be suspended at one extremity, the distance of its centre of percussion is two-thirds of its length.

In a long slender rod of a cylindrical or prismatic shape, the centre of percussion is nearly two-thirds of the length from the axis

of suspension.

In an isosceles triangle, suspended by its apex, the distance of the centre of percussion is three-fourths of its altitude. In a line or rod whose density varies as the distance from the point of suspension, also in a fly-wheel, and in wheels in general, the centre of percussion is distant from the centre of suspension three-fourths of the length.

In a very slender cone or pyramid, vibrating about its apex, the distance of its centre of percussion is nearly four-fifths of its length.

#### On Work.

A unit of work is one pound avoirdupois raised vertically one foot.

If U denotes the units of work in raising W lbs. h feet—

$$\therefore U = Wh.$$

Rule to find the Units of Work in Raising a given Weight a given Height.

Multiply the height in feet by the weight in pounds, the product will be the units of work done.

Example. Find the units of work in raising half a ton 30 feet high.

 $U = 1120 \times 30 = 33600$  units of work.

It is important to observe, in the application of the above formula to practical cases, that the height (h) is the vertical distance through which the centre of gravity of the body whose weight is (W) is raised.

EXAMPLE. Find the units of work in lowering the surface of water in a well one yard; the depth to the surface of water being

40, and diameter 3 feet.

The weight of a cubic foot of water is  $62\frac{1}{2}$  lbs.

The weight of water =  $9 \times .7854 \times 3 \times 62.5 = 1325.36$  lbs. The height through which the centre of gravity is raised = 41.5 feet.

 $U = 1325.36 \times 41.5 = 55002$  units of work.

The work done in raising a body up an inclined plane, or any curved surface, is equal to the work done in raising the body vertically through the height of the inclined plane.

There are 29000 units of work done in sawing a square foot of

green oak.

#### Horse Power.

A horse power is 33000 units of work done in one minute.

Put H, equal to the horse power, and U, the units of work done, in Thours:

 $\therefore 33000 H = \frac{U}{60 T}.$ 

The following results are taken from Morin:

	Line rouse with a country and	
	A Man laboring Eight Hours per Day will perform the follo Units of Work.	wing
	Raising his own body,	4250 3120 2380
	Turning a handle,  Working with his arms and legs, as in rowing,  A Man laboring Six Hours per Day.	2600 4000
	Raising material with a pulley,	1560 1470 1126
	A Man laboring Ten Hours per Day.  Raising material with a wheelbarrow on ramps,	720 470
	Useful Work of a Man raising Water—Duration of Labor, E Hours per Day.	ight
-	With a windlass from deep wells,	2560 1730 2167
The Party of Labor.	With an Archimedean screw, Raising water from a well with a pail and rope,	1505 1054
1	Work of Animals	

A horse, in a common	pumpi	ng engi	ne,		1101	0	300	17550
A mule, ditto, .	20 116		1	200	1.0			11700
An ass, ditto, .	. 34						٠.	3510

Example. Required the horse power of an engine that will saw 368 planks, each being 30 feet by 2 feet 6 inches, in twelve hours.

There are 29000 units of work done in sawing one square foot;

Then 30 × 2.5 × 368 × 29000 = units of work done in sawing the planks.

Put x = the horse power of the engine;

Then  $60 \times 12 \times 33000 \times x = \text{units of work done by the engine}$ in twelve hours.

Hence, 
$$x = \frac{30 \times 2.5 \times 368 \times 29000}{60 \times 12 \times 33000} = 33.7$$
 horse power.

EXAMPLE. How many tons of coals would two men raise, working with a wheel and axle, from a pit whose depth is 20 yards, in 12 hours?

From the Table, a man working with a wheel and axle will do

2600 units of work in one minute.

Then,  $2600 \times 60 \times 12 \times 2 = \text{work done by the two men}$ .

Put x = the tons of coals raised.

Then,  $2240 \times 20 \times 3 \times x = \text{work done by the two men.}$ 

$$\therefore x = \frac{2600 \times 60 \times 12 \times 2}{2240 \times 20 \times 3} = 27.85 \text{ tons raised.}$$

The Traction of Horses at various rates of Travelling.

It is a well known fact, that the traction or force which a horse can exert decreases with the increase of speed.

Rate in miles per hour, 2 3  $3\frac{1}{2}$  4  $4\frac{1}{2}$  5 Force exerted by the horse, 166 lbs. 125 104, 83,  $62\frac{1}{2}$ ,  $41\frac{2}{3}$ .

#### Accumulated Work.

If a force be applied to move a body subject to no resistance whatever, it will be wholly occupied in increasing the speed of the body. In this case the work which is done by the action of the force applied is accumulated in the body, therefore it is called accumulated work.

Put V = the velocity of the body or feet per second.

And W = the weight of the body in pounds.

Accumulated work = 
$$\frac{WV^2}{64}$$
.

If W be measured in tons, and V be measured in miles per hour,

Accumulated work = 
$$\frac{3388}{45} W V^2$$

A railway train 80 tons moves uniformly at the rate of 30 miles per hour, find the accumulated work.

Accumulated work = 
$$\frac{3388 \times 80 \times 900}{45} = 5420800.$$

The horse power of the engine 
$$=\frac{5420800}{33000} = 164$$
 nearly.

Generally the horse power of the engine  $=\frac{77~W~V^2}{33750}$  where W is in tons and V in miles per hour.

The friction of a railway train is from 8 to 10 lbs. per ton.

#### Work done by Machines.

The moving power, which is applied to any machine moving uniformly, is employed in overcoming the resistance of friction, and useful work done at the working points of the machine. Hence,

the aggregate number of units of useful work yielded by any machine at its working point is less than the number received upon the machine directly from the moving power, by the number of units expended upon the resistance of friction. (The machine moving uniformly.)

# General Rule to find the Work done by any Machine.

Find the distance through which the power (P) applied to the machine has travelled in one minute, and let this distance be called (a).

Find the distance through which the weight (W), producing useful work, has travelled in one minute, and let this distance

be (b).

Then a P - b W = work done by friction per minute.

And a P = work applied per minute. b W = useful work done per minute.

# The Horse Power of an Engine.

Let P be the mean effective pressure of the steam on the piston.

l be the length of the stroke in feet.

n be the number of strokes per minute.

.: Horse power of the engine = 
$$\frac{n l P}{33000}$$
.

The nominal horse power  $=\frac{7 n l}{33000}$  as adopted by the Admiralty.

# On the Strength of Animals.

Let P be the force in lbs. that any animal can exert when moving at (v) miles per hour.

Put K = the greatest effort the animal can exert when standing. And c = the greatest number of miles per hour the animal can give itself when unimpeded by any weight.

According to Bouguer,  $P = (1 - \frac{v}{c})$ . K.

Euler, 
$$P=(1-rac{v^2}{c^2})$$
 .  $K$ .

" Euler, 
$$P = \left(1 - \frac{v}{c}\right)^2$$
. K.

It is readily seen that (v) miles per hour is equal to (88 v) feet per minute. Put U the units of work done by the animal per minute,

Then, according to Bouguer, 
$$U=$$
 88  $(v-\frac{v^2}{c})$  .  $K$ .

According to Euler, 
$$U=88\left(v-rac{v^3}{c^2}
ight)$$
 .  $K$ . 
$$U=88v(1-rac{v}{c})^2$$

The values of U will be the greatest when

$$v = \frac{c}{2}$$
. According to Bouguer.

$$v = \frac{c}{\sqrt{3}}$$
. " Euler.

$$v = \frac{c}{3}$$
. Euler.

Substitute these values in the formula for P and U, then there will result:

 $\frac{K}{2}$  = the load of the animal when producing the greatest effect.

$$\frac{4K}{9}$$
 = "

22 c K = the greatest effect, by first formula.

$$\frac{176 \ c K}{3 \sqrt{3}} =$$
 by second formula.

$$\frac{35 \ 2 \ c \ k}{27} =$$
 " by third formula.

# To Calculate the Different Parts of a Crane as respects Mechanical Advantage.

(1.) The number of revolutions of the pinion to one of the wheel, the length of the handle, and the force applied being given, to find the diameter of the barrel.

Rule. Multiply the diameter of the circle described by the winch, or handle, in inches, by the power applied in lbs, and by the number of revolutions of the pinion to one of the wheel; divide this product by the weight to be raised in lbs., and the quotient is the diameter of the barrel in inches.

(2.) The diameter of the barrel, the length of the handle, and the force applied given, to find the number of revolutions of the pinion to one of the wheel.

Rule. Multiply the weight to be raised in lbs. by the diameter of the barrel in inches, and divide the product by the diameter of the circle described by the handle in inches, multiplied by the power applied in lbs., and the quotient is the revolutions of the pinion to one of the wheel.

(3.) The diameter of the barrel, the number of revolutions of the pinion to one of the wheel, and the power applied given, to find the length of the handles.

Rule. Multiply the weight to be raised in lbs. by the barrel's diameter in inches, and divide the product by the power applied in lbs., multiplied by the number of revolutions of the pinion to one of the wheel, and half the quotient is the length of the handles.

(4.) The diameter of the barrel, the revolutions of the pinion to one of the wheel, and length of handles given, to find the power required.

Rule. Multiply the weight to be raised in lbs. by the diameter of the barrel in inches, and divide the product by the diameter of the circle described by the handle multiplied by the revolutions of the pinion to one of the wheel, and the quotient is the power applied.

The handles of a crane should not be less than 2 feet 11 inches or 3 feet from the ground, and the jib to stand at an angle of about 45 degrees.

# Equilibrium and Pressure of Beams.

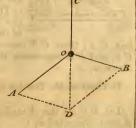
The Parallelogram of Forces.

It has been proved by experiment that three forces, proportional to the two sides of a parallelogram and its diagonal, are in a state of equilibrium when their directions are in the direction of these lines.

Let two forces, represented in direction and magnitude by the lines AO and BO, act at the point O, then a third force CO in direction and magnitude can be found, so that the three forces are in a state of equilibrium.

Draw A D, B D, parallel to O B, O A, respectively; join D O, and produce it to C, making C O equal to O D, then O C is the force required.

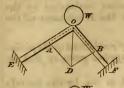
The two forces A O, B O are called components, and C O the resultant of the



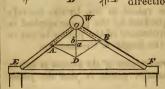
components. The components and resultant are called the paral-

lelogram of forces.

Any resultant force can be readily decomposed into two components, which will be the sides of a parallelogram whose diagonal is the resultant.

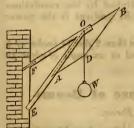


Let the beams OE, OB sustain a weight (W) tons at the point O; draw OD vertical, and make it equal to (W) inches then draw DA, DB parallel to OF and OE respectively; measure DA, DB in inches which will be the pressure in tons in the directions OF and OE.

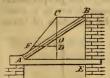


In this case EF is a tie beam to prevent the lower ends of the beams OE, OF from spreading. Draw OD vertically equal to (W) inches, then draw DA, DB parallel to OF, OE and aA, bB, parallel to EF, then AD will be

the thrust in OF, and DB in OE, and Aa equal to bB will be the thrust in the direction of the tie beam EF.



Draw O D vertically equal to (W) inches, and draw D A parallel to O F, and D B parallel to O E, then O B, O A will represent the pressures in the directions O F<sub>1</sub>. O E.



Let AB be a beam whose centre of gravity is O, and resting against an upright wall BE, the lower end resting on an abutment cut in the beam AE at A.

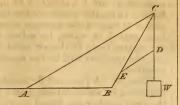
Through the centre of gravity O draw the line CD vertically equal to the weight of the beam, draw BC, DF parallel to EA,

join CA; then CF represents the thrust at A in the direction CF, and FD represents the thrust at B, and also the horizontal thrust at A.

To Compute the Tension of the 'guise' and Shear-leg of a pair of Shears.

Let BC be the shear-leg and AC the guise, and (W) weight in tons supported at C.

Make C as many inches as (W) contains tons, draw D E parallel to A C, then D E measured in inches will be the tension in tons of the guise A C, and C E measured in inches will be the pressure in the direction of the shearleg C E.



To Compute the Tension on the guise arithmetically.

Put 
$$AB = c$$
,  $BC = a$ , and  $AC = b$ .

Then, tension in 
$$A C = \frac{b (b^2 - a^2 - c^2) W}{c V(a+b+c) (b+c-a) (a+c-b) (a+b-c)}$$

And the pressure in 
$$CB = \frac{a \left(b^2 + c^2 - a^2\right) W}{2c \sqrt{(a+b+c)(a+b-c)(b+c-a)(a+c-b)}}$$

# SPECIFIC GRAVITY.

The comparative density of various substances, expressed by the term Specific Gravity, affords the means of readily determining the bulk from the known weight, or the weight from the known bulk; and this will be found more especially useful, in cases where the substance is too large to admit of being weighed, or too irregular in shape to allow of correct measurement. The standard with which all solids and liquids are thus compared, is that of distilled water, one cubic foot of which weighs 1000 ounces avoirdupois; and the specific gravity of a solid body is determined by the difference between its weight in the air and in water. Thus,

If the body be heavier than water, it will displace a quantity of fluid equal to it in bulk, and will lose as much weight on immersion as that of an equal bulk of the fluid. Let it be weighed first, therefore, in the air, and then in water, and its weight in the air be divided by the difference between the two weights, and the quotient will be its specific gravity, that of water being unity.

Example. A piece of copper ore weighs 564 ounces in the air, and 433 ounces in water: required its specific gravity.

56.25 - 43.75 = 12.5 and  $56.25 \div 12.5 = 4.5$ , the specific gravity.

If the body be lighter than water it will float, and displace a quantity of fluid equal to it in weight, the bulk of which will be equal to that only of the part immersed. A heavier substance

must therefore be attached to it, so that the two may sink in the fluid. Then, the weight of the lighter substance in the air must be added to that of the heavier substance in water, and the weight of both united, in water, be subtracted from the sum; the weight of the lighter body in the air must then be divided by the difference, and the quotient will be the specific gravity of the lighter substance required.

Example. A piece of fir weighs 40 ounces in the air, and, being immersed in water attached to a piece of iron weighing 30 ounces, the two together are found to weigh 3.3 ounces in water, and the iron alone 25.8 ounces in the water: required the specific gravity

of the wood.

40 + 25.8 = 65.8 - 3.3 = 62.5; and  $40 \div 62.5 = 0.64$ , the spe-

cific gravity of the fir.

The specific gravity of a *fluid* may be determined by taking a solid body, heavy enough to sink in the fluid, and of known specific gravity, and weighing it both in the air and in the fluid. The difference between the two weights must be multiplied by the specific gravity of the solid body, and the product divided by the weight of the solid in the air; the quotient will be the specific gravity of the fluid, that of water being unity.

Example. Required the specific gravity of a given mixture of muriatic acid and water; a piece of glass, the specific gravity of which is 3; weighing 3\(\frac{3}{2}\) ounces when immersed in it, and 6 ounces

in the air.

Antim Zinc, Cast In Tin, . Steel, Cast co Bismu Silver,

Gold.

Platinum.

#### $6 - 3.75 = 2.25 \times 3 = 6.75 \div 6 = 1.125$ , the specific gravity.

Since the weight of a cubic foot of distilled water, at the temperature of 60 degrees (Fahrenheit), has been ascertained to be 1000 avoirdupois ounces, it follows that the specific gravities of all bodies compared with it, may be made to express the weight, in ounces of a cubic foot of each, by multiplying these specific gravities (compared with that of water as unity) by 1000. Thus, that of water being 1, and that of silver, as compared with it, being 10·474, the multiplication of each by 1000 will give 1000 ounces for the cubic foot of water, and 10474 ounces for the cubic foot of silver.

TABLE OF SPECIFIC GRAVITIES—WATER = 1000.

. 11.352 | Agate, .

20.337 | Sulphur,

Amber..

Metals.	Mercury, 13.586	Crown glass, 2.488
nony, 6.712		Flint glass, 3 329 Rock crystal, 2 653
1011,	Oak wood, 0.925 Cerk, 0 240	
	Ivory, 1826 White wax, 0960	Liquius.
	Inorganic Non-Metallic	Alashal 0.709
ith, 9.882	Bodies.	Oil of turpentine, 0.870

2.590

Milk, . . . Nitric acid.

2.033 Sulphuric acid, .

1.503

Weights of given bulks of water and air for calculating the absolute weights from the specific gravities of bodies.

Cubic inch of distilled water (bar. 30, therm. 62)	Logarithms.
in grains252.458	2.40219
foot in ounces avoir. 997:1369691	2.99875
in pounds do. 62:3210606	
Weight of 100 cubic in, of air in grains do. 30.49	1.48416

# THE MECHANICAL POWERS, AND THEIR APPLICATION.

The simple Mechanical Powers are six in number, viz. the Lever, the Pulley, the Wheel and Axle, the Inclined Plane, the Wedge, and the Screw. All machines are formed by combinations to a greater or less extent of these six elements. The mechanical effects, however, of the whole, are ultimately resolvable into that of the lever.

By means of the Mechanical Powers a great weight may be sustained, or a great resistance slowly overcome, by the application of a small force. Or, a great velocity may be imparted to a small weight or resistance, by the use of a great force or power.

#### The Lever.

Levers are of three orders:

In the first order, the fulcrum is between the weight and the power.

In the second order, the weight is between the fulcrum and the power.

In the third order, the power is between the weight and the

The bent lever has no peculiarity except that of form, which is given to it for convenience in use. Its properties are those of the first order.

In order to preserve an equilibrium between the power and the weight, they must be to each other inversely as their distances from the fulcrum.

Case 1. When the Lever is of the first order, or when the fulcrum is between the power and the weight.

Rule. Divide the weight to be raised by the power to be applied;

the quotient will give the difference of leverage necessary to support the weight in equilibrio. Hence, a small addition either of leverage or weight will cause the power to preponderate.

EXAMPLE 1. A ball weighing 3 tons is to be raised by 4 men, who can exert a force of 12 cwt. Required the proportionate length of

lever.

3 tons = 60 cwt.; and  $\frac{60}{12}$  = 5.

In this example, the proportionate lengths of the lever to maintain the weight in equilibrio, are as 5 to 1. But, although the ball is sustained by a force of only one fifth of its weight, no power is gained, for the weight passes through only one fifth of the space passed through by the power.

EXAMPLE 2. A weight of 1 ton is to be raised with a lever 8 feet in length, by a man who can exert, for a short time, a force of rather more than 4 cwt. Required at what part of the lever the fulcrum

must be placed.

 $\frac{20 \text{ ewt.}}{4 \text{ cwt.}} = 5$ ; i. e., the weight is to the power as 5 to 1; therefore,

 $\frac{8}{5 \times 1} = 1$  foot and a third from the weight.

EXAMPLE 3. A weight of 40 lbs. is placed one foot from the fulcrum of a lever. Required the power to raise the same when the length of the lever on the other side of the fulcrum is five feet.

$$\frac{40 \times 1}{5}$$
 = 8 lbs., the power.

Case 2. When the lever is of the second order, or when the fulcrum is at one end of the lever and the power at the other, with the weight between them.

Rule. As the distance between the power and the fulcrum is to the distance between the weight and the fulcrum, so is the effect to the power.

EXAMPLE 1. Required the power necessary to raise 120 lbs. when the weight is placed six feet from the power and two feet from the

fulcrum.

As 8:2:: 120: 30 lbs., the power.

EXAMPLE 2. A beam 20 feet in length, and supported at both ends, bears a weight of two tons at the distance of eight feet from one end. Required the weight on each support.

 $\frac{40 \text{ cwt.} \times 8 \text{ feet}}{20 \text{ feet}} = 16 \text{ cwt.}$  on the support that is furthest from the

weight; and  $\frac{40 \times 12}{20 \text{ feet}} = 24 \text{ cwt.}$  on the support nearest to the weight.

Case 3. When the lever is of the third order, or the weight is at one end of the lever, the fulcrum at the other, and the power is applied between them.

Rule. As the distance between the power and the fulcrum is

to the length of the lever, so is the weight to the power.

Example. The length of the lever being eight feet, and the weight at its extremity 60 lbs., required the power to be applied six feet from the fulcrum to raise it.

As 6:8:: 60:80 lbs., Ans.

# The Pulley.

Pulleys are of two kinds, fixed and movable.

The fixed pulley affords no economy of power, but merely changes its direction. The movable pulley changes its position with that of the weight, and effects a saving equal to half the power. An equilibrium is preserved between the power and weight, when the weight is equal to the product of the power and twice the number of movable pulleys.

RULE. Divide the weight to be raised by twice the number of pulleys in the lower block; the quotient will give the power neces-

sary to raise the weight.

EXAMPLE. Required the power to raise 600 lbs, when the lower block contains six pulleys.

$$\frac{600}{6 \times 2} = 50 \text{ lbs., the power.}$$

#### The Wheel and Axle.

The wheel and axle act as a revolving lever; and in order to obtain an equilibrium between the power acting on the circumference of the wheel, and the weight or resistance acted on by the circumference of the axle, the power must be to the weight as the radius of the axle is to that of the wheel. One or more radii of the wheel, or winches, are often substituted for the wheel in the simple machine; and in compound machines the action is communicated by teeth or cogs, forming wheel-and-pinion work.

RULE. As the radius of the wheel is to the radius of the axle, so

is the effect to the power.

Example. A weight of 50 lbs. is exerted on the periphery of a wheel whose radius is 10 feet. Required the weight raised at the extremity of a cord wound round the axle, the radius being 20 inches.

 $\frac{50 \text{ lbs.} \times 10 \text{ feet} \times 12 \text{ inches}}{20 \text{ inches.}} = 300 \text{ lbs., the weight.}$ 

#### The Inclined Plane.

The inclined plane acts as a mechanical power by sustaining a portion of the weight to be raised, while the direction of the applied force is changed from the perpendicular to one more or less horizontal, and the weight moves upwards on it in a diagonal between them. Equilibrium is sustained when the power is to the weight as the perpendicular height of the inclined plane is to its inclined length or hypothenuse, when the power acts in a direction parallel to the inclination of the plane; but as the height is to the base when in a direction parallel to the base.

Rule. As the length of the plane is to its height, so is the weight

to the power.

EXAMPLE. Required the power necessary to raise 540 lbs. up an inclined plane 5 feet long and 2 feet high.

As 5:2:: 540: 216 lbs., the power.

The length, in the above rule, must represent that of the inclined surface, or of the base, accordingly as the power acts parallel to either of these surfaces.

# The Wedge.

The wedge may be regarded as two inclined planes, united by a common base, acting on two weights or resistances at once, or on a fulcrum and a weight, between which it moves, generally, in practice, by the impulse of successive blows.

As in the inclined plane, equilibrium consists in the power being to the resistance as the back of the wedge is to its length, or to the length of its side, accordingly as the resistance acts perpendicularly

to the central line of length or to that of the side.

Case 1. When two bodies are forced from one another by means of a wedge, in a direction parallel to its back.

Rule. As the length of the wedge is to half its back or head, so

is the resistance to the power.

EXAMPLE. The breadth of the back or head of the wedge being 3 inches, and the length of either of its inclined sides 10 inches, required the power necessary to separate two substances with a force of 150 lbs.

As  $10:1\frac{1}{2}::150:22\frac{1}{2}$  lbs., the power.

Case 2. When only one of the bodies is movable.

RULE. As the length of the wedge is to its back or head, so is the resistance to the power.

Example. The breadth, length, and force, the same as in the last

example.

As 10:3:: 150:45 lbs., the power.

#### The Screw.

The screw is an inclined plane, and may be supposed to be generated by wrapping a triangle, or an inclined plane, round a cylinder. The base of the triangle is the circumference of the cylinder; its height, the distance between two consecutive cords or threads; and the hypothenuse forms the spiral cord or inclined plane.

RULE. To the square of the circumference of the screw, add the square of the distance between two threads, and extract the square root of the sum: this will give the length of the inclined plane. Its height is the distance between two consecutive cords or threads.

When a winch or lever is applied to turn the screw, the power of the screw is as the circle described by the handle of the winch, or lever, to the internal or distance between the spirals,

# Case 1. When the weight to be raised is given, to find the power.

RULE. Multiply the weight by the distance between two threads of the screw, and divide the product by the circumference of the circle described by the lever. The quotient is the power.

EXAMPLE. Required the power to be applied to the end of a lever three feet long, to raise a weight of five tons with a screw of 1½ inch between the threads.

 $\frac{11200 \text{ lbs.} \times 1.25}{36 \text{ inches} \times 2 \times 3.1416} = 61.9 \text{ lbs., the power.}$ 

# Case 2. When the power is given, to find the weight it will raise.

RULE Multiply the power by the circumference of the circle described by the lever, and divide the product by the distance between two threads of the screw: the quotient will be the weight. The example is the converse of that in the former case.

To Harden and Polish Alabaster.—1. Take a strong solution of alum, strain it, and put it into a wooden trough sufficiently large to contain the figure, which must be suspended in it by means of a thread of silk; let it rest until a sufficient quantity of the salt is crystallized on the cast, then withdraw it, and polish it with a clean cloth and water.

2. Take white wax, melt it in a convenient vessel, and dip the cast or figure into it; withdraw, and repeat the operation of dipping until the liquid wax rests upon the surface of the cast; then let it cool and dry, when it must be polished with a clean brush.

# TOOTHED WHEELS.

The pitch (or the distance between the centres of two contiguous teeth) of cog-wheels is measured on the pitch-line, or extreme circumference of the wheel; and the distance between that line and the centre of the circle is reckoned as the radius of the wheel.

The following rules have been laid down for the diameters and

number of teeth for wheels and pinions.

#### RULE 1.

As the number of teeth in the wheel +2.25, Is to the diameter of the wheel, So is the number of teeth in the pinion +1.5, To the diameter of the pinion.

EXAMPLE. Given the number of teeth in the wheel = 210, the diameter of the wheel = 25 inches, and the number of teeth in the pinion = 30, to find the diameter of the pinion.

As 210 + 2.25 : 25 :: 30 + 1.5 : 3.7102, = the diameter of the pinion.

#### Rule 2.

As the number of teeth in the wheel +2.25, Is to the diameter of the wheel, So is (No. of teeth in pinion + No. of teeth in wheel)  $\div 2$ , To the distance of their centres.

Example. Given the number of teeth in the wheel=210, the diameter of the wheel = 25 inches, and the number of teeth in the pinion = 30, to find the distance at which their centres should be placed.

As  $210 + 2.25 : 25 :: \frac{30 \times 210}{2} : 14.1342$  inches, = the distance of their centres.

# On the Velocity of Wheels, Drums, Pulleys, &c.

When wheels are applied to communicate motion from one part of a machine to another, their teeth act alternately on each other; consequently, if one wheel contains 60 teeth and another 20, the one containing 20 teeth will make three revolutions, while the other makes but one; and if drums or pulleys are taken in place of wheels, the result will be the same, because their circumferences, describing equal spaces, render their revolutions unequal; from this the rule is derived, namely,

Multiply the velocity of the driver by the number of teeth it contains, and divide by the velocity of the driven: the quotient will be the number of teeth it ought to contain. Or, multiply the velocity of the driver by its diameter, and divide by the velocity of the driven: the quotient will be the diameter of the driven.

If the velocities of driver and driven are given with the distance

of their centres,

Then the sum of the velocities: { velocity of driver } :: distance

of centres: { radius of driven. radius of driver.

EXAMPLE 1. If a wheel that contains 75 teeth makes 16 revolutions per minute, required the number of teeth in another to work in it, and make 24 revolutions in the same time.

Here 
$$\frac{75 \times 16}{24}$$
 = 50 teeth. = Ans.

Example 2. A wheel, 64 inches diameter, and making 42 revolutions per minute, is to give motion to a shaft at the rate of 77 revolutions in the same time; required the diameter of a wheel suitable for that purpose.

Here 
$$\frac{64 \times 42}{77}$$
 = 34.9 inches. = Ans.

EXAMPLE 3. Required the number of revolutions per minute made by a wheel or pulley 20 inches diameter, when driven by another of 4 feet diameter, and making 46 revolutions per minute.

Here 
$$\frac{48 \times 46}{20} = 110.4$$
 revolutions. = Ans.

EXAMPLE 4. A shaft, at the rate of 22 revolutions per minute, is' to give motion, by a pair of wheels, to another shaft at the rate of 15½; the distance of the shafts from centre to centre is 45½ inches; the diameters of the wheels at the pitch lines are required.

Here 
$$22 + 15.5 : 22 :: 45.5 in. : \frac{22 \times 45.5}{22 + 15.5} = 26.69 in.$$

the radius of the driven wheel; which, doubled, gives 53:38 inches, the diameter.=1st Ans.

Therefore 45.5 inches - 26.69 inches = 1881 inches, the radius of the driver; which, doubled, gives 37.62 inches, the diameter = 2d Ans.

Example 5. Suppose a drum to make 20 revolutions per minute, required the diameter of another to make 58 revolutions in the same time.

Here  $58 \div 20 = 2.9$ , that is, their diameters must be as 2.9 to 1; thus, if the one making 20 revolutions be called 30 inches, the other will be  $30 \div 2.9 = 10.345$  inches diameter.

EXAMPLE 6. Required the diameter of a pulley, to make 12½ revolutions in the same time as one of 32 inches making 26.

Here 
$$\frac{32 \times 26}{12.5}$$
 = 66.56 inches diameter.

EXAMPLE 7. A shaft, at the rate of 16 revolutions per minute, is to give motion to a piece of machinery, at the rate of 81 revolutions in the same time; the motion is to be communicated by means of two gearing wheels and two pulleys, with an intermediate shaft; the driving wheel contains 54 teeth, and the driving pulley on the axis of the driven wheel is 25 inches diameter; required the number of teeth in the other wheel, and the diameter of the other pulley.

Let the driven wheel have a velocity of 36, a mean proportional

between the extreme velocities 16 and 81;

then,  $\frac{16 \times 54}{36} = 24$ , the number of teeth in the driven wheel.=

And  $\frac{36 \times 25}{81} = 11.11$  inches, diameter of the driven pulley.=

2d Ans.

EXAMPLE 8. Suppose in the last example the revolutions of one of the wheels to be given, the number of teeth in both, and likewise the diameter of each pulley, to find the revolutions of the last pulley.

Here 
$$\frac{16 \times 54}{24} = 36$$
, velocity of the intermediate shaft.=Ans.

Also, 
$$\frac{36 \times 25}{11 \cdot 11} = 81$$
, the velocity of the machine.

Gold Lustre for Stone-ware.—Gold, 6 parts; aqua regia, 36 parts. Dissolve: then add, tin, 1 part. Next add balsam of sulphur, 3 parts; oil of turpentine, 1 part. Mix gradually in a mortan and rub it in until the mixture becomes hard; then add oil of turpentine, 4 parts. It is then ready to be applied to a ground prepared for the purpose.

To Petrify Wood, &c.—Take equal quantities of gem-salt, rock-alum, white vinegar, chalk, and pebbles powdered. Mix all these ingredients: there will happen an ebullition. If, after it is over, you throw into this liquor any porous matter, and leave it there soaking four or five days, they will positively turn into petrifactions.

# STEAM POWER AND THE STEAM-ENGINE.

STEAM is of great utility as a productive source of motive power; in this respect, its properties are-elastic force, expansive force. and reduction by condensation. Elastic signifies the whole urgency or power the steam is capable of exerting with undiminished effect. By expansive force is generally understood the amount of diminishing effect of the steam on the piston of a steam-engine, reckoning from that point of the stroke where the steam of uniform elastic force is cut off : but it is more properly the force which steam is capable of exerting, when expanded to a known number of times its original bulk. And condensation, here understood, is the abstraction or reduction of heat by another body, and consequently not properly a contained property of the steam, but an effect produced by combined agency, in which steam is the principal; because any colder body will extract the heat and produce condensation, but steam cannot be so beneficially replaced by any other fluid capable of maintaining equal results.

The rules formed by experimenters, as corresponding with the results of their experiments on the elastic force of steam at given temperatures vary, but approximate so closely, that the following rule, because of being simple, may in practice be taken in prefer-

ence to any other:

RULE. To the temperature of the steam, in degrees of Fahrenheit, add 100; divide the sum by 177; and the 6th power of the quotient will equal the force in inches of mercury.

EXAMPLE. Required the force of steam corresponding to a tem-

perature of 312°.

$$\frac{312 + 100}{177}$$
 = 232776 = 159 inches of mercury.

To Estimate the Amount of Advantage Gained by Using Steam Expansively in a Steam-Engine.

When steam of a uniform elastic force is employed throughout the whole ascent or descent of the piston, the amount of effect produced is as the quantity of steam expended. But let the steam be shut off at any portion of the stroke—say, for instance, at one half—it expands by degrees until the termination of the stroke, and then exerts half its original force; hence an accumulation of effect in proportion to the quantity of steam.

RULE. Divide the length of the stroke by the distance or space into which the dense steam is admitted, and find the hyperbolic logarithm of the quotient, to which add 1; and the sum is the ratio

of the gain.

Example. Suppose an engine with a stroke of 6 feet, and the

steam cut off when the piston has moved through 2; required the ratio of gain by uniform and expansive force

 $6 \div 2 = 3$ ; hyperbolic logarithm of 3 = 1.0986 + 1 = 2.0986, ratio of effect; that is, supposing the whole effect of the steam to be 3, the effect by the steam being cut off at  $\frac{1}{3} = 2.0986$ .

Again, let the greatest elastic force of steam in the cylinder of an engine equal 48 lbs. per square inch, and let it be cut off from entering the cylinder when the piston has moved 4½ inches, the whole stroke being 18; required an equivalent force of the steam throughout the whole stroke.

 $18 \div 4.5 = 4$ , and  $48 \div 4 = 12$ . Logarithm of 4 + 1 = 2.38629. Then  $2.38629 \times 12 = 28.635$  lbs. per square inch.

In regard to the other case of expansion, when the temperature is constant, the bulk is inversely as the pressure; thus, suppose steam at 30 lbs. per square inch, required its bulk to that of original bulk, when expanded so as to retain a pressure equal to that of the atmosphere, or 15 lbs.

 $\frac{15+30}{15} = 3 \text{ times its original bulk.}$ 

It is because of the latent heat in steam, or water in an aëriform state, that it becomes of such essential service in heating, boiling, drying, &c. In the heating of buildings, its economy, efficiency, and simplicity of application are alike acknowledged; the steam being simply conducted through all the departments by pipes, by extent of circulation condenses—the latent heat being thus given to the pipes, and diffused by radiation. In boiling, its efficiency is considerably increased, if advantage be taken of sufficiently inclosing the fluid, and reducing the pressure on its surface, by means of an air-pump. Thus, water in a vacuum boils at about a temperature of 98°; and in sugar refining, where such means are employed, the syrup is boiled at 150°.

The latent heat of steam at the common pressure of the atmosphere, according to very accurate experiments, is found to be 1000°; and we know that the sensible, or thermometric heat = 212°. Now 212° - 32° = 180°, and 1000° + 180° = 1180°; therefore, steam at 212° is simply highly rarified water, and contains 1180° of heat; hence, to find the latent heat of steam at any other temperature, subtract the sensible heat from 1180°, and add 32° =

the latent heat.

EXAMPLE. Required the latent heat of steam whose sensible heat is 224°.

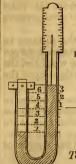
 $1180^{\circ} - 224^{\circ} = 956^{\circ}$ , And  $956^{\circ} + 32^{\circ} = 988^{\circ}$  latent heat.

A cubic inch of water produces about 1700 cubic inches of steam

at 212°, or the common pressure of the atmosphere; but the boiling point varies considerably with the pressure on the surface of the fluid; thus, in a vacuum, water boils at about 90°; under common pressure, at 212°; and when pressed with a column of mercury 4 inches in height, at 216°; each inch of mercury producing by its pressure a rise of about 1° in the thermometer.

The pressure or force of steam in the boiler (less than the weight upon the safety-valve) is generally indicated by a column of mercury in a bent iron tube, which causes the range of the float to be only half the range of the mercury, 2 inches of mercury being

nearly equal to 1 lb. pressure of steam in the boiler, thus:

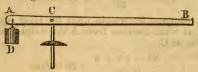


Each inch rise of the float indicates a pressure of nearly 1 lb.

-Level of the mercury when there is no force of steam above the pressure of the atmosphere.

To Calculate the Effect of a Lever and Weight upon the Safety-Valve of a Steam-Boiler, &c.

The lever, under all circumstances, is balanced by a known weight or weights, on the short end, making its point of rest on the valve the centre of motion; so that the weight, added to that of the lever, is the effective weight upon the valve, independent of any other additional weight, thus:



There are three different ways that it may be required to calculate the lever:

1. When a certain pressure is required upon the valve, the distance of the weight upon the lever, and the distance of the valve from the centre of motion given, to find what weight will be required upon the lever at that distance,

From the pressure on the valve in lbs. subtract the weight of the valve in lbs. and the effective weight of the lever, multiply the remainder by the distance between the fulcrum and the valve, and divide the product by the distance between the fulcrum and the

weight, and the quotient is the weight in lbs. required to be placed upon the lever at that distance.

2. When a certain pressure is required upon the valve, the weight upon the lever and distance of the valve from the centre of motion

given, to find where that weight must be placed.

From the required weight upon the valve in lbs. take the weight of the valve, add the effective weight of the lever, multiply the remainder by the distance between the fulcrum and the valve, and divide the product by the weight in lbs. upon the lever, and the quotient is the distance in inches from the fulcrum that the weight must be placed.

3. When the distance of weight, distance of valve from the centre of motion, and weight upon the lever are given, to find what pressure

is upon that valve.

Multiply the weight in lbs. upon the lever by the distance in inches to the fulcrum, divide the product by the distance between the fulcrum and the valve, and the quotient, plus the weight of the valve and effective weight of the lever, equal the weight upon the valve in lbs.

EXAMPLE 1. Suppose the lever AB (as above) to be 24 inches in length, and the valve C placed 5 inches from the centre of motion A, what weight must be placed upon the lever 20 inches from A, to equal 80 lbs., on the valve C, the weight of the lever being 2 lbs., the weight D, which balances the lever,  $4\frac{1}{2}$  lbs., and the weight of the valve 3 lbs.?

2 lbs. weight of the lever.
4.5 " to balance ditto.
3 " weight of the valve.

9.5 lbs.

Then 
$$\frac{\overline{80 - 9.5} \times 5}{20} = 17.625$$
 lbs.

EXAMPLE 2. Suppose the weight upon the lever equal 17.625 lbs., it is required at what distance from A the weight must be placed to equal 80 lbs. at C.

$$\frac{80 - 9.5 \times 5}{17.625} = 20$$
 inches.

EXAMPLE 3. Suppose, as before, that a weight of 17.625 lbs. is placed upon the lever 20 inches from A, required the pressure at C, the distance from the centre of motion being 5 inches, and the effective weight of the lever at that point equal 6½ lbs., also the weight of the valve 3 lbs.

$$\frac{17.625 \times 20}{5} = 70.5 \\
+ 6.5 \\
+ 3 \\
= 80 \text{ lbs.}$$

# To Find the Proper Diameter for a Safety-Valve.

Multiply the bottom surface of the boiler, or surface immediately exposed to the action of the fire, in feet, by the multiplier opposite to the pressure in lbs. on each square inch of the safety-valve, and the square root of the product is the valve's diameter in inches at the narrowest part. If the boiler is to have two safety-valves, then the square root of half the product equal the diameter of each.

Pressure in lbs. per square inch.	Multipliers.	Pressure in lbs. per square inch.	Multipliers.
4		15 20 25	
6	'344	30	
8		40	
12		50	

In constructing steam-engines, the following simple rule for obtaining the nominal horse power is now generally adopted:

The area of the cylinder in square inches multiplied by 7 lbs. pressure, multiplied into the speed of the piston in feet per minute, divided by 33000, equal the nominal horse power.

Thus, area of cylinder  $\times 7$  lbs.  $\times$  feet per minute = nominal H. P. 33000

The length of stroke and relative speed of piston, and number of revolutions per minute, will be found by the following table. In calculating the gross horse power developed in any cylinder, as shown by the *indicator*, it has been customary to allow one-tenth, and sometimes one-eighth, for friction; this is now very properly abandoned, and the following rule for calculating the indicator diagram should be always adopted: the mean pressure as shown on the eard, multiplied into the area of the cylinder, multiplied into the speed of piston, in feet per minute, when the card was taken; this product, divided by 33000, will give the gross or indicated horse power:

ft.	in.	11/00/12	2 39	A Troumont	Thin it	more day.		ft.	60		- 42
				revolutions	per	minute			per	mı	nute.
3	6		$\frac{27}{24\frac{1}{3}}$					189 196		46	
4	6		223					204		66	
5	0		21	Wi 1 10 0 16	•			210	bank	66	
5	6	44 -	191				#	216		66	
6	0	68	181					222		66	
6	6	"	17 1					226		66	
7	0	66	$16\frac{1}{2}$					231		46	
7 8	6	"	15 to 15	5 Tues de let		me ken		236 240	275	66	ambou
1170 870	6	6	14,	6	No.			244	9. 7	66	111
J 102 914	0	66	133		often			247	2.10	66	pared)
			- 3								

The Air-Pump. The diameter of the air-pump should be a little more than half the diameter of the cylinder, or the diameter of the cylinder in inches multiplied by 6 will give the diameter of the air-pump in inches, the length of stroke to be one-half the length of stroke of the piston.

The Condenser should never be less than half the capacity of the cylinder; and in engines where the pressure on the boiler ranges from twelve to twenty pounds on the square inch, a much larger condenser should be given.

The foot and delivery-valve passages should have an area of one-

third of the air-pump.

The Steam-Ports. The area of the steam-ports on the cylinder should never be less than one-twentieth of the area of the cylinder. If the speed of the piston is above 250 feet per minute, the ports should never be less than one-fourteenth the area of the cylinders.

The Cold-Water Pump. The capacity of the cold-water pump should be not less than one-thirty-sixth of the capacity of the cylinder.

The Fly-Wheel. To find the weight of the fly-wheel rim the

following practical rule is generally adopted:

Horse power of the engine × 2000

(velocity of circumference of wheel in feet per second) 2 the weight of the fly-wheel in cwts.

The Fly-Wheel, or Crank-Shaft. The nominal horse power of the engine and speed of the shaft being given, the diameter of this shaft, whether cast or wrought iron, will be found in the Tables of Strength of Shafts.

The Governor. To find the number of revolutions, divide 375 by the square root of the length of the pendulum; half of this quotient is the number of revolutions the balls ought to make per minute.

To find the length of the pendulum, divide 375 by twice the number of revolutions; the quotient squared is the length of the pendulum.

General Proportions of Locomotive Engines.

For the area of the steam-ports when the stroke is 18 inches, the square of the diameter of the cylinder  $\times$  068 = the area in square inches.

For the area of the eduction ports, the square of the diameter of the cylinder in inches  $\times$  128 = the area in square inches.

The breadth of the bridges between the eduction ports and the induction  $= \frac{3}{4}$  inch and 1 inch.

The diameter of the chimney = the diameter of the cylinder.

For the area of the fire-grate, the diameter of the cylinder in inches × '77 = the area in superficial feet.

For the effective heating-surface of the boiler, the square of the diameter of the cylinder in inches  $\times$  5  $\div$  2 = area in square feet.

For the diameter of the feed-pump ram, the square of the diameter of the cylinder in inches × 011 = the diameter in inches.

For the cubical content of the steam-room, the square of the diameter of the cylinder in inches × 9÷40=content in cubic feet.

For the cubical content of inside fire-box above fire-bars, the square of the diameter of the cylinder in inches +4=content in cubic feet.

For the inside diameter of the steam-pipe, the square of the diameter of the cylinder in inches  $\times$  '03 = the diameter in inches.

For the diameter of the branch steam-pipe, the square of the diameter of the cylinder in inches × 021 = the diameter in inches.

For the diameter of the top of the blast-pipe, the square of the diameter of the cylinder in inches × 017 = the diameter in inches.

For the diameter of the feed-pipes, the diameter of the cylinder in inches × 141 = the diameter in inches.

For the diameter of the piston-rod, the diameter of the cylinder in inches  $\div$  7 = the diameter in inches.

For the thickness of the piston, the diameter of the cylinder in inches  $\times 2 \div 7$  = the thickness in inches.

For the diameter of the connecting-rod at the middle, the diameter of the cylinder in inches  $\times$  '21 = the diameter in inches.

For the diameter of the plain part and inside bearing of the crankaxle, the cube root of the square of the diameter of the cylinder in inches × '96 = the diameter in inches.

For the diameter of the outside bearings of the crank for axle, the cube root of the product of the square of the diameter of the cylinders in inches × 396 = the diameter in inches.

For the diameter of the crank-bearing, the diameter of the cylinder in inches × 404 = the diameter in inches.

For the length of the crank-bearing, the diameter of the cylinder in inches × 233 = the length in inches.

### Remarks on Steam-Engine Boilers and their Proportions.

For engines designed to give a gross indicator horse power of at least twice the nominal horse power, the grate surface should be '66 or '69 square feet per nominal horse power, but may be increased to '75 square feet, and should never be diminished to less than '60 square feet as a minimum.

The area of opening over the bridges or through the tubes, should be 125 square feet, or 18 square inches per horse power, and may be increased to 143 square feet, or 20 square inches with advantage, particularly in tubular boilers, and should never be diminished to less than 15 square inches, or 109 square feet per horse power.

The area of chimney should be '076 square feet, or 11 square inches, but may be increased to 13 square inches, and should never be diminished to less than 10 square inches per horse power.

The heating surface in fire-places and flues should be 14 square feet per horse power, exclusive of all bottom surface, but may be increased to 15 square feet, and should never be diminished to less than 12 square feet per horse power.

In calculating tubular boilers the whole surface of the tubes should be taken, and there should be a total of 17 square feet per

horse power in the fire-places and tubes.

In engines designed to work to a gross power in the cylinder by the indicator greater than twice the nominal horse power, these proportions must be increased; or, if the reverse be intended, they may be diminished in proportion.

Of the Pressure of Steam, in Inches of Mercury, at Different Temperatures.

	1		,		the same of
I. Temperature.	II.	III.	IV.	v.	VI.
Fahrenheit.	Dalton.	Ure.	Young.	Macneill.	Tredgold.
WILLIAM IN THE	J , Million III	11 7 11	of the same of	1.30 150-20	STREET
0.0	0.00	The state of	10 10 11	77 1 81 75	South to be
0°	0.08	2 17 44		The section	Section 2
10	0.12		0.77	"A David	town the sta-
20	0.17	0.00	0.11		0.15
32	0.26	0.20	0.18		0.17
40	0.34	0.25	0.20		0.24
50	0.49	0.36	0.36	0.36	0.37
60	0.65	0.52	0.53		0.55
70	0.87	0.73	0.75	0.73	0.78
80	1.16	1.01	1.05	1000	1:11
90	1.59	1.36	1.44	1.36	1.53
100	2.12	1.86	1.95	will be the	2.08
110	2.79	2.45	2.62	2.46	2.79
120	3.63	3.30	3.46	F 255 FT	3.68
130	4.71	4.37	4.54	4.41	4.81
140	6.02	5.78	5.88	- march 188	6.21
150	7.73	7.53	7.55	7.42	7.94
160	9.79	9.60	9.62	Law Links	10.05
170	12.31	12.05	12.14	12.05	12.60
180	15.38	15.16	15.23	1 12 700	15.67
190	18.98	19.00	18.96	18.93	19.00
200	23.21	23.60	23.44	2	23.71
210	28.82	28.88	28.81	28.81	28.86
212	30.00	30.00	30.00	30.00	30.00
220	35.18	35.54	35.19	201 2010	34.92
230	44.60	43.10	42.27	42.63	42.00
240	53.45	51.70	51.66		50.24
		- and and		I was a second	

Of the Temperature of Steam at different Pressures in Atmospheres.

I. Temperature	II.	III.	IV.	· v.	VI.
Fahrenheit.	French Acad.	Dr. Ure.	Young.	Macneill.	Tredgold.
79.45		1 3/			
1st At.	212·0°	212°	212°	212°	212°
2d "	250.5	250.0	240.3	249	250.+
3d "	275.2	275.0	271		274.+
4th "	293.7	291.5	288	290	294.+
5th "	308.8	304.5	302		309.+
6th "	320.4	315.5	2000		322.—
7th "	331.7	325.5	0.000	- 1 A A	
8th "	342.0	336.0	2011-0	337	342. +
9th "	350.0	345	1007		
10th "	358.9		1000		
11th "	366.8		3100		104
12th "	374.0		2003	17.00	372.—
13th "	380.6		1705	0 1 year	
14th "	386.9	111	me.	- V 1 (-	
15th "	392.8	L 92	11		
10011	398.5		Thorn a	11/2 100	
1 ( 011	403.8	m1 2mm	700	THE APP	
10011	408.9	EI	100	1912	
19th " 20th "	418.5		1100	1122 111	414.
30th "	418.5	17		A72	414
40th "	466.6	100	200	1242	
50th "	510.6	07 00	100	115 115	
90011	310 0	77 77		100	
			21	- P. L. V.	

To Prevent Spontaneous Combustion .- It is a fact better ascertained than accounted for, that fixed oils, when mixed with any light kind of charcoal, or substances containing carbon, such as cotton, flax, or even wool, which is not of itself inflammable, heat by the process of decomposition, and after remaining in contact some time, at length burst into flame. This spontaneous combustion takes place in waste cotton which has been employed to wipe machines, and then thrown away and allowed to accumulate into a We have known an instance of the kind in a manufactory for spinning worsteds, where the waste wool, or "slubbings," as it is termed in Yorkshire, was thrown into a corner and neglected. It then heated, and was on the point of bursting into flame, when the attention of the workmen was directed to the heap by the smoke and smell. In cotton mills the danger exists in a still greater degree, and it is believed that the destruction of many cotton factories has been occasioned by this means. The cause of this peculiar property of fixed oils deserves more attention than has hitherto been paid to it.

TABLE

Of the Elastic Force of Steam, and Corresponding Temperature of the Water with which it is in Contact.

Pressure on a SquareInch.	of	t. of	l cha	h.a	lastic Force in Inches of Mercury.	emperature in degrees of Fahrenheit.	l ethe		
on	Force thes of try.	tur	com- with	Ing	orc es y.	tur	com- with lume er.		
ire are	neh	era sgre ren	Vat Vat	are are	P. F.	era	Vat Vat		
Pressure on SquareIncl	Elastic Force in Inches of Mercury.	Temperature in degrees of Fahrenheit,	Steam com- pared with the Volume of Water.	Pressure on a Square Inch.	Elastic Force in Inches of Mercury.	Temperature in degrees Fahrenheit.	Volume of Steam compared with the Volume of Water.		
Pre	Ela	Tei	200 02 0	Pre	Ela	Tei	S and o		
-		121	32	-27		15	100		
lbs. 14.7	30.00	212.0	1700	lbs. 49	99.96	001.0	564		
15	30.60	212.8	1669	50	102.00	281.9	554		
16	32.64	216.3	1573	51	102 00	283·2 284·4	544		
16 17	34.68	219.6	1488	52	106.08	285.7	534		
18	36.72	222.7	1411	53	108.12	286.9	525		
19	38.76	225.6	1343	54	110.16	288.1	516		
20	40.80	228.5	1281	55	112.20	289 3	508		
21	42.84	231.2	1225	56	114.24	290.5	500		
22	44.88	233.8	1174	57	116.28	291.7	492		
23	46.92	236.3	1127	58	118.32	292.9	484		
24	48.96	238.7	1084	59	120.36	294 2	477		
25	51.00	241.0	1044	60	122.40	295.6	470		
26	53.04	243.3	1007	61	124.44	296.9	463		
27	55.08	245.5	973	62	126.48	298.1	456		
28	57.12	247.6	941	63	128.52	299.2	449		
29	59.16	249.6	911	64	130.56	300.3	443		
30	61:21	251.6	883	65	132.60	301.3	437		
31	63.24	253.6	857	66	134.64	302.4	431		
32	65.28	255.2	833	67	136.68	303.4	425		
33	67.32	257.3	810.	68	138.72	304.4	419		
34	69.36	259.1	788	69	140.76	305.4	414		
35	71.40	260.9	767	70	142.80	306.4	408		
36	73.44	262.6	748	71	144.84	307.4	403		
37	75.48	264.3	729	72	146.88	308.4	398		
- 38	77.52	265.9	712	73	148.92	309.3	393		
39	79.56	267.5	695	74	150.96	310.3	388		
40	81.60	269.1	679	75	153.02	311.2	383		
41	83.64	270.6	664	76	155.06	312.2	379		
42	85.68	272.1	649	77	157.10	313.1	374		
43	87.72	273.6	635	78	159.14	314.0	370		
44	89.76	275.0	622	79	161.18	314.9	366		
45	91.80	276.4	610	80	163.22	315.8	362		
46	93.84	277.8	598	81	165.26	316.7	358		
47	95.88	279 2	586	82	167.30	317.6	354		
48	97.92	280.5	575	83	169.34	318.4	350		
In Designation		100		1	THE PERSON	-			
					THE RESERVE TO SHARE THE PARTY NAMED IN				

<sup>\*</sup> This includes the pressure of the atmosphere.

TABLE—(Continued).

Pressure on a Square Inch.	Elastic Force in Inches of Mercury.	Temperature in degrees of Fahrenheit.	Volume of Steam compared with the Volume of Water.	Pressure on a Square Inch.	Elastic Force in Inches of Mercury.	Temperature in degrees of Fahrenheit.	Volume of Steam compared with the Volume of Water.			
1bs. 84 85 86 87 88 89 90 91 92 93 94	171·38 173·42 175·46 177·50 179·54 181·58 183·62 185·66 187·70 189·74 191·78 193·82	319·3 320·1 321·0 321·8 322·6 323·5 324·3 325·1 325·9 326·7 327·5 328·2	346 342 339 335 332 328 325 322 319 316 313 310	lbs. 98 99 100 110 120 130 140 150 160 170 180	199·92 201·96 204·01 224·40 244·82 265·23 285·61 306·03 326·42 346·80 367·25 387·61	330·5 331·3 332·0 339·2 345·8 352·1 357·9 363·4 368·7 373·6 378·4 382·9	301 298 295 271 251 233 218 205 193 183 174 166			
96 97	195·86 197·90	329·0 329·8	307 304	200	408.04	387.3	158			

TABLE

Of the Force and Temperature of Steam in Atmospheres.

Atmos.	Temp. Fah.	Atmos.	Temp. Fah.	Atmos.	Temp. Fah.
1 1 1 1 7	Deg. 212:00	10	Deg. 358.88	19	Deg. 413:78
2	250 52	11	366.85	20	418.46
3 4	275·18 293·72	12 13	374·00 380·66	$\begin{array}{c c} 21 \\ 22 \end{array}$	422.96
5 6	307·50 320·36	14 15	386·94 392·86	23 24	431·42 435·56
7 8	331·70 341·78	16 17	398·48 403·82	25	439:34
9	350.78	18	408.92	50	510.60

To write on Silver with a Black which will never go off.— Take burnt lead and pulverize it. Incorporate it next with sulphur and vinegar, to the consistency of a painting color, and write with it on any silver plate. Let it dry, then present it to the fire so as to heat the work a little, and it is finished.

#### TABLE

Of the Heating Power of various Combustible Substances, exhibiting the utmost Quantity of Water evaporated by the Given Weights, and the smallest Quantity of Air capable of producing Total Combustion.

Species of Combustible.	Pounds of Water which a Pound can heat, from 0° to 212°	Pounds of Boiling Water evaporated by 1 Pound.	Weight of Atmospheric air at 32°, to burn 1 Pound.
Wood, in its ordinary state, .	26	4.72	4.47
Wood charcoal,	73	13.37	11.46
Pit coal,	60	10.90	9.26
Coke,	65	11.81	11.46
Turf,	30	5.45	4.60
Turf charcoal,	64	11.63	9.86
Carburetted hydrogen, Oil,	76	13.81	14:58
Wax,	78	14.18	15.00
Alcohol of commerce,	52	9.56	11.60

To Estimate Distance.—Observe how many seconds elapse between a flash of lightning and the thunder, and multiply them by 1142, the number of feet sound travels in a second, the product will be the distance in feet. The same process may be applied to the flash and report of a gun, or any other sound, provided we can ascertain the time at which it is produced, and the interval that elapses before it reaches the ear.

Illustration. Saw a flash of lightning five seconds before I heard the thunder: required the distance.

$$\frac{5 \times 1142}{3 \times 1760} = \frac{43}{1528}$$
 mile distant.

In the absence of a watch, the pulsations at the wrist may be counted as seconds, by deducting one from every seven or eight.

PRISMATIC DIAMOND CRYSTALS FOR WINDOWS.—A hot solution of sulphate of magnesia, and a clear solution of gum arabic, mixed together. Lay it on hot. For a margin or for figures, wipe off the part you wish to remain clear with a wet towel.

PERFECTLY BLACK HARD GLASS.—Plain paste, 600 parts; zaffre, 3 parts; manganese, 3 parts; iron, 3 parts.

TABLE

# Of Nominal Horse Power of Low Pressure Engines.

der in Inches.	LENGTH OF STROKE IN FEET.												
de	1	1½	2	2½	3 .	31/2	4	41/2	5	51/2	6	7	
4	*34	*39	. 43	146	149	*52	*54	'56	'58	*60	*62		
5	·53	'61 '87	*67 *96	1.04	76 110	1.16	1.22	1.26	1.31	1'35	*96 1*39	1'	
7	1.04	1.19	1'31	1'41	1.20	1'58	1'65	1.72	1.78	1'84	1.89	1	
8	1.36	1 56	1.72	1.85	1.96	2'07	2'16	2.25	2.33	2'40	2.47	2	
10	1.72 2.13	1.97 2.44	2'17	2.34	2.49 3.08	2.62 3.53	2.74 3.38	2'84 3'51	3'64	3 04	3·13 3·87	3	
11	2.57	2.95	3'24	3'49	3.77	3.91	4'15	4 25	4'40	4'54	4.68	4	
12	3.06	3.21	3.86	4'16	4'42	4 65	4.86	5'06	5'24	5'41	5.57	5	
13 14	3.60 4.14	4 12 4 77	4'53 5'25	4 '88 5 '66	5'19 6'01	5°46 6°33	5'64 6'62	5'94 6'88	6°15 7°13	6°35 7°36	6°53 7°58	6 7	
15	4.77	5.48	6.03	6.20	6.90	7'27	7.60	7'90	8'19	8.45	8.70	9	
16	5'45	6'23	6.86	7'39	7'86	8.52	8.62	8.88	9.31	9 61	9.90	10	
17	6.12	7'04	7.75 8.68	8'35 9'36	8'86 9'94	9°34 10°47	9'76 10'94	10°15 1°38	10.52	10'85 12'17	11'17 12'53	11	
18	7.68	8.79	9.63	10.42	11.14	11.66	12.19	12.68	13.13	13.56	13.96	14	
20	8.21	9'74	10.72	11'55	12.27	12.92	13'51	14 05	14'55	15'02	15'46	16	
22	10:30	11.79	12'97 15'44	13'98 16 63	14.85 17.67	15.63	16'62 19'45	17:30	17.65 20.95	18'18	18'71	19	
24 26	12°26 14°39	14'03	18.15	19.52	20.75	21.84	22 56	20'23	24 68	25 39	22°27 26°14	23 27	
28	16'68	16.46 19.09	21'02	22'64	24'06	25.33	26'48	27'54	28'52	29'41	30.31	31	
30	19'15	21.92	24'13	25.99	27.62	29.07	30.40	31.61	32.74	33 80	34*80	36	
32	21.79	24'96	27'51	29'57 33'39	31 42 35 44	33.08	34'59	35°97 40°60	37'26 42'06	38'46 43'41	39°59 44°69	41	
36	27 57	31'56	34.74	37'42	39.77	41'87	43.77	45 52	47.15	48.67	50.11	52	
38	30'72	35.17	38'71	41'69	44'66	46 64	48.77	50.72	52'54	54'23	55.83	58	
40	34 04 37 53	39'97 42'96	42'89	46°20 50°94	49'10 54'13	51'69 56'98	54.04 59.58	56'20 61'96	58'21 64'18	60°09 66°25	61'88 69'21	65 71	
44	41'19	47.15	51.90	55.91	59.38	62 54	66.46	68.00	70.44	72.71	74'85	78	
46	45 02	51'54	56'72	61'10	64'88	68'19	71'43	74.33	76'69	79*47	81 81	86	
48	49 02 53 19	56.11	61'76	66 54 72 19	70.70 76.71	74.42	77'82 84'44	80°94 87°82	90.83 83.83	86 53 93 89	89°08 96°65	93	
50 52	57'55	65.86	72'48	78.08	83.00	87.35	90.52	94'98	98'40	101.22	104.2	110	
54	62'04	71'02	78'17	84.50	89'48	94'20	98'49	102.4	106'1	109'5	1127	118	
56	66'72	76:38	84.07	90.55	96.53	101.30	105.9	110.1	114'1	117'8	121.2	127	
58 60	71'59	81'93 87'68	90'18	97°14 103°9	103.2	108 6	113'6 121'6	118'2	122'4 131'0	126 3 135 2	129°2	136 146	
62	81 79	93.62	103'04	111.0	117'96	124'18	129'81	135.03	139.86	144 37	148'6	156	
64	87 15	99'84	110.0	118.3	125.7	132'3	138°3 147°3	143.9	149'0	153'82	158.4	166	
66 68	92'68	106'1	116.8	125'8 133'6	133.6 141.8	140'7 149'4	147'3 156'2	153 0 162'4	158'5 168'2	163'6 173'6	168'4 178'8	177 188	
70	104.26	119.3	131.3	141.2	150.4	158 3	165.2	172.1	178.2	184.0	189'4	199	
72	110:30	126.5	139'0	149 7	159'1	167'4 176'7	175'1	182'1	188'6	194'7	200'4	211	
74	116.2	133.4	146.8 154'8	158·1 166·8	167'9	176'7	185.4	192'4	199'2	205'7 216'9	211'6 223'3	223 235	
78	129.4	148.2	163.1	175.6	178'6 186'7	186'6 196'5	195°0 205°4	202.9	210.1	218 9	235.3	247	
80	136'2	155'8	171 6	184'8	196'4	206.7	216.1	224.8	232.8	240'4	247.4	260	
82	143:0	163.8	180'2	194'2	206.2	217'3	226'9	237'8	244 6	252.5	260'0	273	
84	150°1 157°4	171'8 180'I	189'1	203.8	216.5 227.0	227'9	238'3	247'8	256'7 269'1	265.0	272'8 286'0	287	
88	164'8	188 6	207'6	223'6	237.5	250.5	261 6	272.0	281.7	290.8	299'4	315	
90	172'3	197'3	217'1	233.9	248'6	261.7	273.6	294'5	291'7	304'2	313.5	329	

TABLE.

Of Nominal Horse Power of High Pressure Engines.

Diam. of Cylin- der in Inches.	LENGTH OF STROKE IN FEET.											
Dian	1	11/2	2	21/2	. 3	3½	4	4½	5	51/2	6	7
2 2½ 3 3½ 4 4½ 5 5½ 6 6½ 7 7½ 8 8½ 9 ½ 10 0½ 11½ 11½ 13 13 14½ 14½ 15 16 17 18 19 20	25 39 577 78 1 02 1 29 1 159 1 159 2 28 2 69 3 160 4 05 5 76 6 39 7 77 1 18 43 9 96 6 6 39 9 11 16 35 1 16 35	299 145 65 65 89 117 148 3221 309 261 309 57 4111 468 59 1140 11332 1140 11536 11332 1140 11536 11431 1536 11431 1536 11431	32 520 520 520 1 29 1 63 3 29 3 39 3 4 53 5 16 6 51 1 2 57 1 1 58 9 72 1 1 58 9 1 2 57 1 1 69 2 2 3 2 58 2 3 2 58 2 3 2 58 3 3 2 58 3 3 2 58 4 53 5 1 6 6 51 1 5 7 5 1 6 7 5 1 6 7 5 1 6 9 2 1 6 7 5 1 7 5 1 8 2 5 1 8	355 544 788 1 106 61 78 78 78 78 78 78 78 78 78 78 78 78 78	37, 183, 113, 147, 186, 6, 187, 187, 187, 187, 187, 187, 187, 187	38 8 60 96 96 96 97 86 68 97 86 68 99 97 86 68 91 17 38 17 3	400 633 911 1 24 1 62 2 05 2 25 2 25 2 312 2 52 3 12 2 6 4 23 4 95 6 4 8 22 9 10 11 16 16 16 18 18 18 18 18 18 18 18 18 18 18 18 18	'42' 666 955 129 168 2113 378 414 45 57 46 25 11 10 53 11 12 75 11 11 12 75 11 16 47 72 11 12 75 11 16 47 72 17 30 45 11 12 75 11 10 53 11 10 10 53 11 10 10 53 11 10 10 53 11	44 68 98 134 221 330 36 53 46 22 73 393 46 22 73 393 46 88 55 44 10 92 11 16 17 17 17 18 19 22 19 22 19 22 19 23 23 23 23 24 25 27 27 27 27 27 27 27 27 27 27 27 27 27	'45, '700 1'01  1'38 81 180 2'28 2'82 2'82 3'42; 5'4'75 5'52 4'75 5'52 4'75 5'52 14'91 11'28 813 9'12 2'20 14'91 11'28 21'758 19'12 2'20'08 23 70 25 28'83 93 55 58'85 94'55' 28'85 94'55' 28'85 94'55' 28'85	46 3 4 1 1 4 2 1 1 4 2 1 1 4 2 1 1 4 2 1 1 4 2 1 1 8 6 1 1 1 8 6 1 1 1 8 6 1 1 1 8 6 1 1 1 1	49 76 110 1 195 2 47 1 95 3 66 3 69 9 78 9 78 9 78 1 12 11 1 17 58 1 19 78 2 2 2 6 2 2 2 6 2 2 3 5 2 3 5 3 5 3 5 4 4 4 1 4 4 1 4 5 1 6 6 7 7 8 1 9 7 8 1 9
20 22 24 26 28 30 32 34 36 38 40 42 44 46 50 52 54 56 58 60	25 53 30 90 36 78 43 17 50 045 65 37 73 80 82 71 92 16 102 1 112 6 123 5 135 0 147 0 159 6 172 6 186 1 200 1 201 7 229 8	29:22 \$5:37 49:38 57:27 65:76 74:88 84:43 94'68 105:5 116:9 128:9 141:4 154:6 168:3 182:6 213:0 299:1 245:8	32 16 38 91 46 32 54 36 63 06 72 39 82 53 92 9 104 2 116 1 129 6 141 8 155 7 170 1 185 3 201 0 217 4 234 5 252 2 270 5 289 5	34'65 41'94 49'89 58'56 67'92 77'97' 71'90'22 112'2 125'0 128'6 152'8 167'7 133'3 199'6 216'5 224'2 252'6 271'6 291'4 311'7	36.81 44.55 53.01 62.25 72.18 82.86 94.26 106.3 119.3 134.0 147.3 162.4 178.1 194.6 212.1 230.1 249.0 268.4 288.7 309.6 331.2	38.76 46.89 55.83 65.52 75.99 87.21 112.0 125.6 136.9 155.1 170.9 124.6 223.2 242.3 262.0 282.6 303.9 325.8	40 53 49 86 58 35 67 68 79 44 91 20 103 7 117 113 3 146 3 162 1 178 7 199 4 214 3 233 4 253 3 270 7 340 8 364 8	42:15 51:90 60:69 71:25 82:62 94:83 107:9 121:8 136:5 152:1 168:6 185:9 204:0 223:0 242:8 263:4 284:9 307:2 330:3 354:6 379:2	43:65:52:95 62:85 73:8 85:56 98:22 111:8 126:2 141:4 157:6 174:6 174:6 230 0 230 0 231:5 272:9 295:2 318:3 342:3 367:2 393:0	45 '06 54 '54 64 '89 76 '17 88 '32 10 1 '40 115 '4 130 '2 146 '0 162 7 180 '2 198 '7 218 '1 238 '4 259 '6 328 '5 353 '4 405 '6	46 38 56 13 66 81 78 42 90 93 104 4 118 7 134 0 150 3 167 5 185 6 204 6 224 5 245 4 267 2 289 9 313 5 338 1 363 6 417 6	48'84 59'10 70'32 82'53 95'70 109'9 125'0 141'1 158'2 176'3 125'3 226'3 226'3 236'3 305'1 330'0 356'1 382'8 410 1 439'5

Proportions of Condensing Engines.

r. r.	20 20 38 88	
Diameter of Con- denser.		part k-pin
Opio	10 111 111 111 111 111 111 111 111 111	
Lgth.   = =	- 80 80 84 44 40 10 00 00 00 L L L L 00 00 00   - 40 40 00 00 00 00 00 00 00 00 00 00 00	\$\frac{2}{3}\$ of piston-rods.  od at thinnest feylinder. Cran feylinder.    Common
Dia. Pig.	- 01 51 01 01 01 00 00 00 00 04 44 44 10 10 00 10 10 10 10 10 10 10 10 10 10	iston-rode thinnest ler. Crai
	5 00 00 44 44 00 00 00 00 00 00 00 00 00	For
Dia. Ctrs.	2 3 1 00 00 00 04 44 70 70 70 70 70 70 70 70 70 70 70 70 70	tl tl de
water pum		a of pisto d at thi cylinder.
Dm. of Colc	244250000000000000000000000000000000000	ey ey
Dm. of Hot mater pum	- 04 04 04 09 04 04 04 05 08 08 04 04 04 04 04 04 04 04 04 04 04 04 04	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
bon quinq	1 4 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	le-rods funecting- diameter diameter
Dm. of Air-	= 11 11 11 11 11 11 11 11 11 11 11 11 11	de-rods funecting diameter diameter
Valve-rod.		ne lan
To .meid		Side-rods full # Connecting-rod diameter of diameter of diameter of
Wth. Links	= wine extra cope wine cope cope cope wine coper-   Coper	
	- 1 + 1 + 1 + 1 + 1 + 2 + 2 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3	air-p.
Tek.	च्येक प्रश्नेक व्योक व्योक व्योक व्योक व्यास प्रति सान् व्योच सान् व्याच माळ माळ माळ माळ माळ	ਫ਼
Wih.		Jo
Lgih. L'E	2 91919099000000	dia.
Piston-rod.	<u>                                     </u>	<b>р</b>
to .msid .	= HHHOOOOOOOOOOOOOOO	the
Lgth.   .m :	= 01 01 01 01 02 02 02 02 02 04 44 44 44 45 10   1	10 .
Dia. veig	= 10 20 20 20 20 20 20 20 20 44 44 44 44 10   = 10 40 40 40 40 40 40 40 40 40 40 40 40 40	iron <sub>7</sub> brass coppe
crk. Journal	- 64 9 - 8 8 8 0 0 0 1 0 0 0 4 0 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	iron 17 brass 19 copper
Length of	- : : 4 9 7 8 8 8 9 0 0 1 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1	po
Diam. of crk. journal.	- 4244 66 66 444 84 84 84 84 84 84 84 84 84 84 84 84	Air-pump rod iron " brass " copp
,		EI T
Valves.	X X X X X X X X X X X X X X X X X X X	nd.
100T to szi2	= 100 C C C C C C C C C C C C C C C C C C	á l
	100 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	7
Valves.	二 の	eyl.
Size of Delivering	**************************************	of ""
30 02:5	221 1122 1122 1132 1132 1144 1144 1154 1154 1154 1154 1154 115	ಣೆ
.qranq-riA	1 2 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	e dia.
To shorts		the
Diameter of	2 8 0 11111 11 11 12 12 12 12 12 12 12 12 12	ds=
		= 10 ends
Ports.	X X X X X X X X X X X X X X X X X X X	tr    to
to saiz	2	-rod= head e tre=} centre
	2 4 9 9 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	ston-ro oss-hea centre
Length of	200000000000000000000000000000000000000	
of Cylinder.	rf01 rf01 rf01 rf01   c	
Diameter	= 040041747 00000000000000000000000000000	oth i
Horse, 19wer,	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	". Depth
11	1	7 75

#### TABLE

Of the Revolutions per Mile of Driving Wheels, and Consumption of Steam and Water for each sized Wheel; taking the steam admitted to each cylinder as exactly one cube foot, at a gross pressure of 98lbs. or 83lbs. on the spring balance.

(LES E)	WHEELS.	Cylinder of Steam			
Diameter.	Circumference.	Revolutions per Mile.	per Mile, and Consumption, taking Cylinder at one Cube Foot.	Water per Mile, taking Steam at	
feet.	ft. in.	No.	cube feet.	gallons.	
10	31 5	168	672	14.0	
$9\frac{1}{2}$	29 101	176.9	707.6	14.74	
9	28 31	186.7	746.8	15 55	
81/2	26 83	197.4	789.6	16.44	
8	25 11/2	210.1	840.4	17.5	
71/2	23 634	224	897.6	18.69	
7	21 117	240	960	20.0	
$6\frac{1}{2}$	20 5	258.6	1034	21.5	
6	18 9.18	280.5	1122	23.37	
$5\frac{1}{2}$	17 3.33	305.6	1222.4	25.45	
5	15 8.48	336.3	1344.4	28.0	
41/2	13 11.1	379.0	1493.6	31.11	
4	12 6.92	420.3	1680.4	35.0	
384	11 9.37	441.1	1792.2	37.33	
31/2	10 11.94	480.1	1920.8	40.0	
3	9 5.08	560.2	2240	46:67	
Con al Con					

Note. - As there are two cylinders at work in a locomotive, consequently there are four cylinders of steam for each revolution.

Modelling Wax.—This is made of white wax, which is melted and mixed with lard to make it malleable. In working it, the tools and the board or stone are moistened with water, to prevent its adhering; it may be colored to any desirable tint with dry color.

TABLE
Of Pressure of Steam, exclusive of that of the Atmosphere.

10000	PRESSURE	in Spent		I	PRESSURE	17	31,00
lbs, on the sq. inch	In inches of mercury.	In atmo-	T'empera- ture in de- grees of Fahrenheit	lbs. on the sq. inch.	In inches of mercury.	In atmospheres.	Tempera ture in degrees o Fahrenhe
-	witte.	CHIIII		1111111	11.12		
1	2'04	*068	2130	51	104.04	3*468	3010
2 3	4.08	136	216	52	106.08	3 536	3021/2
4	6°12 8°16	204	219½ 223	53 54	108'12 110'16	3.604 3.622	204 1/2
5	10.50	340	2251/2	55	112.50	3 740	305 %
5 6 7 8	12°24	*408	2281/2	56	114'24	3 808	3061/2
7	14'28	*476	231	57	116'28	3.876	3071/2
8	16.35	544	234	58	118'32	3 944	3081/2
9 10	18 36 20'40	612	236 239	59 60	120 36 122 40	4'012 4'080	309
11	20 40	748	239	61	122 40	4 080	311
12	24.48	'816	243	62	126.48	4.516	312
13	26 52	*884	2451/2	63	128'52	4.584	313
14	28'56	952	2471/2	64	130 56	4'352	314
15	30.60	1 020	2491/2	65	132 60	4'420	315
16	32'64	1 088 1 156	251/2	66	134'64	4 488	316
17	34.68 36.72	1 1224	253½ 255½	67 69	136 68 138 72	4 '536 4 '624	317 317 1/2
19	33.76	1.292	257	69	140 76	4 692	3181/2
20	40.80	1.360	259	70	142.80	4.760	319
21	43'84	1'428	261	71	144'84	4*828	320
22	41.83	1'496	2621/2	72	146 88	4*896	321
23	46 92	1 564	264	73	148'92	4 964	322
24	43 96 51 00	1 632 1 700	266 267½	74 75	150°96 153°00	5'032 5'100	322½ 323½
25 26	53.04	1.768	269	76	155 04	5.163	324
27 28 29	55 03	1.836	2701/2	77	157 08	5.556	325
23	57 12	1 904	272	78	159'12	5 304	326
29	5916	1'972	2731/2	79	161 16	5.372	327
30	61'20	2'040	275	80	163'20	5'440	3271/2
32	63°24 65°28	2°108 2°176	278	81 82	165°24 167°28	5 508 5 576	328 329
33	67:32	2 244	279	83	169.32	5'644	330
34	69 36	2.315	2801/2	84	171 36	5.712	3301/2
35	71.40	2'380	232	85	173.40	5.780	331
36	73.44	2'448	283	86	175.44	5.848	332
37 38	75'48	2 516	2841/2 286	87 89	177'48	5'916	333
39	77 53 79 56	2°584 2°652	287	89	179°52 181°56	5 984 6 052	333½ 334
40	81.60	2.720	288	90	183 60	6 120	335
41	83'64	2.788	289	91	185'64	6.188	3351/2
42	85 63	2.826	2901/2	92	187.68	6.256	336
43	87.72	2.924	292	93	189.72	6.324	337
44	89'76 91'80	3.060	293 294	94 95	191.76	6 392	338
46	93.84	3.158	2951/2	96	193°80 195'84	6'460 6'528	338½ 339
47	95'88	3.196	297	97	197.88	6'596	340
48	97.92	3.564	293	98	199'92	6'664	3401/2
49	99 96	3.335	299	99	201'96	6.735	341
50	102'00	3'400	330	100	204.00	6.800	342

LINSEED OIL, CLARIFIED, FOR VARNISHES.—Heat in a copper boiler 50 gallons of linseed oil to 280° Fah.; add 2½ lbs. of calcined white vitriol, and keep the oil at the above temperature for half an hour; then remove it from the fire, and in twenty-four hours decant the clear oil, which should stand for a few weeks before it is used for varnish.

#### TABLE

Of the Pressure on a square and circular Inch, respectively, exerted by the elastic force of Steam at various degrees of Temperature, with the Height of the column of Mercury it will support.

1. PRESSURE ON A SQUARE INCH. 1. PRESSURE ON A CIRCULAR INCH.

		100	1					
Temperature, Fahrenheit.	Pressure on a square inch in lbs.	Proportional pressure on a circular inch in lbs.	Inches of Mercury supported.	Temperature, Fahrenheit.	Pressure on a circular inch in lbs.	Proportional pressure on a square inch in lbs.	Inches of Mercury supported,	
0		100	166	0		134		
220	21	1.963	5.15	222	21	3.183	6.56	
222	$\frac{2\frac{1}{2}}{3}$	2.356	6.18	224	3	3.819	7.87	
223	$3\frac{1}{2}$	2.749	7.21	226	$ \begin{array}{c c} 2\frac{1}{2} \\ 3 \\ 3\frac{1}{2} \end{array} $	4.456	9.18	
225	4	3.141	8.24	228	4	5.093	10.5	
227	$4\frac{1}{2}$	3.534	9.27	230	41/2	5.729	11.8	
228	5	3.927	10.3	232	5	6.366	13.1	
230	$5\frac{1}{2}$	4.320	11.3	234	51/2	7 002	14.4	
231	$\begin{array}{c c} 6 \\ 6\frac{1}{2} \end{array}$	4.712	12.3	235	6	7.639	15.7	
233	$6\frac{1}{2}$	5.105	13.4	236	61/2	8.276	17.0	
234	7	5.498	14.4	238	7	8.912	18.3	
235	71/2	5.890	15.4	239	71	9.549	19.7	
236	8 8½	6.283	16.5	241	8	10.18	21.0	
237	81/2	6.676	17.5	242	$\begin{bmatrix} 8\\8\frac{1}{2}\end{bmatrix}$	10.82	22.3	
239	9	7.068	18.5	244	9	11.45	23.6	
240	$9\frac{1}{2}$	7.461	19.6	245	91	12.09	24.9	
241	10	7.854	20.6	247	10	12.73	26.2	
242	$10\frac{1}{2}$	8.247	21.6	248	101	13.36	27.5	
243	11	8.639	22.6	250	11	14.00	28 9	
244	111	9.032	23.7	251	111/2	14.64	30.1	
245	12	9.424	24.7	252	12	15.27	31.2	
252	15	11.78	30.9	259	15	19.09	39.3	
261	20	15.71	41.2	270	20	25.46	52.5	
269	25	19.63	51.5	278	25	31.83	65.6	
276	30	23.56	61.8	287	30	38.19	78.7	
283	35	27.49	72.1	294	35	44.56	91.8	
289	40	31.41	82.4	300	40	50.92	105	
294	45	35.34	92.7	305	45	57.20	118	
300	50	39.27	103	309	50	63.66	131	
II files					1			

# AMALGAMS.

When mercury is alloyed with any metal the compound is called an amalgam of that metal; as, for example, an amalgam of tin, bismuth, &c.

### Amalgam for Electrical Machines.

1. Fuse 1 oz. of zine with  $\frac{1}{2}$  oz. of tin, at as low a temperature as possible; then add  $1\frac{1}{2}$  oz. of quicksilver, previously made hot; mix, pour out, and when cold reduce it to powder, and triturate it with sufficient quicksilver to bring it to a proper consistence.

2. Zinc 1 part; tin 1; quicksilver 2. Melt together.

3. Zinc 2 parts; tin 1; mercury 5.

4. La Beaume's. Pour into a chalked wooden box 6 oz. of quick-silver; put into an iron ladle ½ oz. of beeswax, with 2 oz. of purified zinc, and 1 oz. of grain tin; set it over a brisk fire, and when the metals are melted pour them into the box, avoiding the dross. When cold reduce it to powder, and mix it with lard. Keep it in a box covered with tallow, and spread it on leather for use.

Liquid Amalgam for Silvering Globes, &c.

Pure lead 1 oz; grain tin 1 oz; melt in a clean ladle, and immediately add 1 oz. of bismuth. Skim off the dross, remove the ladle from the fire, and before the metal sets add 10 oz. of quicksilver. Stir together, avoiding the fumes.

Amalgam for Varnishing Plastic Figures.

Melt 2 oz. of tin with  $\frac{1}{2}$  oz. of bismuth, and add  $\frac{1}{2}$  oz. of quick-silver. When cold grind it with white of egg, and apply to the figure.

# VARNISHES.

# Preparations of Lac.

Stick-lac consists of twigs of several kinds of trees encrusted with a resinous matter, produced by the puncture of an insect called the cocus lacca. This, triturated with water, and dried, forms seedlac. The seed-lac, when heated and pressed in cotton bags, forms shell-lac. Lac dye is the coloring matter extracted from stick-lac by water, and evaporated to dryness, with the addition of earthy matters, and formed into square cakes. Seed-lac and shell-lac are chiefly used in varnishes, dissolved in rectified spirits, or rectified wood naphtha. The alcoholic solution is rendered paler, so that it may be used for polishing light colored woods, by digesting it in the sun, or near a fire, for two or three weeks, with good animal charcoal, and then filtering it through paper in a funnel heated with hot water. Shell-lac may be bleached by dissolving it in a solution of potash, or soda, and passing chlorine into the solution.

The precipitated lac is collected, and well washed. Kastner directs 3 parts of carbonate of potash to be dissolved in 24 of water, and 3 of lime added, and the whole digested in a close vessel for twenty-four hours. The clear liquor is poured off, and boiled with 4 parts of shell-lac. When cold, dilute with 4 times its bulk of water, and filter; then add chloride of lime, and afterwards diluted muriatic acid. With these preliminary remarks we come now to the lacquers, or varnishes.

The Famous Brilliant French Varnish for Boots and Shoes.

Take  $\frac{8}{4}$  of a pint of spirits of wine; 5 pints white wine;  $\frac{1}{2}$  pound of powdered gum senegal; 6 oz. loaf sugar; 2 oz. powdered galls; 4 oz. green copperas. Dissolve the sugar and gum in the wine. When dissolved, strain; then put it on a slow fire, being careful not to let it boil. In this state put in the galls, copperas, and the alcohol, stirring it well for five minutes. Then set off, and when nearly cool strain through flannel, and bottle for use. It is applied with a pencil brush. If not sufficiently black a little sulphate of iron, and half a pint of a strong decoction of logwood, may be added, with  $\frac{1}{16}$  oz. pearlash.

#### Black Varnish.

Take any varnish, of the class you wish, 16 parts; lampblack 2 parts. Grind the black in a small quantity of the varnish, then mix it with the remainder.

#### Cabinet-makers' Varnish.

Pale shell-lac 700 parts; mastic 65 parts; strongest alcohol 1000 parts. Dissolve. Dilute with alcohol.

#### Callott's Soft Etching Varnish.

Linseed oil 8 parts; benzoin 1 part; white wax 1 part. Melt and keep it heated until reduced to two thirds.

#### Pale Carriage Varnish.

Copal 32 parts; pale oil 80 parts. Fuse and boil until stringy; then add dried white copperas 1 part; litharge 1 part. Boil again, then cool a little, and mix in spirits of turpentine 150 parts. Strain. While making the foregoing, take of gum animé 32 parts; pale oil 80 parts; dried sugar of lead 1 part; litharge 1 part; spirits of turpentine 170 parts. Pursue the same treatment as before, and mix the two compositions while hot.

#### Second Quality of Carriage Varnish.

Take of gum animé 32 parts; oil 100 parts; spirits of turpentine 150 parts; litharge 1 part; dried sugar of lead 1 part; dried copperas 1 part. Proceed as above.

#### Copal Varnish.

Copal 30 parts; drying oil 25 parts; spirits of turpentine 50 parts. Put the copal into a vessel capable of holding 200 parts,

and fuse it as quickly as possible, then add the oil, previously heated to nearly the boiling point. Mix well, then cool a little, and add the spirit of turpentine; again mix well, and cover up until the temperature has fallen to 140° Fah.; then strain.

### To Dissolve Copal in Spirit.

Take the copal and expose it in a vessel formed like a colander to the front of a fire, and receive the drops of melted gum in a basin of cold water; then well dry them, in a temperature of about 95° Fah. By treating copal in this way it acquires the property of dissolving in alcohol.

### Black Copal Varnish.

Take lamp-black, or ivory-black, in fine powder, and mix it with the varnish.

### Blue Copal Varnish.

Indigo, Prussian blue, blue verditer, or ultra-marine. These substances must be powdered fine. Proceed as before.

### Fine Pale Copal Varnish.

Pale African copal 1 part. Fuse, then add hot pale oil 2 parts. Boil until the mixture is stringy, then cool a little, and add 3 parts of pale spirits of turpentine. Mix well.

### Flaxen Grey Copal Varnish.

Ceruse, which forms the ground of the paste, mixed with a small quantity of Cologne earth, as much English red, or carminated lake, and a particle of Prussian blue, and color the varnish therewith.

## Green Copal Varnish.

Verdigris, crystallized verdigris, compound green (a mixture of yellow and blue). The first two require a mixture of white in proper proportions, from a fourth to two-thirds, according to the tint intended to be given. The white used for this purpose is ceruse, or the white oxide of lead, or Spanish white. Proceed as before.

### Improved Copal Varnish.

Caoutchoucine (white and scentless), strong alcohol, equal parts; copal in the proportion of two pounds to a gallon. Digest in a close vessel, without heat, for one week.

### Pearl Grey Copal Varnish.

White and black; white and blue; for example, ceruse and lamp-black; ceruse and indigo. Mix them with the varnish, according to the tint required.

### Purple Copal Varnish.

Prussian blue and vermilion, or any other blue and red; then proceed as before.

### Red Copal Varnish.

1. Vermilion, red oxide of lead (minium), red ochre, or Prussian red, &c., and proceed as before.

2. Dragon's blood, brick red, or Venetian red, &c., and proceed

as before.

### Violet Copal Varnish.

Vermilion, blue, white, in proportions required to color the varnish.

## White Copal Varnish.

Copal 16 parts; melt, and add hot linseed oil 8 parts; spirits of turpentine 15 parts; finest white lead to color.

### Yellow Copal Varnish.

Yellow oxide of lead, or Naples and Montpelier, both reduced to impalpable powder. These yellows are hurt by contact with iron or steel. In mixing them, therefore, a horn spatula, with a glass mortar and pestle, must be employed. Or gum guttæ, yellow ochre, or Dutch pink, according to the nature and tone of the color to be imitated, and proceed as before.

### Mastic Varnish.

Gum mastic 5 pounds; spirits of turpentine 2 gallons. Mix with a moderate heat (carefully applied), in a close vessel, then add pale turpentine varnish 3 pints. Mix well.

### Another.

Mastic 1 pound; white wax 1 ounce; oil of turpentine 1 gallon. Reduce the wax and mastic small, then digest in a close vessel, with heat, until dissolved.

### Common Oil Varnish.

Resin 4 pounds; genuine beeswax ½ pound; boiled oil 1 gallon. Mix with heat, then add spirits of turpentine 2 quarts.

### Turpentine Varnish.

Resin 1 part; boiled oil 1 part. Melt, then add turpentine 2 parts. Mix well.

### White Hard Spirit Varnish.

Gum sandarach 2½ pounds; alcohol (65 op.) 1 gallon. Place them in a strong, well closed vessel, and apply the heat of warm water, with occasional agitation, until dissolved; then add pale turpentine varnish 1 pint. Mix well, and let the whole rest for twenty-four hours, when it will be ready for use.

### White Spirit Varnish.

Strongest alcohol 100 parts; sandarach 25 parts; tears mastic 6 parts; elemi 3 parts; Venice turpentine 3 parts. Dissolve in a closely corked vessel.

# Varnish for Toys.

Copal 7 parts; mastic 1 part; Venice turpentine ½ part; strongest alcohol 11 parts. Dissolve the copal first, with the aid of a little camphor, then add the mastic, &c., and thin with alcohol, as required.

### To Clean Varnish.

Use a ley of potash, or soda, mixed with a little powdered chalk. Do not make the liquor too strong of the alkali.

### To Polish Varnish.

Take 2 oz. powdered tripoli, put it in an earthen pot, with water to cover it; then take a piece of white flannel, lay it over a piece of cork or rubber, and proceed to polish the varnish, always wetting it with the tripoli and water. It will be known when the process is finished by wiping a part of the work with a sponge, and observing whether there is a fair even gloss. When this is the case, take a bit of mutton suet and fine flour, and clean the work.

### Varnish for Harness.

Take ½ pound of India-rubber; one gallon of spirit of turpentine; dissolve enough to make it into a jelly; then take equal quantities of good hot linseed oil, and the above mixture. Incorporate them well on a slow fire, and it is fit for use.

### A Varnish for Fastening the Leather on Top Rollers in Factories.

Dissolve 23 oz. of gum arabic in water; and a like amount of isinglass dissolved in brandy, and it is fit for use.

# A Varnish to Preserve Glass from the Rays of the Sun.

Reduce a quantity of gum tragacanth to fine powder, and let it dissolve for twenty-four hours in white of eggs well beat up; then rub it gently on the glass with a brush.

### A fine Black Varnish for Coaches and Iron Work.

Bitumen of Palestine 2 oz.; resin 2 oz.; umber 12 oz. Melt them separately, and then mix together over a moderate fire. Then pour upon them, while on the fire, 6 oz. clear boiled linseed oil, stirring the whole from time to time. Take it off the fire, and when moderately cool pour in 12 oz. of essence of turpentine.

### Varnish for Clock Faces.

Spirits of wine 1 pint; divide it into four parts; mix one part with \( \frac{1}{2} \) an oz. of gum mastic in a bottle by itself; one part of spirit and \( \frac{1}{2} \) oz gum sandarach in another bottle; and one part spirit and \( \frac{1}{2} \) oz. whitest part of gum benzoin. Mix and temper them to suit; if too thick add spirit; if too thin a little mastic; if too soft some sandarach or benzoin. When about to use it warm the silvered plate before the fire, and with a flat camel-hair pencil stroke it over till no white streaks appear; this will preserve it for many years.

### Brown Varnish.

Rectified spirit 2 gallons; sandarach 3 pounds; shell-lac 2 pounds; pale turpentine varnish 1 quart. Put them into a tin bottle, cork securely, and agitate frequently, placing the tin occasionally in hot water till the gum is dissolved, then add a quart of pale turpentine varnish.

## Brilliant Amber Spirit Varnish.

Fused amber 4 oz.; sandarach 4 oz.; mastic 4 oz.; highly rectified spirit 1 quart. Expose to the heat of a sand bath, with occasional agitation, till dissolved. The amber is fused in a close copper vessel, having a funnel-shaped projection, which passes through the bottom of the furnace by which the vessel is heated.

### Chinese Varnish.

Mastic 2 oz.; sandarach 2 oz.; rectified spirit 1 pint. Close the matrass with bladder, with a pin hole for the escape of vapor; heat to boiling in a sand or water bath, and when dissolved strain through linen.

### Crystal Varnish.

Picked mastic 4 oz.; rectified spirit 1 pint; animal charcoal 1 oz. Digest, and filter.

### Picture Varnish.

Chio turpentine 2 oz.; mastic 12 oz.; camphor ½ drachm; pounded glass 4 oz.; rectified oil of turpentine 3 pints. This is for oil paintings.

### Canada Varnish.

Clear balsam of Canada 4 oz.; camphene 8 oz. Warm gently, and shake together till dissolved. This varnish is for maps, drawings, &c., which must be first sized over with a solution of isinglass, taking care that every part is covered. When dry, the varnish is brushed over it.

### Tingry's Essence Varnish.

Powdered mastic 12 oz.; pure turpentine  $1\frac{1}{2}$  oz.; camphor  $\frac{1}{2}$  oz.; powdered glass 5 oz.; rectified oil of turpentine 1 quart.

### Common Turpentine Varnish.

This is merely clear pale resin, dissolved in oil of turpentine; usually 5 pounds of resin to 7 pounds of turpentine.

### Amber Varnish.

Amber 16 oz.; melt in an iron pot, and add ½ pint of drying linseed oil, boiling hot, and add 3 oz. resin, and 3 oz. asphalte, each in fine powder. Stir till they are thoroughly incorporated; remove from the fire, and add a pint of warm oil of turpentine.

### Balloon Varnish.

Melt india-rubber in small pieces with its weight of boiled linseed oil, and thin it with oil of turpentine.

Varnish for Engraving on Copper.

Yellow wax 1 oz.; mastic 1 oz.; asphaltum ½ oz. Melt, pour into water, and form into balls for use. A softer varnish for engravers is made thus: Tallow 1 part, and 2 of yellow wax; or, with 2 oz. wax, 1 drachm common turpentine, and 1 drachm olive oil.

Etching Varnishes.

White wax 2 oz.; asphaltum 2 oz. Melt the wax in a clean pipkin, add the asphaltum in powder, and boil to a proper consistence. Pour it into warm water, and form it into balls, which must be kneaded, and put into taffeta for use.

Another.

White wax 2 oz; Burgundy pitch ½ oz; black pitch ½ oz; melt together, and add by degrees 2 oz. powdered asphaltum, and boil it till a drop cooled on a plate becomes brittle.

Another.

Equal quantities of linseed oil and mastic, melted together.

Engraving Mixture for Writing on Steel.

Sulphate of copper 1 oz; sal ammoniac  $\frac{1}{2}$  oz. Pulverize separately, adding a little vermilion to color it, and mix with  $1\frac{1}{2}$  oz. vinegar. Rub the steel with soft soap, and write with a hard, clean pen, without a slit, dipped in the mixture.

Elching Fluids.

For Copper.—1. Aquafortis 2 oz.; water 5 oz. Mix.

2. Callot's Eau Forte for Fine Touches.—Dissolve 4 parts each of verdigris, alum, sea salt, and sal ammoniac, in 8 parts vinegar; add 16 parts water, boil for a minute, and let it cool.

For Steel.—1. Iodine 1 oz.; iron filings ½ drachm; water 4 oz.

Digest till the iron is dissolved.

2. Pyroligneous acid 4 parts by measure; alcohol 1 part. Mix, and add 1 part double aquafortis (sp. gr. 128). Apply it from 1½ to 15 minutes.

Varnish for Engraving on Glass.

Wax 1 oz.; mastic ½ oz.; asphaltum ½ oz.; turpentine ½ drachm.

Another.

Mastic 15 parts; turpentine 7; oil of spike 4.

Le Blond's Varnish.

Keep 4 pounds balsam of copaiva warm in a sand or water bath, and add 16 oz. of copal, previously fused and coarsely powdered, by single ounces, daily, and stir it frequently. When dissolved add a little Chio turpentine.

Sealing Wax Varnish.

Black or colored sealing wax, broken small, and sufficient rectified spirit to cover it; digest till dissolved.

Black Japan.

Boil together a gallon of boiled linseed oil, 8 oz. umber, and 8 oz. asphaltum. When sufficiently cool thin it with oil of turpentine.

### Brunswick Black.

Melt 4 pounds asphaltum, add 2 pounds hot linseed oil, and when sufficiently cool add 1 gallon oil of turpentine.

Varnish for Gun Barrels, after browning them.

Shell-lac 1 oz; dragon's blood ½ oz.; rectified spirit 1 quart. Dissolve and filter.

### Transfer Varnish.

Alcohol 5 oz.; pure Venice turpentine 4 oz.; mastic 1 oz.

### Hair Varnish.

Dissolve 1 part of clippings of pigs' bristles, or horsehair, in 10 parts of drying linseed oil, by heat. Fibrous materials (cotton, flax, silk, &c.), imbued with the varnish and dried, are used as a substitute for hair cloth.

### Glass Varnish.

This is a solution of soluble glass, and is thus made: Fuse together 15 parts powdered quartz (or fine sand), 10 parts potash, and 1 charcoal. Pulverize the mass, and expose it for some days to the air; treat the whole with cold water, which removes the foreign salts, &c.; boil the residue in 5 parts of water until it dissolves. It is permanent in the air, and not dissolved by water. This varnish is used to protect wood, &c., from fire.

### Varnish for Gilded Articles.

Gum-lac 4 parts; dragon's blood 4; annatto 4; gamboge 4; saffron 1. Dissolve each resin separately in 8 parts alcohol, and make a separate tincture with the dragon's blood and annatto, also in 8 parts alcohol each; then mix the former together, and add a sufficient quantity of the tinctures to give the required shade and color to the varnish.

### Gold Varnishes.

Turmeric 1 drachm; gamboge 1 drachm; oil of turpentine 2 pints; shell-lac 5 ounces; sandarach 5 oz.; dragon's blood 7 drachms; thin mastic varnish 8 oz. Digest, with occasional agitation, for fourteen days, in a warm place; then set it aside to fine, and pour off the clear.

### Another.

Dutch leaf 1 part; gamboge 4; gum dragon 4; proof spirit 18. Macerate for twelve hours, then grind on a stone slab.

Varnish for Water Color Drawings.

Canada balsam 1 pint; oil of turpentine 2 parts, mixed. Size the drawing before applying the varuish.

Earthenware Varnish.

Flint glass 1 part; soda 1. Mix.

Magilp.

Mastic varnish 1 part; drying oil 2. Mix.

Another.

Mastic varnish 1 part; drying oil 1. Mix.

Another.

Equal parts of mastic varnish, drying oil, and turpentine. Mix.

Metallic Varnish for Couch Work, &c.

Asphaltum 56 pounds. Melt, then add litharge 9 pounds; red lead 7 pounds; boil, then add boiled oil 12 gallons; yellow resin 12 pounds. Again boil, until in cooling the mixture may be rolled into pills; then add spirit of turpentine 30 gallons; lampblack 7 pounds. Mix well.

Impermeable Varnish.

Boiled oil 100 parts; finely powdered litharge 6 parts; genuine beeswax 5 parts. Boil until sufficiently thick and stringy, then pour off the clear.

Engravers' Stopping-out Varnish.

Take lampblack and turpentine to make a paste.

# PRACTICAL TABLES.

WEIGHT OF METALS-WROUGHT IRON; SQUARE, ROUND, AND FLAT.

Table 1. contains the weight of Square Iron in sizes, from ‡ inch to six inches square, advancing by ‡ inch; and from 6 to 12 inches square, advancing by ‡ inch; and in lengths, from 1 foot to 18 feet. The sizes are arranged in the first column of each page, and the lengths along the top; the weight in lbs. immediately under the lengths, and in a line with the sizes.

Table II. contains the weight of Round Iron in sizes from  $\frac{1}{4}$  inch to 6 inches diameter, advancing by  $\frac{1}{8}$  inch; and from 6 to 12 inches diameter, advancing by  $\frac{1}{4}$  inch; and in lengths, from 1 foot to 18 feet. The sizes, lengths, and weights are arranged as in Table I.

Table III. contains the weight of Flat Iron in widths, from 1 inch to 6 inches diameter, advancing by 1 inch; in thicknesses, from 1 inch to 1 inch, advancing by 1 inch; and in lengths, from 1 to 18 feet. The widths, lengths, and weights are arranged as in the preceding tables, and the thicknesses alongside of the widths.

The tables are all calculated to the nearest tenth of a pound. To the weights of bars of Wrought Iron add  $\frac{1}{160}$ th part for bars of soft steel; and from the same weights subtract  $\frac{1}{14}$ th part for bars

of Cast Iron.

TABLE I.

G.		0.0	0.04		- 0	0.0	F 6	0 0	
Size.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
			0111			0 (3			175
14 30 12 50 84 78	0.2	0.4	0.6	0.8	1.1	1.3	1.5	1.7	1.9
8	0.5	1.0	1.4	1.9	2.4	2.9	3.3	3.8	4.3
2	0.8	1.7	2.5	3.4	4.2	5.1	5.9	6.8	7.6
8	1.3	2·6 3·8	4·0 5·7	5.3	6.6	7·9 11·4	9·2 13·3	10.6 15.2	11.9 17.1
4	1·9 2·6	5.2	7.8	7.6 10.4	9·5 12·9	15.5	18.1	20.7	23.3
8	2.0	9 2	10	104	12.9	19.9	101	201	400
1	3.4	6 8	10.1	13.5	16.9	20.3	23.7	27.0	30.4
11/8	4.3	8.6	12.8	17.1	21.4	25.7	29.9	34.2	38.5
14	5.3	10.6	15 8	21.1	26.4	31.7	37.0	42.2	47.5
1\frac{1}{4} 1\frac{3}{8} 1\frac{1}{2} 1\frac{5}{8}	6.4	12.8	19.2	25.6	32.0	38.3	44.7	51.1	57.5
11	7.6	15.2	22.8	30.4	38.0	45.6	53.2	60.8	68.4
15	8.9	17.9	26.8	35.7	44.6	53.6	62 5	71.4	80.3
18	10.4	20.7	31.1	41.4	51.8	62.1	72.5	82.8	93.2
1 <del>8</del> 1 <del>7</del> 1	11 9	23.8	35.6	47.5	59.4	71.3	83.2	95.1	106.9
100				F1 x	LA LO		Longo	none F	COL
2	13.5	27.0	40.6	54.1	67.6	81.1	94.6	108.2	121.7
21	15.3	30.5	45.8	61.1	76.3	91.6	106.8	122.1	137.4
$2\frac{1}{4}$	17.1	34.2	51.3	68.4	85.6	102.7	119.8	136.9	154.0
28	19.1	38.1	57.2	76.3	95.3	114.4	133.5	152.5	171.6
$2\frac{8}{8}$ $2\frac{1}{2}$ $2\frac{5}{8}$ $2\frac{4}{2}$ $2\frac{7}{8}$	21.1	42.2	63.4	84.5	105.6	126.7	147.8	169.0	190.1
25	23.3	46.6	69.9	93.2	116.5	139.8	163.0	186.3	209.6
28	25.6	51.1	76.7	102.2	127.8	153.4	178.9	204.5	230.0
27/8	27.9	55.9	83.8	111.8	139.7	167.6	195.7	223.5	251.5
			7	7			300	4	
12					4 40 5		010.6	0.10	0000
3	30.4	60.8	91.2	121.7	152.1	182.5	212.9	243.3	273.7
31	33.0	66.0	99.0	132.0	165.1	198.1	231.1	264.1	297.1
31	35.7	71.4	107.1	142.8	178.5	214.2	249.9	285.6	321.3
$\frac{3\frac{3}{8}}{3\frac{1}{2}}$	38.5	77.0	115.5	154.0	192.5	231.0	269·5 289·8	308.0	346.5
35	41.4	82·8 88·8	124·2 133·3	165.6	207·0 222·1	248.4	310.9	331.3	372.7
38	47.5	95.1	133.3	190.1	237.7	285.2	332.7	380.3	427.8
37	50.8	101.5	152.3	203.0	253.8	304.5	355.3	406.0	456.8
98	90.0	101 3	102 3	200 0	200 0	904 9	000 0	100 0	7000
		1		J		1	1	1	

TABLE I.

	1	1	1	1	1	1	1	1	
Size.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs,	lbs.	lbs,	lbs.	lbs.
6,000	2.1	2.3	2.5	2.7	3.0	3.2	3.4	12.5	
14801508476	4.8	5.5	5.7	6.2	6.7		7.6		3.8
8	8.5	9.3	10.1	11.0	11.8		13.5		
5	13.2	14.5	15.8	17.2	18.5		21.1		
3 4	19.0	20.9	22.8	24.7	26.6		30.4		
7	25.9	28.5	31.1	33.6	36.2	38.8	41.4	44.0	
			1						
	153	111/			0.0	- 1	- 1		
1	33.8	37.2	40.6	43.9	47.3	50.7	54.1		
11/8	42.8	47.1	51.3	55.6	59.9	64.2	68.4		77.0
14	52.8	58.1	63.4	68 6	73.9	79.2	84.5	89.8	95.0
18	63·9 76·0	70 3	76·7 91·2	83·1 9s·9	89·5 106·5	95·9 114·1	102·2 121·7	108.6	115.0
$\begin{vmatrix} 1\frac{1}{2} \\ 1\frac{2}{8} \end{vmatrix}$	89.3	98.2	107.1	116.0	125 0	133.9	142.8	129·3 151·7	136.9
13/4	103.5	133.9	124.2	134.6	144.9	155 3	165.6		160·7 186·3
17	118.8	130.7	142.6	154.5	166.4	178.2	190.1	202.0	213.9
18	1100	100 1	1120	1010	100 1	1,02	1001	2020	210 9
2	135.2	148.7	162.2	175.8	189.3	202.8	216.3	229.8	243.4
21	152.6	167.9	183.2	198.4	213.7	228.9	244.2	259 5	274.7
21	171.1	188.2	205.3	222.5	239.6	256.7	273.8	290.9	308.0
28	190.7	209.7	228.8	247.9	266.9	286.0	305.1	324.1	343.2
$2\frac{1}{2}$	211.2	232.3	253.4	274.6	295.7	316.8	337:9	359.0	380.2
25	232.9	256.2	279.5	302.8	326.1	349.4	372.7	396.0	419.3
23	255.6	281.2	306.7	335.3	357.8	383.4	409.0	434.5	460.1
27/8	279.4	307.3	335.3	363.2	391.1	419.1	447.0	475.0	502.9
-	1-1	1000	100	010111		- 1	-0.4	Local II	
3	201.0	004.0	907-0	205.4	127.0	4500	1005	F17.7	E 417.12
3 3 1	304.2	334·6 363·1	365·0 396·1	395·4 429·1	425·8 462·1	456.2	486.7	517·1 561·2	547·5 594·2
31	357.0	392.7	428.4	464.2	499.9	535.6	571.3	607.0	642.7
38	385.0	423.5	462.0	500.5	539.0	577.5	616.0	654.6	693.1
31	414.1	455.5	496.9	538 3	579.7		662.5	703.9	745.3
35	444.2	488.6	533.0	577.4	621.9		710.7	755.1	799.5
38	475.3	522.9	570.4	617.9	665.5		760.5	808.1	855.6
37	507.6	558.3	609.1		710.6		812.1	862.9	913.6
•				-					
100									

TABLE I.

Size.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
Inch.	lbs.	lbs.	lbs.	lbś.	lbs.	lbs.	lbs.	lbs.	lbs.
4	54.1	108.2	162.3	216.3	270.4	324.5	378.6	432.7	486.8
$4\frac{1}{8}$	57.5	115.0	172.6	230.1	287.6	345.1	402.6	460.1	517.7
41	61.1	122.1	183.2	244.2	305.3	366.3	427.4	488.4	549.5
$4\frac{3}{8}$	64.7	129.4	194.1	258.8	323.5	388.2	452.9	517.6	582.3
41/2	68·4 72·3	136.9	205 3	273.8	342.2	410.7	479.1	547.6	616.0
48	76.3	144·6 152·5	216 9 228·8	289·2 305·1	361·5 381·3	433·8 457·6	506.1	578.4	650.7 686.4
484	80.3	160.7	241.0	321.3	401.7	482.0	533·8 562·3	610.1	723.0
47	80 8	100 1	241 U	921 9	401 /	4020	902.9	0427	1250
5	84.5	169.0	253.4	337.9	422.4	506.9	591.4	675.8	760.3
51/8	88.8	177.6	266.4	355.1	443.9	532.7	621.5	710.3	799.1
$5\frac{1}{4}$	93.2	186.3	279.5	372.7	465.8	559.0	652.2	745.3	838.5
58	97.7	195.8	293.0	390.6	488.3	585.9		781.3	878.9
$5\frac{1}{2}$	102.2	204.5	306.7	409.0	511.2	613.4		817.9	920.2
55	107.0	213.5	320.9	427.8	534.8	641.7		855 €	962.6
53	111.8	223:5	335.3	447.0	558.8	670.5			1005.8
578	116.7	233.3	350.0	466.7	583.4	700.0	816.7	933.4	1050.0
		7	10.		ree .	C.			7- 1
	1015	0.40.0	005.0	100 =	200.0	<b>500.0</b>	243.0	0500	1005.0
6	121.7	243.3	365·0 396·1	486.7 528.2	608.3	730.0		973.3	
$\frac{6\frac{1}{4}}{61}$	132·0 142·8	264·1 285·6	428.4	571.3	660·2	792·2 856·9		1056 · £ 1142 · 5	1188·4 1285·3
$6\frac{1}{2}$ $6\frac{3}{4}$	154.0	303.0	462.0	616.0	770.1		1078.1		1386.1
0.4	1910	903 0	4020	0100	1101	0241	10101	12021	1900 1
		7- 1		-		1			
9 7	165.6	331.2	496.9	662.5	828.2	993.8	1159.4	1325.1	1490.7
74	177.7	355.3	533.0	710.7			1243.7		
71	190.1	380.3	570.4	760.5	950.7	1140.8	1331.0	1521.1	1711.2
7½ 7½	203.0	406.0	609.1	812.1	1015.1	1218-1	1421.2	1624.2	1827.2
				W2 h =		100 3	110	11/2	
8.	216.3	432.7	649.0				1514.4		
8‡	230.1	460.1	690.2				1610.5		
81/2	244.2	488 4	732.7				1709.5		2198.0
834	258.8	517.6	776.4	1035.2	1294.0	1552.8	1811.6	2070.4	2329.2
1000 L		1 0	ILL	100	220 0	1000	1 1	707	
9	273.8	E 47.0	991.4	1095.2	1900-0	1649.0	1016.5	2100.2	2564-1
9	219.9	547 6	821.4	1099.2	1909.0	1042.8	1910.9	2190.9	200* 1
	1 -	1	l						

TABLE I.

SQUARE IRON.

	1	1	1	} =	1		1		
Size.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
4	540.8	594.9	649.0	703.1	757-2	811.3	865.3	919.4	973.5
41	575.2		690.2						1035.3
414	610.6	671.6	732.7	793.7		915.8			
43	646.0	711.7	776.4	841.1	905.8		1035.2	1099.9	
41/2	684 5	752.9	821.4		958 3	1026.7	1095.2	1163.6	
45	723·1 762·6	795·4 838·9	867·7 915·2		1012·3		1156·9 1220·2	1229.2	
48 47	803.3	883.7		1044.3				1296·5 1365·7	
48	000 0	000 1	904 0	1044.3	1144.1	12000	1400 5	1909.1	1440.0
-							100		
5	844.8	929:3	1013:8	1098.2	11827	1267.2	1351.7	1436.2	1520.6
51	887.8			1154.2			1420.5		
51		1024.8		1211.2				1583.9	
5 3 8		1074.2		1269.5	1367.2	1464.9	1562.5	1660.2	1757.8
$5\frac{1}{2}$		1124.6						1738.1	
$5\frac{5}{8}$								1818.2	
54		1229.3		1452.8			1788.1		
$5\frac{7}{8}$	1160.0	1283.4	1400.1	1516.7	1633.4	1750.1	1866.7	1983.4	2100.1
6	1000.0	1990.0	1400.0	1501.0	1/7/19.9	1005.0	1040.0	2068:3	0100-0
$6\frac{1}{4}$								2244.7	
$6\frac{1}{2}$								2427.9	
$6\frac{3}{4}$		1694.1							
4	10101	10011	1010 1	2002 2	2000 2	2010 2	21012	2010 2	21122
01 10 D	0.00	PAR D	200	A 177	- 1			100	- X - 1
7	1656.3	1822.0	1987.6	2153.2	2318.8	2484.5	2650.1	2815.7	2981.4
71								3020.4	
$7\frac{1}{2}$								3232.3	
73	2030.2	2233.3	2436.3	2639.3	2842.3	3045.4	3248.4	3451.4	3654.4
0.0				135.10				- 1	
0	21.00	20505	2 4 4 2	201		2014		0.044.5	2221
8	2163'4	23797	2596.0	2812.4	3028.7	3245.0	3461.4	3677.7	3894.0
81	2300.7	2530.7	2760.8	2990.9	3220.9	3451.0	3681.1	3911.1	4141.2
8½ 8¾								4151·7 4399·6	
04	2000 0	2040 0	9109 6	0004,4	00202	9997.0	4140'8	4999'6	4000 4
	( - C)	1000	- 0	1			487.0		1 1000
9	2737.9	3011.7	3285:5	3559:3	3833.1	4106:9	4380.7	4654.5	4928:3
1			2000	550			2000 1		
	-							1	

TABLE I.

Size.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
									-
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
91	289.2	578.4	867.7	1156.9	1446:1	1735.3	2024.5	2313.8	2603.0
91	305.1	610.1		1220.2					
93	321.3	642.7		1285.3					
- 3 - 1	-								20020
100	- 21		1 100 2 10 1	\	-	-	TO THE		
10	337.9	675.8	1013.8	1351.7	1689.6	2027:5	2365.4	2703.4	3041.0
101	355.1			1420.5					
101	372.7			1490.7					
103	390.6			1562.5					
104	330 0	101 9	1111 0	10020	1000 1	_9T0 0	21011	01400	2010 1
2-09.03	-	7.114.7			-			4-14	-
11	409.0	817.0	1996.0	1635.8	2011.8	9453.8	2262-7	2971.7	3680.6
117	427.8			1711.2					
111	447.0			1788.1					
118	466.7			1866.7					
114	400 /	900 4	14001	1900.1	2000 4	20001	5200 0	9199.9	4200 2
310	0.00	Lanc.							
10	100-	050.0	1400.0	1010.0		2010.0	0400.0	2002-0	1070-0
12	486.7	919.9	1460.0	1946.6	2499,9	2919.9	2406.6	2093.5	4379.9
	1		1		1				

GLAZES.—Common earthenware is glazed with a composition containing lead, on which account it is unfit for many pharmaceutical purposes. The following glaze has been proposed, among others, as a substitute: 100 parts of washed sand, 80 of purified potash, 10 of nitre, and 20 of slaked lime; all well mixed, and heated in a blacklead crucible, in a reverberatory furnace, till the mass flows into a clear glass. It is then to be reduced to powder. The goods to be slightly burnt, placed under water, and sprinkled with the powder.

GLAZE FOR PORCELAIN.—Feldspar 27 parts, borax 18, Lynn sand 4, nitre 3, soda 3, Cornwall china clay 3 parts. Melt together to form a frit, and reduce it to a powder, with 3 parts of calcined borax.

Solvent for Old Putty and Paint.—Soft soap mixed with solution of potash or caustic soda; or pearlash and slaked lime mixed with sufficient water to form a paste. Either of these laid on with an old brush or rag, and left for some hours, will render it easily removable.

TABLE I.

### SOUARE IRON.

Size.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
Inch.	lbs.								
91	2892.2	3181.4	3470.6	3759.9	4049.1	4338.3	4627.5	4916.7	5206.0
91	3050.6	3355.6	3660.7	3965.7	4270.8	4575.8	4880.9	5186.0	5491.0
93	3213.3	3534.7	3856.4	4177.3	4498.6	4820.0	5141.3	5462.6	5784.0
	74. T		. 1	9000			DITT.		
	O'C			177		1.1	100	0.0	1
10	3379.2	3717.1	4055.0	4393.0	4730.9	5068.8	5406.7	5744.6	6082.6
101							5682.2		
101	3726.7	4099.4	4472.1	4844.7	5217.4	5590.1	5962.8	6335.4	6708.1
103	3906.3	4297.0	4687.5	5078.2	5468.8	5859.4	6250.0	6644.7	7031.3
11							6543.4		
111							6845.0		
$11\frac{1}{2}$							7152.4		
113	4666.8	5133.5	5600.2	6066.9	6533.6	7000.3	7466.9	7933.6	8400.3
	POR				-	-0	11		
- 1	1000	×0×0 0	×000 0			122		0000	05.40.0
12	4866.6	5353.5	2833.9	6326.5	6813.2	7299.8	7786.5	8273.2	8759.8
72.63	7-17	(3)	7.01	The	- 11	111_	1991		

Scouring Drops for Removing Grease.—1. Alcohol (pure) 6 oz., camphor 2 oz., rectified essence of lemon 8 oz.

- 2. Camphene 3 oz., essence of lemon 1 oz. Mix. Some direct them to be distilled together.
- 3. French. Camphene 8 oz., pure alcohol 1 oz., sulphuric ether 1 oz., essence of lemon 1 dr.
- 4. Spirits of wine 1 pint, white soap 3 oz., ox gall 3 oz., essence of lemon  $\frac{1}{4}$  oz.

Balls, Heel.—1. Melt together 4 oz of mutton suet, 1 oz of beeswax, 1 oz of sweet oil, ½ oz oil of turpentine, and stir in 1 oz

of powdered gum arabic, and ½ oz. of fine lampblack.

2. Beeswax 8 oz., tallow 1 oz., powdered gum 1 oz., lampblack q. s. These are used not merely by the shoemaker, but to copy inscriptions, raised patterns, &c., by rubbing the ball on paper laid over the article to be copied. For copying ancient monumental brasses, a similar compound, colored with bronze powder instead of lampblack, is sometimes employed.

TABLE II.

1111111			3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
7	0.2	0.3	0.5	0.7	0.8	1.0	1.2	1.3	1.5
14 % to 1/2 5/20 % 4 7/2	0.4	0.7	1.1	1.5	1.9	2.2	2.6	3.0	3.4
1	0.7	1.3	2.0	2.7	3.3	4.0	4.6	5.3	6.0
5	1.0	2.1	3.1	4.2	5.2	6.3	7.3	8.3	9.4
34	1.5	3.0	4.5	6.0	7.5	9.0	10 5	11.9	13.4
78	2.0	4.1	6.1	8.1	10.2	12.2	14.2	16.3	18.3
1 1 8	2.7	5.3	8.0	10.6	13.3	15.9	18.6	21.2	23.9
11/8	3.4	6.7	10.1	13.4	16.8	20.2	23.5	26.9	30.2
17	4.2	8.3	12.5	16.7	20.9	25.0	29 2	33.4	37.5
$1\frac{3}{8}$ $1\frac{1}{2}$	5.0	10.0	15.1	20.1	25.1	30.1	35.1	40.2	45.2
$1\frac{1}{2}$	6.0	11.9	17.9	23.9	29.9	35.8	41.8	47.8	53.7
15 13	7.0	14.0	21.0	28.0	35.1	42.1	49.1	56.1	63.1
12	8.1	16.3	24.4	32.5	40.6	48.8	56.9	65.0	73.2
17/8	9.3	18.7	28.0	37.3	46.7	56.0	65.3	74.7	84.0
2	10.6	21.2	31.8	42:5	53.1	63.7	74.3	84.9	95.5
$2\frac{1}{8}$	12.0	24.0	36.0	48.0	59.9	71.9	83.9	95.9	107.9
$     \begin{array}{c}       2\frac{1}{8} \\       2\frac{1}{4} \\       2\frac{3}{8} \\       2\frac{1}{2}    \end{array} $	13.5	26.9	40.3	53.8	67.2	80.6	94.1	107.5	121.0
28	15·0 16·7	30.0	44.9	60.0	74 9	89.9	104.8	119·8 133·5	134.8
25	18.8	36.6	50·1 54·9	66.8 73.2	83:4 91:5	100.1	116·8 128·1	146.3	150·2 164·6
28	20.1	40.2	60.2	80.3	100.4	120 5	140.5	160.6	180.7
$   \begin{array}{r}     2\frac{5}{8} \\     2\frac{8}{4} \\     2\frac{7}{8}   \end{array} $	21.9	43.9	65.8	87 8	109.7	131.7	153.6	175.6	197.5
1 (200			- To .			10		E +1	idl .
3	23.9	47.8	71.7	95.6	119.4	143 ?	167.2	1911	2150
3 <del>1</del> 3 <del>1</del> 3 <del>1</del>	25.9	51.9	77.8	103 7	129.6	155.6	181.5	207.4	233.3
34	28.0	56.1	84.1	112.2	140.2	168.2	196.3	224.3	253.4
$\frac{3\frac{3}{8}}{3\frac{1}{2}}$	30·2 32·5	60.5	90·7 97·5	121·0 130·0	151·2 162·6	181·4 195·1	211.7 227.6	241 9 260·1	272·2 292·6
35	34.9	69.8	104.7	139.5	174.4	209.3	244.2	279.1	314.0
38	37.3	74.7	112.0	149.3	186.7	224.0	261.3	298.7	336.0
$3\frac{7}{8}$	39.9	79.7	119.6	159.5	199.3	239.2	279.0	318.9	358.8

TABLE II.

		1				,			
Size.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
Inch.	lbs.	lbs.	lbs.						
1	1.7	1.8	2.0	2.1	2.3	2 5	2.6	2.8	3.0
38	3.7	4.1	4.5	4.8	5.2		6.0	6.3	6.7
14 80 12 50 84 78	6.6	7.3	8.0	8.6	9.3		10 6	11.3	11.9
5 8	10.4	11.5	12.5	13.6	14.6		16.7	17.3	18.8
34	14.9	16.4	17.9	19.4	20.9				26.9
<del>7</del> 8	20.3	22.4	24.4	26.4	28.4	30.5	32.2	34.5	36.6
1	26.5	29.2	31.8	34 5	37.2	398	42.5	45.1	47.8
11/8	33.6	37.0	40.3	43.7	47.0		53.8	57.1	60.5
11	41.7	45.9	50.1	54.2	58.4		66.8	70.9	75.1
18	50.2	55.2	60.2	65.2	70.3		803	853	90.3
11	59.7	65.7	71.7	77.6	83.6		95 6	101.5	107.5
15	70.1	77.1	84.1	91.1	98.1	105.2	112.2	119.2	126.2
13	81.3	89.4	97.5	105.7	113.8	121.9	130.0		146.3
17	93.3	102.7	112.0	121.3	130.7	140.0	149.3	158.7	168.0
MI	11125	+ 1136 -					1000		
2	106.2	116.8	127.4	138.0	148.6	159 2	169.9		192.1
21/8	119.9	131.9	143.9	155.8	167.8	179.8	181 8	193.8	205.8
21	134.4	147.8	161.3	174.7	188.2	201.6	215.0	228.5	241.9
28	149.8	164.7	179.7	194.7	209.7	224.6	239.6	254.6	269.6
$\frac{2\frac{1}{2}}{2}$	166.9	183.6	200.3	216.9	233.6	250.3	267.0	283.7	300.4
25/8	182·9 200·8	201·2 220·8	219·5 240·9	237.8	256·1 281·1	274·4 301·1	292·7 321·2	311.0	329·3 361·4
24 27	219.4	241.4	263.4	261·2 285·3	307.2	329.2	351.1	373.0	395.0
48	213 4	241 4	200 4	200 0	301 2	929 2	991 1	3130	0900
	1	100		111	1 1		1	159 1 1	
3	238.9	262.8	286.7	310.5	334.4	358.3	382.2	406.1	430.0
31	259.3	285.2	311.1	337.0	363.0	388.9	414.8	440.7	466.7
31	280.4	308.4	336.5	364.5	392.6	420.6	448.6	476.7	504.7
38	302.4	332.6	362.9	393.1	423.4	453.6	483 8	514.1	544.3
31/2	325.1	357.6	390.1	422.7	455.2	487.7	520.2	552.7	585.2
35	348.9	383.7	418.6	455.5	488.4	523.3	558.2	593.1	627.9
38	373.3	410.7	448.0	486.3	522.6	560.0	597.3	634.6	672.0
37	398.6	438.5	478.3	518.2	558.1	598.0	637.8	677.7	717.6
		1					1		

TABLE II.

Size.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.			
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.			
4	- 42.5	84.9	127.4	169.9	212.3	254 8	297.2	339-7	382.2			
41	45.2	90.3	135.5	180.7	225.9	271.0						
41	48.0	95.9	143.9	191.8	239.8							
48	50.8	101.6	152.4	203.3	254.1	304.9						
$4\frac{1}{2}$	53.8	107.5	161.3	215.0	268.8	322.6						
45	56.8	113.6	170.4	227.2	283 9							
48	60.0	119.8	179.7	239·6 252·4	299.5	359.4						
47/8	63.1	126.2	189.3	293.4	315.5	378.6	441.7	504.8	567.8			
5	66.8	133.5	200.3	267.0	333.8	400.5	467:3	534.0	600.8			
5 <del>1</del>	69.7	139.5	209.2	278.9	348.7	418.4		557.8				
51	73.2	146.3	219.5	292.7	365.9	439.0						
5\frac{3}{8}	76.7	153.4	230.1	306.8	383.5	460.2						
51	80.3	160.6	240.9	321.2	401.5	481.8		642.4	722.7			
5 5	84 0	168.0	252.0	336.0	420.0	504.0	588.0	672.0	756.0			
53	87.8	175.6	263.3	351.1	438.9	526.7		702.2	790.0			
57	91.6	183.3	274.9	366.5	458.2	549.8	641.4	733.1	824.7			
1-3-				1 - 1		31/	700	001	51			
6	95.6	191.1	286.7	382.2	477.8	573.3		764.4				
61	103.7	207.4	311.1	414.8	518 5	622.2	725.9	829.6				
$6\frac{1}{2}$ $6\frac{3}{4}$	112.2	224.3	336 5	448.6	560.8	673.0			1009.4			
64	121.0	241.9	362.9	483.8	604.8	725.8	846.7	967.6	1088.6			
4	-		100	10		-	- 541		10			
7	130.0	260.1	390.1	520.2	650.2	780.3	910-3	1040.4	11704			
71	139.5	279.1	418.6	558.2	697.7	837.3		1116.4				
71	149.3	293.7	448 0	597.3	741.6	896.0		1194.6				
78	159.5	318.9	478.4	637.8	797 3	956.7	1116.2					
'4												
100	100			Villa	50V=	MAL.	1 44	200	4.0			
8	169.9	339.7	509.6	679.4	849.3	1019.1	1189.0	1358.8	1528-7			
81	180.7	361 4	542.1	722.8		1084.2	1264.9	1445.6	1626.3			
81/2	191.8	383.6	595.4	767.2		1150.8		1534.5				
88	203 3	406 5	609.8	813.0	1016 3	1219 6	1422.8	1626.1	1829.3			
-70	1000		No.			1397		1100	35			
7717	O ELO	700		THE PARTY		986			1007.4			
9	215.0	430.1	645.1	860.2	1075.2	1290.2	1505.3	1720.3	19354			
		1					1		- 11			

TABLE II.

Size.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
4 44	424.6		509·6 542·1	552.0 587.3	594·5 632·4	637·0 677·6	676·4 722·8	721·9 761·0	
41	479.3		575.4	623.4	671 3	719.3	767.2	815.2	863.1
438	508.2		609·8 645·1	660·6 698·9	711·4 752·6	762·2 806·4	813·0 860·2		914·7 967·7
45	567.9	624.7	681.5	738.2	795.0	851 8	908.6	965.4	1022-2
4\frac{3}{4} 4\frac{7}{8}	599.0		718·8 757·1	778·7 820·2	838·6 883·3	898·5 946·4	958·4 1009·5	1018·3 1072·6	
-8	0000	0010					10000		1100
5	667.5	734.3	801.0	867.8	934 5	1001.3	1068.0	1134.8	1201.5
51	697.3		836.5	906.5	976.2	1046 0	1115.7	1185.4	1255.2
5½ 5¾	731·7 767·0		878·1 920·4		1024·4 1073·8				
5 38 5 12 5 58	803·0 840·0				$1124 \ 3 \ 1176 \ 0$				
53	877.8	965.5	1053.3	141.1	1228.9	1316.6	1404.4	1492.2	1580.0
578	916.3	1008 0	1099.6	191.2	1282.9	1374.5	1466.1	1557.8	1649.4
1000	. L		208						
6 61		1051.1							
$6\frac{1}{2}$	1121.6	1233 8	345.9	458.1 1	570.2	682.4	1794.6	906.7	2018.9
64	1209.6	1330.6	451.5	.572.5	693.4	814.4	1935.4	2056.3	3177.3
Vi I	1000 -	1400 -	1500 01	200 0 1	000 5	050.5	20000	010.00	2010
7 71		1430.5 1 1535.0 1						$\frac{210.8}{272.2}$	
71		1642·6 1 1754·0 1							
73	1994.0	1734.0	.915 5 2	072.9	232.4	391.9	391.9	110-5	870.2
8	1600.6	1868.4	2038.3	200 10	070.00	- 45.00	715.79	007.69	057.4
81	1809.0	1987.7 2	168.4 2	349.02	529.7 2	740.4 2	891.13	071.83	252.5
8 <u>년</u> 8월	1918·1 2032·6	2109.9 2	$301.7   2 \\ 439.1   2$					$ \begin{array}{c c} 260.7 & 3 \\ 455.4 & 3 \end{array} $	452.5
04	4002 0	4200 9 2	45912	042.4 2	040.0	048.919	204 4 0	100 4	0001
9	2150.4	2365.4	580.5	705.53	010.63	225.62	140.63	655.7 2	870.7
	2100 4	2000 4 2	1000 0 2	1 30 0 0	010 0 3	220 0 0	110 0 0	000 1 0	0.01

### TABLE IL

ROUND IRON.

Size.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
Inch.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
9 <del>1</del> 9 <u>1</u> 9 <u>4</u>	227·2 239·6 252·4	479.2	718.8	958.4	1135.8 1198.0 1261.9	1437.6	1677.2	1916.8	2156.4
10 10 <sup>1</sup> / <sub>4</sub> 10 <sup>1</sup> / <sub>2</sub> 10 <sup>3</sup> / <sub>4</sub>	266·3 278·9 292·7 306·8	532.6 557.8 585.4 603.6	836·8 878·1	1115·7 1170·8	1331.4 1394.6 1463.4 1534.0	1673·5 1756·1	1952·5 2048·8	2231·4 2341·5	2510·3 2634·2
11 11 <del>1</del> 11 <del>1</del> 11 <del>2</del> 11 <del>2</del>	321·2 336·0 351·1 366·5	672.0 1 702.2 1	1008·0 1053·3	1344·0 1404·4	1606·1 1680·0 1755·5 1832·7	2016:0	2352·0 2457·7	2688 0 2808 8	3024·0 3159·9
12	382.2	764.4	146.5	528.8	1911.0	2293.2	2675.5	3057.7	3439.9

Bronzing Liquids, for Bronzing Copper Medals, Figures, Instruments, &c.—1. Sal ammoniac 1 dr., oxalic acid 15 gr., vinegar 1 pint. After well cleaning the article to be bronzed, warm it gently, and brush it over with the liquid, using only a small quantity at a time. When rubbed dry, repeat the application till the desired tint is obtained. [For copper medals, electrotype casts, &c.]

2. Sal ammoniae 1 oz., cream of tartar 3 oz., salt 6 oz. Dissolve in a pint of hot water, add 2 oz. of nitre, and 2 oz. of nitrate of copper dissolved in 1 pint of water.

3. Salt of sorrel 1 oz., sal ammoniac 2 oz., white vinegar 14 oz.

[To give an antique appearance to bronze figures, &c.]

4. A diluted solution of muriate of platina. [For copper binding

screws, and other small articles.

5. A weak solution of hydro-sulphuret of ammonia, or of sulphuret of potassium. [For electrotype medals. Another method is the following: Immediately on removing the electrotype cast from the solution, brush it over with good black lead; then heat it moderately, and brush it over with a painting brush, the slightest moisture being used.]

TABLE II.

G.	10.64	11 64	10.64	10 64	14.64	7 = 64	16 ft.	1 17 CL	10 ft
Size.	10 11.	11 16.	12 16.	15 16.	14 16.	10 16.	10 16.	1 / 16.	18 16.
				4000	9 /				
Inch.	lbs.	· lhs.							
91	2271.5	2498.7	2725.8	2953.0	3180.1	3407:3	3634.4	3861.6	4088.7
91	2396.0	2635 6	2875.2	3114.8	3354.4	3594.0	3833.6	4073.2	4312.8
98	2523.8	2776.1	3028.5	3280.9	3533.3	3785.6	4038.0	4290.4	4542.8
100		195		2 -					
10							4260.6		
10計							4462.8		
$10\frac{1}{2}$							4683.0		
103	3068.0	3374.8	3681.6	3988.4	4295.2	4602.0	4908.8	5215.6	5522.4
		147					1		
						1			
11							5139.5		
. 114	1000	1					5376.1	1	
1112							5619.7		
113	3665.4	4031.9	1398.4	4765.0	2131.2	5498.0	5864.6	6231.1	6597.6
	10	967	150						
12	3899-1	4204.3	4586.5	1968-7	5350 0	5733.1	6115.3	6497.5	6879.7
0311	70221	1201 0	1000 9	1 0001	0000 9	0100 1	0110 0	02010	00101
		1		1		1	1		

SOLUTIONS USED IN ELECTROTYPE MANIPULATIONS, &c.

1. Acid Solution of Copper for the Decomposing Cell. Saturated solution of sulphate of copper 2 parts, sulphuric acid 2 parts, water 6 or 8 parts.

2. Gold Solution. Dissolve 2 oz. of cyanide of potassium (by Liebig's method) in a pint of warm distilled water, add ½ oz. of

oxide of gold, and agitate together.

3. Silver Solution. Dissolve 2 oz. of Liebig's cyanide of potassium in a pint of distilled water; add 4 oz. of moist oxide of silver (precipitated by lime water from a solution of the crystallized nitre), and agitate together till the oxide is dissolved.

4. Solution in which Steel Articles are dipped before Electroplating them. Nitrate of silver 1 part, nitrate of mercury 1 part, nitrie

acid (sp. gr. 1.384) 4 parts, water 120 parts.

5. Solution, or Pickle, for immersing Copper Articles in before Electroplating. Sulphuric acid 64 parts, water 64, nitric acid 32, muriatic acid 1. Mix. The article, free from grease, is dipped in the pickle for a second or two.

TABLE III.

-										-
Thick.	Width	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
in.	in.	lbs.								
1	1	0.8	1.7	2.5	3.4	4.2	5.1	5.9	6.8	7.6
1	11	1.1	2.1	3.2	4.2	5.3	6.3	7.4	8.4	9.5
1	11	1.3	2.5	3.8	5.1	6.3	7.6	8.9	10.1	11.4
14 14 14 14	14	1.5	3.0	4.4	5.9	7.4	8.9	10.4	11.8	13 3
1	2	1.7	3.4	5.1	6.8	8.5	10.1	11.8	13.5	15.2
1	24	1.9	3.8	5.7	7.6	9.5	11.4	13.3	15.2	17.1
1	21	2.1	4.2	6.3	8.4	10.6	12.7	14.8	16 9	19.0
141414	$2\frac{3}{4}$	2.3	4.6	7.0	9.3	11.6	13:9	16.3	18.6	20.9
,	3	2.5	5.1	7.6	10.1	12.7	15.2	17.7	20.3	22.8
4	31	2.7	5.5	8.2	11.0	13.7	16.5	19.2	22.0	24.7
1	31	3.0	5.9	8.9	11.8	14.8	17.7	20.7	23.7	26.6
14141414	384	3.5	6.3	9.5	12.7	15.8	19.0	22.2	25.4	28.5
1	4	3.4	6.8	10.1	13.5	16.9	20.3	23.7	27.0	30.4
1	41	. 3.6	7.2	10.8	14.4	18.0	21.5	25.1	28.7	32.3
1	41	3.8	7.6	11.4	15.2	19.0	22.8	26 6	30.4	34.2
14141414	484	4.0	8.0	12.0	16.1	20.1	24 1	28.1	32.1	36:1
1	5	4.2	8.4	12.7	16.9	21.1	25.3	29.6	33.8	38.0
į	51	4.4	8.8	13.3	17.7	22.2	26.6	31.1	35.5	39.9
ī	51	4.6	9.3	13.9	18.6	23.2	27.9	32.5	37.2	41.8
14141414	54	4.9	9.7	14.6	19.4	24.3	29.2	34.0	38.9	43.7
1	6	5.1	10.1	15.2	20.3	25.3	30.4	35.5	40.6	45.6
3	1	1.3	2.5	3.8	5.1	6.3	7.6	8.9	10.1	11.4
පෝත පෝත පෝත පෝක	11	1.6	3.2	4.8	6.3	7.9	9.5	11.1	12.7	14.3
3	11	1.9	3.8	5.7	7.6	9.5	11.4	13.3	15 2	17.1
3	14	2.2	4.4	6.7	8.9	11.1	13.3	15.5	17.7	20.0
8	2	2.5	5.1	7.6	10.1	12.7	15.2	17.7	20.3	22.8
क्षेक क्षेक क्षेक	21	2.9	5.7	8.3	11.4	14.3	17.1	20.0	22.8	25.7
3	21	3.2	6.3	9.5	12.7	15.8	19.0	22.2	25.4	28.5

TABLE III.

-										
Thick.	Width	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
in.	in.	lbs.								
1	1	8.5	9.3	10.1	11.0	11.8	12.7	13.5	14.4	15.2
1	11	10.6	11.6	12.7	13.7	14.8	15.8	16.9	17.9	19.0
14141414	11	12.7	13.9	15.2	16.5	17.7	19.0	20.3	21.5	22.8
1	184	14.8	16.3	17.7	19.2	20.7	22.2	23.7	25.1	26.6
1	2	16.9	18.6	20.3	22.0	23.7	25.4	27.0	28.7	30.4
1	21	19.0	20.9	22.8	24.7	26.6	28.5	30.4	32.3	34.2
14141414	$2\frac{1}{2}$	21.1	23.2	25.3	27.5	29.6	31.7	33.8	35.9	38.0
14	$2\frac{8}{4}$	23.2	25.6	27.9	30.2	32.5	34.9	37.2	39.5	41.8
1	3	25.3	27.9	30.4	33.0	35.5	38.0	40.6	43.1	45.6
1	31	27.5	30.2	33.0	35.7	38.5	41.3	43.9	46.7	49.4
1	31	29.6	32.5	35.5	38.5	41.4	44.4	47.3	50.3	53.2
14141414	834	31.7	34.9	38.0	41.2	44.4	47.5	50.7	53.9	57.0
1	4	33.8	37.2	40.6	43.9	47 3	50.7	54.1	57.5	60.8
1	41	35.9	39.5	43.1	46.7	50.3	53.9	57.5	61.0	64.6
14141414	43	38.0	41.8	45.6	49.4	53.2	57.0	60.8	64.6	68.4
1	484	40.1	44.1	48.2	52.2	56.2	60.2	64.2	68.2	72.2
1	5	42.2	46.5	50.7	54.9	59.1	63.4	65.6	71.8	76.0
14141414	51	41.4	48.8	53.2	57.7	62.1	66.5	71.0	75.4	79.9
1	51	46.5	51.1	55.8	60.4	65.1	69.7	744	79.0	83.6
1	54	48.6	53.4	58.3	63.2	68.0	72.9	77.7	82.6	87.5
1	6	50.7	55 8	60.8	65.9	70.9	76.0	81.1	86.2	91.2
8	1	12.7	13.9	15.2	16.5	17.7	19.0	20.3	21.5	22.8
व्यंक क्षंक क्षंक क्षंक	11	15.8	17.4	19.0	20.6	22 2	23.8	25.3	28 9	28.5
8	11/2	19.0	20.9	22.8	24.7	26.6	28.5	30.4	32.3	34.2
8	18	22 2	24.4	26.6	28.8	31.1	33.3	35.5	37.7	39.9
යාන සාද්ග සාදන	2	25.3	27.9	30.4	33 0	35.5	38.0	40.6	43.1	45.6
8	21	28.5	31.4	34 2	37.1	39.9	428	45.6	48.5	51.3
8	$2\frac{1}{2}$	31.7	34.9	38.0	41.2	44.4	47.5	50.7	53.9	57.0
	1	1	4	1	1	1	0 1		1	

TABLE III.

-										57
Thick	Width.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
	in.	,,,	,	lbs.	lbs.	9.60	,,	200	140	100
in		lbs.	lbs.	108.	los.	lbs.	lbs.	lbs.	lbs.	lbs.
38	234	3.2	7.0	10.5	13.9	17.4	20.9	24.4	27.9	31.4
3	3	3.8	7.6	11.4	15.2	19.0	22.8	26.6	30.4	34.2
දේග දේග දේග දේග	37	4.1	8.2	12.4	16.5	20.6	24.7	28.8	33 0	37.1
8 3	31	4.4	8.9	13.3	17.7	22.2	26.6	31.1	35.5	39.9
8	33	4.8	9.5	14.3	19.0	23.8	28.5	33.3	38.0	42.8
8	1	66 19	40 11	15:0(2	72 1	CVE.	102	10	176	10/3
3	4	5.1	10.1	15.2	20.3	25.3	30.4	35.5	40.6	45.6
w(m m)m m)m	41	5.4	10.8	16.1	21.5	26.9	32.3	37.7	43.1	48.5
3	41	5.7	11.4	17.1	22.8	28.5	34.2	39.9	45.6	51.3
3	43	0.9	12.0	:18.1	24.1	30.1	36 1	42.1	48.2	54.2
		1.4	13. 10	6	34.14		3.50	0.0	-00	1017
യിയ യിയ യിയ യിയ	5	6.3	12.7	19.0	25.3	31.7	38.0	44.4	50.7	57.0
3	54	6.7	13.3	20.0	26.6	33.3	39.9	46.6	53.2	59.9
3	51	7.0	13.9	20.9	27.9	34.9	41.8	48.8	55.8	62.7
3	54	7.3	14.6	21.9	29 2	36.4	43.7	51.0	58.3	65.6
	1 3	11-		70	-	1	200	The N	144.	
3	6	7.6	15.2	22.8	30.4	38.0	45.6	53.2	60.8	68.4
1			J =			/				
1 2	1	1.7	3.4	5.1	6.8	8.2	10.1	11.8	13.5	15.2
1 2	14	2.1	4.2	6.3	8.4	10.6	12.7	14.8	16.9	19.0
13 12 12 12	$1\frac{1}{2}$	2.5	5.1	7.6	10.1	12.7	15.2	17.7	20.3	22.8
1/2	134	3.0	5.9	8.9	11.8	14.8	17.7	20.7	23.7	26.6
1	2	3.4	6.8	10.1	13.5	16.9	20.3	23.7	. 27.0	30 4
12121212	21	3.8	7.6	11.4	15.2	19:0	22.8	26.6	30.4	34.2
1	$2\frac{1}{2}$	4:2	8.4	12.7	16.9	21.1	25.3	29.6	33.8	38.0
1	$ \frac{-2}{2\frac{3}{4}} $	4.6	9.3	13.9	18.6	23.2	27.9	32.5	37.2	41.8
2	-4	10	- 0	100		40 0	1	0	37	
1	3	5.1	10.1	15.2	20.3	25.3	30.4	35.5	40.6	45.6
1	31	5.5	11.0	16.5	22.0	27.5	32.9	38.4	43.9	49.4
13	31	5.9	11.8	17.7	23.7	29 6	35.5	41.4	47.3	53.2
122 122 123 123	33	6.3	12.7	19.0	25.3	31.7	38.0	44.4	50.7	57.0
		2 3	00	0	10.0	15 0	100	21 1	11.	D. C.
1/2	4	6.8	13.5	20.3	27.0	33.8	40.6	47.3	54.1	60.8
1			- 1				1	1		

TABLE III.

-	11	1	1	1	1	1	1	1	1	1
Thiol-	Width.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
ir	ı. in.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
38	24	34.9	36.3	41.8	45.3	48.8	52.3	55.8	59.3	62.7
38	3	38.0	41.8	45.6	49.4	53.2	57.0	60.8	64.6	
8	31	41.2	45.3	49.4	53.6	57.7	61.8	65.9	70.0	74.2
දේක දේක දේක දේක	31/2	44.4	48.8	53.2	57.7	62.1	66.5	71.0	75.4	79.9
8	34	47.5	52.3	57.0	61.8	66.5	71.3	76.0	80 8	85.5
1		V	The pr	10	A1 -	100	-r-		0	
व्यक्तिक व्यक्तिक व्यक्तिक व्यक्तिक	4	50.7	55.8	60.8	65.9	70.9	76.0	81.1	86.2	91.2
38	41	53.9	59.8	64.7	70.0	75.4	80.8	86.2	91.6	97.0
38	41/2	57.0	62.7	68.4	74.2	79.9	85.6	91.3	97.0	102.7
38	484	60.2	66.2	72.2	78.3	84.3	90.3	96.3	102.3	108.4
1	-	20.0	00.5	-	00	00 5	0.7		105 5	
8	5	63.3	697	76.0	82.4	88.7	95.0	101.4	107.7	114.0
8	51	66 5	73.2	79.8	86.5	93.1	99.8	106.5	113.1	119.8
දේශ දේශ දේශ දේශ	51	69.7	76.7	83.7	90.6	97.6	104.5	111.5	118.5	125.5
8	58	72.8	80.2	87.5	94.7	102.0	109.3	116.6	123.9	131.2
3 8	6	Fa.0	00.0	01.0	00.0	100 =	114.	101 5	100.0	100.0
8	0	76.0	83.6	91.2	98.9	106 5	114.1	121.7	129.3	136.9
1	,	10.0	10.0	90.9	22.0	23.7	0=.4	07.0	00.5	20.4
12	1 1 1 1 1 1 1 1 1 1 1 1	16.6	18.6	20.3	27 5		25.4	27.0	28.7	30.4
1212121		21.1	23.2	25.3	33.0	29·6 35·5	31.7	33.8	35·9 43·1	38.0
1 2	11					41.4		40.6		45.6
1	184	29.6	32.5	35.2	38.5	41.4	44.4	47.3	50.3	53.2
1	2	33.8	37.2	40.6	43.9	47.3	50.7	54.1	57.5	60.8
1	21	38.6	41.8	45.6	49.4	53.2	57.0	60.8	64.6	68.4
2	23	42.2	46.5	50.7	51 9	59.1	63.4	65.6	71.8	76.0
12121212	2号	46.5	51 1	55 8	60.4	65.1	69.7	74.4	79.0	83 6
2	44	40 9	91 1	99 0	00 4	05 1	09.1	144	19 0	00 0
1	3	50.7	55.8	60.8	65.9	70.9	76 0	81.1	86.2	91.2
1	31	54.9	60.4	65.9	71.4	76.9	82.4	87.9	93.3	98.8
1	31	59.2	65.1	71.0	76.9	828	88.7	94.6	100.6	106.5
12121212	34	63.3	69.7	76.0	82.4	88.7	95.0	101.4	107.7	114.0
2	4	1000	00 1	.00	32 4	30 1	99 0	1014	1011	1110
1/2	4	67.6	74.4	84.1	87.9	94.6	101.4	108.2	114.9	121.7
2		0. 9	1 1	31.1	3.0	010	101 1	100 2	1110	
,										1

TABLE III.

Thick	Width.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
ir	in.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
1	11	7.2	14.4	- 21.5	28.7	35.9	43.1	50.3	57.4	64.6
1212	11	7.6	15.2	22.8	30.4	38.0	45.6	53.2	60.8	68.4
1 2	13	8.0	16.1	24.1	32.1	40.1	48.2	-56.2	64 2	72.2
1.			200	2.0	30. 3	100 10	(b) 1	0	Th. 12	0.13
12121212	5	8.4	16.9	25.3	- 33 8	42.2	50.7	59.1	67.6	
1 2	54	8.9	17.7	26.6	35.5	44.4	53.2	62.1	71.0	79.9
1 2	51	9.3	18.6	27.9	37.2	46.5	55.8	65.1	74.4	83.7
2	534	9.7	19.4	29.2	38.9	48.6	58.3	68.0	77.7	87 5
1/2	6	10.1	20.3	30.4	40.6	50.7	60.8	70.9	81.1	91.2
2		101	200	50 1	100	00 1	000		011	01 2
5	1	2.1	4.2	6.3	8.4	10.6	12.7	14.8	16.9	19.0
प्रदेश क्षेत्र क्षेत्र क्षेत्र	14	2.6	5.3	7.9	10.6	13.2	15.8	18.5	21.1	23.8
58	11	3.2	6.3	9.5	12.7	15.8	19.0	22.2	25.4	28.5
5 8	184	3.7	7.4	11.1	14.8	18.2	22.2	25.9	29.6	33.3
			1				Dr. 1	155	17000	1 000
age	2	4.2	8.4	12.7	. 16.9	21.1	25.3	29.9	33.8	38.0
orba orba orba orba	24	4.8	9.5	14.3	19.0	23.8	28.5	33.3	38.0	42.8
8"	21	5.3	10.6	15·8 17·4	21.1	26.4	31.7	37.0	42.2	47·5 52·3
150	23	5.8	11.6	17.4	25.2	29.0	94.0	407	40.0	04 0
I	3	6.3	12.7	19.0	25.3	31.7	38.0	44.4	50.7	57.6
to co	31	6.9	13.7	20.6	27.5	34.3	41.2	48.1	54.9	61.8
50	31	7.4	14.8	22.2	29.6	37.0	44.4	51.8	59.2	66.5
onlas onlas metas mes-s	33	7.9	158	23.8	31.7	39.6	47.5	55.5	63.4	71.3
	*	18	101	4.5	the second	10 14	1		4	
ation action action action	4	8.4	16.9	25.3	33.8	42.2	50.7	59.1	67.6	76.0
58	41	9.0	18.0	26.9	35.9	44.9	53.9	62.9	71.8	80.8
50	41	9.5	19.0	28.5	38.0	47.5	57.0	66.5	76.1	85.6
Sic	44	10.0	20.1	30.1	40.1	50.2	60.2	-70.2	80.3	90.3
5	5	10.6	21.1	31.7	42.3	52.8	63.4	73.9	84.5	95.1
הלים מלכו מלכו מלכו	5분	11.1	22.2	33.3	44.4	55.5	66.5	77.6	88.7	998
5	51	11.6	23 2	34.9	46.5	58.1	69.7	81.3	92.9	104.6
50	53	12.1	24.3	36.4	48 6	60.7	72.9	85.0	97.2	109.3
	-		1				- 11			

TABLE III.

Thick.	Width.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
in:	lbs.	lbs.	lbs.	lbs.	ibs.	lbs.	lbs.	lbs.	lbs.	lbs.
12121	4½ 4½	71·8 76 0	79·0 83·6	86·2 91·2	93·4 98·9	100·5 106·5	107·7 114·1	114·9 121·7	122·1 129·3	129·3 136·9
	44	80.3	88.3	96.3	104.3	112.4	120.4	128.4	136.4	144.5
12 12 12 12	5 5 <del>1</del>	84 5 88 7	92·9 97 6	101·4 106·5	109·8 115·4	118·3 124·2	126·7 133·1	$135.2 \\ 142.0$	143.6 150.8	152·1 159·7
1/2 1/2	5½ 5¾	93·0 97·2	102·2 106·9	111·5 116·6	120·8 126·3	130·1 136·0	139 4 145 8	148·7 155·5	158 0 165 2	167·3 174·9
1/2	6	101.4	111.5	121.7	131.8	141.9	152.1	162:2	172.4	182.5
מלינו מלינו מלינו	1 1 <del>1</del>	21·1 26·4	23·2 29·0	25·3 31·7	27·5 34·3	29·6 37·0	31·7 39·6	33.8 42.2	35·9 44·9	38·0 47·5
מקבו מקבו מ	1 1 2 1 3	31·7 37·0	34·8 40·7	38·0 44·4	41·2 48·1	44·4 51·8	47·5 55·5	50·7 59·2	53·9 62·8	57·0 66·5
	2	42.2	46.5	50.7	54.9	60.1	63.4	67.6		
15/00 15/00 15/00 15/00 15/00 15/00 15/00 15/00	$\frac{2\frac{1}{4}}{2\frac{1}{2}}$	47.5 52.8	52·3 58·1 63·9	57·0 63·4 69·7	61·8 68·6 75·5	66.5 $73.9$ $81.3$	71.3 $79.2$ $87.1$		80.8 89.5 98.7	\$5.5 95.0
	2 <del>8</del> 3	58·1 63·3	69.7	76.0	82.4	88.7	95.0	92 9	107.7	104.5
ज्ञिक ज्ञिक ज्ञेक ज्ञेस	3 <del>1</del> 3 <del>1</del>	68·7 73·9	75·5 81·3	82·4 88·7	89·3 96·1	96·1 103·5	103.0	109.9	116.7 125.7	123.6 133.1
558	34	79.2	87.1	95.1	103.0	110.9	118.8	126.8	134.7	142.6
क्षेत्र क्षेत्र	4 41	84·5 89·8	92.9 98.8	101·4 107·8	109·8 116·7	118·3 125·7	126.7 134.7	135·2 143·7	143.6 152.6	152·1 161·6
क्षेत्र क्षेत्र क्षेत्र क्षेत्र	4½ 4½	95·1 100·3	104.6 110.4	114·1 120·4	123.6 130.4	133·1 140·5	$142.6 \\ 150.5$	152·1 160·5	161.6 170.6	171·1 180·6
5/8 5	5	105.6	116·2 122·0		137·3 144·2	147·9 155·3	158.4	169 0		190.1
5/8 5/8 5/8 5/8	5½ 5½ 5¾	110.9 116.2 121.5	127.8	139.4	151.0 157.9		$166.4 \\ 174.3 \\ 182.2$	177.5 185.9 194.3	197.5	209.1
8	J'À	1213	1,50	1101	1979	1700	1642	194.9	200 5	2100

TABLE III.

Thick.	Width.	1 ft.	2 ft.	3 ft.	4 ft.	5 ft.	6 ft.	7 ft.	8 ft.	9 ft.
in.	in.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
5	6	12.7	25.8	38.0	50.7	63.4	76.0	88.7	101.4	114.1
214	1	2.5	5.1	7.6	10.1	12.7	15.2	17.7	20.3	22.8
34	$\frac{1\frac{1}{4}}{1\frac{1}{2}}$	3·2 3·8	6·3 7·6	9·5 11·4	12·7 15·2	15·8 19·0	19·0 22·8	22·2 26·6	25·4 30·4	28·5 24·2
প্ৰাৰ প্ৰাৰ প্ৰাৰ	134	4.4	8.8	13.3	17.7	22.2	26.6	31.1	35.5	39.9
34	2	5.1	10.1	15.2	20.3	25 3	30.4	35.5	40.6	45.6
84	24	5·7 6·3	11.4	17:1	22·8 25·3	28·5 31·7	34·2 38·0	39.9	45.6	51.3
জ্বৰ জ্বৰ জ্বৰ জ্বৰ	$\frac{2\frac{1}{2}}{2\frac{8}{4}}$	7.0	13:	19·0 20·9	27.9	34.9	41.8	48.8	50·7 55·8	57·0 62·7
84	3	7.6	15.2	22.8	30.4	38.0	45.6	53.2	60.9	68.4
84	31	8.2	16.5	24.7	33.0	41.2	49.4	57.7	65.9	74.2
व्यक्त व्यक्त व्यक्त	$\frac{3\frac{1}{2}}{3\frac{8}{4}}$	8·9 8·9	17·7 19·0	26.6 28.5	35·5 38·0	44·4 47·5	53·2 57·0	62·1 66·5	71·0 76·1	79·9 85·6
34	4	10.1	20.3	30.4	40.6	50.7	60.8	70.9	81.1	91.2
84	44	10.8	21.5	32.3	43.1	53.9	64.6	75.4	86.2	97.0
34848484	$\frac{4\frac{1}{2}}{4\frac{3}{4}}$	$11.4 \\ 12.0$	22·8 24·1	34·2 36·1	45.6 48.2	57·0 60·2	$\begin{array}{c} 68.4 \\ 72.2 \end{array}$	79·9 84·3	91.3	102·7 108·4
34	5	12.7	25∙8	38.0	50.7	63.4	76.0	88.7	101.4	114.0
84	51	13 3	26.6	39.9	53.2	66.5	79.8	93 1	106.5	119.8
34 84 84 84	$5\frac{1}{2}$ $5\frac{3}{4}$	13·9 14·6	27·9 29·1	41·8 43·7	55·8 58·3	69.7 72.9	83.7 87.4	97.6 102.0	111·5 116·6	125·5 131·2
84	6	15.2	30.4	45.6	60.8	76.0	91.2	106.2	121.7	136.9
1	13	5.1	10.1	15.2	20.3	25.3	30.4	35.5	40.6	45.6
1	2	6.8	13.5	20.3	27.0	33.8	40.6	47.8	54.1	60.8
1	3	10.1	20.3	30.4	40.6	50.7	60.8	70.9	81.1	91.2
1	4	13.5			54·1 67·6	67.6 84.5	81·1 101·4	94·6 118·3	108·1 135·2	121·7 152·1
1 1	5	20.3			81.1	101.4	121.7	141.9	162.2	182.5

TABLE III.

			4		11					
1,2	اجرا	4000	0 0 001			ril o	_1		4-14	
Thick.	Width.	10 ft.	11 ft.	12 ft.	13 ft.	14 ft.	15 ft.	16 ft.	17 ft.	18 ft.
E	1									
-			11 11 11						J	0.00
100	in.	D. a	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	007
in.	0.0	lbs.	0.0	1000	-			150		lbs.
5 8	6	126.7	139.4	152.1	164.8	177.4	190.1	202.8	215.4	228 1
109	1/0	0.0000.10	0.99	INC.	1 (-11-			1 100	0 5-1	79
84 84	1	25.3	27.9	30.4	33.0	35.5	3810	40.6	43.1	45.6
3	114	. 31.7	34.9	38.0	41.2	44.4	47.5	50.7	53.9	57.0
84	11	- 38.0	41.8	45.6	59.4	53.2	57.(	60.8	64.6	68.4
34	13	44.4	48.8	53.2	57.7	62.1	66:5	71.0	75.4	79.9
0	0	-	Will	00.0	25.0	50.0	ha	01.1	0.0	
अंक अंक अंक अंक	2	50.7	55.8	60.8	65.9	70.9	76.0	81.1	86.2	91.2
4	21	57.0	62.7	68.4	74.2	79.9	85.5	91.3		102.7.
4	21	63.3	69.7	76.0	82.4	88.7	95.0	101.4	107.7	114.0
4	24	69.7	76.7	83.7	90.6	97.6	104.5	111.9	118.5	125.5
0	0	F. 0. 0	00.0	0.1.0	00.0	100.5	114.1	101.5	100.0	1000
क्षेत्र क्षेत्र क्षेत्र	3	76.0	83.6	91.2	98.9	106.5	114:1	121.7	129.3	136 9
4	31	82.4	90.6	98.9	107.1	115.3	123.6	131.8	140.0	
4	31/2	88.7	97.6	106.5	115·4 123 6	124.2	133.1	142.0 152.1	150.8	159.7
34	34	95.1	104.6	114.1	125 6	133.1	142'0	152.1	161.6	171.1
8	4	101.4	111.5	121.7	131.3	141.9	152.1	162.2	172.4	100.5
84 8	41	107.7	118.5	129.3	140.1	150.8	161.6	172.4	183.2	182·5 193·9
84 84	41	114.1	125.5	136.9	148.3	159.7	171.1			
84	43	120.4	132 4	144.5	156.5	168.6	180 6	192.6		216.7
4	44	120 4	102 4	144 0	100 0	1000	100 0	102.0	204 1	2101
3	5	126.7	139.4	152.1	164.8	177.4	190.1	202.8	215.4	228.1
34 34 34	51	133.1	146.4	159.7	173.0	186.3		212.9		
8	51.	139.4	153.3	167.3	181.2	195.2	209.2	223.1	237.0	
84	5辈	145.7	160.3	174.9	189.5	204.0	218.6	233.2		262.3
4	04	110	1000	1110	1000	2010	210 0	2002	2110	2020
84	6	152.1	167.3	182.5	197.7	212.9	228:1	243:3	258.5	273.7
4		1204		2020	1011		22012		2000	
1	11	50.7	55.8	60.8	65.9	70.9	76.0	81.1	86.2	91.2
1	2	67.6	74.4	81.1	87.9	94.6			114.9	1
1	3	101.4	111.5	121.7	131.7	141.9		162.2	1	
1	4	135.2	148.7	162.2	175.7	189.3	202.8		229 8	
1	5	169.0			219.7	236.6				
1	6	202.8		243.3		283.9	304.2			
1										
L .	•	1	-			-	-		-	

### TABLE OF GRADIENTS

And Resistance per Ton for each.

Vertica	I Rise.	Gravity due to	Vertica	al Rise.	Gravity due to	Vertic	al Rise.	Gravity due to
Ratio.	Pr. Mile.	incline per ton.	Ratio.	Pr. Mile.	incline per ton.	Ratio.	Pr. Mile.	incline per ton.
					-	1		377
one in	Feet.	lbs.	one in	Feet.	lbs.	one in	Feet.	lbs.
100	52.80	22:40	74	71.38	32.270	. 47	112.34	47.660
99	53.33	22.626	73	72.32	30.685	46	115.04	48.684
98	53.88	22.858	72	73.33	31.111	45	117.33	
97	54.43	23.092	71	74.36	31.550	44	120.00	50.908
96	55.00	23.334	70	75.43	32.000	43	12278	52.092
95	55 60	23.579	69	76.49	32.464	42	125.71	53.333
94	56.17	23.830	68	77.64	32.940	41	128.78	54.634
93	56.77	24.086	67	78.81	33.432	40	132.00	56.00
92	57.52	24.342	66	80.0	33.940	39	135.38	57.436
91	58.02	24.614	65	81.23	34.460	38	138 95	58.944
90	58.66	24.888	64	82.50	35.0	37	142.70	60.540
89	59.33	25.168	63	83.81	35.555	36	146.66	62.222
88	60.0	25.454	62	85.16	36.108	35	150.84	64.000
87	60.69	25.746	61	86.55	36.720	34	155.30	65.880
86	61.39	26.046	60	88 00	37.333	33	160.0	67.880
85.16	62.00	26.303	59	89.49	37 966	32	165 0	70.0
85	62.12	26.353	58	91.03	38.620	31	170.32	
84	62.86	26.666	- 57	92.63	39.298	30	176.00	74.666
83	63.61	26.988	. 56 .	94.28	40.0	29	182.06	the second of
82	64.39	27.317	55	96.00	40.726	28	188.56	
81	65.20	27.718	54	97.77	41.480	27	195.55	
80	66.0	28.00	53	99 62	42.264	26	203.06	
79	66.83	28.355	52	101.53	1	25	211.20	
78	67.69	28.718	51	103.52		24	220.0	93.336
. 77	68.57	29.090	50	105.60		23	229.56	
76	69.47	29.472	49	107.75	45.716	22	240	101.816
75	70.40	29.867	48	110.00		21	251.43	
	10	2000	10	11000	10000	1000	201 10	10000

To take Impressions from Coins, &c.—Make a thick solution of isinglass in water, and lay it hot on the metal; let it remain for twelve hours, then remove it, breathe on it, and apply gold or silver-leaf on the wrong side. Any color may be given to the isinglass instead of gold or silver, by simple mixture.

Variations in Tides.—The difference in time between high water averages about 49 minutes each day.

TABLE of the Ultimate Breaking Weight, in tons, of cast-iron pillars, calculated from Professor Hodgkinson's Formula.

The length includes every half-foot from 1 to 20, and the diameter every inch from 1 to 24.

The length metades every nativious from 1 to 20, and the diameter every men from 1 to							
NGTII IN EET.	DIA	METER O	F CAST-IR	ON PILLAF	RS IN INCH	ies.	
LENGTHI IN FEET.	1	2	3	4	5	6	
A Bound	tons.	tons.	tons.	tons.	tons.	tons.	
1	44.30	537	2312	6513	14544	28038	
$\hat{1}_{\frac{1}{2}}$	22.23	269	1160	3269	7300	14073	
22	13.63	165	711	2004	4476	8630	
$2 \over 2 \frac{1}{2}$	9.33	113	487	1372	3064	5905	
3	6.84	83	357	1006	2247	4331	
$3\frac{1}{2}$	5.26	64	275	774	1729	3333	
4	4.19	51	219	617	1378	2656	
41	3.43	41.6	179	505	1127	2174	
5	2.87	34.8	150	422	943	1817	
$5\frac{1}{2}$	2.44	29.6	127	359	802	1545	
6	2.11	25.5	110	309	691	1333	
61/2	1.84	22.3	96	270	603	1163	
7	1.62	19.6	84.6	238	532	1026	
71	1:44	17.5	75.2	212	473	912	
8	1.29	15.6	67.4	190	424	817	
81/2	1.16	14.1	60.8	171	382	737	
9	1.06	12.8	55.2	155	347	669	
91	.96	11.7	50.3	142	316	610	
10	.88	10.7	46.1	130	290	559	
101	·81	9.86	42.4	119	267	515	
11	.75	9.11	39.2	110	246	475	
111	.69	8.45	36.3	102	228	441	
12	:65	7.86	33.8	95.3	212	410	
$12\frac{1}{2}$	.60	7:33	31.5	88.9	198	383	
13	. 56	6.86	29.5	83.2	185	358	
131	•53	6.43	27.7	78.0	174	336	
14	.50	6.05	26.0	73.3	163	315	
141	.47	5.70	24.5	69.1	154	297	
15	*44	5.38	23.15	65.23	145.6	280.8	
$15\frac{1}{2}$	.42	5.09	21.90	61.69	137.7	265.5	
16	•40	4.82	20.75	58.45	130.5	251.6	
161/2	377	4:57	19.69	55.47	123.8	238.8	
17	358	4:35	18.72	52.73	117.7	227.0	
17½	341	4.14	17.82	50.19	112.1	216.1	
18	·325 ·310	3.94	16.98	47.85	106.8	205.9	
$18\frac{1}{2}$	297	3·77 3·60	16.21	45.67	101.9	196.6	
19	284	3.44	15.49	43.64	97.45	187.8	
$\frac{19\frac{1}{2}}{20}$	272	3.30	14.82 11.20	41.76	93.24	179.7	
20	212	5.90	1120	40.00	89.32	172.2	

TABLE of the Ultimate Breaking Weight, in tons, of cast-iron pillars.
(Continued.)

н	DIA	METER OF	CAST IR	ON PILLAR	S IN INCI	HES.
LENGTH IN FEET.	7	8	9	10	11	12 =
	tons.	tons.	tons.	tons.	tons.	tons.
1	48838	78982	120691	176361	248552	339982
11/2	24513	39643	60579	88520	124756	170648
2	15031	24310	37147	54282	76501	104643
$2\frac{1}{2}$	10286	16635	25420	37145	52350	71607
3	7544	12202	18645	27246	38398	52523
$3\frac{1}{2}$	5805	9388	14347	20965	29546	40414
4	4626	7482	11433	16707	23546	32207
41/2	3787	6124	9358	13675	19273	26363
5	3166	5120	7824	11433	16113	22039
51/2	2692	4354	6653	9722	13703	18743
6	2322	3755	5738	8385	11818	16165
$6\frac{1}{2}$	2026	3277	5008	7319	10315	14109
7	1787	2889	4415	6452	9094	12439
71/2	1589	2570	3927	5738	8087	11062
8	1424	2302	3519	5142	7247	9913
81/2	1284	2077	3174	4638	6537	8942
9	1165	1885	2880	4209	5932	8114
91	1063	1719	2627	3839	5411	7401
10	974	1575	2408	3519	4959	6783
10½ 11	897	1450	2216	3238	4564	6243 5769
	828 768	1340 1242	2048	2992 2774	4217 3910	5349
$\frac{11\frac{1}{2}}{12}$	714	1156	1898 1766	2581	3637	4975
121	666	1078	1647	2408	3393	4642
13	623	1008	1541	2252	3174	4343
131	585	946	1445	2112	2977	4073
14	550	889	1359	1986	2799	3828
141	518	838	1280	1871	2637	3607
15	489.1	791.0	1208	1766	2489	3405
151	462.6	748.1	1143	1671	2354	3220
16	438.3	708.8	1083	1583	2230	3051
161	415.9	672.6	1028	1502	2117	2895
17	395.3	639.4	977.0	1428	2012	2752
171	376.3	608.6	930.1	1359	1915	2620
18	358.7	580.2	886.5	1295	1826	2497
181	342.4	553 8	846.2	1236	1743	2384
19	327.2	529.2	808.7	1182	1665	2278
191	313.1	506.4	773.8	1131	1593	2179
20	299.9	485.0	741.2	1083	1526	2088

Note.—Example. Find the breaking weight of a cast-iron pillar whose external diameter is 17, and internal diameter 15 inches, and length 18 feet.

TABLE of the Ultimate Breaking Weight, in tons, of cast-iron pillars.

(Continued.)

(Continued.)								
ENGTH IN FEET.	DIA	METER O	F CAST-IRO	ON PILLAF	s in inch	HES.		
LENGTH IN FEET.	13	14	15	16	17	18		
	tons.	tons.	tons.	tons.	tons.	tons.		
1	453524	592195	759158	957714	1191290	1463470		
11/2	227638	297241	381039	480707	597950	734563		
2	139588	182269	233660	294769	366664	450443		
21	95522	124729	159895	201717	250912	308238		
3	70064	91486	117281	147955	184040	226088		
31	53912	70396	90243	113846	141614	178966		
4	42963	56100	71917	90726	112853	138638		
1 41	35187	45920	58867	74263	92375	113481		
× 5	29400	38390	49213	62085	77228	94871		
$5\frac{1}{2}$	25002	32647	41851	52798	65676	80680		
6	21565	28158	36097	45538	56645	69586		
$6\frac{1}{2}$	18821	24576	31505	39745	49439	60734		
7	16593	21667	27776	35040	43587	53545		
7 1	14756	19269	24701	31163	38763	47619		
8	13223	17267	22135	27924	34735	42671		
81/2	11928	15576	19967	25190	31333	38492		
9	10824	14133	18118	22857	28432	34928		
91	9873	12892	16527	20850	25935	31861		
10	9049	11815	15147	19109	23769	29200		
$10\frac{1}{2}$	8329	10875	13941	17588	21877	26876		
11	7695	10048	12882	16250	20214	24832		
111	7135	9317	11944	15067	18743	23025		
12	6637	8667	11110	14016	17434	21418		
$12\frac{1}{2}$	6192	8086	10365	13076	16265	19982		
13	5793	7564	9697	12233	15216	18693		
$13\frac{1}{2}$	5433	7094	9094	11472	14271	17531		
14	5107	6669	8549	10785	13415	16481		
141/2	4811	6282	8054	10160	12638	15526		
15	4542	5931	7603	9591	11930	14656		
$15\frac{1}{2}$	4296	5609	7191	9071	11283	13862		
16	4070	5314	6813	8595	10691	13103		
161	3863	5044	6466	8157	10146	12464		
17	3671	4794	6146	7753	9424	11847		
171	3495	4563	5850	7380	9180	11277		
18	3331	4350	5577	7035	8571	10750		
181	3180	4152	5323	6715	8353	10261		
19	3039	3968	5087	6417	7983	9806		
191	2908	3797	4867	6140	7638	9383		
20	2785	3637	4662	5881	7316	8987		

Along the line marked 18 feet, and in the vertical lines numbered 17 and 15 inches, take the numbers 8751 and 5577; the difference of which, namely 3174, will be the breaking

TABLE of the Ultimate Breaking Weight, in tons, of cast-iron Pillars.

(Continued.)								
LENGTH IN FEET.	DIAMETER OF CAST IRON PILLARS IN INC.							
LEN	19	20	21	22	23	24		
James	tons.	tons.	tons.	tons.	tons.	tons.		
07/14/1	1777940	2138510	2549140	3013880	3536910	4122530		
11/2	892404	1073380	1279490	1512760	1775280	2069230		
2	547224	658204	784589	927630	1088610	1268880		
21/2	374471	450416	536902	634786	744947	868292		
3	274670	330374	393810	465605	546409	636880		
31	211350	254212	303024	358269	420444	490059		
4	168428	202586	241485	285511	335059	390543		
41/2	137865	165825	197666	233703	274260	319671		
5	115257	138632	165251	195378	229286	267248		
$5\frac{1}{2}$	98017	117894	140532	166157	194988	227273		
6	84539	101684	121210	143307	168177	196023		
$6\frac{1}{2}$	73784	88748	105789	125047	146781	171085		
7	65051	78243	93266	110270	129406	150832		
7-5	57851	69584	82944	98067	115085	134140		
8	51840	62353	74326	87876	103126	120200		
81/2	46763	56247	67047	79271	93028	108430		
9	42433	51038	60840	71930	84414	98390		
$9\frac{1}{2}$	38707	46557	55496	65614	77000	89750		
10	35474	42669	50862	60134	70571	82255		
$10\frac{1}{2}$	32651	39272	46814	55348	64954	75708		
11	30168	36286	43254	51140	60014	69951		
$11\frac{1}{2}$	27973	33645	40106	47417	55646	64860		
12	26020	31297 -	37306	44108	51763	60333		
$12\frac{1}{2}$	24275	29199	34805	41150	48292	56288		
13	22710	27315	32560	38497	45178	52658		
$13\frac{1}{2}$	21298	25618	30537	36104	42370 39830	49385 46424		
14	20021	24082	28706 27043	33940 31974	37523	43736		
$14\frac{1}{2}$	18862	22687 21417	25529	30184	35421	41286		
15	17806 16840	20255	24145	28547	33501	39049		
$15\frac{1}{2}$ $16$	15955	19191	22823	27047	31740	36997		
	15142	18213	21711	25669	30123	35111		
$\frac{16\frac{1}{2}}{17}$	14393	17312	20636	24398	28632	33374		
171	13701	16480	19644	23225	27255	31768		
18	13060	15709	18725	23223	25981	30283		
181	12466	14994	17873	21131	24799	28906		
19	11913	14330	17081	20195	23700	27624		
19\frac{1}{2}	11398	13710	16343	19322	22676	26430		
20	10918	13133	15654	18508	21721	25317		
10120	10010	10190	1 10001	10000	211-1	20721		

weight in tons. For practical purposes the pillars should be calculated to bear one half more than the weight to which they are subjected.

# TABLE OF STRENGTHS OF CAST-IRON SHAFTS.

The cube of the diameter of a journal or shaft of sufficient strength is directly as the horse power, and inversely as the number of revolutions of the shaft per minute. Mr. Robertson Buchanan deduced from several experiments that a journal suitable to a 50-horse engine, making 50 revolutions per minute, should be 71 inches in diameter. is from these data the following table has been computed.

# NUMBER OF REVOLUTIONS OF SHAFT PER MINUTE.

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TABLE OF STRENGTHS OF CAST-IRON SHAFTS. (Continued.)

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-									- 6		-		
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7.5		2 30			
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		5 20	1 10 0 10 10 10 10 10 10 10 10 10 10 10		
5.95	BIE	15			
- 123	TACE	261011	10 6 8 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9		
1'vo G see H   Horse Pow'r.					

(Continued. STRENGTHS OF OF TABLE

TABLE

Showing the Strength of the Teeth of Cast-Iron Wheels at a given Velocity.

Pitch of	Thick- ness of	Breadth of teeth	Strength of teeth in horse power at							
teeth in inches. in inches.		3 feet per second.	4 feet per second.	6 feet per second.	8 feet per second.					
3.89	1.9	7.6	20.57	27.43	41.14	54.85				
3.78	1.8	7.2	17.49	23.32	34.98	46.64				
3.57	1.7	6.8	14.73	19.65	29.46	39.58				
3.36	1.6	6.4	12.28	16.38	24.56	32.74				
3.15	1.2	6	10.12	13.20	20.24	26.98				
2.94	1.4	5:6	8.22	10.97	16.44	21.92				
2.73	1.3	5 2	6.58	8.78	13.16	17.54				
2:52	1.2	4:8	5.18	6.91	10.36	13.81				
2.31	1.1	4.4	3.39	5.32	7.98	10.64				
2.1	1.0	4	3.00	4.00	6.00	8.00				
1.89	. 9	3.6	2.18	2.91	4.36	5.81				
1.68	.8	3.5	1.53	2.04	3.06	3.08				
1.47	.7	2.8	1.027	1.37	2.04	2.72				
1.26	. 6	2.4	.64	.86	1.38	1.84				
1.05	.2	2	•375	. 50	.75	1.00				

FURNITURE OIL.—1. Linseed oil 1 pint, alkanet ½ oz. Digest in a warm place till colored, and strain.

2. The same, with \( \frac{1}{4} \) pint of oil of turpentine.

3. Linseed oil 1 pint, alkanet root 1 oz., rose pink 1 oz. Let them stand in an earthen vessel all night.

4. A quart of linseed oil, 6 oz. of distilled vinegar, 3 oz. of spirit of turpentine, 1 oz. of muriatic acid, and 2 oz. of spirit of wine.

5. Linseed oil 8 oz., vinegar 4 oz., oil of turpentine, mucilage, rectified spirit, each \(\frac{1}{2}\) oz.; butter of antimony \(\frac{1}{2}\) oz.; muriatic acid 1 oz. Mix.

6. Linseed oil 16 oz., black rosin 4 oz., vinegar 4 oz., rectified spirit 3 oz., butter of antimony 1 oz., spirit of salts 2 oz.; melt the rosin, add the oil, take it off the fire, and stir in the vinegar; let it boil for a few minutes, stirring it; when cool put it into a bottle, add the other ingredients, shaking all together. [The last two are especially used for reviving French polish.]

7. Linseed oil 1 pint, oil of turpentine  $\frac{1}{2}$  pint, rectified spirit 4 oz., powdered rosin  $1\frac{1}{2}$  oz., rose pink  $\frac{1}{2}$  oz. Mix.

8. Linseed oil 14 oz., vinegar 1½ oz., muriatic acid ½ oz. Mix.

TABLE

Showing how to ascertain the weights of Pipes, of various Metals, and any diameter required.

Thick- ness in parts of an inch.	Wrought iron.	Copper.	Lead.
101 100 0 48 5 0 5 0 10 10 10 14	· 326 · 653 · 976 1 · 3 1 · 627 1 · 95 2 · 277 2 · 6	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 lbs. lead, '483 4 " '967 5½ " 1.45 8 " '1.933 9¼ " 2.417 11 " 2.9 13 " 3.883 15 " 3.887

Rule. To the interior diameter of the pipe, in inches, add the thickness of the metal; multiply the sum by the decimal numbers opposite the required thickness, and under the metal's name; also, by the length of the pipe in feet; and the product is the weight of the pipe in lbs.

1. Required the weight of a copper pipe whose interior diameter is  $7\frac{1}{2}$  inches, its length  $6\frac{1}{4}$  feet, and the metal  $\frac{1}{8}$  of an inch in

thickness.

$$7.5 + .125 = 7.625 \times 1.52 \times 6.25 = 72.4$$
 lbs.

2. What is the weight of a leaden pipe 18½ feet in length, 3 inches interior diameter, and the metal ½ of an inch in thickness?

$$3 + .25 = 3.25 \times 3.867 \times 18.5 = 232.5$$
 lbs.

Note.-Weight of a cubic inch of

Lead	equal	*4103	lb.
Copper, sheet	7.	*3225	- 44
Brass, do.	66	*3037	66
Iron. do.	66 01	*279	66
Iron, cast	65	'263	66
Tin, do.	46	'2636	46
Zinc. do.	44	26	66
Water	66	03617	46

SHI WALLED TO

- Harry Com Bullioner

To solder Tortoise-shell.—Bring the edges of the pieces of shell to fit each other, observing to give the same inclination of grain to each, then secure them in a piece of paper, and place them between hot irons or pincers; apply pressure, and let them cool. The heat must not be so great as to burn the shell, therefore try it first on a piece of white paper.

TABLE

Of the Weight of Cast-Iron Balls.

Diameter in inches.	Weight in lbs.	Diameter in inches.	Weight in lbs.	Diameter in inches.	Weight in lbs.
2	1.10	6	29.72	10	137.71
21	1.57	61	33.62	104	148 · 28
$2\frac{1}{2}$ $2\frac{8}{4}$	2.12	$6\frac{1}{2}$	37.80	101	159.40
	2.86	634	42.35	1084	171.05
3	3.72	7	47.21	11	183 · 29
$\frac{3\frac{1}{4}}{3\frac{1}{2}}$	4.71	74	52.47	111	196.10
$3\frac{1}{2}$	5.80	$7\frac{1}{2}$ $7\frac{3}{4}$	58.06	111	209.43
38	7.26	- 74	64.09	113	223.40
4	8.81	. 8	70.49	12_	237 · 94
4½ 4½ 4¾	10.57	81	77.32	121	253 · 13
$4\frac{1}{2}$	12.55	$8\frac{1}{2}$	84.56	$12\frac{1}{2}$	268 · 97
434	14.76	834	92.24	128	285.37
5	17.12	9	100.39	13	302.41
51	19.93	91	108.98	131	320.80
$5\frac{1}{2}$	22.91	$9\frac{1}{2}$	118.06	$13\frac{1}{2}$	338.81
5\frac{3}{4}	26.18	98	127.63	134	357 . 93

1. What will be the weight of a hollow ball or shell of cast-iron, the external diameter being 9½, and internal diameter 8½ inches?

Opposite 9½ are 118.06, and Opposite 8¾ are 92.24, subtract

25.82 lbs., weight required.

2. Requiring to remove a cast-iron ball 37.8 lbs. in weight, and in diameter 6½ inches, and replace it by one of lead of an equal weight, what must be the diameter of the leaden ball?

Weight of lead to that of east-iron = 1.56,

Then 
$$\frac{6\cdot5^3}{1\cdot56} = \sqrt[3]{176} = 5\cdot6$$
 inches, the diameter.

To transfer Engravings to Plaster Casts.—Cover the plate with ink, and polish its surface in the usual way; then put a wall of paper round it, and when completed pour in some finely powdered plaster of Paris mixed in water; jerk the plate repeatedly, to allow the air bubbles to fly upwards, and let it stand one hour; then take the east off the plate, and a very perfect impression will be the result.

	Ho	0.21	0.63	HAT			
	- cc 41	0.31 0.47 0.63	0.94 1.26 1.57	7 1911	110		
h.	-	0.42	1.26 1.68 2.10	2.52	4 01	7 E	4
ı lengt	14	0.52	1.57 2.10 2.62	3.15 3.67 4.20	4.72	V.	10
foot in	133	0.57	1.73 2.31 2.88	3.46 4.04 4.62	5.19	7	
IRON, per foot in length.	NCH.	0.63 0.94 1.26	1.89 2.52 3.15	3.78 4.41 5.04	5.67	2	No.
D IRC	OF AN INCH.	0.73 1:10 1.47	2.20 2.94 3.67	4.41 5.14 5.87	6.60 7.35 8.07	08.8	1
SOLLE		0.84 1.26 1.68	2.52 5.36 4.20	5.04 5.88 6.72	7.56 8.40 9.24	80.01	48
AND ROLLED	BREADTH IN INCHES AND PARTS  2\frac{2}{3} 2\frac{1}{3} 2\frac{1}{3} 2	0.94 (0.1.41)	2.83 3.78 4.72 4.72	5.66 6.61 7.56	0.10 %	11 · 34 10 13 · 22 15 · 12	
FLAT .	INCHES 23	1.05 1.57 1.57 1.10	3.15 4.20 5.25 4	30 35 40	550	12.60 11 14.70 13 16.80 15	1 100
OF	0'FH IN	152	3.46 4.62 5.77 5	93 08 24	39 9. 55 10. 70 11.		10
WEIGHT	3nead	1			10.	13	0 23.10
	60	1.26	3.78 5.04 6.30	7.56 8.82 10.08	11.34 12.60 13.86	15.12 17.64 20.16	25.20
F THE	148	1.36 2.04 2.73	4.09 5.46 6.82	8 - 19 9 - 55 10 - 92	12.28 13.65 15.01	16.38 19.11 21.84	27 - 39 32 - 76
TABLE OF	48	1.47 2.20 2.94	4.41 5.88 7.35	8.82 $10.29$ $11.76$	13.20 14.70 16.16	17·64 20·58 23·52	29·40 35·28
TAI	6.2 644	1.57 2.36 3.15	4.72 6.30 7.87	9.45 11.02 12.60	14·16 15·75 17·32	18.90 22.05 25.20	31.50 37.80
-711- -701-	4	1.68 2.52 3.36	5.04 6.72 8.40	10.08 11.76 13.44	15·12 16·80 18·48	20.18 23.54 26.88	33.65 40.32 47.04
	Thickness in inches and parts.	= xx  =  4	color tolor	014140 H	-1x -4 v/ss	# # 67 67 57 57	25 cc

TABLE of the Weight of Cast-Iron Pipes, in lengths.

						J					-		
Bore.	Thick.	Long.	Weight.	Bore.	Thick.	Long.	w	eight.	Bore.	Thick.	Long.	Wei	ight.
Inch.	In. 1/4	Ft. 3½	C. qr. lb.	Inch. 6½	In.	Ft.	2	gr. lb.	Inch. 11½	In, 1/2	Ft.	5 0	
11/2	800	$\frac{3\frac{1}{2}}{41}$	$\begin{array}{ccc} & 21 \\ & 21 \end{array}$		5 5 8	9		$\begin{array}{cccccccccccccccccccccccccccccccccccc$		1215/8 24	9	$\frac{6}{7} \frac{1}{2}$	
12	व्यक्त न्युंच	$4\frac{1}{2}$ $4\frac{1}{2}$	1 4		8 204	9	4	1 21		1	9	10 1	
2	150	6	1 8	13	1	9	6	0 14	12	1	9	5 0	24
0.1	ocho v	6	2 0	7	$\frac{1}{2}$	9		0 7	1	102 5/8 8/4 1	9	6 2	
$2\frac{1}{2}$	4 3	6	$\begin{array}{c} 1 & 16 \\ 2 & 10 \end{array}$		नियानीक क्षेत्र	9		3 20		4	9	7 3 10 3	
1 1	14 90 14 90 10	6	3 10	300	1	9	6	2 4	121		9	5 1	16
3	1	9	2 20	71/2	1 2	9		1 6		12 58 84	9	6 3	9
1100		9	1 0 6		12500 24	9		0 22		1	9	8 1 11 0	0 $21$
180	व्यंक नंत्र क्षेत्र क्षेत्र नंत्र क्षेत्र नंत्र क्षंत्र	9	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		1	9		0 0	13		9	5 2	20
30	8 8	9	$\begin{bmatrix} 1 & 3 & 0 \\ 2 & 1 & 0 \end{bmatrix}$	8	1 2	9		2 4	10	1258841	9	7 0	14
$3\frac{1}{2}$	14	9	3 0		क्रिक क्षेत्र	9		1 25			9	8 2	7
	8	9	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		1	9		1 18	131	1	9	11 2 5 3	$\frac{12}{7}$
150	24 5/26	9	2 0 8	81		9	3 3	3 2	102	5 8	9	7 1	12
100	34	9	2 2 0	10.5	12500	9	4 5	2 26		12 58 84 1	9	8 3	16
4	8	9	1 1 10	100	1	9	5 5			10	9	11 3	24
8.0	न्याद्व	9 9	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9		9	4 (	100	14	1 2 5	9 9	$\begin{array}{c} 6 & 0 \\ 7 & 2 \end{array}$	16
50	मिक्र को	9	2 3 21	ð	1258841	9	5 (	- 1		50 34	9	9 1	0
$4\frac{1}{2}$	( පත්ත	9	1 2 2	850	84	9	6 (		1	1	-	12 1	14
2.5	ক্ষান্ত ক্রান্ত নাম ক্রেক ক্রান্ত	9 9	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	91	1	9	8 (		141	125884	9 9	$\begin{array}{c} 6 & 0 \\ 7 & 3 \end{array}$	24 14
-99	8 84	9	3 0 21	02	215/8	9	5 1	0		8 34	9	9 2	2
5	8 8	9	1 2 22		1258341	9	6 1			1	9	12 3	6
rd Sa	12	9	2 1 10			9	8 2		15	$\frac{1}{2}$	9	6 1	21
- do	12 50 64 50 12 50	9 9	$\begin{bmatrix} 2 & 3 & 17 \\ 3 & 1 & 24 \end{bmatrix}$	10	125884 1	9	4 1 5 1		-	34	9 9	9 3	$\frac{7}{26}$
$5\frac{1}{2}$	4 35/8	9	1 3 10	W	8 84	9	6 2	14		14	9	16 3	5
Line	1225	-9	2 2 0	101		9	9 0		$15\frac{1}{2}$	1412841	9	6 2	14
-421	5884	9	3 0 18 3 3 7	$10\frac{1}{2}$	125884	9	4 2 5 3		NOT I	41	9 9	10 0 13 2	10 17
mm de	1	9	5 0 12	- 1	8 34	9	7 (	0 0	1015	11	9	17 1	6
6	050	9	2 0 0		1	9	9 2	0	16	1/2	9	7 0	22
MALE .	প্রত নাম কাত কাব ন	9	2 2 21	11	1258	9	4 8		411	34	9	10 1	20
-	30 00	9	$\begin{bmatrix} 3 & 1 & 17 \\ 4 & 0 & 16 \end{bmatrix}$		5/8 35	9	6 0 7 1		147	1		14 0 17 3	8
1	1	9	5 2 20		1	9	9 3		)	1½ 1½		21 3	4
											,		

 ${
m T~A~B~L~E}$  Of the weight of one foot length of Malleable Iron.

squ	ARE IRON.		ROUN	D IRON.	1 3 1
Scantling	Weight.	Diameter.	Weight.	Circumfer.	Weight.
Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.
1	0.21	1	0.16	11	0.26
3	0.47	38	0.37	11/4	0.41
न्य क्षेत्र क्षेत्र क्षेत्र क्षेत्र क्षेत्र	0.84	र्पं अंक न्हेंग डीकर्स्य स्थे	0.66	13	0.59
\$	1.34	5	1.03	$1\frac{1}{2}$ $1\frac{3}{4}$	0.82
34	1.89	34	1.48	2	1.05
78	2.57	7 8	2.02	$ \begin{array}{c c} 2\frac{1}{4} \\ 2\frac{1}{2} \end{array} $	1.34
1	3.36	1	2.63	$   2\frac{1}{2}$	1.65
11	4.25	11/8	3.33	24	2.01
14 155 155 147 175	5.25	11/4	4.12	3	2.37
18	6.35	$1\frac{8}{8}$ $1\frac{1}{2}$ $1\frac{5}{8}$ $1\frac{8}{4}$ $1\frac{7}{8}$	4.98	134	2.79
$1\frac{1}{2}$	7.56	$1\frac{1}{2}$	5.93	3 1/2	3.24
18	8.87	15	6.96	1 34 1	3.69
17	10.29	14	8.08	0 4	4.23
	11.81		9.27	$4\frac{1}{2}$	5.35
2	13.44	2	10.55	5	6:61
21	17.01	24	13.35	$5\frac{1}{2}$ -	7.99
$2\frac{1}{2}$ $2\frac{8}{4}$	21.00	$2\frac{1}{4}$ $2\frac{1}{2}$ $2\frac{8}{4}$	16.48	6	9.51
24	25.41	27	19.95	61	11.18
8	30.24	3	23.73	7	12·96 14·78
$\frac{3\frac{1}{2}}{4}$	41·16 53·76	31	$\begin{array}{c c} 27.85 \\ 32.32 \end{array}$	$\begin{bmatrix} 7\frac{1}{2} \\ 8 \end{bmatrix}$	16.92
444	68.04	$\frac{3\frac{1}{2}}{28}$	37.09		19.21
5	84.00	3 <u>8</u> 4	42 21	$\frac{8\frac{1}{2}}{9}$	21.53
	120.96	41	53.41	10	26.43
6 7	164.64	5	65.93	12	31.99
1	10201	8 1 4	00 00	124	01.00

FRESCO PAINTING.—Apply any colors that are not injured by lime (according to taste), on a fresh mortared or plastered wall.

To take Fac-similes of Signatures.—Write your name on a piece of paper, and while the ink is wet sprinkle over it some finely powdered gum arabic, then make a rim round it, and pour on it some fusible alloy, in a liquid state. Impressions may be taken from the plates formed in this way, by means of printing ink and the copperplate press.

WATCHMAKER'S OIL, WHICH NEVER CORRODES OR THICKENS.—Take olive oil and put it into a bottle, then insert coils of thin sheet lead. Expose it to the sun for a few weeks, and pour off the clear oil.

TABLE

Of the Dimensions and Weight of Coppers, from 1 to 208 gallons.

The Dimensions taken from lag to brim.

Inches lag to brim.	Gallons.	Weight in lbs.	Inches lag to brim.	Gallons.	Weight in lbs.	Inches lag to brim.	Gallons.	Weight in lbs.
0.8		- 6.1	0.4	1.	0.21	001	00	02.0
98	$\frac{1}{2}$	11/2	24	15	$22\frac{1}{2}$	291	29	431
121	2	3	241/2	16	24	30	30	45
14	3	$4\frac{1}{2}$	25	17	$25\frac{1}{2}$	32	36	54
$14^{1}$ $15\frac{1}{2}$	4	6	251	18	27	34	43	641
164	5	$\begin{array}{c} 6 \\ 7\frac{1}{2} \end{array}$	26	19	281	35	48	72
173	6	9	$26\frac{1}{2}$	20	30	36	53	791
184	7	$10\frac{1}{2}$	263	21	313	37	58	87
$19\frac{1}{2}$	7 8	12-	27	22	33	38	63	$94\frac{1}{2}$
201	9	$13\frac{1}{2}$	274	23	$34\frac{1}{2}$	39	67	1001
21	10	15	$27\frac{1}{2}$	24	36	40	71	1061
$21\frac{1}{2}$	11	161	278	25	371	45	104	156
22	12	18	28	26	39	50	146	219
221	13	$19\frac{1}{2}$	281	27	401	55	208	312
231	14	21	29	28	42	7		
-FIA						100.1		0.00

Weight of Cast-Iron Plates, per superficial foot.

From one-eighth of an inch to one juch thick.

lbs. oz.	% inch.	lbs. oz.					
4 138	9 105	14 8	19 58	24 23	29 0	33 13 <del>8</del>	38 104

THE MANNER OF SOLDERING FERRULES FOR TOOL HANDLES, &c.—Take your ferrule, lap round the jointing a small piece of brass wire, then just wet the ferrule, scatter on the joining ground borax, put it on the end of a wire, and hold it in the fire till the brass fuses. It will fill up the joining, and form a perfect solder. It may afterwards be turned in the lathe.

Cast Engravings.—Take the engraved plate you intend to copy, and arrange a support of suitable materials round it, then pour on it the following alloy in a state of perfect fusion: tin 1 part; lead 64 parts; antimony 12 parts. These "east plates" may be worked off on a common printing-press, and offer a ready mode of procuring cheap copies of the works of our celebrated artists.

TABLE
Of the Bore and Weight of Cocks.

Content of Copper.	Bore of Cock.	Weight of Cock.	Content of Copper	Bore of Cock.	Weight of Cock.
Gallons.	Inches.	Pounds.	Gallons.	Inches.	Pounds.
50	11/2	7	200	$2\frac{8}{4}$	30
50	13/4	8	260	3	34
80	2	12	340 -	31	44
120	21/4	19	420	$3\frac{1}{2}$	56
150	$2\frac{1}{2}$	26	430 and		70
	100 1 60	1 22 1	upwards.	- 0	300

Three-fourths of the diameter of the bore, taken at the hinder part, will give the diameter of the cock at the mouth.

TABLE

Of the Weight of Lead, per superficial foot.

From one-sixteenth of an inch to one inch thick.

Thickness.	Weight.	Thickns.	Weight.	Thickns.	Weight.	Thickness.	Weight.
inch. 1-16th	lbs. 3 <del>8</del>	inch. 1-8th	- lbs. 7 ½	inch. 1-4th	lbs. 14%	inch. 3-4ths.	lbs.
1-12th	5	1-6th	10	1-3rd	194	1 inch	59
1-10th	6	1-5th	12	1-half	$29\frac{1}{2}$		

## Weight of Lead Pipe of the usual thicknesses.

	Per foot in length.										
1-inc	h bore			1 lb. 1	OZ.						
34	66			1 lb. 8	oz. —	1 lb.	12 oz.	2	2 lbs.		
-1	" ofe	11	.0	2 lbs.	12700	2 lbs.	11 oz	9	2 lbs.	14 oz.	
11	"		1. 11	3 lbs.	- I out	3 lbs.	11 oz.	- 4	lbs.	7 oz.	
11/2	"		0.0	4 lbs.	124	4 lbs.	11 oz.	. — !	5 lbs.	9 oz.	
2	05 KL		20	5 lbs. 9	oz	· 7 lbs.		- 8	3 lbs.	5 oz.	
21	166 000 300	20	10.1	7 lbs.	South and	8 lbs.	9 07	10	O lbs.		

# Weight of Copper Tubing. Of the usual thickness.

When the inside diameter is  $\frac{1}{4}$  of an inch, 3 ounces;  $\frac{3}{4}$  of an inch, 5 ounces;  $\frac{1}{2}$  of an inch, 6 ounces;  $\frac{5}{8}$  of an inch, 8 ounces; and  $\frac{3}{4}$  of an inch, 10 ounces per foot.

#### STRENGTH OF MATERIALS.

Materials of construction are liable to four different kinds of strain, viz., stretching, crushing, transverse action, and torsion or twisting: the first of which depends upon the body's tenacity alone; the second, on its resistance to compression; the third on its tenacity and compression combined; and the fourth, on that property by which it opposes any acting force tending to change from a straight line, to that of a spiral direction, the fibres of which the body is composed.

In bodies, the power of tenacity and resistance to compression, in the direction of their length is as the cross-section of their area multiplied by the results of experiments on similar bodies, as exhi-

bited in the following table:

TABLE

Showing the Tenacities, Resistances to Compression, and other Properties of the common Materials of Construction.

F 10 20 A	Abs	olute.	Compa	red with C	Cast Iron.
Names of Bodies.	Tenacity in lbs. per sq. inch.	Resistance to compres- sion in lbs per sq. in.	Its strength is	Its extensi- bility is	Its stiffness is
Ash	14130		0 23	2.6	0.089
Beech	12225	8548	0.15	2.1	0.073
Brass	17968	10304	0.435	0.9	0.49
Brick	275	562	_		11 - 110
Cast iron	13434	86397	1.000	1.0	1.000
Copper (wrought)	33000	All there	driver to the		A
Elm	9720	1033	0.21	2.9	0.073
Fir or Pine white	12346	2028	0.23	2.4	0.1
" red yellow.	11800	5375	0.3	2.4	0.1
" yellow.	11835	5445	0.25	2.9	0.087
Granite	n 12	10910	- 12	N	
Gun-metal (copper) 8, and tin 1	35838		0.65	1.25	0.535
Malleable iron	56000	_	1.12	0.86	1.3
Lareh	12240	5568	0.136	2.3	0.058
Lead	1824	1 21=	0.096	2.5	0.0385
Mahogany, Honduras	11475	8000	0.24	2.9	0.487
Marble	551	6060	MIT		(40)
Oak	11880	9504	0.25	2.8	0.093
Rope (1in. in circum.)	200	A PERCONS	COL.	-	11/1-
Steel	128000		WHILE !	-04	Media
Tin (cast)	4736	2007	0.182	0.75	0.25
Zinc (sheet)	9120	1	0.365	05.	0.76

TABLE

Of the Comparative Strength and Weight of Ropes and Chains.

Circum. of rope in inches.	Weight per fathom in lbs.	Diameter of chain in inches.	Weight per fathom in lbs.	Proof strength in tons and cwt.	Circum. of rope in inches.	Weight per fathom in lbs.	Diameter of chain in inches.	Weight per fathom in lbs.	Proof strength in tons and cwt.
$3\frac{1}{2}$	23	5 16	$5\frac{1}{2}$	$1  5\frac{1}{2}$	10	23	7 8	43	10 0
41	43	38	8	$1 \ 16\frac{3}{4}$	108	28	15	49	11 11
5	$5\frac{8}{4}$	7 16	101	2 10	111	$30\frac{1}{2}$	1 in.	56	13 8
$5\frac{8}{4}$	7	1/2	14	$3  5\frac{1}{2}$	$12\frac{1}{4}$	36	116	63	14 18
$6\frac{1}{2}$	98	9	18	4 3½	13	39	11/8	71	16 14
7	111	5 8	22	5 2	133	45	3	79	18 11
8	15	11	27	6 41/2	$14\frac{1}{2}$	$48\frac{1}{2}$	$1\frac{1}{4}$	87	20 8
834	19	34	32	7 7	$15\frac{1}{4}$	56	1,5	96	22 13
91/2	21	13	37	8 131	16	60	18/8	106	24 18

Note.—It must be understood, and also borne in mind, that in estimating the amount of tensile strain to which a body is subjected, the weight of the body itself must also be taken into account; for according to its position so may it approximate to its whole weight, in tending to produce extension within itself; as in the almost constant application of ropes and chains to great depths, considerable heights, &c.

# Resistance to Lateral Pressure, or Transverse Action.

TABLE

Of Data, containing the Results of Experiments on the Elasticity and Strength of various Species of Timber.

Species of Timber.	Value of E.	Value of S.	Species of Timber.	Value of E.	Value of 8.
Teak, Poona, English Oak, Canadian do., . Dantzie do.,	174·7 122·26 105 155·5 -86·2 70·5 119 98	2462 2221 1672 1766 1457 1383 2026 1556	Elm,	50·64 88·68 133 158·5 90 63 76 105·47	1013 1632 1341 1102 1100 1200 900 1474

The strength of a square or rectangular beam to resist lateral pressure, acting in a perpendicular direction to its length, is as the breadth and square of the depth, and inversely as the length. Thus, a beam twice the breadth of another, all other circumstances being alike, equals twice the strength of the other; or twice the depth, equal four times the strength, and twice the length, equal only half the strength, &c., according to the rule.

To find the dimensions of a beam capable of maintaining a given weight, with a given degree of deflection, when supported at both ends.

Rule. Multiply the weight to be supported in lbs. by the cube of the length in feet; divide the product by 32 times the tabular value of E, multiplied into the given deflection in inches; and the quotient is the breadth multiplied by the cube of the depth in inches.

Note 1.—When the beam is intended to be square, then the fourth root of the quotient is the breadth and depth required.

Note 2.—If the beam is to be cylindrical, multiply the quotient by 17, and the fourth root of the product is the dameter.

EXAMPLE. The distance between the supports of a beam of Riga fir is 16 feet, and the weight it must be capable of sustaining in the middle of its length is 8000 lbs., with a deflection of not more than \$\frac{2}{3}\$ of an inch; what must be the depth of the beam, supposing the breadth 8 inches?

$$\frac{16 \times 8000}{90 \times 32 \times 75} = 15175 \div 8 = \sqrt[3]{1897} = 1235$$
 in., the depth.

To determine the absolute strength of a rectangular beam of timber, when supported at both ends, and loaded in the middle of its length, as beams in general ought to be calculated to, so that they may be rendered capable of withstanding all accidental cases of emergency.

Rule. Multiply the tubular value of S by four times the depth of the beam in inches, and by the area of the cross section in inches; divide the product by the distance between the supports in inches, and the quotient will be the absolute strength of the beam in lbs.

Note 1.—If the beam be not laid horizontally, the distance between the supports, for calculation, must be the horizontal distance.

Note 2.—One fourth of the weight obtained by the rule is the greatest weight that ought to be applied in practice as permanent load.

Note 3.-If the load is to be applied at any other point than the middle, then the strength will be as the product of the two distances is to the square of half the length of the beam between the supports; or, twice the distance from one end, multiplied by twice from the other, and divided by the whole length, equal the effective length of the beam.

EXAMPLE. In a building 18 feet in width, an engine boiler of 5½ tons is to be fixed, the centre of which is to be 7 feet from the wall; and having two pieces of red pine, 10 inches by 6, which I can lay across the two walls for the purpose of slinging it at each end, may I with sufficient confidence apply them, so as to effect this object?

$$\frac{2240 \times 5.5}{4} = 6160 \text{ lbs. to carry at each end.}$$

And 18 feet -7 = 11, double each, or 14 and 22, then

$$\frac{14 \times 22}{13}$$
 = 17 feet, or 204 inches, effective length of beam.

Tabular value of S, red pine, 
$$=\frac{1341 \times 4 \times 10 \times 60}{204} = 15776$$
 lbs.

the absolute strength of each piece of timber at that point.

To determine the dimensions of a rectangular beam capable of supporting a required weight, with a given degree of deflection, when fixed at one end.

Rule. Divide the weight to be supported in lbs., by the tabular value of E, multiplied by the breadth and deflection, both in inches; and the cube root of the quotient, multiplied by the length in feet, equal the depth required in inches.

EXAMPLE. A beam of ash is intended to bear a load of 700 lbs. at its extremity, its length being 5 feet, its breadth 4 inches, and the deflection not to exceed  $\frac{1}{2}$  of an inch.

Tabular value of E = 119 × 4 × 5 = 238 the divisor; then  $700 \div 238 = \sqrt[3]{2.94} \times 5 = 7.25$  inches, depth of the beam.

To find the absolute strength of a rectangular beam, when fixed at one and loaded at the other.

Rule. Multiply the value of S by the depth of the beam, and by the area of its section, both in inches: divide the product by the leverage in inches, and the quotient equal the absolute strength of the beam in lbs.

EXAMPLE. A beam of Riga fir, 12 inches by  $4\frac{1}{2}$ , and projecting  $6\frac{1}{2}$  feet from the wall; what is the greatest weight it will support at the extremity of its length?

Tabular value of S = 1100  

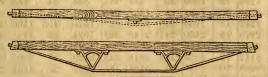
$$12 \times 4.5 = 54$$
 sectional area,  
Then, 
$$\frac{1100 \times 12 \times 54}{78} = 9138.4 \text{ lbs.}$$

When fracture of a beam is produced by vertical pressure, the fibres of the lower section of fracture are separated by extension, whilst at the same time those of the upper portion are destroyed by compression; hence exists a point in section where neither the one nor the other takes place, and which is distinguished as the point

of neutral axis. Therefore, by the law of fracture thus established, and proper data of tenacity and compression given, as in the table (p. 135), we are enabled to form metal beams of strongest section with the least possible material. Thus, in cast iron, the resistance to compression is nearly as  $6\frac{1}{2}$  to 1 of tenacity; consequently a beam of cast iron, to be of strongest section, must be of the following form, and a parabola in the direction of its length,

ing form, and a parabola in the direction of its length, the quantity of material in the bottom flange being about 6½ times that of the upper. But such is not the case with beams of timber; for although the tenacity of timber be on an average twice that of its resistance

of timber be on an average twice that of its resistance to compression, its flexibility is so great that any considerable length of beam, where columns cannot be situated to its support, requires to be strengthened or trussed by iron rods, as in the following manner:



and these applications of principle not only tend to diminish deflection, but the required purpose is also more effectively attained, and that by lighter pieces of timber.

To ascertain the absolute strength of a cast-iron beam of the preceding form, or that of strongest section.

RULE. Multiply the sectional area of the bottom flange in inches by the depth of the beam in inches, and divide the product by the distance between the supports, also in inches; and 514 times the quotient equal the absolute strength of the beam in cwts.

The strongest form in which any given quantity of matter can be disposed is that of a hollow cylinder; and it has been demonstrated that the maximum of strength is obtained in east iron when the thickness of the annulus or ring amounts to \$\frac{1}{2}\$th of the cylinder's external diameter; the relative strength of a solid to that of a hollow cylinder being as the diameters of their sections.

TORTOISE-SHELL GROUND FOR METAL.—Cover the plates intended to represent the transparent parts of the tortoise-shell with a thin coat of vermilion in seed-lac varnish. Then brush over the whole with a varnish composed of linseed oil boiled with umber until it is almost black. The varnish may be thinned with oil of turpentine before it is used. When the work is done it may be set in an oven, with the same precautions as the black varnish

Force in Pile-Driving.—In a sandy soil the greatest force of a pile-driver will not drive a pile over fifteen feet.

#### TABLE

Showing the Weight or Pressure a Beam of Cast Iron, 1 inch in breadth, will sustain, without destroying its elastic force, when it is supported at each end, and loaded in the middle of its length, and also the deflection in the middle which that weight will produce.

Length.	6 fe	et.	7 fee	et.	8 fee	et.	9 fc	et.	10 f	eet.
Depth in inches.	Weight in lbs.	Deflection in inches.	Weight in lbs.	Deflection in inches.						
2-110	21/2 (	1977	DOM: 0	11 70	67 0	2.46	35,010	0.500	7.8	1001/101
3	1278	.24	1089	.33	954	426	855	.54	765	66
31.	1739	-205	1482	.28	1298	.365	1164	•46	1041	.57
4	2272	·18	1936	.245	1700	32	1520	.405	1360	.2
$4\frac{1}{2}$	2875	.16	2450	217	2146	.284	1924	.36	1721	·443
5	3560	.144	3050	196	2650	256	2375	.32	2125	•4
6 7	5112	.12	4356	.163	3816	.213	3420	.27	3060	.33
7	6958	.103	5929	.14	5194	.183	4655	.23	4165	•29
8	9088	.09	7744	.123	6784	.16	6080	.203	5440	.25
	-101		9801	.109	8586	142	7695	.18	6885	.22
10			12100	.098	10600	128	9500	.162	8500	•2
11					12826	117	11495	.15	10285	182
12	1300				15264	107	13680	135		.17
13 14	1				- 11		16100	125	14400	154
14			L.				18600	.119	16700	·143
-12 -0	12 fe	eet.	14 fe	et.	16 fe	et.	18 fe	et.	20 f	eet.
6	2548	.48	2184	.65	1912	.85	1699	1.08	1530	1:34
7	3471	.41	2975	.58	2603	.73	2314	.93	2082	1.14
8	4532	.36	3884	.49	3396	.64	3020	.81	2720	1.00
9	5733	.32	4914	.44	4302	.57	3825	.72	3438	.89
10	7083	.28	6071	.39	5312	.51	4722	.64	4250	.8
11	8570	26	7346	.36	6428	.47	5714	.59	5142	·73
12	10192	.24	8736	.33	7648	.43	6796	.54	6120	·67
13	11971	.22	10260	.31	8978	.39	7980	.49	7182	·61
14	13883	.21	11900	-28	10412	.36	9255	.46	8330	.57
15	15937	.19	13660	.26	11952	.34	10624	43	9562	.23
16	18128	.18	15536	.24	13584	.32	12080	•40	10880	.2
17	20500	.17	17500	.23	15353	.3	13647	.38	12282	.47
18	22930	16	19656	.21	17208	.28	15700	.36	13752	:44
100 00	1 -1	10.00	d 100	1/2 1/2	1000	and h	o of W		3 44 4	1000

Note.—This table shows the greatest weight that ever ought to be laid upon a beam for permanent load; and, if there be any liability to jerks. &c., ample allowance must be made; also, the weight of the beam itself must be included.

To find the weight of a cast-iron beam of given dimensions.

Rule. Multiply the sectional area in inches by the length in feet, and by 3.2, the product equal the weight in lbs.

Ex. Required the weight of a uniform rectangular beam of cast iron, 16 feet in length, 11 inches in breadth, and  $1\frac{1}{2}$  inch in thickness.

#### $11 \times 1.5 \times 16 \times 3.2 = 844.8$ lbs.

### Resistance of Bodies to Flexure by Vertical Pressure.

When a piece of timber is employed as a column or support, its tendency to yielding by compression is different according to the proportion between its length and area of its cross section; and supposing the form that of a cylinder whose length is less than seven or eight times its diameter, it is impossible to bend it by any force applied longitudinally, as it will be destroyed by splitting before that bending can take place; but when the length exceeds this, the column will bend under a certain load, and be ultimately destroyed by a similar kind of action to that which has place in the transverse strain.

Columns of cast iron, and of other bodies, are also similarly circumstanced, this law having recently been fully developed by the experiments of Mr. Hodgkinson on columns of different diameters,

and of different lengths.

When the length of a cast-iron column with flat ends equals about thirty times its diameter, fracture will be produced wholly by bending of the material. When of less length, fracture takes place partly by crushing and partly by bending. But, when the column is enlarged in the middle of its length from one and a half to twice its diameter at the ends, by being cast hollow, the strength is greater by  $\frac{1}{7}$ th than in a solid column containing the same quantity of material.

To determine the dimensions of a support or column to bear, without sensible curvature, a given pressure in the direction of its axis.

Rule.—Multiply the pressure to be supported in lbs. by the square of the column's length in feet, and divide the product by twenty times the tabular value of E; and the quotient will be equal to the breadth multiplied by the cube of the least thickness, both being expressed in inches.

Note 1.—When the pillar or support is a square, its side will be the fourth root of the quotient.

 $2\,$  If the pillar or column be a cylinder, multiply the tabular value of E by 12, and the fourth root of the quotient equal the diameter.

Ex. 1. What should be the least dimensions of an oak support, to bear a weight of 2240 lbs., without sensible flexure, its breadth being 3 inches, and its length 5 feet?

Tabular value of E = 105.

and 
$$\frac{2240 \times 5^2}{20 \times 105 \times 3} = \sqrt[3]{8.888} = 2.05$$
 inches.

Ex. 2. Required the side of a square piece of Riga fir, 9 feet in length, to bear a permanent weight of 6000 lbs.

Tabular value of E = 96,

and 
$$\frac{6000 \times 9^2}{20 \times 96} \times \sqrt[4]{253} = 4$$
 inches nearly.

### TABLE

Of the Dimensions of Cylindrical Columns of Cast Iron to sustain a given load or pressure with safety.

ameter inches.		(har	Lı	ENGTH	or ]	Heigi	IT IN	FEET	200	APPENDED	D JAME
Diameter in inches.	4	6	8	10	12	14	16	18	20	22	24
Promise of the second	LL/LI T	Annual Control	. 7	VEIGE	IT OR	Loai	D IN	Cwts	Z To	10.10	20 Louis
A CHILDREN	P.130 1	011/	7 100	370		7 7	1012	0.01	mit.	100	June La
2	72	60	49	40	32	26	22	." 18	15	13	1110
$\frac{1}{2\frac{1}{2}}$	119	105	91	77	65	55	47	40	34	29	25
3	178	163	145	128	111	97	84	73	64	56	49
$3\frac{1}{2}$	247	232	214	191	172	156	135	119	106	94	83
4	326	310	288	266	242	220	198		160	144	130
$4\frac{1}{2}$	418	400	379	354	327	301	275	251	229	208	189
5	522	501	479	452	427	394	365		310	285	262
6	607	592	573	550	525	497	469		413	386	360
7	1032	1013	989	959	924	887	848	808	765		200
8	1333	1315	$\frac{1289}{1672}$	1259		1185	1142				959
9	$\frac{1716}{2119}$	1697 2100		1640			1515	1467		1364	
11	2570	2550			$\frac{2007}{2450}$						
12	3050	3040			2930						
	5550	0010	5520	2010	2000		2000	2.00	2.50		1000

#### Practical Utility of the preceding Table.

Ex. Wanting to support the front of a building with cast-iron columns 18 feet in length, 8 inches in diameter, and the metal 1 inch in thickness; what weight may I confidently expect each column capable of supporting without tendency to deflection?

Opposite 8 inches diameter and under 18 feet = 1097 Also opposite 6 in. diameter and under 18 feet = 440 = 657 cwt.

Note.-The strength of cast iron as a column being 1'0000 wrought iron

(oak) Dantzic " = '1088 red deal

#### Elasticity of Torsion, or Resistance of Bodies to Twisting.

The angle of flexure by torsion is as the length and extensibility of the body directly, and inversely as the diameter; hence the length of a bar or shaft being given, the power, and the leverage the power acts with, being known, and also the number of degrees of torsion that will not affect the action of the machine, to determine the diameter in cast iron, with a given angle of flexure.

Rule. Multiply the power in lbs. by the length of the shaft in feet, and by the leverage in feet; divide the product by fifty-five times the number of degrees in the angle of torsion; and the fourth root of the quotient equal the shaft's diameter in inches.

Ex. Required the diameters for a series of shafts 35 feet in length, and to transmit a power equal to 1245 lbs., acting at the circumference of a wheel  $2\frac{1}{2}$  feet radius, so that the twist of the shafts on the application of the power may not exceed one degree.

$$\frac{1245 \times 35 \times 2.5}{55 \times 1} = \sqrt[4]{1981} = 6.67 \text{ inches in diameter.}$$

### Relative Strength of Metals to resist Torsion.

Cast iron Swedish bar iron . =1:05Copper . = .48 English do. . . =1.12Yellow Brass . = '511 | Shear steel . . . Gun-metal . . Cast do. . = '55

### Map Colors.

YELLOW.

1. Dissolve gamboge in water.

2. Make a decoction of French berries, strain, and add a little gum arabic.

1. Make a decoction of Brazil dust in vinegar, and add a little gum and alum.

2. Make an infusion of cochineal, and add a little gum.

A weak mixture of sulphate of indigo and water, to which add a little gum.

#### GREEN.

1. Dissolve crystals of verdigris in water, and add a little gum.

2. Dissolve sap green in water, and add gum.

TABLE

Of the Weight of a Superficial Foot of Plate or Sheet Iron, Copper, and Brass, in pounds.

-	1		1					1	)			
	1	ron.	1	No.	Iron.	Copper.	Brass.		No	Iron.	Copr.	Brass.
	$\frac{1}{32}$	1.25		1	12.5	14.5	13.75	T	16	2.2	2.9	2.75
20	1 6	2.5	a delit in man	2	12	13.9	13.2		17	2.18	2.52	2.4
1	18	ő	9	3	11	12.75	12.1	6.	18	1.86	2.15	2.04
Thickness in parts of an inch.	3 16	7.5	gauge.	4	10	11.6	11	gauge.	19	1.7	1 . 97	1.87
100	1	10		5	8.74	10.1	9.61	re g	20	1.54	1.78	1.69
9 0	5 16	12.5	wire	6	8.12	9.4	8 . 93	· K	21	1.4	1.62	1.54
art	8	15	the	17	7.5	8.7	8.25	the	22	1 · 25	1-45	1.37
ii.	7 16	17.5	¥.	- 8	6.86	7.9	7.54	b.	23	1:12	1.3	1:23
688	1/2	20	ers ers	9	6 · 24	7.2	6.86	ess	24	1	1.16	1.1
okn	9 16	22.5	Thickness	10	5.62	6.5	6.18	Thickn	25	.9	1.04	.99
1.11	5	25	1	11	5	5.8	5.5	Thi	26	.8	.92	.88
	11	27.5	-	12	4.38	5.08	4.81		27	.72	.83	.79
	8 4	30		13	3.75	4.34	4.12		28	• 64	.74	.7
	7	35	-0.	14	3.12	3.6	3.43	-	29	.56	· 64	.61
	1	40		15	2.82	3 · 27	3.1	1	30	.5	.58	. 55
			1	-	and the last	- 34		-	-	0	10	

Note.—No. 1 wire gauge equal  $\frac{5}{16}$ ths of an inch.

The great variety of thicknesses into which copper is manufactured, cause in trade the weight to be named whereby to determine the thickness required, the unit being that of a common sheet, so designated, viz. 4 feet by 2 feet, in lbs., thus:

	b. plate	is $\frac{3}{16}$ ths	of an i	nch in	thicknes
" 461	61	1	46.		"
" 28	66	1	46		66
"-111	16	3 2			66
1 2 1		3,3			The same of

The thickness of lead is also in common determined or understood by the weight, the unit being that of a square or superficial foot; thus:

4	lbs.	lead "	is $\frac{1}{16}$ th	of an in	ch in thic	kness.
73		66	1 0 1	"	"	
11		66	3	"		
		"	1	44	44	

#### Comparative Weights of Different Bodies.

Bar iron being 1,	Cast iron being 1,
Cast iron = '95	Bar iron $= 1.0$
Steel = 1.02	Steel = 1.08
Copper $= 1.16$	Brass = 1.16
Brass = 1.09	Copper $= 1.21$
Lead = 1.48	Lead = 1.56

1. Suppose I have an article of plate iron, the weight of which is 728 lbs., but want the same of copper, and of similar dimensions, what will be its weight?

$$728 \times 1.16 = 844.48$$
 lbs.

2. A model of dry pine, weighing 32½ lbs., and in which the iron for its construction forms no material portion of the weight, what may I anticipate its weight to be in cast iron?

$$32.5 \times 16 = 520$$
 lbs.

Note.—It frequently occurs, in the formation or construction of models, that neither the quality nor condition of the timber can be properly estimated; and, in such cases, it may be a near enough approximation to reckon 15 lbs. of cast fron to each lb. of model.

SILVERING POWDER, &c., for silvering copper, covering the worn parts of plated goods, &c.—1. Nitrate of silver 30 gr., common salt 30 gr., cream of tartar 3½ dr. Mix. Moistened with water, and rubbed on dial plates or other copper articles, it coats them with silver.

- 2. Silver precipitated from its nitric solution by copper 20 gr., alum 30 gr., cream of tartar 2 dr., salt 2 dr.
- 3. Precipitated silver ½ oz, common salt 2 oz, muriate of ammonia 2 oz, corrosive sublimate 1 dr. Make it into a paste with water. Copper utensils are previously boiled with tartar and alum, and rubbed with this paste, then made red hot, and afterwards polished.
- 4. Dissolve muriate of silver in a solution of hyposulphite of soda, and mix this with prepared hartshorn, or other suitable powder.

PLATINA FOR SPRINGS.—Platinum 1 part; gold 12 parts. Add the platinum to the gold in a state of fusion.

#### Tables by which to facilitate the Mensuration of Timber.

1. Flat or Board Measure.

Breadth in inches.	Area of a lineal foot.	Breadth in inches.	Area of a lineal foot.	Breadth in inches.	Area of a lineal foot.
4	.0208	4	•3334	8	.6667
1	.0417	41/4	*3542	81	.6875
1 1 2 8 4	.0625	41/2	.375	81/2	.7084
1	.0834	48/4	.3958	83	.7292
11	1042	5	.4167	9	75
11/2	125	51	.4375	91	.7708
18	1459	$5\frac{1}{2}$	•4583	91	:7917
2	1667	$5\frac{3}{4}$	•4792	9 3	:8125
21/4	1875	6	. 5	10	*8334
$2\frac{1}{2}$	.2084	61	• 5208	101	.8542
$2\frac{3}{4}$	2292	$6\frac{1}{2}$	• 5416	101	-875
3	.25	$6\frac{8}{4}$	. 5625	103	8959
31	2708	7	.5833	11	.9167
31	2916	71	6042	111	9375
38	:3125	71	.625	113	9583
4		$7\frac{2}{4}$	.6458	113	9792
			-30 - 28		

#### Application and Use of the Table.

1. Required the number of square feet in a board or plank  $16\frac{1}{2}$  feet in length, and  $9\frac{9}{4}$  inches in breadth.

Opposite  $9\frac{3}{4}$  is  $8125 \times 16.5 = 13.4$  square feet.

2. A board 1 foot 23 inches in breadth, and 21 feet in length; what is its superficial content in square feet?

Opposite  $2\frac{3}{4}$  is 2292, to which add the 1 foot.

Then  $1.2292 \times 21 = 25.8$  square feet.

3. In a board  $15\frac{1}{2}$  inches at one end, 9 inches at the other, and  $14\frac{1}{2}$  feet in length, how many square feet?

 $\frac{15.5+9}{2} = 12\frac{1}{4}$ , or 1.0208; and 1.0208 × 14.5 = 14.8 square feet.

To give Iron a temper to cut Porphyry.—Make your iron red hot, and plunge it into distilled water from nettles, acanthus, and pilosella, or in the very juice pounded out from these plants.

PASTE FOR CLEANING METALS.—Take oxalic acid 1 part; rottenstone 6 parts. Mix with equal parts of train oil and spirits of turpentine to a paste.

2. Cubic or Solid Measure.

		1	:	lı	<u> </u>
Mean ¼	Cubic feet	Mean ¼	Cubic feet	Mean ¼	Cubic feet
girth in	in each	girth in	in each	girth in	in each
inches.	lineal foot.	inches.	lineal foot.	inches.	lineal foot.
7 10 34			THE STATE OF THE S		
6	.25	14	1.361	22	3.362
$6\frac{1}{4}$	.272	141	1.41	221	3.438
$6\frac{1}{2}$	•294	141	1.46	$22\frac{1}{2}$	3.516
$6\frac{2}{4}$	•317	148	1.511	223	3.598
7	.340	15	1.562	23	3.673
71	.364	151	1.615	281	3.754
71	•39	151	1 668	231	3.835
7 ½ 7 ¾	•417	158	1.722	233	3.917
8	•444	16	1.777	24	4.
81	.472	161	1.833	247	4.084
81/2	.501	161	1.89	243	4.168
8 3 4	.531	163	1.948	245	4.254
9	.562	17	2.006	25	4-34
91	.594	174	2.066	251	4.428
91	.626	17.3	2.126	251	4.516
93	.659	173	2.187	25%	4.605
10	-694	18	2.25	26	4.694
101	.73	181	2.313	261	4.785
101	.766	181	2.376	261	4 876
10%	.803	183	2.442	264	4.969
11	•84	19	2.506	27	5 062
111	.878	191	2.574	274	5.158
111	•918	191	2.64	271	5 • 252
118	.959	193	2.709	27 \$	5.348
12	1.	20	2.777	28	5.444
124	1.042	201	2.898	281	5.542
$12\frac{1}{2}$	1.085	$20\frac{1}{2}$	2.917	$28\frac{1}{2}$	5.64
133	1.129	$20\frac{3}{4}$	2.99	283	5.74
13	1.174	21	3.062	29	5.84
131	1.219	$21\frac{1}{4}$	3.136	291	5.941
131	1 · 265	$21\frac{1}{2}$	3 · 209	291	6.044
$13\frac{3}{4}$	1.313	218	3.285	298	6.146
-03	200 1200		2 -1 (1)	4.01	0 8
		-			

In the cubic estimation of timber, custom has established the rule of \$\frac{1}{4}\$ the mean girt being the side of the square considered as the cross sectional dimensions; hence, multiply the number of cubic feet per lineal foot, as in the Table of Cubic Measure, opposite the \$\frac{1}{4}\$ girth, and the product is the solidity of the given dimensions in cubic feet.

Suppose the mean 4 girth of a tree 214 inches, and its length 16 feet, what are its contents in cubic feet?

 $3.136 \times 16 = 50.176$  cubic feet.

#### CAST METAL CYLINDERS.

The Cylinders are solid, each 1 foot in length.

Diameter.	Iron.	Copper.	Brass.	Lead.
inches.	lbs.	lbs.	lbs.	lbs.
1	2.5	3.0	2.9	3.9
2	9.8	12.0	11.4	15.5
3	22.1	27.0	25.8	34:8
4	39.3	47.9	45.8	61-9
5	61.4	74.9	71.6	96.7
6	88.4	107.8	103.0	139.3
7	120.3	146.8	140.2	189.6
8	157 · 1	191.7	183 · 2	247.7
9 .	198.8	242.7	231.8	313.4
10	245.4	299.5	286 · 2	387.0

#### CAST-IRON PIPES.

Table showing the Weight of Pipes 1 foot long, of bores from 1 inch to 12 inches in diameter, advancing by ½ of an inch; and of thicknesses from ¼ of an inch to 1¼ inches, advancing by ½ of an inch.

1.00									517
bore.	1	<u>\$</u>	1/2	<u>5</u>	84	78	1	11	11/4
in.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
1	3.1	5.1	7.4	10.0	12.9	16.1	19.6	23.5	27.6
11/4	3.7	6.0	8.6	11.5	14.7	18.3	22.1	26.2	30.7
$1\frac{1}{2}$	4.3	6.9	9.8	13.0	16.6	20.4	24.5	29.0	33 7
184	4.9	7.8	11.1	14.6	18.4	22.6	27.0	31.8	36.8
2	5.2	8.8	12.3	16.1	20.3	24.7	29.5	34.5	39.9
$2\frac{1}{4}$	6.1	9.7	13.2	17.6	22.1	26.8	31.9	37.3	43.0
$2\frac{1}{2}$	6.7	10.6	14.7	19.2	23.9	28.9	34.4	40.0	46.0
28	7.4	11.5	160	20.7	25.7	31.1	36 8	42.8	49.1
3	8.0	12.4	17.2	22.2	27.6	33.3	39.3	45.6	52.2
31	8.6	12.3	18.4	23.8	29.5	35.4	41.7	48.3	55.2
$3\frac{1}{2}$	9.2	14.2	19.6	25.3	31.3	37.6	44.2	51.1	58-3
33	9.8	15.2	20.9	26.9	33.1	39.7	46.6	53.8	61.4
4	10.4	16.1	22.1	28.4	35.0	41.9	49.1	56.6	64.4
41	11.1	17.1	23.4	30.0	36.9	44.1	51.6	59.4	67.6
41	11.7	18.0	24.5	31.4	38.7	46.2	54.0	62.1	70.6
434	12.3	18.9	25.8	33.0	40.5	48.3	56.5	64.9	73.6
5	12.9	19.8	27.0	34.5	42.3	50.5	58.9	67.6	76.7
51	13.5	20.7	28.2	36.1	44.2	52.6	61.4	70.4	79.8
$5\frac{1}{2}$	14.1	21.6	29.5	37.6	46.0	54.8	63.8	73.2	82.8
		1				1	1	-	

#### CAST-IRON PIPES.

(Continued.)

	71	1	1	1	1			1	1
bore.	1	8 -	1/2	5 8	84	7 8	1	11/8	11/4
in.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.	lbs.
5 4	14.7	22.6	30.7	39.1	47.9	56.9	66.3	76.0	85.9
6	15.3	23.5	31.9	40.7	49.7	59.1	68.7	78.7	88.8
61	16.0	24.4	33.1	42.2	51.5	61.2	71.2		92.0
$6\frac{1}{2}$	16.6	25.3	34.4	43.7	53.4	63.4	73.4	84.2	95.1
68	17.2	26.2	35 6	45.3	55.2	65.3	76.1	87.0	98.2
7	17.8	27.2	36.8	46.8	56.8	67.7	78.5		101.2
71	18.4	28.1	38.1	48.1	58.9	69.8		92.5	104.2
$7\frac{1}{2}$ $7\frac{8}{4}$	19.0	29.0	39.1	49.9	60.7	72.0			
	19.6	29.7	40.5	51.4	62.6	74.1			110.5
8	20.0	30.8	41.7	52.9	64.4	76.2			
81	20.9	31.7	43.0	54.5	66.3	78.4			
81	21.7	32.9	44.4	56.2	68.3	80.8		106.5	119.9
8 3 4	22.1	33.6	45.4	57.5	70.0	82.7		109.1	1227
9	22.7	34.5	46.6	59.1	71.8	84.8	98.2		
91	23.3	35.4	47.9	60.6	73.6	87.0	100.6	114.6	128.9
$9\frac{1}{2}$	23.9	36.4	49.1	62.1	75.5	89 1	103.1	117.4	131.9
98	24.6	37.3	50.3	63.7	77.3	91.3	105.5	120:1	135.0
10	25.2	38.2	51.5	65.2	79.2	93.4	108.0	122.8	138.1
101	25.8	39.1	52:8	667	81.0	95.6	110.4	125.6	141.1
$10\frac{1}{2}$	26.4	40.0	54.0	68.3	82.8	97.7	112.9	128.4	144.2
10#	27.0	41.0	55.2	69.8	84.7	99.9	115.4	131.5	147.3
11	27.6	41.9	56.5	71.3	86.5	102.0	117.8	133.9	150.3
114	28.2	42.8	57.7	72.9	88.4	104.2	120.3	136.7	153.4
$11\frac{1}{2}$	28.8	43.7	58.9	74.4	90.2	106.3	122.7	139.4	156.4
114	29.5	44.6	60.1	75.9	92.0	108.2	125.2	142.2	159.5
12	30.1	45.6	61.4	77.5	93.6	110.6	127.6	145.0	162.6

#### Strength of Journals of Shafts.

Mr. Buchanan's rule is: The cube root of the weight in cwts. is nearly equal to the diameter of the journal; it being prudent to make the journal a little more than less, and to make a due allowance for wearing.

Ex. What is the diameter of a journal of a water-wheel shaft, 13 feet long, the weight of the wheel being 15 tons?

By Mr. B.'s rule,

 $\sqrt[3]{15} \times 20 = 6.7$ , or 7 inches diameter.

By Mr. Tredgold's rule.

 $\frac{3360}{500} \times 13 = 873 \sqrt[3]{873} = 9\frac{1}{2}$  inches diam. Weight in the middle, -

Weight equally distributed,  $33600 \times 13 = 436800 \sqrt[3]{\frac{436800}{10}}$ 

#### To resist Torsion or Twisting.

It is obvious that the strength of revolving shafts\* is directly as the cubes of their diameters and revolutions; and inversely as

the resistance they have to overcome.

Mr. Robertson Buchanan, in his Essay on the Strength of Shafts, gives the following data, deduced from several experiments, viz : That the fly-wheel shaft of a 50-horse-power engine, at 50 revolutions per minute, requires to be 71 inches diameter; and therefore the cube of this diameter, which is = 421.875, serves as a multiplier to all other shafts in the same proportion; and, taking this as a standard, he gives the following multipliers, viz.:

For the shaft of a steam-engine, water-wheel, or any shaft connected with a first power, For shafts in inside of mills, to drive smaller machinery, or connected with the 400 200 100

From the foregoing, the following rule is derived, viz.: The number of horse power a shaft is equal to is directly as the cube of the diameter and number of revolutions; and inversely as the above multipliers.

Ex. 1. When the fly-wheel shaft of a 45-horse-power steam engine makes 90 revolutions per minute, what is the diameter of the journal?

$$\frac{45 \times 400}{90} = 200 \sqrt[3]{200} = 5\frac{3}{10}$$
 inches diameter.

Ex. 2. The velocity of a shaft is 80 revolutions per minute, and its diameter is 3 inches; what is its power?

$$\frac{3^3 \times 80}{400} = 5.4 \text{ horse power.}$$

Ex. 3. What will be the diameter of the shaft in the first example, when used as a shaft of the second mover.+

$$\frac{5.8}{1.25} = 4.64$$
, or  $\frac{\sqrt[3]{45 \times 200}}{90} = 4\frac{6}{10}$  inches diameter.

\* Shafts here are understood as the journals of shafts, the bodies of shafts being gene-

rally made square.

† The diameters of the second movers will be found by dividing the numbers in the table by 125, and the diameters of the third movers, by dividing the numbers by 156.

6	07.0	4 70	40	35	30	S to	90	16	14	12	10	9	00:	7	6	O1	4	He	orse Po	wer.
	13.4																		10	sanot i
-	11.4										-		-			_		1	- 1101	a sundr
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8	10.4	7.6	9.5	8.9	00 0 4-	· ·	7 0	1 -1	6.7	6.3	5.9	5.7	0,0	5.5	07	4.7	4.5	ng	20	ABL
10.	8.6	9.2	8.8	8.4	9	7.4	7 -	6.6	6.2	500	5.6	5.5	5.1	4.9	4.6	4.4	4.	100	25	E of
9:	9.1	္ ထု	00	7.0	7.	7	0.0	6	5.0	57	57	0,	4:	4.	4.	4.1	တ္	100	30	the
	00 0	x	7	7	7	<u></u>	, o	000	07	57	4	4	4	4	4	ల	<u> </u>	Ton	24.5 1/3	diam
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86	000	9.6	7.4	7.1	6.9	000	0 0	0.00	54	5.2	4.7	4.5	4.4	4.2	4.	3.7	හ වැ	9.11	40	of si
000	on a	7 -7 \$ &	7.2	6.9	6.7	٠. و	7 0	4 2	5.2	O.	46	4.4	4.2	4.	3.8	3.6	<u>့</u>		45	hafts
-	77.	78.0	-	100		7.81		0 3	-10				VI.	-		111	-	ING	50	bein
-				10.7		-			-	-	-	-	-	-		-	VI -	NCHES	T U.S.	ng the first m
100	7.4	117.10			TU	23.00	- 13	1 30	1	75	111			11			000	Drai	55	e fire
7.4	-7 - 	7.0	6.6	6.3	9	טי פ	3	4.	4.5	4.4	4.1.	4.	3.9	3.6	တ	33	က်	DIAMETER	60	ons.
7:3	7.2	0000	6.4	6.1	5.00	٥، رو 4 ب	7 A	4.7	4.4	4.3	4.	03 08	တ်	3.6	00	3.2	2.9	7.7	65	vers,
1	-70	00	6	CT (	en c	- C	4 10	4	4	4	00	යා	င္သ	ප	లు	ලා	22	di o	701	or h
-		- 91	-	-			20.0	-	_			710	-					DJ. H	70	avin
6.9	6.7	6.2	٠ 6	7	6	20 0	ò	100	4.3	4.1	8	3.7	9.6	3.4	లు		8	101	75	9 40
6.	9.9	6.7	6.9	5.6	ت ت ن	ابر ابر	4 6	4.4	4.2	4.	3.7	3.6	ಲ್	3.4	00 10	ಯ	2.7		80	0 for
6.8	6.5		5.0	01	OT	4 4	4	4.	4.	<u>ي</u>	ಲ್	3.	00	00	00:	2:0	10	Hite	00 01	· thei
A-70700	der 2			-	_		-	_	-	-		Ar VI	1		_		-	0.000	0.1	r mi
	000						_				_				_			0.0 V	90	TABLE of the diameters of shafts, being the first movers, or having 400 for their multipliers  REVOLUTIONS.
6.6	6.5	, 00 00	9.6	5.3	- ·	4.7	4 6	4.2	4.	8.8	3.6	00	3.4	50.50	ċ	2.8	2.6	4	95	iers.
6.4	6:1	0 0	5.6	5.2	ې ر	4.6	4.7	4.1	3.9	3.7	3.5	3.4	ಪ್ರ	20	2.9	2.8	2.6	100	100	
6.2	000	or or	5.5	5.5	4.9	4.6	4.7	4.	3.8	3.6	3.4	లు	3.2	3.1	2.9	2.7	22:01	N.	105	130

It is a well known fact, that a cast-iron rod will sustain more torsional pressure than a malleable iron rod of the same dimensions; that is, a malleable iron rod will be twisted by a less weight than what is required to wrench a cast-iron rod of the same dimensions.

When the strength of malleable is less than that of cast iron to resist torsion, it is stronger than cast iron to resist lateral pressure,

and that is in proportion as 9 is to 14.

From the foregoing, it is easy for the millwright to make his shafts of the iron best suited to overcome the resistance to which they will be subject, and the proportion of the diameters of their journals, according to the iron of which they are made.

Ex. What will be the diameter of a malleable iron journal to sustain an equal weight with a cast-iron journal of 7 inches diameter?

 $7^3 = 343.$ 

As  $14:343::9:220\frac{1}{2}$ ; now  $\frac{3}{2}/220.5 = 6.04$  inches diameter.

#### Strength of Wheels.

The arms of wheels are as levers fixed at one end, and loaded at the other; and, consequently, the greatest strain is upon the end of the arm next the axle. For that reason, all arms of wheels should

be strongest at that part, and tapering toward the rim.

The rule for the breadth and thickness of arms, according to their length and number in the wheel, is as follows: Multiply the power or weight acting at the end of the arm by the cube of its length; the product of which, divided by 2656 times the number of arms multiplied by the deflection, will give the breadth and cube of the depth.

Ex. Suppose the force acting at the circumference of a spurwheel to be 1600 lbs., the radius of wheel 6 feet, and number of arms 8, and let the deflection not exceed  $\frac{1}{10}$ th of an inch.

$$\frac{1600 \times 6^3}{2656 \times 8 \times 1} = 163 = \text{breadth and cube of the depth.}$$

Let the breadth be 2.5 inches; therefore  $\frac{163}{2.5} = 65.2$ ; which is

equal to the cube of the depth. Now the cube root of 65.2 is nearly 4.03 inches: this, consequently, is the depth or dimension of each arm in the direction of the force.

Note.—When the depth at the rim is intended to be half that of the axes, use 1640 as a divisor instead of 2656.

The teeth are as beams, or cantilevers, fixed at one end, and loaded at the other. The

The teeth are as beams, or cantilevers, fixed at one end, and loaded at the other. The rule applying directly to them where the length of the beam is the length of the teeth and the depth the thickness of the teeth. For the better explanation of the rule the following example is given.

Ex. The greatest power acting at the pitch line of the wheel is

6000 lbs., and the thickness of the teeth 1½ inch. the length of the teeth being 0.25 feet; it is required to determine the breadth of the teeth.

$$\frac{6000 \times 0.25}{212 \times 1.5^2} = \frac{1500}{477} = 3.2$$
 inches, the breadth required.

In order that the teeth may be capable of offering a sufficient resistance after being worn by friction, the breadth thus found should be doubled; therefore, in the above example, the breadth should be 6.4, or say 6.4 inches.

The following data are gleaned from experiments, which are therefore valuable, and of much use to the practical mechanic:

Rule. Multiply the breadth of the teeth by the square of the thickness, and divide the product by the length; the quotient will be the proportional strength in horse power, with a velocity of 2.27 feet per second.

Ex. What is the power of a wheel, the teeth of which are 6 inches broad, 1.5 inch thick, and 1.8 inch long, and revolving at

the velocity of 3 feet per second?

$$\frac{5^3 \times 6}{1 \cdot 8} \times \frac{13 \cdot 5}{1 \cdot 6} = 7 \cdot 5$$
, strength at 2.27 feet per second, then

$$2.27:7.5::3 = \frac{7.5 \times 3}{2.27} = 9.91$$
 horse power

Rule. The pitch is found by multiplying the thickness by 2.1, and the length is found by multiplying the thickness by 1.2.

Ex. The thickness being 2 inches, what is the pitch and length?

$$2 \times 2.1 = 4.2$$
, pitch.  
 $2 \times 1.2 = 2.4$ , length.

For table of the proportions of wheels, see next page.

Note.—The breadth of the teeth, as commonly executed by the best mechanics, seems to be from about twice to thrice the pitch.

Bean Shot Corper —Take copper, melt it, and pour it in a small stream into boiling water.

FEATHER SHOT COPPER.—Take copper, melt it, and pour it in a

small stream into cold water.

TO PRESERVE WALLS FROM DAMPNESS.—When the walls are about two feet high, use for one row of stones or bricks a mixture of tar. pitch, and fine sand, in the same way as mortar. The composition must be previously melted to a proper consistence.

To PREVENT IRON FROM RUSTING.—Warm your iron till you cannot bear your hand on it without burning yourself. Then rub it with new and clean white wax. Put it again to the fire till it has soaked in the wax. When done rub it over with a piece of serge. This prevents the iron from rusting afterwards.

	*]	CABLE of	the Prope	ortions of I	Wheels.	
Pitch in in.	Thickness in inches.	Breadth in in.	Length in in.	Horse power, at 2'27 feet per second.	Horse power, at 3 feet per second,	Horse power, nt 6 feet per second,
4.2	2.	8.	2.40	13.33	17.61	35.23
3 99	1.9	8.	2-28	13.03	15.90	31.80
3.78	1.8	7.2	2.16	10.80	14 27	28.54
3.57	1.7	6.8	2.04	9.63	12.72	25.54
3:36	1.6	64	1.92	8.53	11 27	22.54
3.15	1:5	6.	1.80	7.59	9.91	19.82
2.94	1.4	5 6	1.68	6.53	8.63	17.26
273	1.3	5 2	1.56	5.63	7.44	14.88
2.52	1.2	4.8	1.44	4.80	6.34	12.68
2.31	1.1	4.4	1.32	4 03	5.32	10 64
2.10	1.	4.	1.20	3.33	4.40	8.81
1.89	•9	4· 3 6	1.08	2.70	3.57	7.14
1 68	·8 ·7	3.2	.96	2.13	2.81	5.62
1.47	•7	2.8	·8 ±	1.63	2.15	4.30
1.26	·6 ·5	2.4	72	1.20	1.59	3.18
1.05	.2	2.	.60	.83	1.10	2.20

### ALLOYS, OR MISCELLANEOUS METALS.

Chaudet's Medal Metal.

Copper 100 parts; tin 4.17. Cast in moulds formed of cupel bone ash.

Lead in Grains.

Lead, melt it, and pour it in a small stream from a height of three or four feet into cold water.

#### Bell Metals.

1. Copper 25 parts; tin 5. Mix.

2. Copper 79 parts; tin 26. Mix.

3. Copper 78 parts; tin 22. Mix.

Common Bell Metal.

Copper 100 parts; tin 50. Mix.

Parisian Bell Metal.

Copper 72 parts; tin 26½; iron 1½. This alloy is used for the bells of small ornamental clocks.

Bath Metal.

Brass 32 parts; spelter 9. Mix.

Another.

Brass 35 parts; zinc 9. Mix.

Brass.

Copper 3 parts. Melt, then add zinc 1 part.

Button Makers' Fine Brass.

Brass 8 parts; zinc 5. Mix.

Button Makers' Common Brass.

Button brass 6 parts; tin 1; lead 1. Mix.

Bright Brass Color.

Brass reduced to fine powder.

Red Brass Color.

Copper filings 3 parts; bole 2. Mix.

Fine Brass.

Copper 2 parts; zinc 1. Mix.

Brass for Wire.

Copper 34 parts; calamine 56. Mix.

To give Plates of Copper a Brass Color.

Expose the plates, after being sufficiently heated, to the fumes of zinc.

To Brass Copper Vessels.

Argol 1 part; amalgam of zine 1; muriatic acid 2; water to fill the vessel. Mix.

Brass or Hard Solder.

Brass 2 parts; zinc 1. A little tin is occasionally added.

Jewellers' Metal.

Copper 30 parts; brass 10; tin 7. Mix.

Fusible Alloys.

1. Bismuth 8 parts; lead 5; tin 3. This is fusible at boiling water heat.

2. Zinc, lead, and bismuth equal parts. This may be fused in a

bit of writing paper, and will melt even in hot water.

3. Lead 3 parts; tin 2; bismuth 5. Mix. This alloy melts at 197° Fah. In using this composition to make casts of seals, gems, &c., it should be employed at the lowest possible temperature at which it will keep fluid; for this purpose it is as well to let it become pasty, and then foreibly impress the substances together.

4. Bismuth 2 parts; tin 3 parts; lead 5. Melt. This alloy fuses

in boiling water.

German Silver.

1. Nickel 1 part; zinc 1; copper 2.

When intended for rolling into plates, use the following:

2. Nickel 25 parts; zinc 20; copper 60; to which may be added 3 of lead.

3. Pure copper 55 parts; nickle 23; zinc 17; iron 3; tin 2.

Fine White German Silver.

Iron 1 part; nickel 10; zinc 10; copper 20. Mix.

German Silver for Castings, &c.

Lead 3 parts; nickel 20: zinc 20; copper 60. Mix.

Genuine German Silver.

Copper  $40\frac{1}{2}$  parts: nickel  $31\frac{1}{2}$ : zinc  $25\frac{1}{2}$ ; iron  $2\frac{1}{2}$ . Mix.

Gilding Metal.

Copper 4 parts; brass 1; tin 1. Fuse together.

Another.

Copper 14 parts; zinc 6; tin 4.

To Separate Gold from Gilt Copper or Silver.

Take a solution of borax in water, apply to the gilt surface, and sprinkle over it some finely powdered sulphur; make the article red hot, and quench it in water; then scrape off the gold, and recover it by means of lead.

Gold in Grains.

Gold 3 parts; silver 1. Granulate by pouring it in a smail stream, from a moderate height, into cold water; then dissolve the silver with nitric acid, and wash well in pure water; next heat the grains, to give them a proper lustre.

Common Gold.

Spanish copper 16 parts; silver 1; gold 2. Melt together.

Onian's Fusible Metal.

Tin 2 parts; lead 3: bismuth 5. Melt. This alloy melts at 197° Fah. The addition of a little mercury renders it still more fusible.

Alloy for Flute Key Valves.

Lead 4 parts; antimony 2. Fuse.

Pewter.

1. Tin 100 parts; antimony 17. Mix.

2. Zinc 1 part; copper 3; lead 8; tin 60. Melt the copper, then add the rest.

3. Fine. Tin 50 parts; antimony 4: bismuth 1; copper 1. Mix, as before.

4. French. Lead 9 parts; tin 41. Mix.

Keller's Medal Alloy. 89; zinc 2.

Tin 9 parts; copper 89; zinc 2.

Gun Metal:

Brass 100 parts; spelter 13; tin 6. Mix.

Another.

Copper 9 parts; tin 1.

Pinchbeck:

1. Brass 2 parts: copper 3. Melt under charcoal dust.

2. Copper 5 parts: zinc 1 Melt the copper, then add the zinc.

Tin Filings.

Take grain tin. melt it in an iron vessel, and stir it, while cooling, until it becomes a powder: then sift it.

ALLOYS. 157

Tin in Grains.

Take Cornish grain tin, melt it, and pour it into a wooden box, well rubbed on the inside with whiting or chalk; close the cover, and continue shaking it violently until the tin is reduced to powder; then wash it in clean water, and dry it immediately.

Mosaic Gold, or Molu.

Take copper and zinc, equal parts. Melt at the lowest temperature that will fuse the former; then mix by stirring, and add more zinc, until the fused alloy becomes perfectly white; lastly, pour it into moulds. The proportion of zinc to the copper is from 50 to 55 per cent., exclusive of what is lost by the heat employed.

Hard White Metal.

Tin 1 part; spelter 3; brass 20. Mix.

Turners' Brass.

Brass 98 parts; lead 2. Mix.

Titania, or Britannia Metal.

1. Plate brass 2 parts; tin 2; bismuth 2; antimony 2; copper 1; arsenic 1. Mix, and add this alloy, at discretion, to melted tin.

2. Spanish. Of Spanish Titania metal there are two kinds. The first is made thus: Antimony 4 parts; tin 2; arsenic 1. The second is made in the following manner: Scrap iron 1 part; antimony 2; nitre a little. Melt, and harden one pound of tin with 2 oz. of this composition. A little arsenic improves the color of this alloy.

Tutenag.

Tin 2 parts; bismuth 1. Fuse.

Type Metal.

Lead 11 parts; antimony 2. Fuse.

Ring Gold.

Spanish copper 6 parts; silver 3; gold 5; Mix.

Prince Rupert's Metal.
Copper 2 parts; melt, and add zinc 1 part.

White Metal.

Brass 1 part; tin 2; antimony 4.

Another.

Lead 20 parts; bismuth 12; antimony 1. Fuse.

Yellow Dipping Metal.

Copper 19 parts; spelter 6. Mix.

A Metal that resembles Silver.

Tin 2 oz.; copper 1 lb. This alloy will make a pale bell metal that will roll and ring very near to sterling silver.

Silver Dust.

Take silver, dissolve it in nitric acid, and precipitate it with slips of bright copper; wash the powder in spirits, and dry it.

Imitation Platina.

Pale brass 8 parts; spelter 5. Mix.

Dessaussy's Steel.

Copper 100 parts; tin 14. This alloy may be hardened and sharpened in a similar way to steel.

Stereotype Metal.

Lead 18 parts; antimony 4 parts; bismuth 2 parts. Melt.

Another.

Lead 16 parts; antimony 3 parts; tin 5 parts; copper 2 parts.

Lead 20 parts; tin 8; antimony 1.

Speculum Metal.

Copper 43 parts; tin 20. Mix.

Another.

Copper 7 parts; melt, and add zine 3 parts, tin 4.

Prince's Metal.

Copper 3 parts; zinc 1.

Another.

Brass 8 parts; zinc 1.

Another.

Zinc and copper, equal parts. Mix.

To make Iron resemble Gold.

Take of linseed oil 3 oz.; tartar 2 oz.; yolk of eggs, boiled hard and beaten, 2 oz.; aloes ½ oz.; saffron 5 grains; turmeric 2 grains. Boil together in an earthen vessel, and with it wash the iron, and it will look like gold. Should there not be linseed oil enough more may be added.

Queen's Metal.

Lead 1 part; bismuth 1; antimony 1; tin 9. Mix.

Another.

Tin 9 parts; bismuth 1; lead 2; antimony 1. Mix by melting.

Another.

Tin 1000 parts; regulus of antimony 80; bismuth 10; copper 40. Melt the copper, then expertly add the rest, and mix well together.

Purified Quicksilver.

Quicksilver 1 part; iron filings 1. Distil in an iron retort, into a vessel containing water.

Mock Gold.

Platina 7 parts; copper 16; zinc 1. Fuse together.

Bronze Metals.

For medals, and small castings-copper 95 parts; tin 4.

Another. Copper 89 parts; tin 8; zinc 3.

Another.

Ancient. Copper 100 parts; tin 7; lead 7.

Another.

Kelly's. Copper 91 parts; zinc 6; tin 2; lead 1.

Blanched Copper.

Copper 8 parts; arsenic ½ part.

Manheim Gold.

Copper 3 parts; zinc 1. Melt separately, then suddenly mix them, and strr well.

Red Tombac.

Copper 11 parts; zinc 2. Mix.

#### FURNITURE PASTE.

1. Melt 1 pound of beeswax with  $\frac{1}{4}$  pint of linseed oil, and add  $\frac{1}{2}$  oz alkanet root; keep it at a moderate heat till sufficiently colored; then remove from the fire, add  $\frac{1}{4}$  pint of oil of turpentine, strain through muslin; and put it into small gallipots to cool.

2. Scrape 4 oz. of wax, and put it into a pipkin with as much oil of turpentine as will cover it, and 4 oz. of powdered resin; melt with a gentle heat, and stir in sufficient Indian red to color it.

3. Equal weights of beeswax, spirit of turpentine, and linseed

oil.

#### Bronze Powder.

The best methods of preparing these powders are probably kept

secret. The following are some of the published recipes:

1. Gold leaf, or alloys of gold, reduced to powder by grinding them with sulphate of potash, or with honey, and washing away the extraneous matter with hot water, and drying the metallic powder.

2. Dutch metal, and other similar alloys, treated in the same

way

5. Verdigris 4 oz.; tutty 2 oz.; sublimate 1 dr.; borax 1 dr.; nitre 1 dr. Mix them into a paste with oil, and fuse the mixture in a crucible. This has failed in some hands, perhaps from the tutty

being factitious.

4. Mix together 100 parts of sulphate of copper, and 50 of crystallized carbonate of soda; apply heat till they unite. Powder the mass, when cold, and add 15 parts of copper filings; mix well, and keep it at a white heat for twenty minutes. Wash and dry the product.

Balls for Scouring—Breeches Balls, Clothes Balls.

1. Bathbrick 4 parts; pipeclay 8; pumice 1; softsoap 1; ochre, umber, or other color, to bring it to the desired shade, q. s.; ox-gall to form a paste. Make it into balls, and dry them.

2. Pipeclay 4 oz.; fuller's-earth ½ oz.; whiting ½ oz.; white

pepper 4 oz; ox-gall sufficient to form it into a paste.

3. Pipeclay 3 oz.; white pepper 1 dr.; starch 1 dr. orris powder 1½ dr. It may be kept in powder, or formed into balls, as above.

#### MENSURATION OF CIRCLES.

Table of the Diameters, Circumferences, and Areas of Circles.

C .					· · · ·			
Diam. in inchas.	es. m	Area in square inches.	Diam. in inches.	nm.	Area 10 square inches.	Diam. in inches.	m.	Area in square inches.
inc	Jircum m mches	rea qua	le Pu	Circum in mches	Area 100 square inches	nch	Circum in inches.	Area in square inches
100	2 3	A s.=	Ğ.7	5 =	A S.I	A -	2 -	A s.ii
	1			10.200	10.500	110	00.054	20 217
	1000	00000	4	12.566	12.566	9	28.274	63.617
18	1963	*00306	18 14	12.959	13 364	1814	28.667	65.396
18	.3927	.01227	4	13.351	14.186		29 059	67.200
16	•5890	.02761	30 1/2 50	13.744	15.033	8 1 2 5 8 1 2 5 8	29.452	69.029
1	.7854	.04909	1 2	14.137	15.904	1 2	29.845	70.882
1.6	.9817	.07670	5 8	14.529	16.800	5 8	30.237	72.759
16 83 6 145 6 867 6	1.1781	.11044	3	14.922	17.720	3	30:630	74.662
7	1:3744	15033	8 4 7 8	15.315	18.665	84 7 8	31.023	76.588
1 : 1	the second states	I Company		A 1-1	Course of	1	07.470	
2 9	1.5708	19635	5	15 708	19.635	10	31.416	78.540
1.8	1.7671	24850	1 8	16:100	20.629	1/8	31.808	80 515
129 1658 11684 13678 1785	1.9635	.30680	14 88 12 58	16.493	21.647	14 88 12 58	32.201	82 516
1.6	2 1598	.37122	8	16.886	22:690	8	33.594	84.540
34	2.3562	44172	$\frac{1}{2}$	17.278	23.758	1/2	32 986	86.590
13	2.5525	•51849	5	17.671	24.850	5 8	33.379	88.664
78	2.7489	.60132	丑	18.064	25.967	3/4	33.772	90.762
1.5	2.9452	69030	84 78	18.457	27.108	34 7 8	34.164	92.885
1	3.141	·785	6	18.849	28.274	11	34.557	95.033
0.00	3.141			18.849	29.464		34.950	95.055
8		·994 1·227	8	19.635	30.679	8	35.343	99:402
8	3·927 4·319		4		31.919	1	35.735	101 623
8	4.712	1.484	8	20 027 20 420	33.183	8	36.128	
5	5.102	1.767	2 5	20.813	34.471	5	36.521	106.139
8	5.497	2·073 2·405	8.	21 205	35.784	8	36.913	108.434
10 14 00 12 50 04 70	5.890	2.761	18 14 80 12 50 84 70	21 203	37.122	1/20 1/40 cito 1/20 1/20 20/41 7/20	37.306	110.753
	9.990	2.401		21 998	31122	- 0	.01 000	110 755
2	6.283	3.141	7	21.991	38 484	12	37.699	113.097
18	6.675	3.546	1	22:383	39.871	1	38.091	115.466
1	7.068	3.976	1	22.776	41.282	1	38.484	117.859
8	7.461	4.430	8	23.169	42.718	38	38.877	120.276
1/2	7.854	4.908	1 1	23 562	44.178	$\frac{1}{2}$	39.270	122.718
5	8.246	5.411	18148812588478	23.954	45.663	1/8 1/4 8/80 1/81 5/80 8/4 7/8	39 662	125.184
84	8.639	5.939	84	24 347	47.173	84	40.055	127.676
21 10 14 30 12 50 64 70	9.032	6 491	7 8	24.740	48.707	7 8	40 448	130.192
	9.424	7.068	8	25.132	50.265	13	40.840	132.732
1 1	9.817	7.669		25.525	51.848	1 1 8	41.233	135.297
1	10.510	8.295	8	25.918	53.456	8	41 626	137.886
3	10.602	8.946	3	26.310	55.088	8	42 018	140.500
8	10.995	9 621	8	26.703	56.745	8	42.411	143.139
5	11.388	10.320	5	27.096	58.426	5.	42.804	145.802
8	11.781	11.044	8	27.489	60.132	8	43.197	148.489
00 1/0 1/4 s/0 1/2 5/0 s/4 7/E	12.173	11.793	18 14 50 12 50 84 70	27.881	61.862	14 000 102 500 004 700	43.589	
8	12110	11 100	8	21 001	01 0021	8		

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
14	43.98	153.93	19	59.69	283:52	24	75.39	452.39
1 - 1	44.37	156.69	1 8	60.08	287.27	18	75.79	457.11
42	44.76	159.48	4	60.47	291.03	1	76.18	461.86
्रक्ष नेत्र त्यंक क्षेत्र नेव	45.16	162.29	8	60.86	294.83	36 12 58 34	76.57	466.63
$\frac{1}{2}$	45.55	165.13	12 58	61.26	298.64	1/2	76.96	471.43
5	45.94	167.98	58	61.65	302.48	\$	77.36	476.25
Ž	46.33	170.87	8 4 7 8	62.04	306.35		77.75	481.10
8	46.73	173.78	78	62.43	310.24	78	78.14	485.97
015	47.12	176.71	20	62.83	314.16	25	78.53	490.87
1814	47.51	179.67	18	63.22	318.09	1 8	78.93	495.79
4	47.90	182.65	1	63.61	322.06	4	79:32	500.74
250 - 162 take exte	48 30	185 66	S\$0 -\$0 5\$0 \$\$4 7-\$0	64.01	326.05	8	79.71	505.71
2 5	48.69	188.69	2	64.40	330.06	2	80.10	510.70
*	49.08	191.74	8	64.79	334.10	1 5 5 6 6 7 7 8	80.50	515.72
4	49.48	194.82	4	65.18	338.16	4	80.89	520.76
78	49.87	197.93	-8	65.28	342.25	Ś	81.28	525.83
16	50.26	201.06	21	65.97	346.36	26	81.68	530.93
1814	50.65	204.21	1 8	66.36	350.49	1/8	82:07	536.04
1/4	51.05	207.39	14	66.75	354.65	1/4	82:46	541.18
- 골	51.44	210 59	38	67.15	358.84	8	82.85	546.35
0 1	51.83	213.82	38 1/2 5/8	67.54	363.05	1/2	83.25	551.54
5 8	52.22	217.07	\$	67.93	367.28	S 122 5 50 8 4	83.64	556.76
8 4	52.62	220.35	84	68.32	371.54	84	84:03	562.00
78	53.01	223.65	7/8	68.72	375.82	78	84:43	567.26
17	53.40	226.98	22	69.11	380.13	27	84.82	572.55
1 8	53.79	230.33	1 8 1 4	69.50	384.46	18.	85:21	577.87
1	54.19	233.70	4	69.90	388.82	4	85:60	583.20
8 8	54.58	237.10	8	70.29	393.20	8	86.00	588.57
1 2 5	54.97	240.52	8 1 2	70.68	397.60	००० न्य ५०० ०५४ न्य	86.39	593.95
5 8	55.37	243.97	5.8	71.07	402.03	8	86.78	599.37
8 4 7 8	55.76	247.45	34	71.47	406.49	4	87.17	604.80
1	56.15	250.94	78	71.86	410.97	8	87.57	610.26
18	56.54	254.46	23	72.25	415.47	28	87.96	615.75
1 18	56.94	258.01	1/8	72.64	420.00	1/8	88 35	621.26
1	57 33	261.58	1/4	73.04	424.55	1	88.75	626.79
3	57.72	265.18	38	73 43	429.13	8	89.14	632.35
$\frac{1}{2}$	58.11	268 80	$\frac{1}{2}$	73.82	433.73	14 spo 162 5/2 sp4	89.53	637.94
5	58.21	272.44	5	74.21	438.36	5	89.92	643.54
7.	58.90	276.11	8 4	74 61	443.01	3	90 32	649.18
78	59.29	279.81	-7	75.00	447.69	7 8	90.71	654.83

Diam.	Circum.	-Area.	Diam.	Circum.	Aīea,	Diam.	Circum.	Area.
29	91.10	660.52	34	106.8	907.92	39	122:5	1194.5
	91:49	666.22	1 8	107.2	914.61	1 8	122.9	1202.2
Ĭ	91.89	671.95	1	107.5	921.32	1	123.3	1209.9
10148012508472	92.28	677.71	निसंक्ष्मित नियं क्ष्मित क्षेत्र क्षेत्र निय	107.9	928.06		123.7	1217.6
1/2	92.67	683.49	1/2	108.3	934.82	व्यक्त न्या ध्येक क्षेत्र	124.0	1225.4
5	93.06	689 29	5 8	108.7	941 60	5	124.4	1233.1
34	93.46	695.12	34	109.1	948.41	84	124.8	1240.9
78	93.85	700.98	8	109.5	955.25	7 8	125.2	1248.7
30	94.24	706.86	35	109.9	962.11	40	125.6	1256.6
101480101050847	94.64	712.76	न्क्र नृक्ष क्षेत्र नृष्य क्षेत्र क्ष्म्य नृद्	110.3	968.99	1 8	126.0	1264.5
4	95.03	718.60	4	110.7	975.90	4	126.4	1272.3
8	95.42	724.64	8	111.1	992.84	व्हेळ जूव क्षेत्र	126.8	1280.3
$\frac{1}{2}$	95.81	730.61	2	111 5	889.80	2	127.2	1288.2
8	96.21	736.61	8	111.9	996.78	8	127.6	1296.2
34	96.60	742.64	*	112.3	1003.71	2	128.0	1304.2
8	96.99	748.69	8	112.7	1010.81	7/8	128.4	1312.2
31	97.38	754.76	36	113.0	1017 87	41	128.8	1320.2
8	97.78	760.86	1 8 1 4	113.4	1024.95	8	129.1	1328.3
4	98.17	766.99	4	113.8	1032.06	1 4	129.5	1336.4
8	98.56	773.14	8	114.2	1039.19	8	129·9 130·3	1344·5 1352·6
2	98.96	779.31	2	114·6 115·0	1046·39 1053·52	1 2 5	130 7	1360.8
8	99.35	785·51 791·73	8	115.4	1060.73	5/80 85/4	131.1	1369.0
न्य न्य क्षेत्र न्य क्षेत्र क्ष्य न्य	99.74 100.13	797.97	30 12 50 x4 70	. 115.8	1067.95	7 8	131.5	1377.2
32	100.5	804.24	37	116.2	1075.21	42	131.9	1385.4
	100.9	810.54		116.6	1082.48	1 8	132.3	1393.7
8	101.3	816.86	1	117.0	1089.79		132.7	1401 9
3	101.7	823.21	.3	117.4	1097.11	न्स क्षेत्र न्या क्ष	133.1	1410.2
1	102.1	829.57	i	117.8	1104.46	1	133.5	1418.6
5	102.4	835.97	5	118.2	1111.84	5	1339	1426.9
3	102.8	842:39	3	118.5	1119.24	8	134.3	1435.3
10146012150505470	103.2	848.83	1 to 1 4 cito 1 2 5 to cit 7 to	118.9	1126.66	7 8	134.6	1443.7
33	103.6	855:30	38	119.3	1134.11	43	135.0	1452.2
	104.0	861.79	1 8	1197	1141.59	1 8	135.4	1460.6
i	104.4	868.30	1	120.1	1149.08	1	135.8	1469.1
بأبه بإج مؤه جاء مؤه هاء عرفه	104.8	874.84	14 500 12 50034 70	120.5	1156.61	8	136 2	1477.6
1 1	105.2	881.41	1/2	120.9	1164.15	1	136.6	1486.1
5	105.6	888.00	5	121.3	1171.73	5 8	137:0	1494.7
34	106.0	894.61	3	121.7	1179.32	84 7 8	137.4	1503.3
7	106.4	901.25	7	122.1	1186.94	3	137.8	1511.9

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
-44	138.2	1520.53	46	144.5	1661.90	48	150.7	1809.56
1 8	138.6	1529.18	1 8	144 9	1670 95	1/8	151.1	1818.99
10 14 spo 12 spo at 14	139.0	1537.86	-10 -14 m18 -10 150 004 -10	145.2	1680.01	14 38	151.5	1828.46
38	139.4	1546.55	38	145.6	1689 10	8	151.9	1837.93
$\frac{1}{2}$	139.8	1555.28	$\frac{1}{2}$	146.0	1698.23	122 500 374 718	152.3	1847.45
96	-140.1	1564.03	3	146.4	1707:37	8	152.7	1856 99
2	140.5	1572.81	4	146.8	1716.54	4	153.1	1866.55
8	140.9	1581.61	8	147.2	1725 73	8	153.5	1876.13
45	141.3	1590.43	47	147.6	1734.94	49	153:9	1885.74
	141 7	1599.28		148.0	1744.18	1 8	154.3	1895:37
8	142.1	1608.15	8	148.4	1753.45		154.7	1905.03
3	142.5	1617 04	3	148.8	1762.73	14 38	155.1	1914.70
10 14 000 10 500 m4 70	142.9	1625.97	10 14 00 10 50 m470	149.2	1772.05	1 2	155.5	1924.42
5	143.3	1634.92	5	149.6	1781.39	5.	155.9	1934.15
3 4	143.7	1643.89	3 4	150.0	1790.76	347	156.2	1943.91
る	144.1	1652.88	7 8	150.4	1800.14	7 8	156.6	1953.69

Diam.	Circum.	Area in square in.	Area in square feet.	Diam in.	Circum.	'Area in square in.	Area in square feet.
50	157.0	1963.5	13.63	55	172.7	2375.8	16.49
14 12 84	157.8	1983.1	13.77	4	173.5	2397.4	16.64
2	158.6	2002.9	13.90	$\frac{1}{2}$	174.3	2419:2	16.80
4	159.4	2022.8	14.04	: 84	175.1	2441.0	16.95
51	160.2	2042.8	14.18	56	175.9	2463.0	17.10
14 12 84	161.0	2062.9	14.32	1	1767	2485.0	17.25
$\frac{1}{2}$	161.7	2083.0	14.46	1/2	177.5	2507.1	17.41
84	162.5	2103.3	14 60	茎	178.2	2529.4	17.56
52	100.0	0100.5	14.54	e 17	1400	0.22.2	1 h h o
	163·3 164·1	2123·7 2144·1	14.74	57	179.0	2551.7	17.72
14 1-7-21 RI4	164.9		14 89	1 4	179.8	2574.1	17.87
2 8	165.7	2164·7 2185·4	15·03 15·17	2 2	180.6	2596.7	18:03
4	109.1	21854	19.17	4	181.4	2619:3	18.19
53	166.5	2206.1	15.32	58	182.2	2642.0	18.34
1	167.2	2227.0	15.46	1	182.9	2664.9	18:50
1/2	168.0	2248.0	15.61	1/2	183.7	2687.8	18.68
84	168.8	2269 0	15.75	84	184.5	2710.8	18.82
-							
54	169.6	2290.2	15.90	59	185.3	2733.9	18.98
4	170.4	2311.4	16.05	4	186.1	2757.1	19.14
1 8 4	171.2	2332.8	16.20	1/2	186.9	2780.5	19:30
4	172.0	2354.2	16.34	#	187.7	2803.9	19 47
			1 1				

Diam.	Circum.	Area in square in.	Area in square feet.	Diam in.	Circum.	Area in square in.	Area in square fee
2-07-		- 11 00	THE C	x	SE box	wat ve	1 14
2,0	1.00	A 111	1075) 0	11/2	1000	0.0.0 200	7 0
60	188.4	2827.4	19.63	69	216.7	3739.2	25.96
1	189.2	2851.0	19.79	1	217.5	3766.4	26.15
1	190.0	2874.7	19.96.	1/2	218.3	3793.6	26.34
84	190-8	2898.5	20.12	34	219.1	3821.0	26.53
	1.448	1. (4.)	4270 ( = )	me.		708 30	
61	191.6	29224	20.29	70	219.9	3848.4	26.72
1	192.4	2946.4	20.46	14	220.6	3875.9	26.91
1/2	193.2	2970.5	20.62	1/2	221.4	3903.6	27.10
34	193.9	2994.7	20.79	3/4	222.2	3931.3	27.30
11	11601		MITT A	111	- 101	COST CO.	
62	194.7	3019.0	20.96	71	223.0	3959.2	27.49
1	195.5	3043.4	21.13	1/4	223.8	3987.1	27.68
i	196.3	3067.9	21.20	1 2	224.6	4015.1	27.87
14 1/2 8/4	197.1	3092.5	21.47	3 4	225.4	4043.2	28.07
	1 Ha		AROL IN		1000	Charles I will de-	
63	197.9	3117.2	21.64	72	226.1	4071.5	28.27
4	198.7	3142.0	21.81	1	226.9	4099.8	28.47
1/2	199.4	3166 9	21.98	1/2	227.7	4128 2	28.66
34	200.2	3191.9	22.16	84	228.5	4156.7	28.86
-				-			-
64	201.0	3216.9	22.34	73	229.3	4185.3	29.06
1	201.8	3242.1	22.51	4	230.1	4214.1	29.26
1	202.6	3267.4	22.68	1/2	230.9	4242.9	26.46
84	203.4	3292.8	22.86	34	231.6	4271.8	29.66
65	204.2	3318.3	23.04	74	232.4	4300.8	29.86
4	204.9	3343.8	23.22	1	233.2	4329.9	30.06
1 2	205.7	3369.5	23.39	1	234.0	4359.1	30.26
84	206.5	3395.3	23.57	3 4	234.8	4388.4	30.47
4	2000	0030 0	20 01	4	2010	1000 1	00 11
66	207:3	3421.2	23.75	75	235.6	4417.8	30.67
1	208.1	3447.1	23.93	1	236.4	4447:3	30.88
1	208.9	3473.2	24.11	1 2	237.1	4476.9	31.09
34	209.7	3499.3	24:30	34	237.9	4506.6	31.30
•				*			100
67	210.4	3525.6	24.48	76	238.7	4536.4	31.50
1	211.2	3552.0	24.66	14	239.5	4566.3	31.71
1 1 2	212.0	3578.4	24.84	1 2	240.3	4596.3	31.91
84	212.8	3605.0	25.03	34	241.1	4626.4	32.12
00	010.0	0.001.0	07.00	hh	041.0	10=0.0	00.00
68	213.6	3631.6	25 22	77	241.9	4656.6	32.33
1 4	214.4	3658.4	25.40	4	242.6	4686 9	32.54
1 2 8 4	215.1	3685·2 3712·2	25·59 25·77	1/2 8/4	243.4	4717.2	32·75 32·96

Diam.	Circum.	Area in	Area in	Diam.	Circum.	Area in	Area in
in.	inches.	square in.	square feet	in.	inches.	square in.	square fee
78	245.0	4778:3	-33.18	87	273.3	5944.6	41.28
1	245.8	4809.0	33.39	1	274.1	5978.9	41.52
1	246.6	4839.8	33.60	1	274.8	6013.2	41.75
12 84	247.4	4870.7	33.81	12 84	275.6	6047.6	41.99
4	ATI T	10.0	55 01	<b>4</b>	2100	0041 0	41 33
79	248.1	4901.6	34.03	88	276.4	6082.1	42.23
4	248.9	4932.7	34.24	1	277.2	6116.7	42.47
$\frac{1}{2}$	249.7	4963.9	34 46	1/2	278.0	6151.4	42.71
3	250.5	4995.1	34.68	84	278.8	6186.2	42 95
915		150	1 100				
80	251.3	5026.5	34.90	89	2796	6221.1	43.20
1	252.1	5058.0	35.12	4	280.3	6256.1	43.44
1	252.8	5089.5	35.34	1	281.1	6291.2	43.68
84	253.6	5121.2	35.56	12 84	281.9	6326.4	43.92
*		2017-1-1	A	4	-010		
81	254.4	5153.0	35.78	90	282.7	6361.7	44 17
- N	255.2	5184.8	36.00	1	283.5	6397-1	44.42
14 12 84	256.0	5216.8	36.22	1 2	284.3	6432.6	44 66
8	256.8	5248.8	36 44	84	285.1	6468.2	44.81
4	2000	02100	00 11	4	2001	0100 2	1101
82	257.6	5281:0	36.67	91	285.8	6503.8	45.16
1	258.3	5313:2	36 90	1/4	286.6	6539.6	45'41
1/2	259.1	5345.6	37.12	14 12 84	287.4	6575.5	45.66
34	259.9	5378.0	37:34	34	288.2	6611.5	45'91
83	260.7	5410.6	37.57	92	289.0	6647.6	46.16
70.70	261.5	5443.2	37.79		289.8	6683.8	46 41
1	262.3	5476.0	38.02	1/4 1/2	290.5	6720.0	46.66
14 12 84	263.1	5508 8	38.25	84	291.3	6756.4	46.91
4	2001	00000	00 70	4	1 4 6	0.001	1911
84	263.8	5541.7	38.48	93	292.1	6792.9	47.17.
4	264.6	5574.8	38.71	1	292.9	6829.4	47.43
1/2	265.4	5607.9	38.94	1/2	293.7	6866.1	47.68
34	266.2	5641.1	39.07	84	294.5	6902.9	47.93
AF	0		841	7	1 1 2 2	1	
35	267:0	5674.5	39.40	94	295.3	6939.7	48.19
1	267.8	5707.9	39.63	1	296.0	6976.7	48.45
1	268.6	5741.4	39.87	1/2	296.8	7013.8	48.70
84	269.3	5775.0	40.10	84	297.6	7050.9	48.96
36	270:1	5808.8	40.33	95	298.4	7088.2	49.22
	270.9	5842.6	40.57		299.2	7125.5	49.48
14 12 84	271.7	5876.5	40.80	1/2	300.0	7163.0	49.64
2	272.5	CONTRACTOR OF THE PARTY OF THE		\$ H		7200.5	50.00
4	2120	5910.5	41.04	4	300.8	12000	00 00

Diam. in.	Circum. inches.	Area in square in.	Area in square feet.	Diam. in.	Circum. inches.	Area in square in.	Area in square feet
96	301.5	7238-2	50.26	121	380.1	11499.0	79.85
1	302.3	7275.9	50.52	122	383.2	11689.9	81.18
1/2	303.1	7313:8	50.78	123	386.4	11882.3	82.51
34	303.9	7351.7	51.05	124	389.5	12076.3	83.86
				125	392.7	12271.8	85.22
97	304.7	7389.8	51.35			U. T (0)	N. Dark
14 12	305.2	7427.9	51.57	126	395.8	12469.0	86.59
	306.3	7466.2	51.84	127	398.9	12667.7	87.97
4	307.0	7504.5	52.11	128	402.1	12867.9	89 36
				129	405.2	13069 8	90.76
98	807.8	7542.9	52.38	130	408.4	13273.2	92.17
1	308.6	7581.5	52.65	= 1	7 373	31 15	= 1/4
1/2	309.4	7620.1	52.91	101	411.0	104500	00.50
34	310.2	7658.8	53.18	131	411.5	13478.2	92.59
00	011.0	70077	50.45	132	414.6	13684.8	95 03
99	311.0	7697.7	53.45	133	417·8 420·9	13892·9 14102·6	96·47 97·93
14	311.8	7736.6	53.72	134	420.9	14313.9	99.40
1 2 8	313.3	7775.6	54.26	150	4241	14919.9	9940
100	314.1	7814·7 7854·0	54.54	165		PLA BY	EIL
100	914 1	78040	94 94	136	427.2	14526.7	100.88
101	317.3	8011.7	55.63	137	430.3	14741.1	102.36
102	320.4	8091.2	56.74	138	433.5	14957-1	103.87
103	323.5	8332.3	57.86	139	436.6	15174.7	105.37
104	326.7	8494.9	58.99	140	439.8	15393.8	106.90
105	329.8	8659.0	60.13				
100	0200	00000	00.15	141	442.9	15614.5	108.43
106	333.0	8824.7	61.28	142	446.1	15836·8	109.97
107	336.1	8992.0	62.44	143	449.2	16060.6	111.53
108	339.2	9160 9	63.61	144	452.3	16286.0	113.09
109	342.4	9331.1	64.80	145	455.5	16513-0	114.67
110	345.5	9503.3	65.99		200		100
		THE LAN	0771	140	4=0.0	10541	110.00
111	348.7	9676.9	67.20	146	458.6	16741.5	116.26
112	351.8	9852.0	68.41	148	461.8	16971.7	117·86 119·46
113	355.0	10028.7	69.64	148	464.9	17203·4 17436·6	121.08
114.	358.1	10207.0	70.88	150	471.2	17671.5	122.71
115	361.2	10386.9	72.13	100	4/1 2	110113	122/1
		F16 11	19 19 1	70.1-		100	12 1 1
116	364.4	10568.3	73.39	151	474.3	17907.9	124.36
117	367.5	10751.3	74.66	152	477.5	18145.9	126.01
118	370.7	10935.9	75.94	153	480.6	18385.4	127.67
119	373.8	11122.0	77.23	154	483.8	18626.5	129.35
120	376.6	11309.7	78 54	155	486.9	18869.2	131.03

TABLE

Of the Circumferences and Areas of Circles, from 1 to 50 feet, advancing by an inch.

Diam. ft. & in.	Circumference in feet and in.	Area in feet.	Diam. ft. & in.	Circumference in feet and in.	Area in feet.
1 ft.	3 15	.7854	8	13 41	14.1862
1	3 45	9217	4	13 74	14.7479
2	3 8	1.0690	5	13 101	15.3206
3	3 11	1.2271	6	14 15	15.9043
4	4 21/8	1.3962	7	14 45	16.4986
5	4 5 8	1.5761	8	14 77	17.1041
6	4 81	1.7671	9	14 11	17.7205
7	4 115	1 9689	10	15 21	18.3476
8	5 24	2.1816	11	15 51	18.9858
9	5 57	2.4052	5 ft.	15 81	19.6350
10	5 9	2.6398	1	15 118	20.2947
11	6 21	2.8852	2	16 28	20.9656
2 ft.	6 38	3.1416	3	16 53	21.6475
1	$\frac{6}{6}$	3.4087	4	16 9	22.3400
2 3	6 95	3.6869	5	$17  0\frac{1}{3}$ $17  3\frac{1}{4}$	23.0437
4	7 0 <del>3</del> 7 3 <del>3</del>	$3.9760 \\ 4.2760$	7		23.7583
5	7 3 <del>7</del> 7 7	4.5869	8	8	24·4835 25·2199
6	7 101	4.9087	9	17 9 <del>§</del> 18 0 <del>§</del>	25.9672
7	8 1\frac{3}{8}	5.2413	10	18 37	26.7251
8	$8  ext{ } 4\frac{1}{3}$	5.5850	11	18 7 18	27.4943
9	8 75	5.9395	6 ft.	$18 \ 10\frac{1}{8}$	28.2744
10	8 103	6 3049	1	19 11	29.0649
11	$9 1\frac{7}{8}$	6.6813	2	19 48	29.8668
3 ft.	9 5	7.0686	5	19 73	30.6796
1	9 81	7.4666	4	19 105	31.5029
2	9 118	7.8757	5	$20  ext{ } 1\frac{7}{8}$	32.3376
3	10 21	8 2957	6	$20  ext{ } 4\frac{7}{8}$	33.1831
4	$10  5\frac{5}{8}$	8.7265	7	20 81	34.0391
5	10 84	9.1683	8	$20 \ 11\frac{1}{2}$	34.9065
6	10 117	9.6211	9	21 25	35.7847
7	11 3	10.0846	10	$21  5\frac{1}{2}$	36.6735
8	11 61	10.5591	11	21 84	37.5736
9	$11   9\frac{3}{8}$	11.0446	7 ft.	21 117	38.4846
10	$12   5\frac{1}{2}$	11.5409	1	22 3	39 4060
11	12 35	12:0481	2	$\frac{22}{8}$	40.3388
4 ft.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	12:5664	3	22 94	41.2825
2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13.0952 13.6353	4	23 08	42.2367
2	15 1	19.0999	5	23 21	43.2022

Diam. t. & in.	Circumference in teet and in.	Area in feet.	Diam. ft. & in.	Circumference in feet and in.	Area in feet.
6	23 64	44.1787	3	45 41	99.4021
7	23 11	45.1656	4	35 71	100.8797
- 8	24 11	46.1638	5	35 105	102:3689
9	24 41	47.1730	6	36 11	103.8691
10	$24 7\frac{1}{4}$	48.1926	7	36 41	105:3794
11	24 108	49.2236	8	36 74	106.9013
8 ft.	25 1	50.2656	9	36 107	108.4342
1	$25  ext{ } 4\frac{5}{8}$	51.3178	10	37 28	109.9772
2	25 7 3	52.3816	11	37 51	111.5319
3	25 11°	53.4562	12 ft.	37 84	113.0976
4	26 21	54.5412	1	37 111	114.6732
5	26 51	55.6377	2 -	$38 \ 2\frac{5}{8}$	116.2607
6	26 8	56.7451	3	38 58	117.8590
.7	26 111	57.8628	4	38 87	119.4674
8 :	27 28	58 9920	5	39 0	121:0876
9	27 5星	60.1321	6	39 31	122 7187
10	27 9	61.2826	7	39 68	124:3598
11	28 01	62.4445	8	39 94	126 0127
9 ft.	28 31	63.6174	9	40 05	127.6765
1	28 68	64.8006	10	40 34	129.3504
2	28 91	65.9951	11	40 67	131:0360
3	29 05	67.2007	13 ft.	40 10	132.7326
4	29 33	68.4166	1	41 11	134:4391
5	29 7	69.6440	2	41 48	136.1574
6	29 101	70.8823	3	$41 7\frac{1}{2}$	137.8867
7	30 11	72.1309	4	41 105	139.6260
8	30 48	73.3910	5.	42 15	141.3771
9	30 71	74.6620	6	42 47	143.1391
10	30 115	75.9433	7	42 8	144.9111
11	31 14	77.2362	8	42 111	146.6949
0 ft.	31 5	78.5400	9	43 21	148.4896
1	31 81	79.8540	10	43 51	150.2943
2	31 111	81.1795	11	43 85	152.1109
3	32 28	82.5160	14 ft.	43 114	153.9384
4	32 51	83.8627	1	44 27	155 7758
5	32 85	85.2211	2	44 6	157.6250
6	32 114	86.5903	3	44 91	159:4852
7	33 27	87.9697	4	45 01	161.3553
8	33 6 1	89.3608	5	45 31	163.2373
9	33 91	90.7627	6	45 65	165.1303
10	$34  0 \frac{3}{8}$	92.1749	7	45 98	167.0331
11	34 31	93.5986	8	46 07	168.9479
11 ft.	34 65	95.0334	9	46 4	170.8735
1	34 98	96.4783	10	46 71	172.8091
2	35 07	97.9347	11	46 114	174.7565

Diam. ft, & in.	Circumfere	ence d in.	Area in feet.	Diam. ft. & in.	Circur in fee	nference t and in.	Area in feet.
15 ft.	47 1	1	176.7150	9	58	103	276.1171
1	47 4		178.6832	10	59	2	278.5761
2	47 7		180.6634	11	59	51/8	281.0472
3	47 10		182.6545	19 ft.	59	81	283.5294
4	48 2		184 6555	1	59	111	286.0210
5	48 5		186.6684	2	60	$2\frac{1}{2}$	288.5249
6	48 8	i	188.6923	3	60	55	291.0397
7	48 11	3	190.7260	4	60	83	293:5641
8	49 2		192.7716	5	60	117	296.1107
9	49 5	8	194.8282	6	61	31	298.6483
10	49 8	7	196.8946	307	61	$6\frac{1}{4}$	301.2054
11	50 0		198.9730	8	61	$9\frac{1}{2}$	303.7747
16 ft.	50 3	1.	201.0624	9	61	$0\frac{1}{2}$	306.3550
1	50 6	1	203.1615	10	62	35	308.9448
2	50 9	5.	205.2726	11	62	63	311.5469
3	51 0	1 2	207:3946	20 ft.	62	97	314.1600
4	51 3	3	209.5264	1	63	11	316.7824
5	51 6	1	211.6703	2	63	41	319.4173
6	51 10		213.8251	3	63	78	322.0630
7	52 1	1 8	215.9896	4	63	111	324.7182
8	52 4	1	218.1662	5	61	15	327:3858
9	52 7	3	220.3537	6	64	48	330.0643
10	52 10	1	222.5510	7	64	77	332.7522
11	53 1	5	224.7603	8	64	11	335.4525
17 ft.	53 4	7	226.9806	9	65	24	338.1637
- 1	53 8	19	229.2105	10	65	58	340.8844
2	53 11		231.4525	011	65	81	343.6174
3	54 21	1	233.7055	21 ft.	65	115	346.3614
4	54 5	8.	235.9682	1	66	28	349.1147
5	54 81		238.2430	2	66	57	351.8804
6	54 115	3	240.5287	3	66	9	354.6571
7	55 24	-	242.8241	4	66	01	357.4432
8	55 6	914	245.1316	5	67	38	360.2417
9	55 91	3	247.4500	6	67	$6\frac{1}{2}$	363.0511
10	56 04		249.7781	0.70	67	95	365.8698
11	56 31	1	252.1184	8	68	08	368.7011
18 ft.	56 64		254.4696	9	68	37	371.5432
1	56 95	3.	256.8303	10	68	7	374.3947
2	57 03	7.	259.2033	11	68	101	377.2587
3	57 4	7	261.5872	22 ft.	69	18	380.1336
4	57 71		263.9807	1	69	41	383.0177
5	57 104		266.3864	2	69	75	385.9144
6	58 1		268.8031	3	69	104	388.8220
7	58 4	1	271.2293	4	70	17	391 7389
8	58 75	5	273 6678	5	70	5	394.6683

Diam. ft. & in.	Circum in feet	and in.	Area in feet.	ft. & in.		and in.	Area in feet.
116	70	81	397.6087	3	82	51	541.1896
10.70	70	111	400.5583	4	82	85	544.6299
18	71	21	403.5204	5	82	117	548 0830
9	71	55	406.4935	6	83	3	551.5471
10	71	88	409.4759	7	83	61	555.0201
711	71	$11\frac{7}{8}$	412.4707	8	83	$9\frac{?}{4}$	558.5059
23 ft.	72	3	415.4766	9	84	08	562.0027
111	72	61	418.4915	10	84	31	565.5084
2	72	93	421.5192	11	84	65	569.0270
. 3	73	$0\frac{1}{2}$	424.5577	27 ft.	84	97	572.5566
4	73	35	427.6055	1	85	1	576.0949
5	73	63	430.6658	2	85	41	579.6463
6	73	97	433.7371	3	85	81	583.2085
117	74	1	436.8175	4	85	113	586.7796
18	174	41	439.9106	5	86	$1\frac{1}{2}$	590.3637
009	74	71	443:0146	6	86	45	593.9587
10	74	105	446.1278	107	86	77	597 5625
11	75	15	449.2536	8	86	11	601.1793
24 ft.	75	48	452 3904	9	87	21/8	604 8070
1	75	77	455.5362	: 10	87	51	608.4436
2		1i°	458.6948	11	87	88	612.0931
3	76	21/8	461.8642	28 ft.	87	$11\frac{1}{2}$	615 7536
4	76	51	465.0428	0.1	88	25	619-4228
5	76	81	468:2341	2	88	58	623.1050
6		115	471 4363	3	. 88	9	626.7982
3.7	77	$2\frac{3}{4}$	474.6476	4	89	01	630.5002
8	77	57	477.8716	5	: 89	31	634.2152
9	77	9	481.1065	6	89	68	637.9411
10	78	01	484.3506	7	89	91	641.6758
11	78	31	487.6073	8	90	05	645.4235
25 ft.	78	63	490.8750	9	90	33	649.1821
1	78	91	494.1516	10	90	67	652.9495
172	79	03	497.4411	111		111	656.7300
13	79	37	500.7415	29 ft.	91	11	660.5214
4	79	71	504.0510	10-10	91	48	664 3214
5		111	507:3732	2	91	71	668.1346
6	80	11	510.7063	. 3	- 91	105	671.9587
7	80	48	514.0484	4	92	134	675.7915
8	80	75	517.4034	5	.92	47	679.6375
059		108	520.7692	6	92	81	683.4943
10	81	17	524.1441	7		111	687.3598
11	81	5	527.5318	8	93	23	691-2385
26 ft.	81	81	530.9304	9.	93	$5\frac{1}{2}$	695.1280
1		111	534.3379	10	93	85	699.0263
2	82	28	537.7583	11	93	11%	702.9377

Diam. ft. & in.	Circumference in feet and in.	Area in feet.	Diam.	Circumference in feet and in.	Area in feet.
30 ft.	94 27	706.8600	9	106 04	894.6196
30 Jt.	94 6	706.8600	10	106 38	899.0413
2		714.7350	11	106 65	903.4763
. 3		718.6900	34 ft	106 98	907.9224
4	0	722.6537	1	107 07	912:3767
5	$95   3\frac{1}{2}$ $95   6\frac{5}{4}$	726.6305	2	107 4	916.8445
6	95 0 <del>8</del> 95 93	730.6183	3	107 71	921.3232
7	$96 \ 0\frac{7}{8}$	734 6147	4	107 101	925.8103
8	96 4	738.6242	5	108 18	930.3108
9	96 71	742.6447	6	108 45	934.8223
10	95 108	746.6738	7	108 74	939.3421
11		750.7161	8	108 107	943.8753
31 ft	$97   1\frac{1}{2}$ $97   4\frac{5}{4}$	754.7694	9	108 108	948.4195
1	G I	758.8311	10		952.9720
2	$97   7\frac{8}{4}$ $97   10\frac{7}{8}$	762 9062	11	$109  5\frac{1}{8}$ $109  8\frac{1}{4}$	957.5380
3	98 2	766.9921		109 84	000 ***
4	$\frac{98}{98} \frac{2}{5\frac{1}{8}}$	771.0366	35 ft. 1	109 11 <del>8</del> 110 2 <del>§</del>	962:1150
5	98 83	775.1944	$\frac{1}{2}$	110 2 <del>8</del> 110 5 <del>8</del>	
6	98 111	779.3131	3		971 2989
7	99 25	783.4403	4		975.9085
8	99 54	787.5808	5		980·5264 985·1579
9	$99   8\frac{7}{8}$	791.7322	6	- 8	Control of the contro
10	100 0	795.8322	7	4	989·8003 994·4509
11	100 0	800.0654	8	- 0	999.1151
32 ft.	100 68	804.2496	9.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
1	100 08	808:4422	10	$112  5\frac{1}{4}$ $112  6\frac{7}{8}$	1003.7902
2	$100  \frac{32}{101}$	812.6481	11	0	1008.4736
3	$101  0_{\frac{3}{4}}$	816.8650			1013 1705
4	101 67	821.0904	36 ft	- B	1017.8784
5	101 10	825.3291		- *	1022:5944
6	$101 \ 10$ $102 \ 1\frac{1}{8}$	829.5787	2	113 78	1027:3240
7	$102  1\frac{8}{8}$	833.8368	3	$113 \ 10\frac{5}{8}$	1032.0646
8	$102  48 \\ 102  7\frac{1}{2}$	838.1082	5	114 18	1036.8134
9	$102 \ 10\frac{2}{8}$	842.3905	6	114 47	1041.5758
10	103 13	846.6813	7	114 8.	1046:3491
11	103 47	\$50.9855	8		1051 1306
33 ft.	103 8	855.3006	9	-4	1055.9257
1	103 111	859.6240	10	. 8	1060.7317
2	$103 \ 11\frac{1}{8}$ $104 \ 2\frac{1}{4}$	863.9609	10	115 9 <del>1</del> 115 11 <del>\$</del>	1065.5459
3	104 58	868.3087		0	1070·3738 1075·2126
4	104 85	872.6649	37 ft.	0	
5	104 114	877.0346	2		1080.0594
6	105 27	881.4151	3	8	1084.9201
7	105 6	885.8040		2	1089.7915
8	105 9 1	890.2064	4		1094.6711
-	100 98	000 4004	5	$117 6\frac{1}{9}$	1099.5644

Diam.	Circum ference	m = ( = -1 )	Diam.	Circumference	The same of the sa
ft & in.	in feet and in.	Area in feet.	ft. & in.	in feet and in.	Area in feet.
6	117 95	1104.4687	3	129 7	1336:4071
7	118 04	1109.3810	4	$129  10\frac{1}{8}$	1341.8101
8	118 4	1114.3071	5	130 18	1347.2271
9	118 71	1119.2440	6	130 18	1352 6551
10	118 104	1124 1891	7	130 75	1358.0908
11	119 18	1129.1478	8	$130 \ 10\frac{8}{4}$	1363.5406
38 ft.	119 18	1134.1176	9	131 1法	1369.0012
30 Jt.	$119   4\frac{1}{2}$ $119   7\frac{5}{8}$	1139.0953	10	131 5	1374.4697
2	119 104	1144 0868	11	131 8 <del>1</del>	1379.9521
3	120 2	1149.0892	42 ft.	131 118	1385 4456
1214	120 2	1154.0997	1 1	132 21	1390.2467
80 5 A	120 88	1159:1239	2	132  25	1396:4619
6	120 08	1164.1591	3	$132  3\frac{8}{8}$	1401.9880
7	120 118	1169.2023	4	$132 \ 11\frac{7}{8}$	1407 9880
8	$121   2\frac{5}{8}$	1174.2592	5	133 3	1413.0698
9	$121  \frac{38}{8}$	1179:3271	- 6	$133   6\frac{1}{8}$	1418.6287
10	$121 \ 11\frac{7}{8}$	1184.4030	7	$133  9\frac{1}{4}$	1424.1952
11	121 118	1189.4927	8	134 04	1429.7759
	$122  6\frac{1}{4}$	1194:5934	9	134   02   134   35	1435.3675
39 ft.	$122   04   122   9\frac{1}{2}$	1199.7195	10	134 63	1440.9668
2	$123  0\frac{1}{4}$	1204 8244	11	$134   0\frac{1}{4}$	1446.5802
3	123 35	1209.9577	43 ft.	135 1	1452.2046
4	123 63	1215.0990	1 1	135 41	1457.8365
5	$123   0\frac{7}{8}$	1220.2542	2	135 71	1463.4827
6	124 11	1225.4203	3	135 101	1469 1397
7	124 41	1230.5943	4	$136 \ 1\frac{5}{8}$	1474.8044
8	124 78	1235.7822	5	136 44	1480.4833
9	$124 \ 10\frac{1}{2}$	1240.9810	6	136 7 7	1486 1731
10	$125  1\frac{5}{8}$	1246 :1878	7	136 11	1491.8705
11	125   18   125   48	1251.4084	1 8		1497.5821
	125 77		9		1503:3046
40 ft.	$125 \frac{78}{8}$ $125 11$	1256.6400 1261.8794	10		1509.0348
2	$125   11   126   2\frac{1}{4}$	1267 1327	11	137 8\frac{3}{8} 137 11\frac{1}{8}	1514.7791
3	126 5 <del>8</del>	1272.3970	44 ft.	138 23	1520.5344
4	$126  8\frac{1}{2}$	1272 5970	1	$138  5\frac{7}{8}$	1526.2971
5	126 115	1282.9553	2	138 9	1532.0742
6	120 118	1288-2523	3	139 01	1537.8622
7	$127   5\frac{7}{8}$	1293.5572	4	139 31	1543.6578
8	127   9	1298 8760	5	139 68	1549.4776
9	128 07	1304.2057	6	$139  0\frac{8}{8}$	1555.2883
10	128 38	1309.5433	7	140 02	1561.1165
11	128 61	1314.8949	8	$140  04 \\ 140  3\frac{7}{8}$	1566.9591
41 ft.	128 95	1320.2574	9	140 3g 140 7g	1572.8125
1	129 04	1325.6276	10	140 101	1578.6735
2	129 37	1331.0119	10	140 108	1584.5488
4	120 08	1001 0119	11	111 14	1001 0100

Diam. ft. & in.	Circumference in feet and in.	Area in feet.	Diam, ft. & in.	Circumference in feet and in.	Area in feet.
47 0	7.47 48	1500 1050	-	740 57	
45 ft.	141 48	1590.4350	7	149 57	1778 2795
1	$141  7\frac{1}{2}$	1596.3286	8	149 87	1784.5148
2	141 104	1602 2366	9	130 01	1790.7610
3	142 17	1608.1555	10	150 31	1797.0145
4	142 5	1614 0819	11	150 68	1803.2826
5	$142 8\frac{1}{8}$	1620.0226	48 ft.	$150 9\frac{1}{2}$	1899.5616
6	142 114	1625.9743	1	$151  0\frac{5}{8}$	1815.8477
7	143 28	1631.9334	2	151 34	1822 1485
8	$143  5\frac{1}{2}$	1637.9068	3	151 67	1828.4602
9	143 84	1643.8912	4	151 101	1834 7791
10	143 117	1649.8831	5	152 14	1841.1127
11	144 3	1655.8892	6	152 48	1847:4571
46 ft.	144 61	1661.9064	7	152 71	1853.8087
000 1	144 91	1667 9308	8	152 105	1860.1750
2	145 08	1673.9698	9	153 13	1866-5521
3	145 31	1680.0196	10	153 47	1872 9365
4	145 65	1686.0769	11	153 81	1879.3355
5	145 93	1692.1485	49 ft.	153 111	1885.7454
6	146 1	1698-2311	1	154 23	1892-1724
7	146 41	1704 3210	2	154 51	1898:5041
8	146 71	1710:4254	3	154 8	1905 0367
9	146 108	1716.5407	4	154 117	1911.4965
10	147 14	1722.6634	5	$155 \ 2\frac{7}{8}$	1917.9609
11	147 45	1728.8005	6	155 6	1924.4263
17 ft.	147 72	1734.9486	7	155 91	1930.9188
1	147 11	1741.1039	8	156 01	1937:3159
2	148 21	1747.2738	9	156 31	1943.9140
3	148 5½	1753.4545	10	156 65	1950.4392
4	148 88	1759.6426	11	156 93	1956.9691
5	148 111	1765.8452	50 ft.	$150 \ 9\frac{4}{4}$ $157 \ 0\frac{7}{8}$	1963.5000
6	140 112	1772:0587	30 16.	191 08	1909 9000

To Preserve Steel Goods.—Caoutchoue 1 part; turpentine 16 parts. Dissolve with a gentle heat, then add boiled oil 8 parts. Mix by bringing them to the heat of boiling water; apply it to the steel with a brush, in the way of varnish. It may be removed with turpentine. The oil may be wholly omitted.

Size.—Oil size is made by grinding yellow ochre or burnt red ochre with boiled linseed oil, and thinning it with oil of turpentine. Water size (for burnished gilding) is parchment size ground with yellow ochre.

SILICA AND CARBON.—Silica is the base of the mineral world. Carbon the base of the organized.

### IVORY.

How to Soften it. - Take 3 oz. spirits of nitre, and 15 of spring water; mix together; drop in the Ivory, and let it soak. In three

or four days it will be so soft as to obey your fingers.

How to Dye Ivory when Softened.—If you desire to dye Ivory when thus softened, dissolve, in spirits of wine, such colors as you wish to use. When the spirit of wine is sufficiently tinged with the color you have put in plunge in your Ivory, and leave it there till it is dyed to suit you. Then take out the Ivory and give it what form you please.

How to Harden Ivory.—To harden the Ivory afterwards, wrap it up in a sheet of white paper, cover it with dry, decrepitated salt, and lay it by for twenty-four hours, when it will be restored to its

original hardness.

To re-Whiten Ivory which has Turned a Brown Yellow.—There are two ways of doing this, namely: 1. Slack some lime in water, into which drop the ivory; decant it gently, and boil till it looks quite white. 2. To polish it afterwards, set it in the turner's wheel, and after having worked it, take some rushes and pumice stone, mix a subtile powder with water, and rub till it becomes perfectly smooth; then heat it by turning it over a piece of linen or sheepskin, and when hot rub it with a little whitening diluted with olive oil; then rub it with a little dry whitening alone, and finally with a piece of soft white rag, and the Ivory will look remarkably white.

How to Dye Ivory Black.—Immerse the Ivory in a boiling solution of logwood, then take it out, and wash it in a solution of copperas.

Blue.—There are two ways of reaching this color. The first is to soak the Ivory in a solution of verdigris in nitric acid, which will make it green; then dip it into a solution of boiling hot pearlash, and it will turn blue. The second way is as follows: Immerse the Ivory in a solution of sulphate of indigo and water, partly neutralized with potash.

Green.—Steep blued Ivory in a solution of nitro-muriate of tin, and then in a decoction of fustic. Another and a more instantaneous plan is to immerse it in a solution of acetate of copper.

Yellow.—Steep the Ivory in a bath of neutral chromate of potash,

and afterwards in a boiling solution of acetate of lead.

Red.—Soak the Ivory for a short time in a solution of tin, and then in a decoction of cochineal.

Violet.—Moisten the Ivory with a solution of tin, as before; then immerse it in a decoction of logwood.

Purple.—Soak the Ivory in a solution of sal ammoniac into four times its weight of nitrous acid.

Fluid for Marking Ivory.—Take nitrate of silver, 2 parts; nitric

acid, 1 part; water, 7 parts. Mix.

Etching Fluid for Ivory .- Take of diluted sulphuric acid and diluted muriatic acid, equal parts. Mix.

CENTRE.

Etching Varnish for Ivory .- White wax, 2 parts; tears of mastic,

2 parts. Mix.

To Gild Ivory.—Immerse it in a solution of nitro-muriate of gold, and then, while yet damp, expose it to hydrogen gas. Wash it afterwards in clean water. Another plan of gilding Ivory is by immersing it in a fresh solution of proto-sulphate of iron, and afterwards in a solution of chloride of gold.

To Polish Ivory.—Use a rubber and putty and water.

The hardest, toughest, whitest, and most translucent ivory has the preference in the market; and the tusks of the sea horse are considered to afford the best. Ivory has the same constituents as the teeth of animals: three-fourths being phosphate, with a little carbonate of lime; one-fourth cartilage. With regard to dyeing Ivory, it may in general be observed, that the colors penetrate better before the surface is polished than afterwards. Should any dark spots appear, they may be cleared up by rubbing them with chalk; after which the Ivory should be dyed once more to produce a perfect uniformity of shade. On taking it out of the boiling hot dye bath, it should be plunged immediately into cold water, to prevent the chance of fissures being caused by the heat.

## CENTRE,

In a general sense, denotes a point equally remote from the extremes of a line, surface, or solid.

Centre of Attraction

Of a body, is that point into which if all its matter is collected, its action upon any remote particle would still be the same.

Centre of Equilibrium

Is the same, in respect to bodies immersed in a fluid, as the centre of gravity is to bodies in free space.

Centre of Friction

Is that point in the base of a body on which it revolves, into which if the whole surface of the base and the mass of the body were collected, and made to revolve about the centre of the base of the given body, the angular velocity destroyed by its friction would be equal to the angular velocity destroyed in the given body by its friction in the same time.

Centre of Gravity

Of any body, or system of bodies, is that point upon which the body, or system of bodies, acted upon only by the force of gravity, will balance itself in all positions; hence it follows, that, if a line or plane, passing through the centre of gravity, be supported, the body or system will be also supported.

#### Centre of Gyration

Is that point into which, if the whole mass were collected, a given force, applied at a given distance, would produce the same angular velocity in the same time as if the bodies were disposed at their

respective distances.

This point differs from the Centre of Oscillation only in this, that, in the latter case, the motion is produced by the gravity of the body; but, in the former, the body is put in motion by some other force, acting at one place only.

### COHESION

Is that species of attraction which, uniting particle to particle, retains together the component parts of the same mass; being thus distinguished from Adhesion. or that species of attraction which takes place between the surfaces of similar or dissimilar bodies. The absolute cohesion of solids is measured by the force necessary to pull them asunder. Thus, if a rod of iron be suspended in a vertical position, having weight attached to its lower extremity till the rod breaks, the whole weight attached to the rod, at the time of fracture, will be the measure of its cohesive force, or absolute cohesion.

The particles of solid bodies, in their natural state, are arranged in such a manner, that they are in equilibrium in respect to the forces which operate on them; therefore, when any new force is applied, it is evident that the equilibrium will be destroyed, and that the particles will move among themselves till it be restored. When the new force is applied to pull the body asunder, the body becomes longer in the direction of the force, which is called the extension; and its area, at right angles to the direction of the force, contracts. When the force is applied to compress the body, it becomes shorter in the direction of the force, which is called the compression; and the area of its section, at right angles to the force, expands. In either case, a part of the heat, or any fluid that occupies the pores or interstices of the body, before the new force was made to act upon it, will be expelled.

PLATINA-MOHR.—Zinc two parts: platinum one part. Melt and reduce the alloy to powder, which must be treated with dilute sulphuric acid until all the zinc is washed out; then wash it with water, digest it in a ley of potash, and again wash it with water. This powder possesses the property of converting alcohol into vinegar.

THE VELOCITY OF SOUND.—It has been ascertained, by careful investigation, that sound passes in water at a speed of 4,708 feet

per second.

# MECHANICAL LAWS OF ELASTIC FLUIDS.

Boyle's or Mariotte's Law.

The elastic force of a gas or air at a given temperature is inversely proportional to the space which it occupies.

Let p = elastic force of a gas when it occupies the space s. P = do. S.

$$\therefore P = \frac{p \, s}{S}$$

The elastic force of any gas at a given temperature is proportional to its density.

The density of any body is the weight of a cubic unit of it,

usually one cubic foot.

Let p = the elastic force when the density is d. And k = do. do. unit.  $\therefore p = k d$ .

Dalton's and Gay-Lussac's Law.

All gases, under the same pressure, undergo equal expansions

for equal increments of temperature.

It was ascertained by these eminent philosophers, that 100 measures of air expand to 137.5 measures on being heated from 32° to 212° of Fahrenheit's thermometer, hence

37.5 = increments of 100 measures for 180 degrees of heat.

$$\frac{375}{100}$$
 = do. 1 180 do.  $\frac{375}{180}$  = do. 1 1 do.

$$=\frac{1}{480}=a.$$

Let V = volume of any gas at the temperature t. V = do. do. t'.

Then, 
$$V = \frac{1+a(t'-32)}{1+a(t-32)} \cdot V$$
 accurately.  
=  $\left\{1+a(t'-t)\right\} V$  very nearly.

Amonton's Law.

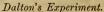
This law is the relation between the elastic force, the density, and the temperature, of any gas. If, then, the volume of a gas be constant, its elastic force will increase; and, if the elastic force is constant, its volume will increase for every increase of temperature. It is important to connect these quantities by an equation.

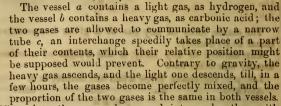
Put p = elastic force of a gas at the temperature  $\theta^{\circ}$  and density d. Then,  $p = k d (1 + a \theta)$ 

where k is a constant quantity depending on the nature of the gas,

and  $a = \frac{1}{480}$ .

When a light and heavy gas are once mixed, they do not exhibit any tendency to separate; in this respect they differ from mixed liquids.





Gases diffuse into the atmosphere and into each other with different degrees of rapidity. The velocity with which air will

rush into a vacuum is 1348 feet per second.

To determine the velocity with which the air of the atmosphere will rush into a space containing rarer air:

Let v = velocity of air, of density (d), rushing into a void.

V = velocity of air rushing into air of density D.

$$\therefore V = v \left(1 - \frac{D}{d}\right)$$

There will always be a current so long as (D) and (d) are unequal.

Illuminating Gases.

Pure hydrogen burns with too feeble a flame to be employed for the purpose of illumination. Carburetted hydrogen has the property of precipitating its carbon; in the act of burning, its solid particles become incandescent, and diffuse a strong light. The more

carbon the gas contains the more brightly does it burn.

Two measures of hydrogen gas, with one measure of the vapor of carbon, form the carburetted hydrogen found in coal mines, and is also evolved in ditches, from decomposing vegetable matter. Another kind of carburetted hydrogen, called olefiant gas, is formed by two measures of hydrogen and two measures of gaseous carbon. This gas burns with a brighter flame than the common carburetted hydrogen.

The best substances for furnishing a gas rich in luminiferous materials are pit coal, resin, oil, fats of all kinds, tar, wax, &c.

The volume of gas discharged from the end of a pipe is directly proportional to the square of its diameter, and inversely as the square root of its length. Let n = number of cubic feet of gas discharged per hour through a length of pipes l feet and diameter D.

$$\therefore n = \frac{3162 D^2}{\sqrt{l}}$$

This formula is applicable only when the gas is transmitted through the pipes, without being let off in its way by burners. If the main send off branches for burners, then, for the same length, the diameter may be reduced; or, for a like diameter, the length may be increased.

STAINS, TO REMOVE.—Stains of *iodine* are removed by rectified spirit. *Ink* stains by oxalic acid or superoxalate of potash. *Iron moulds* by the same; but if obstinate, it has been recommended to moisten them with *ink*, then remove them in the usual way.

Red spots on black cloth, from acids, are removed by spirits of

hartshorn, or other solutions of ammonia.

Stains of Marking Ink, or Nitrate of Silver, to remove. 1. Wet the stain with fresh solution of chloride of lime, and after ten or fifteen minutes, if the marks have become white, dip the part in solution of ammonia or of hyposulphite of soda. In a few minutes wash with clean water.

2. Stretch the stained linen over a basin of hot water, and wet

the mark with tincture of iodine.

Browning, or Bronzing Liquids, for Gun Barrels.—1. Aquafortis  $\frac{1}{2}$  oz., sweet spirit of nitre  $\frac{1}{2}$  oz., spirit of wine 1 oz., sulphate of copper 2 oz., water 30 oz., tincture of muriate of iron 1 oz. Mix.

2. Sulphate of copper 1 oz., sweet spirit of nitre 1 oz., water 1

pint. Mix. In a few days it will be fit for use.

3. Sweet spirit of nitre 3 oz., gum benzoin 1½ oz., tincture of muriate of iron ½ oz., sulphate of copper 2 dr., spirit of wine ½ oz.

Mix, and add 2 lbs. of soft water.

4. Tincture of muriate of iron  $\frac{1}{2}$  oz., spirit of nitric ether  $\frac{1}{2}$  oz., sulphate of copper 2 scruples, rain water  $\frac{1}{2}$  pint. The above are applied with a sponge, after cleaning the barrel with lime and water. When dry, they are polished with a stiff brush, or iron scratch brush.

Bronzing Liquids for Tin Castings.—Wash them over, after being well cleaned and wiped, with a solution of 1 part sulphate of iron, and 1 of sulphate of copper, in 20 parts of water; afterwards with a solution of 4 parts verdigris in 11 of distilled vinegar; leave for an hour to dry, and then polish with a soft brush and coleothar.

Solverts for Gutta Percha—Benzole readily dissolves it: so do chloroform and bisulphuret of carbon.

TABLE

Of Squares, Cubes, Square and Cube Roots of Numbers.

	~	a 1		G 1	
Number.	Square.	Cube.	Square Root.	Cube, Root.	Number.
1 1				44-	
1	1	1	1.0	1.0	month of a di
2	4	8	1.414213	1.25992	2
3	9	27	1.732050	1.44225	3
4	16	64	- 2.0	1.58740	4
5	25	125	2.236068	1 70997	5
6	36	216	2.449489	1.81712	6
7	49	343	2.645751	1.91293	7 171130
8	64	512	2.828427	2.0	8
9	81	729	3.0	2.08008	9
10	. 100	1000	3 162277	2.15443	10
11	121	1331	3.316624	3.22398	11
12	144	1728	3.464101	2.28942	12
13	169	2197	3.605551	2 35133	13
14	196	2744	3.741657	2.41014	14
15 16	225 256	3375 4096	3·872983 4·0	2·46621 2·51984	15 16
17	289	4913	4.123105	2.57128	17
18	324	5832	4.242640	2.62074	18
19	361	6859	4.358898	2.66840	19
20	400	8000	4.472136	2.71441	20
21	441	9261	4.582575	2.75892	21
22	484	10648	4.690415	2.80203	22
23	529	12167	4.795831	2.84386	23
24	576	13824	4.898979	2.88449	24
25	625	15625	50	2.92401	25
26	676	17576	5.099019	2.96249	26
27	729	19683	5.196152	3.0	27
28	784	21952	5.291502	3.03658	28
29	841	24389	5.385164	3.07231	29
30	900	27000	5.477225	3.10723	30
31	961	29791	5.567764	3.14138	31
32	1024	32768	5.656854	3.17480	32
33	1089	35937	5.744562	3.20753	33
34	1156	39304	5.830951	3.23961	34
35	1225	42875	5.916079	3.27106	35
36 37	1296 1369	46656	6.082762	3·30192 3·33222	36 37
38	1369	50653 54872	6.164414	3.36197	38
39	1521	59319	6.244998	3.39121	39
40	1600	64000	6.324555	3.41995	40
41	1681	68921	6.403124	3.44821	41
4.1	1001	0002	- 1001mg	J 11041	400
		- De la company			

	1			900	0 000
Number.	Square.	Cube.	Square Root.	Cuhe Root.	Number.
	3 W/1 S/// J	1		, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1000
42	1764	7,4988	6.480740	3.47602	42
43	1849	79507	6.557438	3.50339	43
44	1936	85184	6.633249	3.53034	44
45	2025	91125	6.708203	3.55689	45
46	2116	97336	6.782330	3.58304	46
47	2209	103823	6.855654	3.60882	47
48	2304	110592	6.928203	3.63424	- 48
49	2401	117649	7.0	3.65930	49
50	2500	125000	7.071067	3.68403	50
51	2601	132651	7.141428	3.70842	51
52	2704	140608	7.211102	3.73251	52
53	2809	148877	7.280109	3.75628	53
54	2916	157464	7.348469	3.77976	54
55	3025	166375	7.416198	3 80295	55
56	3136	175616	7.483314	3.82586	56
57	3249	185193	7.549834	3.84850	57
58	3364	195112	7.615773	3.87087	58
59	3481	205379	7.681145	3.89299	59
60	3600	216000	7.745966	3.91486	60
61	3721	226981	7:810249	3.93649	61
62	3844	238328	7.874007	3.95789	62
63	3969	250047	7.937253	3.97905	63
64	4096	262144	8:0	4.0	64
65	4225	274625	8:062257	4.02072	65
66	4356	287496	8.124038	4.04124	66
67	4489	300763	8.185352	4 06154	67
68	4624	314432	8.246211	4.08165	68
69	4761	328509	8.306623	4.10156	69
70	4900	343000	8.366600	4.12128	70
71	5041	357911	8.426149	4.14081	71
72	5184	373248	8.485281	4.16016	72
73	5329	389017	8.544003	4.17933	73
74	5476	405224	3.602325	4.19833	74
75	5625	421875	8.660254	4.21716	75
76	5776	438976	8717797	4.23582	76
77	5929	456533	8.774964	4.25432	77
78	6084	474552	8.831760	4.27265	78
79	6241	493039	8.888194	4.29084	79
80	6400	512000	8.944271	4.30886	80
81	6561	531441	9.0	4.32674	81
82	6724	551368	9.055385	4.34448	82
83	6889	571787	9.110433	4.36207	83
84	7056	592704	9.165151	4.37951	84
85	7225	614125	9.219544	4.39682	85
86	7396	636056	9.273618	4.41400	86
87	7569	658503	9.327379	4.43104	87
(17)	1000	300000	0 021010	4 40104	
		100-11-01	1	78-1-1	1

104	SQUARES,	OUBLS, SQUAR	L 10010, AND O	UBE ROOTS.	
Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
88	7744	681472	9.380831	4 44796	88
89	7921	704969	9.433981	4.46474	89
90	8100	729000	9.486833	4.48140	90
91	8281	753571	9.539392	4.49794	91
92	8464	778688	9.591663	4.51435	92
93	8649	804357	9.643650	4.53065	93
94	8836	830584	9.695359	4.54683	94
95	9025	857375	9.746794	4.56290	9.5
96	9216	884736	9.797959	4.57885	96
97	9409	912673	9.848857	4.59470	97
98	9604	941192	9.899494	4.61043	98
99	9801	970299	9.949874	4.62606	99
100	10000	1000000	10.0	4.64158	100
101	10201	1030301	10.049875	4.65700	101
102	10404	1061208	10 099504	4.67232	102
103	10609	1092727	10.148891	4.68754	103
104	10816	1124864	10 198039	4.70266	104
105	11025	1157625	10.246950	4.71769	105
106	11236	1191016	10.295630	4.73262	106
107	11449	1225043	10.344080	4.74745	107
108	11664	1259712	10.392304	4.76220	108
109	11881	1295029	10.440306	4.77685	109
110	12100	1331000	10.488088	4.79141	110
111	12321	1367631	10.535653	4.80589	111
112	12544	1404928	10.583005	4.82028	112
113	12769	1442897	10.630145	4.83458	113
114	12996	1481544	10.677078	4.84880	114
115	13225	1520875	10.723805	4.86294	115
116	13456	1560896	10.770329	4.87699	116
117	13689	1601613	10.816653	4.89097	117
118	13924	1643032	10.862780	4.90486	118
119	14161	1685159	10.908712	4.91868	119
120	14400	1728000	10.954451	4.93242	120
121	14641	1771561	11.0	4 94608	121
122	14884	1815848	11.045361	4.95967	122
123	15129	1860867	11.090536	4.97318	123
124	15376	1906624	11.135528	4.98663	124
125	15625	1953125	11.180339	5.0	125
126	15876	2000376	11.224972	5.01329	126
127	16129	2048383	11.269427	5.02652	127
128	16384	2097152	11.313708	5.03968	128
129	16641	2146689	11.357816	5.05277	129
130	16900	2197000	11.401754	5.06579	130
131	17161	2248091	11.445523	5.07875	131
132	17424	2299968	11.489125	5.09164	132
133	17689	2352637	11.532562	5.10446	133
134.	17956	2406104	11.575836	5.11722	134

1	Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
F	135	18225	2460375	11.618950	5.12992	135
	136	18496	2515456	11.661903	5 14256	136
	137	18769	2571353	11.704699	5.15513	137
	138	19044	2628072	11.747340	5.16764	138
1	139	19321	2685619	11.789826	5.18010	139
1	140	19600	2744000	11.832159	5.19249	140
	141	19881	2803221	11.874342	5.20482	141
1	142	20164	2863288	11.916375	5.21710	142
	143	20449	2924207	11.958260	5.22932	143
	144	20736	2985984	12.0	5.24148	144
	145	21025	3048625	12.041594	5.25358	145
	146	21316	3112136	12.083046	5.26563	146
	147	21609	3176523	12.124355	5.27763	147
	148	21904	3241792	12.165525	5.28957	148
	149	22201	3307949	12.206555	5.30145	149
	150	22500	3375000	12.247448	5.31329	150
	151	22801	3442951	12.288205	5.32507	151
	152	23104	3511808	12:328828	5.33680	152
	153	23409	3581577	12.369316	5.34848	153
	154	23716	3652264	12.409673	5.36010	154
	155	24025	3723875	12.449899	5.37168	155
	156	24336	3796416	12.489996	5.38321	156
	157	24649	3869893	12.529964	5.39469	157
ļ	158	24964	3944312	12.569805	5.40612	158
	159	25281	4019679	12.609520	5.41750	159
	160	25600	4096000	12.649110	5.42883	160
	161	25921	4173281	12.688577	5.44012	161
	162	26244	4251528	12.727922	5.45136	162
	163	26569	4330747	12.767145	5.46255	163
	164	26396	4410944	12.806248	5.47370	164
	165	27225	4492125	12.845232	5.48480	165
	166	27556	4574296	12.884098	5.49586	166
	167	27889	4657463	12.922848	5.50687	167
	168	28224	4~41632	12.961481	5.51784	168
	169	28561	4826809	13.0	5.52877	169
	170	28900	4913000	13.038404	5.53965	170
	171	29241	5000211	13.076696	5.55049	171
	172	29584	5088448	13.114877	5.56129	172
	173	29929	5177717	13.152946	5.57205	173
	174	30276	5268024	13.190906	5.58277	174
	175	30625	5359375	13.228756	5.59344	175
	176	30976	5451776	13.266499	5.60407	176
	177	31329	5545233	13 304134	5.61467	177
	178	31634	5639752	13.341664	5.62522	178
	179	32041	5735339	13.379088	5.63574	179
	180	32400	5832000	13.416407	5.64621	180
	181	32761	5929741	13.453624	5.65665	181
			1	1		

Number.	Square.	Cube.	Square Root.	Cube Root.	Numbe
182	33124	6028568	13.490737	5.66705	182
183	33489	6128487	13.527749	5.67741	183
184	33856	6229504	13.564660	5.68773	184
185	34225	6331625	13.601470	5.69801	185
186	34596	6434856	13.638181	5.70826	186
187	34969	6539203	13.674794	5.71847	187
188	35344	6644672	13.711309	5.72865	188
189	35721	6751269	13.747727	5.73879	189
190	36100	6859000	13.784048	5.74889	190
191	36481	6967871	13.820275	5.75896	191
192	36864	7077888	13.856406	5.76899	192
193	37249	7189057	13.892444	5.77899	193
194	37636	7301384	13.928388	5.78896	194
195	38025	7414875	13.964240	5.79889	195
196	38416	7529536	14.0	5.80878	196
197	38809	7645373	14.035668	5.81864	197
198	39204	7762392	14.071247	5.82847	198
199	39601	7880599	14.106736	5.83827	199
200	40000	8000000	14.142135	5.84803	200
201	40401	8120601	14.177446	5.85776	201
202	40804	8242408	14.212670	5.86746	202
203	41209	8365427	14.247806	5.87713	203
204	41616	8489664	14 282856	5.88676	204
205	42025	8615125	14.317821	5:89636	205
206	42436	8741816	14.352700	5.90594	206
207	42849	8869743	14.387494	5.91548	207
208	43264	8998912	14.422205	5.92499	208
209	43681	9129329	14.456832	5.93447	209
210	44100	9261000	14.491376	5.94392	210
211	44521	9393931	14.525839	5.95334	211
212	41944	9528128	14.560219	5.96273	212
213	45369	9663597	14.594519	5.97209	213
214	45796	9800344	14.628738	5.98142	214
215	46225	9938375	14.662878	5.99072	214
216	46656	10077696	14.696938	6.0	216
217	47089	10218213	14.730919	6.00924	217
218	47524	10360232	14 764823	6.01846	218
219	47961	10503459	14.798648	6.02765	219
220	48400	10648000	14.832397	6.03681	220
221	48841	10793861	14.866068	6.04594	221
222	49284	10941048	14.899664	6.05504	222
223	49729	11089567	14.9331.84	6.06412	223
224	50176	11239424	14.966629	6.07317	224
225	50625	11390625	15.0	6.08220	225
226	51076	11543176	15.033296	6 09119	226
227	51529	11697083	15.066519	6.10017	227
228	51984	11852352	15.099668	6.10911	228

Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
229	52441	12008989	15.132746	6.11803	229
230	52900	12167000	15.165750	6.12692	230
231	53361	12326391	15.198684	6.13579	231
232	53824	12487168	15.231546	6.14463	232
233	54289	12649337	15.264337	6.15344	233
234	54756	12812904	15.297058	6.16224	234
235	55225	12977875	15.329709	6.17100	235
236	55696	13144256	15.362291	6.17974	236
237	56169	13312053	15.394804	6.18846	237
238	56644	13481272	15.427248	6.19715	238
239	57121	13651919	15.459624	6.20582	239
240	57600	13824000	15.491933	6.21446	240
241	58081	13997521	15.524174	6.22308	241
242	58564	14172488	15.556349	6 23167	242
243	59049	14348907	15.588457	6:24025	243
244	59536	14526784	15.620499	6.24879	244
245	60025	14706125	15.652475	6.25732	245
246	60516	14886936	15.684387	6.26582	246
247	61009	15069223	15.716233	6.27430	247
248	61504	15252992	15.748015	6.28276	248
249	62001	15438249	15 77 97 33	6.29119	249
250	62500	15625000	15.811388	6.29960	250
251	63001	15813251	15.842979	6.30799	251
252	63504	16003008	15.874507	6.31635	252
253	64009	16194277	15.905973	6.32470	253
254	64516	16387064	15.937377	6.33302	254
255	65025	16581375	15.968719	6.34132	255
256	65536	16777216	16.	6.34960	256
257	66049	16974593	16.031219	6.35786	257
258	66564	17173512	16.062378	6.36609	258
259	67081	17373979	16.093476	6.37431	259
260	67600	17576000	16 124515	6.38250	260
261	68121	17779581	16.155494	6.39067	261
262	68644	17984728	16.186414	6.39882	262
263	69169	18191447	16.217274	6.40695	263
264	69696	18399744	16.248076	6.41506	264
265	70225	18609625	16.278820	$6\ 42315$	265
266	70756	18821096	16.309506	6 43122	266
267	71289	19034163	16.340134	6.43927	267
268	71824	19248832	16.370705	6.44730	268
269	72361	19465109	16.401219	6.45531	269
270	72900	19683000	16.431676	6 46330	270
271	73441	19902511	16.462077	6.47127	271
272	73984	20123648	16.492422	6.47922	272
273	74529	20346417	16.522711	6 48715	273
274	75076	20570824	16.552945	6.49506	274
275	75625	20796875	16.583124	6.50295	275

Number.	Square.	Cube.	Square Root.	Cube Root.	Number
276	76176	21024576	16.613247	6.51083	276
277	76729	21253933	16.643317	6.51868	277
278	77284	21484952	16 673332	6.52651	278
279	77841	21717639	16.703293	6.53433	279
280	78400	21952000	16.733200	6.54213	280
281	78961	22188041	16.763054	6.54991	281
282	79524	22425768	16.792855	6.55767	282
283	80089	22665187	16.822603	6.56541	283
284	80656	22906304	16.852299	6.57313	284
285	81225	23149125	16.881943	6.28084	285
286	81796	23393656	16.911534	6.28823	286
287	82369	23639903	16:941074	6.59620	287
288	82944	23887872	16.970562	6.60385	288
289	83521	24137569	17.0	6.61148	289
290	84100	24389000	17.029386	6.61910	290
291	84681	24642171	17.058722	6.62670	291
292	85264	24897088	17.088007	6.63428	292
293	85849	25153757	17.117242	6.64185	293
294	86436	25412184	17:146428	6.64939	294
				24/0.22	294
295	87025	25672375	17.175564	6.65693	
296	87616	25934336	17.204650	6.66444	296
297	88209	26198073	17.233687	6.67194	297
298	88804	26463592	17.262676	6.67942	298
299	89401	26730899	17.291616	6.68688	299
300	90000	27000000	17.320508	6.69432	300
301	90601	27270901	17 349351	6.70175	301
302	91204	27543608	17.378147	6.70917	302
303	91809	27818127	17.406895	6.71657	303
304	92416	28094464	17.435595	6.72395	304
305	93025	2837 2625	17.464249	6.73131	305
306	93636	28652616	17.492855	6.73866	306
307	94249	28934443	17.521415	6.74599	307
308	94864	29218112	17.549928	6.75331	308
309	95481	29503629	17.578395	6.76061	309
310	96100	29791000	17.606816	6.76789	310
311	96721	30080231	17.635192	6.77516	311
312	97344	30371328	17.663521	6.78242	312
313	97969	30664297	17.691806	6.78966	313
314	98596	30959144	17.720045	6.79688	314
315	99225	31255875	17.748239	6.80409	315
316	99856	31554496	17.776388	6.81128	316
317	100489	31855013	17 804493	6.81846	317
318	101124	32157432	17.832554	6.82562	318
319	101761	32461759	17.860571	6.83277	319
320	102400	32768000	17.888543	6.83990	320
321	103041	33076161	17.916472	6.84702	321
322	103684	33386248	17.944358	6.85412	322

Number.	Square.	Cube.	Square Root.	Cube Root	Number.
323	104329	33698267	17:972200	6.86121	323
324	104976	34012224	18:0	6.86828	324
325	105625	34328125	18:027756	6.87534	325
326	106276	34645976	18.055470	6.88238	326
327	106929	34965783	18.083141	6.88941	327
328	107584	35287552	18.110770	6.89643	328
329	108241	35611289	18.138357	6.90343	329
330	108900	35937000	18.165902	6.91042	330
331	109561	36264691	18.193405	6.91739	331
332	110224	36594368	18.220867	6.92435	332
333	110889	36926037	18:248287	6.93130	333
324	111556	37259704	18.275666	6.93823	334
335	112225	37595375	18:303005	6.94514	335
336	112896	37933056	18.330302	6.95205	336
337	113569	38272753	18-357559	6.95894	337
338	114244	38614472	18.384776	6.96581	338
339	114921	38958219	18.411952	6 97268	339
340	115600	39304000	18.439088	6.97953	340
341	116281	39651821	18.466185	6.98636	341
342	116964	40001688	18.493242	6.99319	342
343	117649	40353607	18.520259	7.0	343
344	118336	40707584	18.547237	7.00679	344
345	119025	41063625	18.574175	7.01357	345
346	119716	41421736	18.601075	7.02034	346
347	120409	41781923	18.627936	7.02710	347
348	121104	42144192	18.654758	7.03384	348
349	121801	42508549	18.681541	7.04058	349
350	122500	42875000	18.708286	7.04729	350
351	123201	43243551	18.734994	7.05400	351
352	123904	43614208	18.761663	7.06069	352
353	124609	43986977	18.788294	7.06737	353
354	125316	44361864	18.814887	7.07404	354
355	126025	44738875	18.841443	7.08069	355
356	126736	45118016	18.867962	7.08734	356
357	127449	45499293	18.894443	7.09397	357
358	128164	45882712	18.920887	7.10058	358
359	128881	46268279	18.947295	7.10719	359
360	129600	46656000	18.973666	7.11378	360
361	130321	47045881	19.0	7.12036	361
362	131044	47437928	19.026297	7.12693	362
363	131769	47832147	19.052558	7.13349	363
364	132496	48228544	19.078784	7.14003	364
365	133225	48627125	19:104973	7.14656	365
366	133956	49027896	19:131126	7.15309	366
367	$134689 \\ 135424$	49430863	19.157244	7.15959	367
368	100000000000000000000000000000000000000	49836032	19:183326	7.16609	368
369	136161	50243409	19.209372	7.17258	369

Number	Square.	Cube.	Square Root.	Cube Root.	Number.
370	136900	50653000	19.235384	7.17905	370
371	137641	51064811	19.261360	7.18551	371
372	138384	51478848	19.287301	7.19196	372
373	139129	51895117	19.313207	7.19840	373
374	139876	52313624	19.339079	7.20483	374
375	140625	52734375	19.364916	7.21124	375
376	141376	53157376	19 390719	7.21765	376
377	142129	53582633	19.416487	7.22404	377
378	142884	54010152	19.442222	7.23042	378
379	143641	54439939	19.467922	7.23679	379
380	144400	54872000	19.493588	7.24315	380
381	145161	55306341	19.519221	7.24950	381
382	145924	55742968	19:544820	7.25584	382
383	146689	56181887	19.570385	7.26216	383
384	147456	56623104	19 595917	7.26848	384
385	148225	57066625	19.621416	7 27478	385
386	148996	57512456	19.646882	7.28107	386
387	149769	57960603	19.672315	7.28736	387
388	150544	5411072	19.697715	7.29363	388
389	151321	58863859	19.723082	7.29989	389
390	152100	59319000	19.748417	7:30614	390
391	152881	59776471	19.773719	7.21238	391
392	153664	60236288	19.798989	7.31861	392
393	154449	60698457	19.824227	7:32482	393
394	155236	61162984	19.849433	7:33103	394
395	156025	61629875	19.874606	7.33723	395
396	156816	62099136	19:899748	7.34342	396
397	157609	62570773	19.924858	7.34959	397
398	158404	63044792	19.949937	7.35576	398
399	159201	63521199	19.974984	7.36191	399
400	160000	64000000	20.0	7.36806	400
401	160801	64481201	20.024984	7:37419	401
402 403	161604 162409	64964808 65450827	20·049937 20·074859	7·38032 7·38643	402 403
403	163216	65939264	20.099751	7:39254	404
404	164025	66430125	20.124611	7.39254	404
406	164836	66923416	20.149441	7.40472	406
407	165649	67419143	20:174241	7.41079	407
408	166464	67917312	29.199009	7.41685	408
409	167281	68417929	20:223748	7.42291	409
410	168100	68921000	20.248456	7.42895	410
411	168921	69426531	20.273134	7.43499	411
412	169744	69934528	20.297783	7.44101	412
413	170569	70444997	20:322401	7.44703	413
414	171396	70957944	20.346989	7.45303	414
415	172225	71473375	20.371548	7.45903	415
416	173056	71991296	20.396078	7.46502	416

Number.	Square.	Cube.	Square Root.	Cuhe Root.	Number.
417	173889	72511713	20.420577	7.47099	417
418	174724	73034632	20.445048	7.47696	418
419	175561	73560059	20.469489	7.48292	419
420	176400	74088000	20.493901	7.48887	420
421	177241	74618461	20.518284	7.49481	421
422	178084	75151448	20.542638	7.50074	422
423	178929	75686967	20.566963	7.50666	423
424	179776	76225024	20.591260	7.51257	424
425	180625	76765625	20.615528	7.51847	425
426	181476	77308776	20.639767	7.52436	426
427	182329	77854483	20.663978	7.53024	427
428	183184	78402752	20.688160	7.53612	428
429	184041	78953589	20.712315	7.54198	429
430.	184900	79507000	20.736441	7.54784	430
431	185761	80062991	20.760539	7.55368	431
432	186624	80621568	20.784609	7.55952	432
433	187489	81182737	20.808652	7.56535	433
434	188356	81746504	20.832666	7.57117	434
435	189225	82312875	20.856653	7 57698	435
436	190096	82881856	20.880613	7.58278	436
437	190969	83453453	20.904545	7.58857	437
438	191844	84027672	20.928449	7.59436	438
439	192721	84604519	20.952326	7.60013	439
440	193600	85184000	20.976177	7.60590	440
441	194481	85766121	21.0	7.61166	441
442	195364	86350888	21.023796	7.61741	442
443	196249	86938307	21.047565	7.62315	443
414	197136	87528384	21.071307	7.62888	444
445	198025	88121125	21.095023	7.63460	445
446	198916	88716536	21.118712	7.64032	446
447	199809	89314623	21.142374	7.64602	447
448	200704	89915392	21.166010	7.65172	448
449	201601	90518849	21.189620	7.65741	449
450	202500	91125000	21.213203	7.66309	450
451	203401	91733851	21.236760	7.66876	451
452	204304	92345408	21.260291	7.67443	452
453	205209	92959677	21.283796	7.68008	453
454	206116	93576664	21.307275	7.68573	454
455	207025	94196375	21.330729	7.69137	455
456	207936	94818816	21.354156	7.69700	456
457	208849	95443993	21.377558	7.70262	457
458	209764	96071912	21.400934	7.70823	458
459	210681	96702579	21.424285	7.71384	459
460	211600	97336000	21.447610	7.71944	460
461	212521	97972181	21.470910	7.72503	461
462	213444	98611128	21:494185	7.73061	462
463	214369	99252847	21.517434	7.73618	463
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Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
464	215296	99897344	21.540659	7.74175	464
465	216225	100544625	21.563858	7 74731	465
466	217156	101194696	21.587033	7.75286	466
467	218089	101847563	21.610182	7.75840	467
468	219024	102503232	21.633307	7.76393	468
469	219961	103161709	21.656407	7.76946	469
470 1	220900	103823000	21.679483	7.77498	470
471	221841	104487111	21.702534	7.78049	471
472	222784	105154048	21.725561	7 78599	472
473	223729	105823817	21.748563	7.79148	473
474	224676	106496424	21.771541	7.79697	474
475	225625	107171875	21.794494	7.80245	475
476	226576	107850176	21.817424	7.80792	476
477	227529	108531333	21.840329	7.81338	477
478	228484	109215352	21.863211	7.81884	478
479	229441	109902239	21.886068	7.82429	479
480	230400	110592000	21.908902	7.82973	480
481	231361	111284641	21.931712	7.83516	481
482	232324	111980168	21.954498	7.84059	482
483	233289	112678587	21.977261	7.84601	483
484	234256	113379904	22.0	7.85142	484
485	235225	114084125	22.022715	7.85682	485
486	236196	114791256	22:045407	7.86222	486
487	237169	115501303	22 068076	7.86761	487
488	238144	116214272	22.090722	7.87299	488
489	239121	116930169	22.113344	7.87836	489
490	240100	117649000	22.135943	7.88373	490
491	241081	118370771	22.158519	7.88909	491
492	242064	119095488	22.181073	7.89444	492
493	243049	119823157	22.203603	7.89979	493
494	244036	120553784	22.226110	7 90512	494
495	245025	121287375	22.248595	7.91045	495
496	246016	122023936	22.271057	7.91578	496
497	247009	122763473	22.293496	7.92109	497
498	248004	123505992	22.315913	7.92640	498
499	249001	124251499	22:338307	7.93171	499
500	250000	125000000	22 360679	7.93700	500
501	251001	125751501	22.383029	7.94229	501
502	252004	126506008	22.405356	7.94757	502
503	253009	127263527	22.427661	7.95284	503
504	254016	128024064	22:449944	7.95811	504
505	255025	128787625	22.472205	7.96337	505
506	256036	129554216	22.494443	7.96862	506
5,07	257049	130323843	22.516660	7.97387	507
508	258064	131096512	22.538855	7.97911	508
509	259081	131872229	22.561028	7.98434	509
510	260100	132651000	22.583179	7.98956	510
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Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
511	261121	133432831	22.605309	7.99478	511
512	262144	134217728	22.627417	8.0	512
513	263169	135005697	22.649503	8.00520	513
514	264196	135796744	22.671568	8.01040	514
515	265225	136590875	22.693611	8.01559	515
516	266256	137388096	22.715633	8.02077	516
517	267289	138188413	22.737634	8.02595	517
518	268324	138991832	22.759613	8:03112	518
519	269361	139798359	22.781571	8.03629	519
520	270400	140608000	22.803508	8:04145	520
521	271441	141420761	22.825424	8:04660	521
522	272484	142236648	22.847319	8.05174	522
523	273529	143055667	22.869193	8.05688	523
524	274576	143877824	22.891046	8.06201	524
525	275625	144703125	22.912878	8.06714	525
526	276676	145531576	22.934689	8.07226	526
527	277729	146363183	22.956480	8.07737	527
528	278784	147197952	22.978250	8.08248	528
529	279841	148035889	23.0	8.08757	529
530	280900	148877000	23.021728	8.09267	530
531	281961	149721291	23.043437	8:09775	531
532	283024	150568768	23.065125	8.10283	532
533	284089	151419437	23:086792	8.10791	533
534	285156	152273304	23.108440	8.11298	534
535	286225	153130375	23:130067	8.11804	535
536	287296	153990656	23.151673	8.12309	536
537	288369	154854153	23.173260	8.12814	537
538	289444	155720872	23.194827	8.13318	538
539	290521	156590819	23.216373	8.13822	539
540	291600	157464000	23.237900	8.14325	540
541	292681	158340421	23.259406	8.14827	541
542	293764	159220088	23.280893	8.15329	542
543	294849	160103007	23.302360	3.15830	543
544	295936	160989184	23.323807	8.16331	544
545	297025	161878625	23 345235	8.16830	545
546	298116	162771336	23.366642	8.17330	546
547	299209	163667323	23.388031	8.17828	547
548	300304	164566692	23.409399	8:18326	548
549	301401	165969149	23.430749	8.18824	549
550	302500	166375000	23.452078	8.19321	550
551	303601	167284151	23.473389	8.19817	551
552	304704	168196608	23.494680	8:20313	552
553	305809	169112377	23.515952	8.20808	553
554	306916	170031464	23.537204	8.21302	554
555	308025	170953875	23.558438	8.21796	555
556	309136	171879616	23.579652	8.22289	556
557	310249	172808693	23.600847	8.22782	557
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Number	Square	Cube	Square Root	Cube Root.	Number.
558	311364	173741112	23.622023	8.23274	558
559	312481	174676879	23.643180	8.23766	559
560	313600	175616000	23.664319	8.24257	560
561	314721	176558481	23:685438	8.24747	561
562	315844	177504328	23.706539	8.25237	562
563	316969	178453547	23.727621	8.25726	563
564	318096	179406144	23.748684	8.26214	564
565	319225	180362125	23.769728	8.26702	565
566	320356	181321496	23.790754	8.27190	566
567	321489	182284263	23.811761	8.27677	567
568	322624	183250432	23.832750	8.28163	568
569	323761	184220009	23.853720	8:28649	569
570	324900	185193000	23.874672	8:29134	570
571	326041	186169411	23.895606	8.29619	571
572	327184	187149248	23 916521	8.30103	572
573	328329	188132517	23.937418	8.30586	573
574	329476	189119224	23.958297	8.31069	574
575	330625	190109375	23.979157	8.31551	575
576	331776	191102976	24.0	8:32033	576
577	332929	192100033	24.020824	8:32514	577
578	334084	193100552	24.041630	8.32995	578
579	335241	194104539	24 062418	8 33475	579
580	336400	195112000	24 083189	8:33955	580
581	337561	196122941	24.103941	8:34434	581
582	338724	197137368	24.124676	8:34912	582
583	339889	198155287	24.145392	8.35390	583
584	341056	199176704	24.166091	8.35867	584
585	342225	200201625	24.186773	8:36344	585
586	343396	201230056	24.207436	8.36820	586
587	344569	202262003	24.228082	8:37296	587
588	345744	203297472	24.248711	8:37771	588
589	346921	204336469	24.269322	8.38246	589
590	348100	205379000	24.289915	8.38720	590
591	349281	206425071	24.310491	8.39194	591
592	350464	207474688	24.331050	8.39667	592
593	351649	208527857	24.351591	8.40139	593
594	352836	209584584	24.372115	8:40611	594
595	354025	210644875	24.392621	8.41083	595
596	355216	211708736	24.413111	8.41554	596
597	356409	212776173	24.433583	8.42024	597
598	357604	213847192	24.454038	8.42494	598
599	358801	214921799	24:474476	8.42963	599
600	360000	216000000	24.494897	8:43432	600
601	361201	217081801	24.515301	8.43900	601
602	362404	218167208	24.535688	8.44368	602
603	363609	219256227	24.556058	8.44836	603
604	364816	220348864	24.576411	8.45302	604
783	241	- 18 77	1 1 1 1 1 1	64.2017	557

Number.	Square.	Cube.	Square Root.	Cube Root.	Numbe
605	366025	221445125	24.596747	8.45769	605
606	367236	222545016	24.617067	8.46234	606
607	368449	223648543	24.637370	8.46700	607
608	369664	224755712	24.657656	8.47164	608
609	370881	225866529	24.677925	8.47628	609
610	372100	226981000	24.698178	8.48092	610
611	373321	228099131	24.718414	8.48555	611
612	374544	229220928	24.738633	8.49018	612
613	375769	230346397	24.758836	8.49480	613
614	376996	231475544	24.779023	8.49942	614
615	378225	232608375	24.799193	8:50403	615
616	379456	233744896	24.819347	8 50864	616
617	380689	234885113	24.839484	8.51324	617
618	381924	236029032	24.859605	8.51784	618
619	383161	237176659	24.879710	8.52243	619
620	384400	238328000	24.899799	8.52701	620
621	385641	239483061	24.919871	8 53160	621
622	386884	240641848	24.939927	8.53617	622
623	388129	241804367	24.959967	8.54075	623
624	389376	242970624	24.979992	8.54531	624
625	390625	244140625	25.0	8.54987	625
626	391876	245314376	25.019992	8 55443	626
		246491883	25.039968		627
627 628	393129 394384	247673152	25.059968	8.55898	628
	395641	248858189	25.079872	8.56353	629
629				8.56808	630
630	396900	250047000	25.099800	8.57261	631
631	398161	251239591	25.119713	8.57715	
632	399424	252435968	25.139610	8.58168	632
633	400689	253636137	25.159491	8 58620	633
634	401956	254840104	25.179356	8.59072	634
635	403225	256047875	25.199206	8.59523	635
636	404496	257259456	25.219040	8.59974	636
637	405769	258474853	25.238858	8.60425	637
638	407044	259694072	25.258661	8.60875	638
639	408321	260917119	25.278449	8.61324	639
640	409600	262144000	25.298221	8.61773	640
641	410881	263374721	25.317977	8.62222	641
642	412164	264609288	25:337718	8.62670	642
643	413449	265847707	25 357444	8.63118	643
644	414736	267089984	25.377155	8.63565	644
645	416025	268336125	25.396850	8.64012	645
646	417316	269586136	25.416530	8.64458	646
647	418609	270840023	25.436194	8.64904	647
648	419904	272097792	25.455844	8.65349	648
649	421201	273359449	25.475478	8.65794	649
650	422500	274625000	25.495097	8.66239	650
651	423801	275894451	25.514701	8.66683	651

Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
652	425104	277167808	25 534290	8:67126	652
653	426409	278445077	25.553864	8.67569	653
654	427716	279726264	25.573423	8:68012	654
655	429025	281011375	25.592967	8.68454	655
656	430336	282300416	25.612496	8 68896	656
657	431649	283593393	25 63 2011	8-69337	657
658	432964	284890312	25.651510	8.69778	658
659	434281	286191179	25.670995	8.70218	659
660	435600	287496000	25.690465	8.70658	660
661	436921	288804781	25.709920	8-71098	661
662	438244	290117528	25:729369	8-71537	662
663	439569	291434247	25.748786	871975	663
664	440896	292754944	25:768197	8 72414	664
665	442225	294079625	25.787593	8 72851	665
666	443556	295408296	25.806975	873289	666
667	414889	296740963	25 826343	8-73726	667
668	446224	298077632	25.845696	8-74162	668
669	447561	299418309	25.865034	8 74598	669
670	448900	300763000	25.884358	8.75034	670
671	450241	302111711	25.903667	8 75469	671
672	451584	303464448	25-922962	8.75903	672
673	452929	304821217	25-942243	8 76338	673
674	454276	306182024	25-981510	8-76771	674
675	455625	307546875	25 980762	\$ 77205	675
676	456976	308915776	26.0	877638	676
677	458329	310288733	26 019223	8:78070	677
678	459684	311665752	26.038433	878502	678
679	461041	313046839	26.057628	878934	679
630	462400	314432000	26.076809	879365	680
681	463761	315821241	26.095976	8.79796	681
682	465124	317214568	26.115129	8.80227	682
683	466489	318611987	26.134268	8.80657	683
684	467856	320013504	26.153393	8.81086	684
685	469225	321419125	26.172504	8.81515	685
686	470598	322828856	26.191601	8.81944	686
687	471969	324242703	26.210684	8.82373	687
688	473344	325660672	26-229754	8.82800	688
689	474721	327082769	26-248809	8.83228	689
650	476100	328509000	26.267851	S·83655	690
691	477481	329939371	26-286878	8.84082	691
692	478864	331373883	26.305892	8 84508	692
693	480249	332812557	26.324893	8.84934	693
694	481636	334255384	26.343879	8.85359	694
695	483025	335702375	26 362852	8.85784	695
696	484416	337153536	26:381811	8.86209	693
697	485809	338608873	26:400757	8 86633	697
698	487204	340065392	26:419689	8.87057	698

Number.	Square.	Cube.	Square Root,	Cube Root.	Number.
699	488601	341532099	26:438608	8.87480	699
700	490000	343000000	26.457513	8.87904	700
701	491401	344472101	26.476404	8.88326	701
702	492804	345948408	26.495282	8.88748	702
703	494209	347428927	26.514147	8.89170	703
704	495616	348913664	26.532998	8.89592	704
705	497025	350402625	26.551836	8.90013	705
706	498436	351895816	26.570660	8.90433	706
707	499849	353393243	26.589471	8.90853	707
708	501264	354894912	26.608269	8.91273	708
709	502681	356400829	26.627053	8.91693	709
710	504100	357911000	26.645825	8.92112	710
711	505521	359425431	26.664583	8.92530	711
712	507944	360944128	26.683328	8.92949	712
713	508369	362467097	26.702059	8 93366	713
714	509796	363994344	26.720778	8.93784	714
715	511225	365525875	26.739483	8.94201	715
716	512656	367061696	26.758176	8.94618	716
717	514089	368601813	26.776855	8.95034	717
718	515524	370136232	26.795522	8.95450	718
719	516961	371694959	26.814175	8.95865	719
720	518400	373248000	26.832815	8.96280	720
721	519841	374805361	26.851443	8.96695	721
722	521284	376367048	26.870057	8.97110	722
723	522729	377933067	26.888659	8.97524	723
724	524176	379503424	26.907248	8.97937	724
725	525625	381078125	26.925824	8.98350	725
726	527076	382657176	26.944387	8.98763	726
727	528529	384240583	26.962937	8.99176	727
728	529984	385828352	26.981475	8.99588	728
729	531441	387420489	27.0	9.0	729
730	532900	389017000	27.018512	9.00411	730
731	534361	390617891	27.037011	9.00822	731
732	535824	392223168	27.055498	9.01232	732
733	537289	393832837	27.073972	9.01643	733
734	538756	395446904	27.092434	9.02052	734
735	540225	397065375	27.110883	9.02462	735
736	541696	398688256	27.129319	9.02871	736
737	543169	400315553	27.147743	9.03280	737
738	544644	401947272	27.166155	9.03688	738
739	546121	403583419	27.184554	9.04096	739
740	547600	405224000	27.202941	9.04504	740
741	549081	406869021	27.221315	9.04911	741
742	550564	408518488	27.239676	9.05318	742
743	552049	410172407	27.258026	9.05724	743
744	553536	411830784	27.276363	9.06130	744
745	555025	413493625	27.294688	9.06536	745
		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.14971	A SECTION	204

Number.	Square.	Cube.	Square Root.	Cuhe Root.	Number.
746	556516	415160936	27:313000	9-06942	746
747	558009	416832723	27:33130)	9.07347	747
748	559504	418508992	27.349588	9.07751	748
749	561001	420189749	27:367864	9 08156	749
750	562500	421875000	27:386127	9.08560	750
751	564001	423564751	27.404379	9-08963	751
752	565504	425259008	27.422618	9.09367	752
753	567009	426957777	27:440845	9 09770	753
754	568516	428661064	27:459060	9.10172	754
755	570025	430368875	27:477263	9.10574	755
756	571536	432081216	27.495454	9.10976	756
757	573049	433798093	27:513633	9.11378	757
758	574564	435519512	27:531799	9.11779	758
759	576081	437245479	27:549954	9.12180	759
760	577600	438976000	27.568097	9.12580	760
761	579121	440711081	27.586228	9.12980	761
762	580644	442450728	27.604347	9.13380	762
763	582169	444194947	27.622454	9.13779	763
764	583696	445943744	27.640549	9.14178	764
765	585225	447697125	27.658633	9.14577	765
766	586756	449455096	27.676705	9.14975	766
767	588289	451217663	27:694764	9.15373	767
768	589824	452984832	27 712812	9.15771	768
769	591361	454756609	27:730849	9.16168	769
770	592900	456533000	27:748873	9.16565	770
771	594441	458314011	27-766886	9.16962	771
772	595984	460099648	27.784888	9.17358	772
773	597529	461889917	27.802877	9.17754	773
774	599076 i	463684824	27.820855	9.18150	774
775	600625	465484375	27.838821	9.18545	775
776	602176	467288576	27.856776	9.18940	776
777	603729	469097433	27.874719	9.19334	777
778	605284	470910952	27.892651	9.19728	778
779	606841	472729139	27.910571	9:20122	779
780	608400	474552000	27-928480	9.20516	780
781	609961	476379541	27-946377	9-20909	781
782	611524	478211768	27.964262	9.21302	782
783	613089	480048687	27-982137	9.21695	783
784	614656	481890304	28.0	9.22087	784
785	616225	483736625	28:017851	9-22479	785
786	617796	485587656	28.035691	9-22870	786
787	619369	487443403	28.053520	9.23261	787
788	620944	489303872	28:071337	9.23652	788
789	622521	491169069	28.089143	9-24043	789
790	624100	493039000	28.106938	9-24433	790
791	625681	494913671	28.124722	9.24823	791
792	627264	496793088	28:142494	9.52213	792

Number.	Square.	Cube.	. Square Root.	Cube Root.	Numbe
793	628849	498677257	28.160255	9.25602	793
794	630436	500566184	28.178005	9.25991	794
795	632025	502459875	28.195744	9.26379	795
796	633616	504358336	28.213472	9.26767	796
797	635209	506261573	28.231188	9.27155	797
798	636804	508169592	28.248893	9.27543	798
799	638401	510082399	28.266588	9.27930	799
800	640000	512000000	28.284271	9.28317	800
801	641601	513922401	28.301943	9.28704	801
802	643204	515849608	28.319604	9.29090	802
803	644809	517781627	28:337254	9.29476	803
804	646416	519718464	28.354893	9.29862	804
805	648025	521660125	28.372521	9.30247	805
806	649636	523606616	28.390139	9.30632	806
807	651249	525557943	28.407745	9.31017	807
808	652864	527514112	28.425340	9.31401	808
809	654481	529475129	28.442925	9.31785	809
810	656100	531441000	28.460498	9 32169	810
811	657721	533411731	28:478061	9.32553	811
812	659344	535387328	28:495613	9.32936	812
813	660969	537367797	28.513154	9.33319	813
814	662596	539353144	28:530685	9:33701	814
815	664225	541343375	28:548204	9 34083	815
816	665856	543338496	28.565713	9.34465	816
817	667489	545338513	28.583211	9.34847	817
818	669124	547343432	28:600699	9.35228	818
819	670761	549353259	28.618176	9.35609	819
820	672400	551368000	28.635642	9.35990	820
821	674041	553387661	28.653097	9.36370	821
822	675684	555412258	28.670542	9.36750	822
823	677329	557441767	28.687976	9:37130	823
824	678976	559476224	28.705400	9.37509	824
825	680625	561515625	28.722813	9.37888	825
826	682276	563559976	28.740215	9.38267	826
827	683929	565609283	28.757607	9.38646	827
828	685584	567663552	28.774989	9.39024	828
829	687241	569722789	28.792360	9.39402	829
830	688900	571787000	28.809720	9.39779	830
831	690561	573856191	28.827070	9.40156	831
832	692224	575930368	28.844410	9.40533	832
833	693889	578009537	28.861739	9.40910	833
834	695556	580093704	28'879058	9.41286	834
835	697225	582182875	28.896366	9.41280	835
836	698896	584277056	28.913664	9.41002	836
837	700569	586376253		9.42038	830
838	700569	588480472	28.930952		838
839	703921	590589719	28.948229	9:42789 9:43164	839
000	100021	990999119	28.965496	3.40104	000

Number.	Square.	Cube.	Square Root.	Cube Root.	Number.
840	705600	592704000	28.982753	9.43538	840
841	707281	594823321	29.0	9:43913	841
842	708964	596947688	29.017236	9.44287	842
843	710649	599077107	29.034462	9.44660	843
844	712336	601211584	29.051678	9.45034	844
845	714025	603351125	29.068883	9.45407	845
846	715716	605495736	29.086079	9.45779	846
847	717409	607645423	29.103264	9.46152	847
848	719104	609800192	29.120439	9.46524	848
849	720801	611960049	29.137604	9.46896	849
850	722500	614125000	29.154759	9.47268	850
851	724201	616295051	29.171904	9.47639	851
852	725904	618470208	29.189039	9.48010	852
853	727609	620650477	29.206163	9.48381	853
854	729316	622835864	29.223278	9.48751	854
855	731025	625026375	29.240380	9.49122	855
856	732736	627222016	29.257477	9.49491	856
857	734449	629422793	29.274562	9.49861	857
858	736164	631628712	29:291637	9.50230	858
859	737881	633839779	29:308701	9.50599	859
860	739600	636056000	29:325756	9.50968	860
861	741321	638277381	29.342801	9.51336	861
862	743044	640503928	29.359836	9.51705	862
863	744769	642735647	29.376861	9.52073	863
864	746496	644972544	29.393876	9.52440	864
865	748225	647214625	29:410882	9.52807	865
866	749956	649461896	29.427877	9.53174	866
867	751689	651714363	29.444863	9.53541	867
868	753424	653972032	29.461839	9.53908	868
869	755161	656234909	29.478805	9.54274	869
870	756900	658503000	29.495762	9.54640	870
871	758641	660776311	29.512709	9.55005	871
872	760384	663054848	29:529646	9.55371	872
873	762129	665338617	29.546573	9.55736	873
874	763876	667627624	29.563491	9.56101	874
875	765625	669921875	29:580398	9.56465	875
876	767376	672221376	29.597297	9.56829	876
877	769129	674526133	29.614185	9.57193	877
878	770884	676836152	29.631064	9.57557	878
879	772641	679151439	29.647934	9.57920	879
880	774400	681472000	29.664793	9.58283	880
881	776161	683797841	29.681644	9.58646	881
882	777924	686128968	29.698484	9.59009	882
883	779689	688465387	29.715315	9.59371	883
884	781456	690807104	29.732137	9.59733	884
885	783225	693154125	29:748949	9.60095	885
886	784996	695506456	29.765752	9.60456	886

Number.	Square.	Cube.	Square Root.	Cube Root.	Number
887	786769	697864103	29.782545	9.60818	887
888	788544	700227072	29.799328	9.61179	888
889	790321	702595369	29.816103	9.61539	889
890	792100	704969000	29.832867	9.61900	890
891	793881	707347971	29.849623	9.62260	891
892	795664	709732288	29.866369	9.62620	892
893	797449	712121957	29.883105	9.62979	893
894	799236	714516984	29.899832	9.63339	894
895	801025	716917375	29.916550	9.63698	895
896	802816	719323136	29.933259	9:64056	896
897	804609	721734273	29.949958	9.64415	897
898	806404	724150792	29.966648	9.64773	898
899	808201	726572699	29.983328	9.65131	899
900	810000	729000000	30.0	9.65489	900
901	811801	731432701	30.016662	9.65846	901
902	813604	733870808	30.033314	9.66204	902
903	815409	736314327	30.049958	9.66560	903
904	817216	738763264	30.066592	9.66917	904
905	819025	741217625	30.083217	9.67274	905
906	820836	743677416	30.099833	9.67630	906
907	822649	746142643	30.116440	9.67986	907
908	824464	748613312	30.133038	9.68341	908
909	826281	751089429	30.149626	9.68697	909
910	828100	753571000	30.166206	9.69052	910
911	829921	756058031	30.182776	9.69406	910
912	831744	758550528	30.199337	9.69761	912
913	833569	761048497	30.215889	9.70115	912
	835396	763551944	30.232432	9.70113	913
914 915	837225	766060875	30.248966	9.70409	914
916	839056	768575296	30.265491	9.70023	
	840889	771095213	30.282007		916
917	842724	773620632	30.298514	9.71530	917
918				9.71883	918
919	844561	776151559	30.315012	9.72236	919
920	846400	778688000	30.331501	9.72588	920
921	848241	781229961	30.347981	9.72941	921
922	850084	783777448	30.364452	9.73293	922
	851929	786330467	30.380915	9.73644	923
924	853776	788889024	30.397368	9.73996	924
925	855625	791453125	30.413812	9.74347	925
926	857476	794022776	30.430248	9.74698	926
927	859329	796597983	30.446674	9.75049	927
928	861184	799178752	30.463092	9.75399	928
929	863041	801765089	30.479501	9.75750	929
930	864900	804357000	30.495901	9.76100	930
931	866761	806954491	30.512292	9.76449	931
932	868624	809557568	30.528675	9.76799	932
933	870489	812166237	30.545048	9.77148	933

Number.	r. Square. Cube.		Square Root.	Cube Root.	Number	
934	872356	814780504	30.561413	9.77497	934	
935	874225	817400375	30.577769	9.77846	935	
936	876096	820025856	30.594117	9.78194	936	
937	877969	822656953	30.610455	9.78542	937	
938	879844	825293672	30.626785	9.78890	938	
939	881721	827936019	30.643106	9 79238	939	
940	883600	830584000	30.659419	9.79586	940	
941	885481	833237621	30.675723	9.79933	941	
942	887364	835896888	30.692018	9.80280	942	
943	889249	838561807	30.708305	9.80627	943	
944	891136	841232384	30.724583	9.80973	944	
945	893025	843908625	30.740852	9.81319	945	
946	894916	846590536	30.757113	9.81665	946	
947	896809	849278123	30.773365	9.82011	947	
948	898704	851971392	30.789608	9.82357	948	
949	900601	854670349	30.805843	9.82702	949	
950	902500	857375000	30.822070	9.83047	950	
951	904401	860085351	30.838287	9.83392	951	
952	906304	862801408	30.854497	9.83736	952	
953	908209	865523177	30.870698	9.84081	953	
954	910116	868250664	30.886890	9.84425	954	
955	912025	870983875	30.903074	9.84769	955	
956	913936	873722816	30.919249	9.85112	956	
957	915849	876467493	30.935416	9.85456	957	
958	917764	879217912	30.951575	9 85799	958	
959	916681	881974079	30.967725	9.86142	959	
960	921600	884736000	30.983866	9.86484	960	
961	923521	887503681	31.0	9.86827	961	
962	925444	8902771.28	31.016124	9.87169	962	
963	927369	893056347	31.032241	9.87511	963	
964	929296	895841344	31.048349	9 87853	964	
965	931225	898632125	31.064449	9.88194	965	
966	933156	901428696	31.080540	9.88535	966	
967	935089	904231063	31.996623	9.88876	967	
968	937024	907039232	31.112698	9.89217	968	
969	938961	909853209	31.128764	9.89558	969	
970	940900	912673000	31.144823	9.89898	970	
971	942841	915498611	31.160872	9.90238	971	
972	944784	918330048	31 176914	9.90578	972	
973	946729	921167317	31.192947	9.90917	973	
974	948676	924010424	31.208973	9 90917	974	
975	950625	926859375	31 224990	9.91596	975	
976	950525	929714176	31.240998	9.91935	976	
977	954529	932574833	31.256999	9.92273	977	
978	956484	935441352	31.272991	9 92213	978	
979	958441	938313739	31.288975	9 92012	979	
980	960700	951192000	31.304951	9.93288	980	
300	200100	331132000	01 00 4001	0 00200	200	

Number.	Square.	c. Cube. Square Root.		Cube Root.	Number.	
981	962361	944076141	31:320919	9.93626	981	
982	964324	946966168	31.336879	9.93963	982	
983	966289	949862087	31.352830	9 94300	983	
984	968256	952763904	31.368774	9.94637	984	
985	970225	955671625	31.384709	9.94974	985	
986	972196	958585256	31.400636	9.95311	986	
987	974169	961504803	31.416556	9.95647	987	
988	976144	964430272	31.432467	9.95983	988	
989	978121	967361669	31.448370	9.96319	989	
990	980100	970299000	31.464265	9.96655	990	
991	982081	973242271	31.480152	9.96990	991	
992	984064	976191488	31.496031	9.97326	992	
993	986049	979146657	31.511902	9.97661	993	
994	988036	982107784	31.527765	9.97995	994	
995	990025	985074875	31.543620	9.98330	995	
996	992016	988047936	31.559467	9.98664	996	
997	994009	991026973	31.575306	9.98999	997	
998	996004	994011992	31.591138	9.99332	998	
999	998001	997002999	31.606961	9.99666	999	
1000	1000000	1000000000	31.623776	10.	1000	

SILVER, TO PURIFY AND REDUCE.—Silver, as used in the arts and coinage, is alloyed with a portion of copper. To purify it, dissolve the metal in nitric acid slightly diluted, and add common salt, which throws down the whole of the silver in the form of chloride. To reduce it into a metallic state several methods are used: 1. The chloride must be repeatedly washed with distilled water, and placed in a zinc cup; a little diluted sulphuric acid being added, the chloride is soon reduced. The silver when thoroughly washed is quite pure. In the absence of a zinc cup, a porcelain cup containing a zinc plate may be used. The process is expedited by warming the cup.

2. Digest the washed chloride with pure copper and ammonia. The quantity of ammonia need not be sufficient to dissolve the chloride. Leave the mixture for a day, then wash the silver thoroughly.

3. Boil the washed and moist chloride in solution of pure potash, adding a little sugar: when washed it is quite pure.

Welding Composition.—Mix borax with \$\frac{1}{10}\$th of sal ammoniae, fuse the mixture, and pour it on an iron plate. When cold, pulverise it, and mix it with an equal weight of quick lime, sprinkle it on iron, which is heated to redness, and replace it in the fire. It may be welded below the usual heat.

## BLACKING RECIPES.

Liquid Blacking, for Boots and Shoes.—1. Ivory black, 3 oz.; molasses, 2 oz.; sweet oil, ½ oz. Mix to form a paste. Add gradually ½ oz. of oil of vitriol, and then half a pint of vinegar, and 1½ pint of water, or sour beer. Some prefer mixing the oil of vitriol with the sweet oil.

2. Ivory black, 2 lbs.; molasses, 2 lbs.; sweet oil, ½ lb. Mix, and add \( \frac{3}{2} \) lb. oil of vitriol, and enough beer or vinegar to make up a

gallon.

3. Ivory black, 3 lbs.; molasses, 4 lbs.; vinegar, 1 pint; oil of

vitriol, 8 oz.; water, 1 gallon.

4. Ivory black, 2 lbs.; neat's-foot oil, 4 oz. Mix, and add 3 quarts of sour beer or vinegar, and a spoonful of any kind of spirits; stir till smooth, and add 2 oz. of oil of vitriol, and sprinkle on it ½ drachm of powdered resin. Then boil together 3 pints of sour ale with a little logwood, and ½ oz of Prussian blue, 3 oz. of honey, and 8 oz. of molasses. Mix, but do not bottle it for two or three days.

5. Ivory black, 8 oz.; brown sugar, or molasses, 8 oz.; sweet oil, 1 oz.; oil of vitriol,  $\frac{1}{2}$  oz.; vinegar, two quarts. Mix the oil with the molasses, then add the oil of vitriol and vinegar, and lastly the

ivory black.

Blacking for Dress Boots —1. Gum, 8 oz.; molasses, 2 oz.; ink, 1 pint; vinegar, 2 oz.; spirit of wine, 2 oz. Dissolve the gum and molasses in the ink and vinegar, strain, and add the spirit.

2. To the above add 1 oz. of sweet oil, and \(\frac{1}{4}\) oz. of lampblack. [These are applied with a sponge, and allowed to dry out of the

dust. They will not bear the wet.]

3. Beat together the whites of 2 eggs, a table-spoonful of spirit of wine, a lump of sugar, and a little finely powdered ivory black to thicken.

Blacking, without Polishing.—Molasses, 4 oz.; lampblack, ½ oz.; yeast, a table-spoonful; 2 eggs; a tea-spoonful of olive oil; a teaspoonful of turpentine. Mix well. To be applied with a sponge,

without brushing.

India Rubber Blacking.—Ivory black, 60 lbs.; molasses, 45 lbs.; vinegar (No. 24), 20 gallons; powdered gum, 1 lb.; India rubber oil, 9 lbs. (The latter is made by dissolving, by heat, 18 oz. of India rubber in 9 lbs. of rape oil,) Grind the whole smooth in a paint mill. Then add, by small quantities at a time, 12 lbs. of oil of vitriol, stirring it strongly for half an hour a day for a fortnight.

Paste Blacking. - 1. Oil of vitriol, 2 parts; sweet oil, 1 part;

molasses, 3 parts; ivory black, 4 parts. Mix.

2. This may be made with the ingredients of liquid blacking, using sufficient vinegar, in which a little gum has been dissolved, to form a paste. Make it into cakes, and dry it.

3. (Bailey's Blacking Balls.) Bruised gum tragacanth, 1 oz.; water, 4 oz. Mix, and add 2 oz. of neat's-foot oil, 2 oz. of fine ivory black, 2 oz. of Prussian blue. Mix, and evaporate to a proper consistence.

Blacking for Harness.—1. Isinglass or gelatine, \(\frac{1}{4}\) oz; powdered indigo, \(\frac{1}{4}\) oz; soft soap, 4 oz; logwood, 4 oz; glue, 5 oz. Boil together in 2 pints of vinegar, till the glue is dissolved; then strain

through a cloth, and bottle for use.

2. Melt 8 oz. of beeswax in an earthen pipkin, and stir into it 2 oz. of ivory black, 1 oz. of Prussian blue ground in oil, 1 oz. of oil of turpentine, and ½ oz. of copal varnish. Make it into balls. To be applied with a brush, and polished with an old handkerchief.

3. Molasses ½ lb.; lampblack, 1 oz.; yeast, 1 spoonful; of sugar candy, olive oil, gum tragacanth, and isinglass, 1 oz. each; a cow's gall. Mix all together with 2 pints of stale beer, and let it stand

before the fire for an hour.

Heel Balls.—1. Melt together 4 oz. of mutton suet, 1 oz. of beeswax, 1 oz. of sweet oil,  $\frac{1}{2}$  oz. oil of turpentine, and stir in 1 oz. of powdered gum arabic, and  $\frac{1}{2}$  oz. of fine lampblack.

2. Beeswax, 8 oz.; tallow, 1 oz.; powdered gum, 1 oz.; lamp-

black, q. s.

Heel balls are used not merely by the shoemaker, but to copy inscriptions, raised patterns, &c., by rubbing the ball on paper laid over the article to be copied.

BLACKLEAD PENCILS.—The easiest way of producing, not only blacklead, but all sorts of pencils, is by the following process, which at once combines simplicity, cheapness, and the finest quality.

Take white or pipe-clay: put it into a tub of clean water, to soak for twelve hours, then agitate the whole, until it resembles milk, let it rest two or three minutes, and pour off the supernatant milky liquor into a second vessel, allow it to settle, pour off the clear, and dry the residue on a filter. Then add blacklead, any quantity. Powder it, and calcine it at a white heat in a loosely covered crucible, cool, and carefully pulverize, then add prepared clay, prepared plumbago, equal parts. Water to mix. Make them into a paste, and put it into oiled moulds of the size required, dry very gradually, and apply sufficient heat to give the required degree of hardness; lastly, the pieces should be taken carefully from the moulds, and placed in the grooves of the cedar. The more clay and heat employed the harder the crayon; less clay and heat of course produces a contrary effect. The shade of black may also be varied in the same way. Each mould must be made of four pieces of wood, nicely fitted together.

BLACK FOR MINIATURE PAINTERS.—Take camphor, and set it on the fire, and collect the soot by means of a saucer or paper funnel inverted over it.

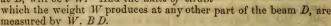
## STRAIN AND STRESS OF MATERIALS.

Let A B be a beam of timber, firmly fixed in a wall at A, and a weight, W, measured in pounds avoirdupois, acting at the extremity B, at right angles to A B.

If A B be one foot, and the weight W be one pound, then the strain produced at A is

called a unit of strain.

If the beam A B be (l) feet long, and the weight be (W) pounds, then the *units of strain* produced at A, by the weight acting at B, will be l W. And the *units of strain* 



Let AB = 10 feet, and the weight W be equal to 112 lbs., and BD = 7 feet.

The units of strain at  $A = 112 \times 10 = 1120$ .

The units of strain at  $D = 112 \times 7 = 784$ .

The greatest strain on the beam is at A, at which place the beam would break if it was equally strong throughout.

If the weight W be uniformly distributed over the whole length of the beam AB, as in fig. 2, the units of strain at A will be only one-half as great as that produced by the weight W acting as in fig. 1.

The units of strain at A, which are produced by the beam itself, are equal to the weight of the beam multiplied by half its length.

The beam A B, fig. 3, is equally strong between the points A and B, when the underside of it is a common parabola.

Hence, from a square beam, one-third part of it may be cut off without diminishing its strength.

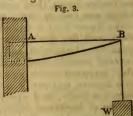
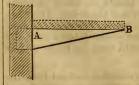


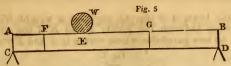
Fig. 1.

Fig. 4.



diminishing its strength.

If the weight W be uniformly distributed over the whole length of the beam A B, as in fig. 4; then the beam is equally strong when the underside of it is a straight line. In this case, one half the beam may be cut away without



Let the weight W (fig. 5) be sustained by a beam A B, which rests on two props at C and D.

The pressure on the prop at C is equal to W. B E: A B.

The pressure on the prop at D is equal to W. A E : A B.

The units of strain at E are equal to W. A E. B E: A B.

The units of strain at G are equal to W. A E. BG: AB.

The units of strain at F are equal to W. B E. A F: A B.

The greatest strain, which is produced by the weight W, is at E. The units of strain at the middle of the beam, produced by the weight W acting at E, are equal to  $\frac{W.\ A\ E}{2}$ .

Let A B = 18 feet, and a weight of 112 lbs. be placed at E, which is 8 feet from A.

Apply these numbers to the above formulæ and their results.

The pressure on the prop at C is equal to  $\frac{10 \times 112}{18} = 62.5$  lbs.

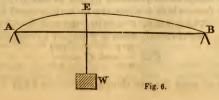
The pressure on the prop at D is equal to  $\frac{8 \times 112}{18} = 49.8$  lbs.

The units of strain at E are equal to  $\frac{10 \times 8 \times 112}{18} = 497.77$ .

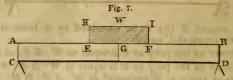
The units of strain on the middle are equal to  $\frac{8 \times 112}{2} = 448$ .

When the weight W is laid on the middle of the beam A B, the units of strain on the middle are equal to  $\frac{W. A B}{4}$ .

If the weight W be uniformly distributed along the beam A B, the *units of strain* on the middle of it will be equal to  $\frac{W. AB}{8}$ ; which is only one half the strain that is produced by the weight having been laid on the middle.



When the beam A B (fig. 6), supports a weight W, at E, it is equally strong between the points A and B, if the upper sides, A E, B E, be two parabolas whose vertex is A and B respectively.



Let the weight W have a bearing EF (fig. 7), equal on both sides of the centre G, and also let the weight be equally distributed on the bearing E F.

The units of strain at G are equal to  $\frac{W.AB}{4} - \frac{W.EF}{8}$ 

Now, if the weight W were a sphere, and were laid on the middle of the beam at G, the units of strain at G would be equal to W.AB

4

If the same weight be formed into a cube, whose side is EF, the units of strain at the centre G will be less than in the case of the

Fig. 8.

sphere by  $\frac{W.EF}{g}$ 

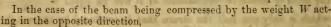
Let A B be any beam suspended vertically from the point A (fig. 8): and let the sectional area be constant from A to B, where a weight W lbs. is acting to extend the beam.

Put a = area of the section of the beam in square inches.

l = length of the beam in feet before the weight is applied to elongate it.

e = the elongation produced by the weight W. E = weight which would be necessary to make

e equal to l. The quantity E is called the modulus of elasticity of the material of which the beam is composed.



Put c = compression produced by the weight W.

C = force which is necessary to make c equal to half of (l). The quantity C is called the modulus of elasticity of the material, when it is subject to compression.

$$E = \frac{Wl}{ae}$$
 and  $C = \frac{Wl}{ae}$ 

Units of work done to elongate the beam e feet  $=\frac{We}{2}$ .

Units of work done to compress the beam c feet  $=\frac{Wc}{2}$ .

Mean results of experiments on four different kinds of Cast-iron bars, 10 feet long and 1 square inch in section.

Weight laid on bar per square inch = W.	Extension of bar in inches = 12 e.	Set of bar in inches.	The value of $\frac{12 W}{e}$ .
lbs.	inches.	008001	1242
1054	.009	# 6780F o	117085
1581	.0137	.00022	115131
2108	.0186	.00055	113308
3161	.0287	.00107	110150
4215	.0391	.00175	107802
5269	.0500	.00265	105377
6323	.0613	.00372	103142
7376	.0734	.00517	100496
8430	.0859	.00664	98139
9484	.0995	.00844	95316
10538	.1136	.01062	92762
11591	.1283	.01306	90347
12645	.1448	.01609	87329
13700	.1668	.02097	82133
14793	.1859	.02410	79576
00/7/	1,134	10.2	128867

Hence, the breaking weight per square inch of section is 14793 lbs. = 6.6 tons nearly; and the ultimate extension is .1859 inches, or  $\frac{1}{64}$ , of the whole length, 10 feet.

If we deduct the set '0209 from '1859, we shall have '165 inches for the elongation produced by the weight 14793 lbs.

∴ 
$$E = \text{modulus of elasticity} = \frac{14793 \times 10 \times 12}{.165} = 10758545.$$

.: Breaking weight = 6.6 tons × area of section in square inches.

If the weight 5269 be taken, the modulus of elasticity will be considerably increased. Deduct .00175 the set from .05, leaving .04825 inches for the elongation due to the weight 5269 lbs.

∴ 
$$E = \text{modulus of elasticity} = \frac{5269 \times 10 \times 12}{.04825} = 13104249.$$

This difference in the modulus of elasticity arises from the circumstance of the law of elasticity not being proportional to the weight.

TABLE

Of the Tensile Strength of Wrought Iron.
The Bar was 10 feet long and 1 square inch section.

Weight laid on the Bar W.	Extension of the Bar or value of 12 e.	Set of Bar.	The value of 12 W e		
lbs.	inches.	inches.	11-1		
1262	.00520		242665		
3785	•01690	.0005	223998		
6309	.02772	.0005	227608		
8833	.03790	.0005	233061		
11356	.04854	.0005	233966		
13880	.05950	.0007	233285		
16404	.06980	.0007	235016		
18928	.08170	.00130	231675		
21452	.09310	.00270	230415		
23975	10570	.00410	226824		
26499	12040	.00680	220092		
29023	14500	.0120	200157		
30284	19910	.0120	6-1/		
	•23660	1082	after bearing the weight 17 hours.		
31546	•24200	.1083	130357		
ditto	•24490	•1111	after five minutes.		
35332	2.04	1.874	17320		

The bar broke with a weight of 24 tons per square inch of section. Hence the tensile force of wrought iron is nearly four times as great as the tensile force of cast iron.

TABLE
Of the Compressive Strength of Wrought Iron.
The Bar was 10 feet long and 1 square inch section.

Weight laid on the Bar, or (W).	Decrement of length, or the value of 12 c.	Weight laid on the bar, or (W).	Decrement of length, or the value of 12 c.
lbs.	inches.	lbs.	inches.
5098	.028	23018	•119
9578	.052	25258	•130
14058	•073	27498	•142
16298	•085	29738	•154
18538	•096	31978	.174
20778	•107	34218	•214

The crushing force of wrought iron is 12 tons per square inch. It is a curious fact, that cast iron is decreased in length nearly double what wrought iron is, by the same weight; but the wrought iron bar will sink to any degree with little more than 12 tons per square inch, whilst cast iron will bear 43.56 tons to produce the same effect.

A wrought bar will bear a compression of  $\frac{1}{863}$  of its length,

without its utility being destroyed.

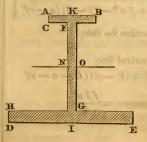
Compression of Cast Iron.

Mean results of experiments on four different kinds of Cast Iron, 10 feet long, and 1 square inch in section.

Weight laid on the bar (W).	Decrement of length, or the value of 12 c.	Set of bar in mches.	The value of $\frac{12 W}{c}$ .
lbs.	inches.	inches.	
2065	.01875	.00047	110119
4129	.03878	.00226	106485
6194	.05978	.00400	103617
8259_	.07879	.00645	104822
10324	.09944	.00847	103819
12388	12030	.010875	102980
14453	•14163	.01405	102049
16518	16338	.01712	101101
18583	18505	.02051	100420
20464	20624	.02484	100114
24777	•24961	•03220	99263
-28906	•29699	•04300	97331
33031	*35341	•06096	93463

The crushing or compressive force of cast iron per square inch is 43.56 tons, which has been obtained from eleven kinds of cast iron. But the tensile force of cast iron is 6.6 tons; therefore the compressive force is equal to the square of the tensile force, or (6.6)<sup>2</sup>.

#### Transverse Strength of Beams.



To find the neutral line, forces of extension, forces of compression, moments of extension, and moments of compression of a beam subject to transverse flexure.

Let the form of the section of the beam be that of the figure A B D E, where BC, HE, represent sections of the top and bottom ribs, FG that of the vertical one connecting them, and N O pass through the neutral line.

Put a, a' = NI, NK, respectively.

$$c, c' = D H, A C,$$
 respectively.  
 $b, b' = D E, A B,$  do.

 $\beta$  = the thickness of the vertical rib.

f, f' = tensile and compressive forces of the material, in a square inch of section, as exerted at a distance (a) on opposite sides of the neutral line.

For the determination of the neutral line

$$f \left\{ ba^{2} - (b - \beta) (a - c)^{2} \right\} = f' \left\{ b' a'^{2} - (b' - \beta) (a' - c')^{2} \right\}$$

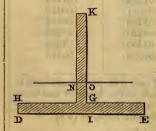
And a + a' = D, where D is the whole depth of the beam.

For moderate strains per square inch 
$$f = f'$$
  
 $\therefore ba^2 - (b-\beta)(a-c)^2 = b'(D-a)^2 - (b'-\beta)(D-a-c')^2$ 

Moments of extension = 
$$\frac{f}{3a} \left\{ ba^3 - (b-\beta)(a-c)^3 \right\}$$

$$\text{Moments of compression} = \frac{f}{3 \ a} \left\{ \ b' \ a'^3 - (b' - \beta) \ (a' - c')^3 \right\}$$

If W be the weight laid on the middle, and l equal length between supports,

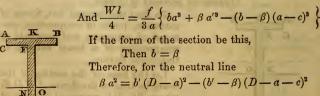


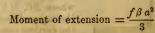
If the form of the section be this, Then  $b' = \beta$ 

Therefore, for the neutral line  $b a^2 - (b - \beta)(a - c)^2 = \beta (D - a)^2$ . Moment of extension

$$= \frac{f}{3 a} \left\{ b a^3 - (b - \beta) (a - c)^3 \right\}$$

Moment of compression =  $\frac{f\beta a'^3}{3a}$ 





Moment of compression

$$= \frac{f}{3 a} \left\{ b' a'^3 - (b' - \beta) (a' - c')^3 \right\}$$

And 
$$\frac{Wl}{4} = \frac{f}{3a} \left\{ \beta a^3 + b' a'^3 - (b' - \beta) (a' - c')^3 \right\}$$

If the form of the section be this,

Then,  $b = \beta$  and  $b' = \beta$ 

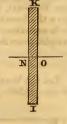
Therefore, for the neutral line 2a = D

or the neutral line is in the middle of the section.

Moment of extension = 
$$\frac{f \beta D^2}{12}$$

Moment of compression 
$$=\frac{f\beta D^2}{12}$$

$$\therefore Wl = \frac{2f\beta D^2}{3}$$



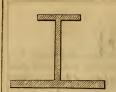
## Transverse Strength of Cast-Iron Bars.

Length of Bar between supports, with its dimensions.	Breaking weight laid on middle.	Ultimate deflexion in inches.	Mean of experi- ments.
	lbs.		
$4\frac{1}{2}$ feet, with 1 inch square	440	1.779	3
9 feet, with 2 inches square	1338	3.0032	6
13½ feet, with 3 inches square	2861	4.667	5
63 feet, with 3 inches square	6117	1.2916	3

From the three last experiments we find  $\frac{2f}{3} = 1490$ .

$$W = 1490 \times \frac{\beta D^2}{l}$$

For a cast-iron beam, where W is the breaking weight in lbs.,  $\beta$  is the breadth of the beam measured in inches, D the depth of the beam measured in inches, and l the length of beam between supports measured in feet.



The best dimensions of a beam, whose section is given in the figure, are when the bottom flange contains six times as much area as the top flange. And the breaking weight of such beams may be found by the following admirable rule:

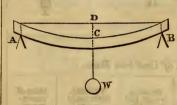
Multiply the sectional area of the bottom flange in square inches, by the depth of the

beam in inches, and divide the product by the distance between the supports, measured in feet, then 2.14 times the quotient will give the breaking weight in tons.

A cast-iron bar is not weakened by passing half the breaking weight over it 96,000 times, with a velocity of 81 feet per minute.

## Deflection of Beams.

Let the beam be supported at A and B, and weight W applied at the middle C.



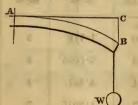
$$\therefore DC = \frac{Wl^3}{4 E\beta D^3}$$

E = the modulus of elasticity of the material.

 $\beta$  = breadth of beam in in.

D = depth of beam in inches.

l = length of beam in inches.



Let the beam be supported at A, and a weight W applied at the other extremity.

$$\therefore B C = \frac{4 W l^3}{E\beta D^3}$$

Rule for finding the ultimate deflexion of a cast-iron beam:

Ultimate deflexion D C in inches  $=\frac{3 \ \hat{t}^2}{40 \cdot D}$  for first figure.

Ultimate deflexion B C in inches  $=\frac{6\ l^2}{5\ D}$  for second figure,

where l is measured in feet and D in inches.

These values for the ultimate deflexion are independent of the breadth of the beam.

Find the ultimate deflexion of a cast-iron bar, the distance between the supports being 24 feet, and depth 4½ inches.

Ultimate deflexion = 
$$\frac{3}{40} \frac{l^2}{D^2} = \frac{3 \times 24^2}{40 \times 4\frac{1}{2}} = 9.6$$
 inches.

If the weight W be uniformly distributed along the beam, the deflexion will be in all cases  $\frac{5}{8}$  of the deflexion which is produced by the weight acting on the middle, or in the case of having only one support, acting at the extremity.

## Transverse Flexure of a Wrought-Iron Bar by Pressure acting Horizontally.

Length of bar 14 feet  $7\frac{1}{2}$  inches, depth of bar in direction of pressure 1.515 inches, breadth 5.523 inches, distance between supports 13 feet 6 inches. The experiment was continued to the limit of perfect elasticity, or to that point at which the elasticity was sensibly injured.

Weight applied, acting horizontally.	Deflexions after five minutes.	Sets after five minutes.	Ratio of weights to deflexions.		
lbs.	inches.	inches.	- U-1 11		
- 28	.051	.0	549\		
56	.112	.0	500		
112	• 232	.0	483		
168	•344	.001	488		
224	•458	.002	489		
280	.571	.003	490		
336	.684	.003	491		
392	•800	.004	490		
448	•916	.006	489 86 501 4		
504	1.005	.007	501 \ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\		
560	1.124	.008	Wean 498 050		
616	$1\cdot 222$	.010	504		
672	1.332	.011	504		
728	1.434	.017	508		
784	1.547	.019	507		
840	1.693	.019	496		
896	1.823	.019	492		
952	1.933	.020	493		
1008	2.044	.021	493		
1064	2.165	.022	491/		

To find the weight which a wrought-iron beam is capable of bearing without injuring its elasticity.

$$W = \frac{1073 \beta D^2}{l} \text{ lbs.} = \frac{\beta D^2}{2 l} \text{ tons, nearly.}$$

 $\beta$  and D are measured in inches, and l in feet, being the distance between the supports.

What is the weight that can be laid on a wrought-iron bar, 20 feet long, 3 inches broad, and 6 inches deep, without injuring its elasticity?

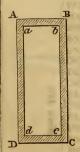
$$W = \frac{3 \times 36}{40} = \frac{108}{40} = 2.7 \text{ tons.}$$

The deflexion of a wrought-iron beam, supported at each end, and loaded in the middle, when the elastic limit is obtained.

Deflexion in inches = 
$$.0167 \times \frac{l^2}{D}$$
.

The length, l, is measured in feet, and D, the depth, in inches. Taking the bar given in the last example,

Deflexion = 
$$\cdot 0167 \times \frac{400}{6} = 1.11$$
 inches.



Hollow Rectangular Beams.

Let A B C D be the section of a hollow rectangular beam.

Let 
$$AD = D$$
, and  $ad = d$   
 $AB = B$ , and  $ab = b$   

$$\therefore Wl = \frac{2f}{2D} \left\{ BD^3 - bd^3 \right\}$$

where W is the weight applied at the middle between the supports, and f is a constant depending on the nature of the material.

FLUID FOR ETCHING ON COPPER.—Verdigris 4 parts; salt 4; sal ammoniac 4; alum 1; water 16; strong vinegar 12. Dissolve with heat.

ACID FOR ETCHING ON STEEL.—Pyroligneous acid 5 parts; alcohol 1; nitric acid 1. Mix the first two, then add the nitric acid.

#### TABLE

Of Experiments on the Transverse Strength of Rectangular Tubes of Wrought-Iron, supported at each end, and the weight laid on the middle.

Distance between the supports.	Weight of tubes between the sup- ports.	Breaking weights, exclu- sive of the weights of the tubes.	External depth of the tubes.		Thickness of the plates of the tubes.	
Feet.		Tons.	Inches.	Inches.	Inches.	
30.0	42.62 cwt.	57.5	24	16	.525	
7.5	72.36 lbs.	4.454	6	4	·1325	
30.0	23.09 ewt.	22.84	24	16	.272	
7.5	35.53 lbs.	1.409	6	4	.065	
3.75	9.65 "	1.1	3	2	.061	
3.75	4.34 "	• 3	3	2	.03	
45.0	130.36 cwt.	114.76	36	24	.75	
3.75	9.65 lbs.	1.1	3	2	.061	
30.0	39 cwt.	54.3	24	16	•50	

In several of these experiments the tubes gave way by the metal at the top becoming wrinkled.

In similar tubes the strength, and consequently the breaking weight, is proportional to (1.9) power of the lineal dimensions.

From these experiments the breaking weight may be obtained as follows:

$$W = \frac{3}{4 l D} \left\{ B D^3 - b d^3 \right\}$$
 in tons.

The breadths and depths are measured in inches, and the length in feet.

If the thickness of the metal be equal to t inches completely round the section,

Then, 
$$W = \frac{3}{4Dt} \left\{ BD^3 - (B-2t)(D-2t)^3 \right\}$$

the breaking weight in tons for a wrought-iron tube, whose form of section is

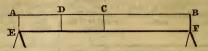
What is the breaking weight of a rectangular tube 40 feet long, depth 2 feet 6 inches, thickness of plate ‡ inch, and breadth 18 inches?



$$W = \frac{3}{4800} \left\{ 18 \times 30^3 - 17.5 \times 29.5^3 \right\}$$

$$=\frac{1}{1600}\left\{486000-449267\right\}=22.96$$
 tons.

From a great number of well arranged experiments, on the strength of iron beams and tubes, it follows that they may be safely reduced in strength from the middle towards the extremities in the ratio indicated by theory.



Let AB be a beam supported at its extremities E and F, and put F equal to the necessary strength at the middle of the beam.

Then, the necessary strength at 
$$D=F imes rac{A~C^2-C~D^2}{A~C^2}$$

The tensile force of wrought iron is to its compressive force as 2 to 1.

Hence, the plate on the upper side of hollow wrought-iron tubes should contain an area twice as great as the plate on the under side.

#### Strength of Cast-Iron Pillars.

The breaking weight of solid cylindrical cast-iron pillars.

In solid pillars, with their ends rounded, and moveable,

Breaking weight in tons = 
$$14.9 \times \frac{d^{3.6}}{h.7}$$
 . . . (1)

In solid pillars, with their ends flat, and incapable of motion,

Breaking weight in tons = 
$$44.16 \times \frac{d^{3.6}}{11.7}$$
 . . . (2)\*

where l is the length of pillar in feet, and d the diameter in inches. In hollow pillars of cast-iron, where D, d are the external, internal diameters, and l the length: both ends of the pillar were moveable.

Breaking weight in tons = 13 
$$\times \frac{D^{3\cdot6} - d^{3\cdot6}}{l^{1.7}}$$

In hollow cast-iron beams, whose ends were flat and firmly fixed,

Breaking weight in tons = 44.3 
$$\frac{D^{3.6}-d^{3.6}}{l^{1.7}}$$

Of three cylindrical pillars of steel, wrought and cast iron, and wood, all of the same length and diameter, the first having its ends

<sup>\*</sup> Formula (1) was obtained from the mean result of eighteen pillars, varying in length from 121 times the diameter down to 15 times. The formula (2) was derived from eleven pillars, with flat ends, varying in length from 73 to 25 times the diameter.

rounded, the second with one end round and the other end flat, and the third with both ends flat, the strengths are as 1, 2, and 3.

These formula and results were obtained from experiments on pillars, varying in length from 121 times the diameter down to 15 times.

#### Effects of Temperature upon the Strength of Cast-Iron.

The strength of cast-iron is not reduced when its temperature is raised to 600°, which is nearly that of melting lead; and it does not differ very widely whatever the temperature may be, provided the bar be not heated so as to be red hot.

#### EXAMPLE.

Find the strength of a hollow cylindrical cast-iron pillar, 14 feet long, 6.2 inches external diameter, and 4.1 inches internal; the pillar being flat and well supported at the ends.

$$14^{1.7} = 88.801$$
  $6.2^{3.6} = 712.22$  and  $4.1^{3.6} = 160.7$ 

.: Breaking weight in tons = 
$$44.3 \times \frac{D^{3.6} - d^{3.6}}{l^{1.7}}$$

$$=44.3\times\frac{712.22-160.7}{88.801}$$

#### = 275

#### Comparative Strength of Long Pillars.

If the strength of cast-iron pillars be 1000, then wrought-iron will be 1745, cast-steel 2518, Dantzic oak 108.8, and red deal 78.5.

The strength of similar pillars is as the square of their linear

#### Resistance to Torsion.

- Let l = length of prism from the fixed end to the point of application of the lever used to twist it.
  - r =radius of prism, if round.
  - b, d = breadth and thickness, if rectangular.
    - W = the weight acting by means of the lever to twist the prism.
    - L =length of the lever to which the weight W is applied.
    - $\theta =$ angle of torsion.
    - R = resistance to torsion at the time of fracture.
    - C =constant for each species of body.

$$\pi = 3.14159$$
, &c.

For a cylinder,

$$2 L l W = C \pi \theta r^4$$
 and  $2 W L = \pi R r$ .

For a square,

6 
$$L l W = C \theta d'$$
 and 6  $W L = \sqrt{2 \cdot R} d'$ .

For a rectangle, 
$$3Ll W(b^2+d^2) = C\theta b^3 d^3$$
 and  $3WL \sqrt{b^2+d^2} = Rb^2 d^3$ 

The Ultimate Resistance of a Cast-iron Beam to Torsion. In a cylinder,  $WL = 51055 r^3$ .

In a square prism,  $WL = 7660 d^3$ .

In a rectangular prism, WL = 10834  $\sqrt{b^2 + d^2}$ 

All the dimensions are taken in inches.

Strength of Ropes.

The cohesion of hempen fibres is 6400 lbs. for every square inch of section.

Breaking weight in tons =  $\frac{\text{circumference squared}}{4}$ 

the circumference being measured in inches.

Ex.—Find the breaking weight of a rope 6 inches in circumference.

Breaking weight  $=\frac{36}{4}=9$  tons.

For a common cable,

Breaking weight in tons  $=\frac{\text{circumference squared}}{5}$ 

These are practical rules and easy of application.

## PROCESSES FOR STAINING WOODS.

Mahogany Color (Dark).—Boil ½ lb. of madder and 2 oz. of logwood in a gallon of water; then brush the wood well over with the hot liquid. When dry, go over the whole with a solution of 2

drachms of pearlash in a quart of water.

Mahogany Color (Light).—Brush over the surface with diluted nitrous acid, and when dry apply the following, with a soft brush: Dragon's blood, 4 oz.; common soda, 1 oz.; spirit of wine, 3 pints. Let it stand in a warm place, shake it frequently, and then strain. Repeat the application until the proper color is obtained.

To Stain Maple a Mahogany Color.—Dragon's blood, 1 oz; alkanet, 2 oz; aloes, 1 dr.; spirit of wine, 16 oz. Apply it with a

sponge or brush.

Rosewood.—Boil 8 oz. of logwood in 3 pints of water until reduced to half; apply it, boiling hot, two or three times, letting it dry between each. Afterwards put in the streaks, with a camel's hair pencil, dipped in a solution of copperas and verdigris in a decoction of logwood.

Ebony.—Wash the wood repeatedly with a solution of sulphate of iron; let it dry, then apply a hot decoction of logwood and nutgalls for two or three times. When dry, wipe it with a wet sponge; and when dry again, polish with linseed oil.

Red.—1. Take a pound of Brazil wood and mix it with a gallon of stale urine. Pour over the wood while boiling hot. Before it dries it should be laid over with alum water. 2. A fine red may also be obtained by a solution of dragon's blood in spirits of wine.

Yellow.—Nitric acid, lightly diluted, will produce a fine yellow on wood. Sometimes, if the wood is not in proper condition, it will create a brown. Care must be taken that the acid used be not too strong, or it will render the wood nearly black.

Blue.—Take of alum 4 parts; water 85 parts. Boil.

Purple.—To produce this color, take of logwood 11 parts; alum

3 parts; water 29 parts. Boil.

Mahogany.—1. Linseed oil 2 pounds; alkanet 3 ounces. Heat them together and macerate for six hours, then add resin 2 ounces; beeswax 2 ounces. Boiled oil may be advantageously used instead of the linseed oil.

2. Brazil-wood (ground); water sufficient; add a little alum and

potash. Boil.

3. Logwood 1 part; water 8 parts. Make a decoction, and apply it to the wood; when dry, give it two or three coats of the following varnish: dragon's blood 1 part; spirits of wine 20 parts. Mix.

To take Stains out of Mahogany.—Spirits of salts 6 parts; salt of lemons 1 part. Mix, then drop a little on the stains, and rub

them until they disappear.

To Stain Musical Instruments.—Crimson: Boil one pound of ground Brazil wood in three quarts of water for an hour; strain it, and add half an ounce of cochineal; boil it again for half an hour gently, and it will be fit for use.

Purple: Boil a pound of chip logwood in three quarts of water

for an hour; then add four ounces of alum.

## LOGARITHMS.

Logarithms literally signify ratios of numbers; hence Logarithmic Tables may be various, but those in common use for the facilitating of arithmetical operations generally are of the following corresponding progressions, viz.:—

Arithmetical, 0, 1, 2. 3. &c., or series of logarithms. Geometrical, 1, 10, 100, 1000, &c., or ratio of numbers.

And thus it may be perceived, that if the log. of 10 be 1, the log. of any number less than 10 must consist wholly of decimals, because increasing by a decimal ratio. Again; if the log. of 100

be 2, the log. of any intermediate number between 10 and 100 must be 1, with so many decimals annexed; and in like manner, the log. of any intermediate number between 100 and 1000, must be 2, with decimals annexed proportionally, as before.

#### Application and Utility of Common Logarithmic Tables.

The whole numbers of the series of logarithms, as 1, 2, 3, &c., are called the indices, or characteristics of the logarithm, and which must be added to the logarithm obtained by the table, in proportion to the number of figures contained in the given sum. Thus suppose the logarithm be required for a sum of only two figures, the index is 1; if of three figures, the index is 2; and if of four figures, the index is 3, &c.; being always a number less by unity than the number of figures the given sum contains.

#### EXAMPLES.

The index of 8 is 0, because it is less than 10.
The index of 80 is 1, because it is less than 100.
The index of 800 is 2, because it is less than 1000.
The index of 8000 is 3, because it is less than 10,000, &c.

The index of a decimal is always the number which denotes the significant figure from the decimal point, and is marked with the sign, thus, —, to distinguish it from a whole number

#### EXAMPLES.

The index of 32549 is -1, because the first significant figure is the first decimal.

The index of '032549 is - 2, because the first significant figure is the second decimal.

The index of '0032549 is — 3, because the first significant figure is the third decimal, &c., of any other sum.

If the given sum for which the logarithm is required contains or consists of both integers and decimals, the index is determined by the integer part, without having any regard to the other.

#### 1. To find the logarithm of any whole number under 100.

Look for the number under N in the first page of any Logarithmic Table; then immediately on the right of it is the logarithm required, with its proper index. Thus the log. of 64 is 1.806180, and the log. of 72 is 1.857332.

2 To find the logarithm of any number between 100 and 1000, or any sum not exceeding 4 figures.

Find the first three figures in the left-hand column of the page under N, in which the number is situated, and the fourth figure, at the top or bottom of the page; then the logarithm directly under the fourth figure, and in a line with the three figures in the column on the left, with its proper index, is the logarithm required. Thus, the log. of 450 is 2.653213, and the log. of 7464 is 3.872972. Or, the log. of 378.5 is 2.578066, and that of 7854 is —1.895091.

3. To find the number indicated by a given logarithm.

Look for the decimal part of the given logarithm in the different columns, and if it cannot be found exactly, take the next less. Then under N in the left-hand column, and in a line with the logarithm found, are three figures of the number required, and on the top of the column in which the found logarithm stands is one figure more; place the decimal point as indicated by the logarithmic index, which determines the sum properly valued, as required.

which determines the sum, properly valued, as required.

If the logarithm cannot be found exactly in the tables, subtract from it the next less that can be found, and divide the remainder by the tabular difference; the quotient will be the rest of the figures of the given number, which, being annexed to the tabular number

already found, is the proper number required.

Ex. Required, the number answering to the logarithm 3.233568.

Given logarithm . . . . = 3.233568Next less is the log. of 1712 = 3.233504

Remainder . . . . 64

Tab. Diff. = 253, and  $\frac{64}{253}$  = 2.5

Hence the number required = 1712.25.

For practical purposes in mechanics, logarithms are seldom resorted to, unless for the raising of the powers of numbers or extraction of their roots. These operations, when tables are at hand, they very much facilitate; involution or the raising of powers, being performed simply by multiplication, and evolution, or the extraction of roots, by division, as in simple arithmetic.

Ex. 1. Required, the square or second power of 25.791.

Log. of 25.791 = 1.411468

Multiplied by 2 the power required.

Logarithm 2.822936 indicated number or square required = 665.175.

Ex. 2. What is the cube of 30.7146?

Logarithm = 1.487345 Multiplied by 3 the power required.

Logarithm 4.462035 indicated number or cube required = 28975.7.

Ex. 3. Required, the square root of 365.

Log.  $=\frac{2.562293}{2}=1.281146$  indicated number or root =19.105.

Ex. 4. Find the cube root of 12345.

 $Log. = \frac{4.091491}{3} = 1.363830$  indicated number or root = 23.116.

and districted the Transport of Sangarana

For Table of Logarithms, see p. 483.

Engraving in Alto-Relievo.—In the common operation of engraving, the desired effect is produced by making incisions upon the copper-plate with a steel instrument of an angular shape, which incisions are filled with printing-ink, and transferred to the paper by means of a roller, which is passed over its surface. There is another mode of producing these lines or incisions, by means of diluted nitrous acid, in which the impression is taken in the same way. Another method of engraving is done upon a principle exactly the reverse, for instead of the subject being cut into the copper, it is the interstice between the lines which is removed by diluted aquafortis, and the lines are left as the surface, from which the impression is taken by means of a common type-printing press, instead of a copper-plate press.

covered with lampblack, whatever is required upon the plate; and when the varnish is thoroughly dry, the acid is poured upon it, and the interstice of course removed by its action upon the uncovered part of the copper. If the subject is very full of dark shadows, this operation will be performed with little risk of accident, and with the removal of very little of the interstice between the lines; but if the distance between the lines is great, the risk and difficulty is very much increased, and it will be requisite to cut away the parts which surround the lines with a graver, in order to prevent the dabber with the printing-ink from reaching the bottom, and thus producing a blurred impression. It is obvious, therefore, that the more the plate is covered with work, the less risk there will be in the preparation of it with the acid, after the subject is drawn,

This is effected by drawing with common turpentine varnish,

from those places where there is little shading.

GLASS, SOLUBLE.—Mix ten parts of carbonate of potash, fifteen of quartz (or of sand free from iron of alumina), and one part of charcoal. Fuse together. The mass is soluble in four or five parts of water; and the filtered solution evaporated to dryness yields a transparent glass, permanent in the air.

and the less trouble will there be in removing the interstice, if any,

TABLE

By which to Determine the various Distances of the Movable Points in a Parallel Motion.

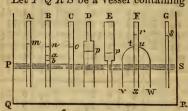
10/2	111	mant so	1.10	2 110		10	بليثيب				
Radius of beams in feet.	Parallel bars in feet.	Length of radius rods in feet and inches.	Radius of beams in feet.	Parallel bars in feet.	Length of radius rods in feet and inches.	Radius of beams in feet.	Parallel bars in feet.	Length of radius rods in feet and inches.	Radius of beams in feet.	Parallel bars in feet.	Length of radius rods in feet and inches.
4 feet.	$\begin{array}{c c} 2 \\ 2\frac{1}{4} \\ 2\frac{1}{2} \\ 2\frac{8}{4} \\ 3 \\ \hline \end{array}$	$ \begin{vmatrix} 2 & 0 \\ 1 & 4\frac{3}{8} \\ 0 & 10\frac{7}{8} \\ 0 & 6\frac{7}{8} \\ 0 & 4 \end{vmatrix} $	6½ feet.	3 3 1 3 1 3 2 3 4 4 4 4 4 1 2		8½ feet.	384 4 44 4 45 5 54 5 54	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	10½ feet.	5 5 5 5 5 5 5 6 6 6	
4½ feet.	2 2\frac{1}{2} 2\frac{1}{2} 2\frac{3}{4} 3 3\frac{1}{4}	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	et.	3 34 152 84	5 4	- 3	5\frac{1}{4} 5\frac{1}{2} 4 4\frac{1}{4}\frac{1}{4} 4\frac{1}{4}\frac{1}{4} 4\frac{1}{4}	6 3 5 3 <del>3</del>	et.	614 612 684 514 5284	6 31
5 feet.	2 2\frac{1}{2} 2\frac{1}{2} 2\frac{8}{4} 3	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	7 feet.	4 4 <sup>1</sup> / <sub>4</sub> 4 <sup>1</sup> / <sub>2</sub> 4 <sup>8</sup> / <sub>4</sub> 5	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9 feet.	484 5 14 5 54 5 584 6	4 6 3 95 3 2½ 2 8½ 2 2¾ 1 10 1 6	11 feet	$ \begin{array}{c} 6 \\ 6\frac{1}{4} \\ 6\frac{1}{2} \\ 6\frac{8}{4} \end{array} $	5 6 4 9½ 4 2 3 7¾ 3 1¾ 2 8⅓ 6 6⅓
5½ feet.	3\frac{1}{4} 3\frac{1}{2} 2\frac{1}{4} 2\frac{1}{2} 3\frac{3}{4} 3\frac{1}{2}	$ \begin{array}{c cccc} 0 & 7\frac{8}{4} \\ \hline 4 & 8\frac{8}{8} \\ 3 & 7\frac{1}{4} \\ 2 & 9 \\ 2 & 1 \end{array} $	7½ feet.	3 1/2 3 3/4 4 4 1/4 4 4 1/2 4 4/4 5	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9½ feet.	$ \begin{array}{r} 4\frac{1}{2} \\ 4\frac{3}{4} \\ 5 \\ 5\frac{1}{4} \\ 5\frac{3}{4} \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	11½ feet.	5½84 6 6¼ 6½84 7 74	$\begin{array}{cccc} 6 & 6\frac{1}{2} \\ 5 & 9 \\ 5 & 0\frac{1}{2} \\ 4 & 5 \\ 3 & 10\frac{1}{8} \\ 3 & 4 \\ 2 & 10\frac{1}{8} \\ 2 & 6 \end{array}$
-	31/4 31/2 33/4 28/4 3 31/4	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	et.	5½ 3½ 3¾ 4	5 9½ 4 9¾	eet.	6 4\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	5 9½ 5 0 4 3½ 3 8½	12 feet.	5\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
6 feet.	31/4 31/2 38/4 4 41/4	$ \begin{array}{cccc} 1 & 9\frac{1}{2} \\ 1 & 4\frac{1}{4} \\ 1 & 0 \\ 0 & 8\frac{1}{2} \end{array} $	8 feet.	41/4 41/2 48/4 5 51/4	4 0 3 3\frac{9}{4} 2 8\frac{9}{8} 2 2\frac{3}{4} 1 9\frac{9}{8} 1 5\frac{1}{4}	10 feet.	5\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12	7 7 1 1 2 2 7 7 7 7 7 7 7 7 7 7 7 7 7 7	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

## CAPILLARY ATTRACTION.

If a number of glass tubes, open at both ends, be immersed, the water will rise to the same height in each tube, so long as the diameter of the tube exceeds the fifteenth of an inch; in all tubes less than this, the water will rise higher in the tube whose diameter is the least. Such tubes, whose diameters are less than one fifteenth of an inch, are called capillary tubes, from the Latin word capillus, signifying a hair.

### Phenomena of Capillary Attraction.

Let PQRS be a vessel containing water to the line PS. The



ter to the line PS. The water will rise in the capillary tubes ABC to the heights mno, which are inversely proportional to their diameter. If B be broken at o, the water will not rise to the top of it, but will stand at b, a little below the top, whatever be the length or

diameter of the tube. And, if the tube be taken out of the water and laid horizontally, the water will recede from the end that was immersed.

If a tube D be composed of two different bores, the water will rise to the height p; and if another tube, E, of the same form and size, be immersed, with its smaller end downwards, the water will rise in it to the same height p.

If the vessel Fvw be plunged into water, and by exhaustion the water is raised to the capillary tube Ftw, it will alterwards ascend to the height r, which is just the same as in a capillary tube G of the same bore as Ftw, and length Fx.

In tubes of the same matter, immersed in the same fluid, the product of the elevations by the diameter is a constant quantity.

In a glass tube, immersed in water, this constant has been found by Muschenbrock, '039; by Weitbrecht, '0428; by Monge, '042; by Atwood '053.

From these numbers, the diameter of a tube may be found, in which the water will rise, by capillary attraction, the height 7 inches.

Diameter = 
$$\frac{.039}{7}$$
 = .0056 inches, nearly.

The constant quantity, here referred to, is called the modulus of capillary attraction.

The following moduli are from Brewster; they were obtained

with a glass tube of '0561 of an inch diameter, by means of an improved apparatus:

A Transaction of the Control of the	1	11	1
Name of Fluid.	Modulus.	Name of Fluid.	Modulus.
no promis de l'Unione -	of the state of		
Company Control Section	11 12		
Water,	0327	Oil of hyssop,	.0195
Very hot water,	.0301	Oil of rosemary,	.0193
Muriatic acid,	.0248	Oil of bergamot,	.0192
Oil of boxwood,	.0240	Oil of amber,	.0192
Oil of cassia,	.0236	Oil of anise seeds,	.0192
Nitrous acid,	.0232	Oil of Barbadoes tar,	.0191
Oil of rapeseed,	0227	Laudanum,	.0191
Castor oil,	.0226	Oil of cloves,	.0187
Nitric acid,	.0222	Oil of turpentine,	.0187
Oil of spermaceti,	.0220	Oil of lemon,	.0187
Oil of almonds,	.0217	Oil of lavender,	.0184
Oil of olives,	0215	Oil of camomile,	.0184
Balsam of Peru,	.0212	Oil of peppermint, .	.0184
Muriate of antimony,	.0209	Oil of sassafras,	.0184
Oil of rhodium,	0205	Highland whisky,	.0184
Oil of pimento,	0203	Brandy,	.0183
Cajeput oil,	.0200	Oil of wormwood,	.0183
Balsam of capivi,	.0200	Oil of dill seed,	.0182
Oil of thyme,	.0199	Oil of ambergris,	.0181
Oil of bricks, distilled	.0199	Oil of juniper,	.0180
from spermaceti oil,		Oil of nutmeg,	.0180
Oil of caraway seeds,	.0198	Alcohol,	.0178
Oil of rue,	.0198	Oil of savine,	.0174
Oil of spearm nt,	.0197	Ether,	.0160
Balsam of sulphur, .	.0196	Oil of wine,	.0153
Oil of sweet fennel	.0195	Sulphurie acid,	.0112
seeds,	0200		

These experiments were made with a tube, carefully cleaned and dried after each experiment. A dry tube will raise the water to a less height than a wet one.

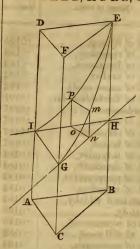
When capillary tubes are plunged into mercury, it falls instead of rising, as is the case with other fluids; and its fall is such, that when it is multiplied by the diameter of the tube, the product is a

constant quantity 015 (Cavendish).

When water is made to pass through a capillary tube of such a bore that the fluid is discharged only by successive drops, the tube, when electrified, will furnish a constant and accelerated stream; and the acceleration is proportional to the smallness of the bore. A jet of warm water will rise to a much greater height than a jet of cold water, though the water in both cases moved through the

same aperture, and was influenced by the same pressure. A syphon which discharges cold water only by drops, will furnish warm water in an uninterrupted stream.

Let CEEB, ADEB, be two plates of glass, having their sides



two praces of glass, having their sides E B joined together with wax, and their surfaces smooth and clean; and also their sides, A D, C F, separated slightly so as to form the angle ABC. If this apparatus be plunged in a vessel, so that IHG represent the water's surface, then the water will rise between the plates of glass, by capillary attraction, to the height IEG, so that the boundary of the water on the planes FEBC, DEBA, will be the hyperbolas GE and IE, having for their asymptotes the surface of the fluid and the line EH.

The height, n m, to which the water will rise, is regulated entirely by the same laws which prevail in the case of the tubes; calling the distance, n o, between the plates the diameter of

the tube.

Hence the height, nm, is equal to the height in a tube whose diameter

is equal to no; and so on for any other point.

All phenomena of capillary attraction are exhibited equally both in air and in vacuo, and they are entirely independent of the thickness of the material composing the tubes and plates.

The elevation and depression is not proportional to the density of the liquid; water stands much higher in a glass tube than

alcohol.

## WOODS.

#### How to Polish Wood.

Take a piece of pumice-stone and water, and pass repeatedly over the work until the rising of the grain is cut down. Then take powdered tripoli and boiled linseed oil, and polish the work to a bright surface.

#### To Gather and Preserve Woods.

Woods should be gathered and exposed in a dry situation, to a heat of from 90° to 150° Fah., until sufficiently dry. The larger kinds are more easily chipped before drying.

#### To Preserve Woodwork.

Take boiled oil and finely powdered charcoal; mix to the consistence of paint, and give the woodwork two or three coats with it. This composition is well adapted for casks, water-spouts, &c.

#### To produce Figures on Wood.

Slack some lime in stale wine. Dip a brush in it, and form on the wood figures to suit your fancy. When dry, rub it well with a rind of pork.

## STEAM-ENGINE.

To Estimate, by means of an Indicator, the Amount of Effective Power produced by a Steam-Engine.

Rule. Multiply the area of the piston in square inches by the average force of the steam in lbs., and by the velocity of the piston in feet per minute; divide the product by 33,000, and  $\frac{7}{10}$  ths of the quotient equal the effective power.

Ex. Suppose an engine with a cylinder of 371 inches diameter, a stroke of 7 feet, and making 17 revolutions per minute, or 238 feet velocity, and the average indicated pressure of the steam 16.73 lbs. per square inch; required the effective power.

Area = 1104.4687 inches  $\times 16.73$  lbs.,  $\times 238$  feet.

 $= \frac{133.26 \times 7}{93.282}$  horse power.

To determine the proper Velocity for the Piston of a Steam-Engine.

Rule. Multiply the logarithm of the nth part of the stroke at which the steam is cut off by 2.3, and to the product of this add 7. Multiply the sum by the distance in feet the piston has travelled when the steam is cut off, and 120 times the square root of the product will equal the proper velocity for the piston in feet per minute.

Ex. Let the steam be cut off in an 8-feet stroke when the piston has travelled 1th of the length; required its proper velocity.

Logarithm of 4 = 0.60206Multiplied by

1.384738

To which add

2.084738

 $\sqrt{4.169476} = 2.04 \times 120 = 245$  feet, velocity per minute.

TABLE
Of Approximate Velocities for the Pistons of Steam-Engines.

	1-14-1-6-4	Number of				
1111000	per minute.	revolutions per minute.	Length of stroke in feet.	Velocity in feet per minute.	Number of revolutions per minute	
2	160	40	11/2	186	62	
$\frac{2}{2\frac{1}{2}}$	1774	351	2	200	50	
3	192	32		2121	421	
31/2	203	29	$\frac{2\frac{1}{2}}{2\frac{3}{4}}$	2171	391	
4	214	268	3	222	37	
41	2201	$24\frac{1}{2}$	31	231	33	
$\frac{4\frac{1}{2}}{5}$	230	23	4	236	291	
51/2	. 2361	$21\frac{1}{2}$	$4\frac{1}{2}$ $5$	243	27	
6	240	20	5	$247\frac{1}{2}$	243	
7	245	$17\frac{1}{2}$	$5\frac{1}{2}$	253	23	
8	256	16	6	264	22	

#### Of the Parallel Motion in a Steam-Engine.

When the power from the piston is communicated by means of a beam or lever moving upon an axis, the parallel motion becomes a very important portion of the machine; for then it forms the link of connexion, and by its properties renders the action of alternate circular motion, and reciprocating vertical motion, mutually agreeable, thereby properly insuring to the piston-rod a truly direct line to that of the cylinder; but to effect this, the greatest degree of exactitude of the various parts is required, otherwise extra friction is created, and the effective power of the engine proportionately diminished.

# THE PROPERTIES AND MISCELLANEOUS EFFECTS OF HEAT.

Linear Expansion of Metals from 32° to 212°. - FARADAY.

		J	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	J. 0 01 10 1		1011	
part in			322	Gold,	1 part in	19.79	. 682
"			351	Bismuth,	46		. 719
66			403	Iron,	- "	1.11	. 812
46			500	Antimony,	66		. 923
66			524	Palladium,	66		. 1000
66			581	Platinum,	46		. 1100
66	•		584	Flint Glass,	"		. 1248
	part in	part in	part in	part in 322   " 351   " 403   " 500   " 524   " 581	part in 322   Gold, " 351   Bismuth, " 403   Iron, " 500   Antimony, " 524   Palladium, " 581   Platinum,	part in 322   Gold, 1 part in Bismuth, "Bismuth, "	" 351 Bismuth, "

TABLE

Of the Expansion of Water by Heat.—By Dalton.

Temperature.	Expansion.	Temperature.	Expansion
12° Fahrenheit.	100236	122° Fahrenheit.	101116
22	100090	132	101367
32	100022	142	101638
42	100000	152	101934
52	100021	162	102245
62	100083	172	102575
72	100180	182	102916
82	100312	192	103265
92	100477	202	103634
102	100672	212	104012
112	100880		-

#### TABLE

Of the Heating Power of various Combustible Substances, exhibiting the utmost quantity of Water evaporated by the given Weights, and the smallest quantity of Air capable of producing total Combustion. Dr. Ure.

Species of Combustible.	Pounds of water which a pound can heat from 0° to 212°.		Weight of at- mospheric air at 320 to burn 1 pound.
D., C., ()., J.,	95.00	0.00	Smallest quantity.
Perfectly dry wood,	35.00	6.36	5.96
Wood in its ordinary state,	26.00	4.72	4.47
Wood charcoal,	73.00	13.27	11.46
Pit coal,	60.00	10.90	9.26
Coke,	65.00	11.81	11.46
Turf,	30.00	5.45	4.60
Turf charcoal,	64.00	11.63	9.86
Carburetted hydrogen gas, Oil,	76.00	13.81	14.58
Wax,	78.00	14.18	15.00
Tallow,	52.60	9.56	11.60

## TABLE

Of boiling points of water holding various proportions of salt in solution.

ATTOM Andonés v	Parts of Salt.	Degrees of Fahrenheit.	Degrees of Reaumer.	Degrees of Centigrade.
Saturated solution	36·37 33·34	226·6 224·9	86·2 85·7	107·8 107·2
	30.30	223.7	85·2 84·7	106·5 105 8
66 66	24·25 21·22	221·4 220·2	84·1 83·6	105·2 104·6
66 66	18·18 15·15 12·12	219 217·9	83 82.6	103·9 103·3
66 66	9·09 6 06	216·7 215·5 214·4	82·1 81·6 81·1	102·6 102 101·3
Sea-water	3.03	213·2 212	80·5 80	100·7 100
the second second second			N Comment	OCCUP

## Expansion of Liquids in Volume from 32° to 212° Fahrenheit.

1000	parts of	water	become	1046
44	- "	oil	"	1080
66	"	mercury	"	1018
66	66	spirits of win	e "	1110
66	66	air	46	1373

Of the Linear Dilatation of Solids by Heat. Dimensions which a bar takes at 212°, whose length at 32° is 1 000000.

a our ranco	00 212 , 000000	congue at 02 to 10	000001
Cast iron,	1.00111111	Cast brass,	. 1.0018750
Steel (rod),	1.00114470	Silver,	. 1.0018900
Steel, not tem- )	1.00107875	Tin,	
pered,	1.00101919	Lead,	. 1.00284836
Ditto, temper-	1.00136900	Zinc,	. 1.00294200
ed yellow, . 5	1 00130800	Glass from 32°)	1.00086130
Ditto, at a high-	1.00123956	to 212°,	1.00090130
er rate,	1 00125550	Glass from 212°)	1.00091827
Iron,	1.00118203	to 392°,	1 00091021
Soft iron, forged, .	1.00122045	Glass from 392°)	1.00101114
Gold,	1 00150000	to 572°, 5	1 00101114
Copper,	1.00191000		

Of	Canacities	of Rodies	for	Heat	referred	to	Water	as ti	he Standard.
OI	Cupulcuco	J Douces	101	11000	10/01/00	00	" acci	WO 11	ec Dianaui u.

Of Capacitics of Boates	0. 11000	rejection to the most no time som	react to.
Water,	1.0000	Iron,	·1300
Olive oil,	7100	Hardened steel,	1230
		Steel softened by fire,	
Oil of turpentine,	4720	Soft bar iron,	·1190
Quieksilver,	0330	Brass,	1160
		Copper,	·1140
Pit coal,		Zine,	
Chalk,	2700	Ashes of charcoal,	.0909
Sea salt,		Silver,	
Sulphur,		Tin,	.0704
Ashes of cinders,	. 1855	White lead,	.0670
		Gold,	
Ashes of elm wood,	. 1402	Lead,	.0420

TABLE

Of the Expansion of Atmospheric Air by Heat.

Degrees of Fahrenheit.			Bulk.	Degrees of Fahrenheit.	Bulk.		
32°	1000	65°	1077	100°	1152		
35'	1007	70	1089	120	1194		
40	1021	75	1099	140	1285		
45	1032	80	1110	160	1275		
50'	1043	85	1121	180	1815		
55	1055	90	1132	200	1364		
60	1066	95	1142	212	1376		

The pressure or gravity of the atmosphere, being equal to a column of water 34 feet in height, is the means or principle on which rests the utility of the common pump, also of the syphon, and all other such hydraulic applications. In the pump, the internal pressure on the surface of the liquid is removed by the action of the bucket; and as by degrees the density becomes lessened, so the water rises by the external pressure to the above-named height; and at such height it will remain, unless by some derangement of construction taking place, the atmospheric fluid is allowed to enter and displace the liquid column. But observe, if the temperature of the water or other liquid be so elevated that steam or vapor arise through it, then, according to the vapor's accumulation of density, may the action of the pump be partially or wholly destroyed; and the only means of evasion in such cases is to place the working bucket beneath the surface of the liquid which is required to be raised.

TABLE Of the Degrees of the three Thermometrical Scales,
Above Boiling Point of Water.

(76E T	1	1	h	,	Loove	DOUITIE	TOIL	T OI	vater.	-	1 ,	-	181	110
Fahren- heit.	Centi- grade.	Reau- mur.	Fahren- heit.	Centi- grade.	Reau- mur.	Fahren- heit.	Centi- grade.	Reau- mur.	Fahren- heit.	Centi- grade.	Reau- mur.	Fahren- heit.	Centi- grade.	Reau-
392	200	<del></del>	356	180	 144	320	160	128	284	<del></del> 140	112	248	120	96
391	199		355	179	130	319	159		283	139		247	119	1) X
390. 389.		159	354 353		143	318 317		127	282 281		111	246 245		95
388	198	11	352	178		316	158		280	138		244	118	La Co
387	197	158	351	177	142	315	157	126	279	137	110	243	117	94
386	197	157	350		141	314	191	125	278	10.	109	242	1 1 100	93
385	196	10.	349	176	141	313 312	156	120	277	136	103	241	116	00
384 383	195	156	348 347	175	140	311	155	124	276 275	135	108	240 239	115	92
382	130	190	346	110	140	310	199	124	274	199	100	238	110	94
381	194	155	345	174	139	309	154	123	273	134	107	237	114	91
380	193	199	344	173	199	308	153	125	272	133	107	236	113	91
379 378	100	154	343	1.0	138	307 306	100	122	271 270	100	106	235 234	110	90
377	192		341	172		305	152		269	132		233	112	
376	191	153	340	171	137	304	151	121	268	131	105	232	111	89
375	191		339	1.1		303	191	- 01	267	191		231	68	
374	190	152	338	170	136	302	150	120	266	130	104	230	110	88
$\frac{373}{372}$	100		337 336	169		301	149		265 264	129		229 228	109	
371	189	151	335	100	135	299	110	119	263	120	103	227	100	87
370	188	150	334	168	104	298	148	110	262	128	7.00	226	108	0.0
369	187	150	333	167	134	297	147	118	261	127	102	225	107	86
368	101	149	332 331	101	133	$\frac{296}{295}$	141	117	260	121	101	224	101	85
367 366	186		330	166		293	146	100	259 258	126	-01	$\begin{array}{c} 223 \\ 222 \end{array}$	106	
365	185	148	329	165	132	293	145	116	257	125	100	221	105	84
364	100	2.0	328	100	102	292	110	220	256	220	200	220	100	/ 41
363	184	147	327	164	131	291	144	115	255	124	99	219	104	83
362 361	1.00	171	326 325	1.00	101	290 289	1.40	110	254 253	100	00	218 217	001	09
360	183	146	324	163	130	288	143	114	252	123	98	216	103	82
359	182		323	162	100	287	142		251	122	3	215	102	1/100
358		145	322	1	129	286		113	250		97	214	and i	81
357	181		321	161	- 1	285	141	1 1	249	121	100	213	101	16.
	1	1	1	-	1		1	1	-	10	5 0	-	11 -	15

To convert the Degrees in the three Scales into each other.

To convert Centigrade or Reaumur's into Fohrenheit's Degrees.—Multiply the number of degrees by 9, divide the product by 5 for Centigrade, or by 4 for Reaumur's; add 32 to the quotient, and the sum will be degrees of Fahrenheit.

To convert Fahrenheit's into Centigrade or Reaumur's Degrees.—Subtract 32 from the number of degrees, and divide the remainder by 9; multiply the quotient by 5 for Centigrade, or 4 for Reaumur's; the products will be the required degrees respectively.

1		DEG	REES		1112						DOA	LIEG.		400
Com	para	tive	Table	of	the _	Degree	es of	the	three	Ther	mon	etrico	al Sce	ales.
Fahr't	Cent.	Rea.	Fahr't	Cent.	Ren.	Fahr't	Cent.	Rea.	Fahr't	Cent.	Rea.	Fabr't	Cent.	Rea.
212	100	80	167	75	60	122	50	40	77	25	20	32	0	0
211			166	-	-	121			76			31		
210	99	79	165	74	59	120	49	39	75	24	19	30	- 1	- 1
209	98		164	73		119	48		74	23	-01	29	- 2	
208 207	.50	78	163		58	118	. 0	38	73 72		18	28 27		- 2
206	97		162 161	72		117	47		71	22		26	- 3	
205	96	77	160	71	57	115	46	37	70	21	17	25	- 4	- 3
204	90		159	11		114	40		69	21		24	-	
203	95	76	158	70	56	113	45	36	68	20	16	23	- 5	- 4
202	600		157		7-0	112	1170	111	67			22		
201	94	75	156	69	55	111	44	35	66	19	15	21	- 6	- 5
200	93		155	68	2.7	110	43		65	18		20	- 7	- 5
199	00	74	154	00	54	109		34	64	10	14	19	1,17	- 6
198 197	92		153	67	17.1	108	42		63	17	()	18	- 8	18
196	TO	73	152		53	107	16.5	33	62	120	13	17 16	-	- 7
195	91	10	150	66	407.3	105	41	90	61	16	10	15	- 9	
194	90	72	149	65	52	104	40	32	59	15	12	14	-10-	- 8
193	00		148	00	02	103	10	94	58	10	12	13	-10	- 0
192	89	71	147	64	51	102	39	31	57	14	11		-11	37
191	88		146		01	101		91	56	10	11	11	10	- 9
190	88	70	145	63	50	100	, 38	20	55	13	10	10	-12	10
189	87	10	144	62	30	99	37	30	54	12	10	9	-13	-10
188	1000	CO	143		49	98	788 V	00	53			8	able	-11
187 186	86	69	142	61	49	97	36	29	52	11	9	7	-14	70
185	0.5	00	141	20	100	96	0.5	00	51 50	10		6	77	3474
184	85	68	140	60	48	94	35	28	49	10	8	5 4	-15	12
183	84	67	138	59	47	93	34	27	48	9	-		-16	151
182	5-01	0.1	137		47	92		21	47		7	2	1	-13
181	83	0.0	136	58	988	91	33	0.0	46	8		1	-17	17
180	82	66	135	57	46	90	32	26	45	7	6	0	-18	-14
179	-	0-	134	31	7.6.4	89	52		44			- 1		15
178	81	65	133	56	45	88	31	25	43	6	5	- 2	-19	-15
177	00	2.1	132		126	87	0.0		42		-	- 3	=X ()	
176 175	80	64	131	55	44	86	30	24	41	5	4	- 4	-20	-16
174	79	00	130 129	54	6440	85 84	29		40 39	4	10	- 5 - 6	-21	100
173		63	129	04	43	83	20	23	38	T	-3	- 7		-17
172	78	00	127	53	6.14	82	28		37	3	1	- 8	-22	93.
171	77	62	126		42	81	1	22	36	2	2	0	1	-18
170	300		125	52	100	80	27		35	2	1	-10	-23	0
169	76	61	124	51	41	79	26	21	34	1	1	-11	-24	-19
168	10	1	123	0.	5005	78			33	1		-12	-	7
YES	20		LUQ BU		1910		400		1000	0.6		-13	-25 -	-20

TABLE of the Weight of Substances of Construction, showing the weight of a cubic inch, and a cubic foot, in ounces and pounds avoirdupois, and also the number of cubic inches in one pound, of the substances most used in construction.

Names of Bodies.	Weight of a cubic foot.		Weight of a cubic inch.		Number of
rantes of bodies.	in oz.	in lbs.	in oz.	in lbs.	cubic inches in a pound.
Copper, cast, .	8788	549.25	5.086	3178	3.146
Copper, sheet, .	8915	557.18	5.159	.3225	3.103
Brass, cast,	8396	524.75	4.852	3037	3.293
Iron, cast,	7271	445.43	4.203	.263	3.802
Iron, bar,	7631	476.93	4.410	.276	3.623
Lead,	11344	709.00	6.456	4103	2.437
Steel, soft,	7833	489.56	4.527	.2833	3.230
Steel, hard,	7816	488.50	4.517	2827	3.537
Zinc, cast,	7190	449.37	4.156	.26	3.845
Tin, cast,	7292	455.75	4.215	.2636	3.790
Bismuth,	9880	619.50	5.710	3585	2.789
Gun-metal,	8784	549.00	5.0075	3177	3.147
Sand,	1520	95.00	.8787	.055	18.190
Coal,	1250	78.12	.7225	.0452	22.120
Brick,	2000	125.00	1.156	.0723	13.824
Stone, paving, .	2416	151.00	1.396	.0873	11.443
Slate,	2672	167.00	1.544	.0967	10.347
Marble,	2742	171.37	1.585	.0991	10.083
White lead,	3160	197.50	1.826	.1143	8.750
Glass,	2880	180.00	1.664	.1042	9.600
Tallow,	945	59.06	.5462	*0087	29.258
Cork,	240	15.00	.138	.0197	115.200
Larch,	544	34.00	315	.0201	50.823
Elm,	556	34.75	321	.0201	49.726
Pine, pitch,	660	41.25	382	.024	41.890
Beech,	696	43.50	403	0252	39.724
Teak,	745	46.56	·431	.027	37.113
Ash,	760	47.50	440	0275	36.370
Mahogany,	852	53.25	493	:0308	32.449
Oak,	970	60.62	561	.0351	28.505
Oil of turpentine,	870	54.37	.503	0315	31.771
Olive oil,	915	57.18	•529	.0331	30.220
Linseed oil,	932	58.25	.539	.0337	29.655
Spirits, proof, .	927	57.93	.536	03352	29.288
Water, distilled,	1000	60.50	.578	03617	27.648
" sea,	1028	64.25	.594	0372	26.894
Tar,	1015	63:43	.587	0367	27.242
Vinegar,	1026	64.12	.593	037	26.949
Mercury,	13568	848.00	7.851	•4908	2.037

Conducting	Power	of M	<b>I</b> aterials	used	in the	Construction	of Houses.

		Mr. Hutchinson.	
Slate,	. 100	Oak wood,	. 33.66
Keene's cement,	. 19.01	Asphalt,	. 45.19
Plaster and sand,	. 18.70	Chalk (soft),	• 56.38
Plaster of Paris,	. 20.26	Stock brick,	. 60.14
Roman cement,		Bathstone,	. 61.08
Beech wood,		Fire brick,	
Lath and plaster,	. 25.55	Lead,	. 521.34
Fir wood,	. 27.60	400	

Air and gases are very imperfect conductors. Heat appears to be propagated through them almost entirely by conveyance, the heated portions of air becoming lighter, and diffusing the heat through the mass in their ascent as in liquids. Hence, in heating a room with hot air, the hot air should be introduced at the lowest part. The advantage of double windows for warmth depends, in a great measure, on the sheet of air confined between them through which heat is very slowly transmitted.

Capacity of Bodies for Transmitting Heat.

The capacity which bodies possess of transmitting heat, does not depend upon their transparency; or bodies are not all transparent to heat in the same proportion that they are transparent to light. The following plates of an equal thickness of 1031 inches allowed very different proportions of heat to pass through them.

Of 100 rays transmitted from an Argand oil lamp there were:

of 100 rays transmitted no	ша,	n Argand on lamp there were:	
Rock salt,	92	Emerald, 29	9
Mirror glass,	62	Gypsum, 20	0
Rock crystal,	62	Fluor spar, 1	5
		Citric acid, 1	
Rock crystal, smoky & brown	57	Rochelle salt, 1	$^2$
Carbonate of lead,	52	Alum, 19	2
Sulphate of barytes,	33.	Sulphate of copper,	0
		THE RESERVE OF THE PARTY OF THE	

## SOLDERS.

For Lead.—Melt one part of block tin, and, when in a state of fusion, add 2 parts of lead. Resin should be used with this solder.

For Tin.—Pewter, 4 parts; tin, 1; bismuth, 1. Melt them

For In.—Pewter, 4 parts; tin, 1; bismuth, 1. Melt them together and run them into slips. Resin is also used with this solder.

For Gold.—Pure gold, 12 parts; silver, 2; copper, 4.

For Brass.—Brass, 2 parts; zinc, 1.

For Iron.—Good tough brass, with a small quantity of borax.

For Pewter.—Bismuth, 2 parts; lead, 1; tin, 2.

For Copper.—Copper, 2 parts; zinc, 1.

For Silver.—Silver, 5 parts; brass, 6; zinc, 2.

Hard Solder.—Copper, 2 parts; zine, 1.

Soft Solder .- Tin, 2 parts; lead, 1 part.

TABLE

Of proportions for making Shafting with Half-lap Couplings, showing length of Neck and sizes of Coupling-box. (Manchester Rules.)

Diameter of Neck.	Length of Neck.	Diameter of Coupling.	Length of Lap.	Length of Box.	Diameter of Box.
Inches.	Inches.	Inches.	Inches.	Inches.	Inches.
2	4	31/4	$2\frac{1}{4}$	5 <del>1</del>	$5\frac{1}{2}$
21/4	$\frac{1}{4\frac{1}{2}}$	31/2	$2\frac{4}{2}$	6	6
21	5	4	3	61	63
$2\frac{1}{2}$ $2\frac{3}{4}$	$5\frac{1}{2}$	$rac{4rac{1}{2}}{4rac{8}{4}}$	34 5½ 3¾	7	71
3	6	$4\frac{8}{4}$	31/2	$7\frac{1}{2}$	$7\frac{1}{2}$ $7\frac{2}{4}$
31/4	61	5	33	8	81
3 3 3 3 3	$6\frac{1}{4}$ $6\frac{1}{2}$ 7	and awalence		4	11 / 10 / 10
$\frac{4}{4\frac{1}{2}}$ 5	tra Table	6	4	$8\frac{1}{2}$	$9\frac{1}{2}$
$4\frac{1}{2}$	$7\frac{1}{2}$	$6\frac{1}{2}$	$4\frac{1}{2}$	9	$10\frac{1}{2}$
5	8	71	5	$9\frac{1}{2}$	117
5 ½	81	$8\frac{1}{2}$	$5\frac{1}{2}$	11	$12\frac{1}{4}$
6	9	9	6	12	$13\frac{1}{2}$
$\frac{6\frac{1}{2}}{7}$	$9\frac{1}{2}$	98	$6\frac{1}{2}$	13	144
$7\frac{1}{2}$	10 <del>1</del> 11 <del>1</del>	$10\frac{1}{2}$	71/2	14	16
8	12	12	8	$\frac{-}{16\frac{1}{2}}$	18
8 <del>1</del>	$12\frac{12}{12\frac{1}{2}}$	121	8 <del>1</del>	$10\frac{1}{2}$	19
92	$13\frac{1}{3}$	13	9	18	20
91	14	-	_		
10	141	14	10	181	22
11	15.	16	11	20	24
12	. 16	171 .	12	21	26

\* Gradations of Temperature.

The following are interesting facts in the range of temperature:

166° Greatest artificial cold. (Faraday.)

150 Liquid nitrous oxide freezes.
122 Liquid sulphuretted hydrogen

122 Liquid sulphuretted hydrogen freezes. 105 Liquid sulphurous acid freezes.

91 Greatest artificial cold measured by Walker.

56 Greatest natural cold observed by a "verified" thermometer. (Sabine.)

70 Greatest natural cold observed at Fort Reliance by Back. (Doubtful.)

58 Estimated temperature of planetary space. (Fourier.)

47 Sulphuric ether freezes.

39 Mercury freezes.

Below Zero (Fah.)

30 Liquid cyanogen freezes. (Faraday.)

13 Mean temperature at the Pole. (Arago.)

11 A mixture of two parts alcohol and one part water freezes.
7 A mixture of equal parts alcohol and water freezes.

20° Strong wine freezes. Vinegar freezes. 28 30 Milk freezes. 32 Ice melts. Mean temperature at Edinburgh. 41 Mean temperature of London. 50.7 60 Mean temperature at Rome. 81.5 Mean temperature at the equator. Heat of the human blood. 98 Ether boils 98 100 Phosphorus melts. 173 Alcohol boils. Highest natural temperature observed of a hot wind 117 in Upper Egypt, (Burckhardt.) 133 Wood-spirit boils. 149 Spermaceti melts. 151.34 Beeswax melts. 212 Water boils. 226 Sulphur melts. 2.12 Nitric acid boils. A compound of equal parts of tin and bismuth melts. 283 442 The surface of polished steel acquires a pale straw 460 color. 476 Bismuth melts. 554 Phosphorus boils. 560 Oil of turpentine boils. 580 The surface of polished steel acquires a uniform deep blue. Sulphuric acid boils. (Dalton.) 590 Lead melts. 594 600 Linseed oil boils. Lowest ignition of iron in the dark. 635 Mercury boils.

Zine melts.

Iron bright red in the dark. 662 700 752 810 Antimony melts. Iron red hot in the twilight. 884 1077 Red heat fully visible in the daylight. 1141 Heat of a common fire. (Daniell.) 1869 Brass melts. Silver melts. 1873 1996 Copper melts. 2016 Gold melts. Steel melts. 2500 Cast-iron melts. 2786

3080 Platinum melts.

The line of perpetual congelation has a variable altitude in different climates.

At the equator it is 14760 feet. At the Alps "8120 " In Iceland "3084 "

At the polar regions ice is perpetually observed at the surface of the earth.

## PROPERTIES OF NUMBERS.

1. A Prime Number is that which can only be measured by 1 or unity.

2. A Composite Number is that which can be measured (or divided

without a remainder) by some number greater than unity.

3. A Perfect Number is that which is equal to the sum of all its divisors, or aliquot parts: thus  $6 = \frac{6}{9} + \frac{6}{7} + \frac{6}{6}$ .

4. If an odd number divides an even number, it will also divide

the half of it.

5. If the last digit of any number be divisible by 2, the whole number is divisible by 2.

6. If the two last digits be divisible by 4, the whole number is

divisible by 4.

7. If the three last digits be divisible by 8, the whole number is divisible by 8.

8. If a number terminate with 5, it is divisible by 5; and if it

terminate with 0, it is divisible by either 10 or 5.

9. If the sum of the digits constituting any number be divisible by 3 or 9, the whole is divisible by 3 or 9; and if also the last digit is even, the whole number is divisible by 18.

10. If the sum of the digits of any number be divisible by 6, and

the right hand digit by 2, the whole is divisible by 6.

11. If the sum of the 1st, 3d, 5th, &c., digits of any number be equal to that of the 2d, 4th, 6th, &c., that number is divisible by 11.

Thus 327943 contains 11 = 29813 times exactly.

12. If a square number be either multiplied or divided by a square, the product or quotient is a square; and conversely, if a square number be either multiplied or divided by a number that is not a square, the product or quotient is not a square.

13. The product arising from two different prime numbers cannot

be a square number.

14. The product of no two different numbers prime to each other (that is, 1 being the common measure) can make a square, unless each of those numbers be a square.

15. The square root of an integral number, that is not a complete square, can neither be expressed by an integer nor by any rational

fraction; so with the cube root of an integer.

16. Every prime number greater than *two*, is made up of 4 times some number, +1 or -1; that is, of one of the forms 4n + 1, or 4n - 1.

17. Any prime number greater than 3, divided by 6, will leave a remainder of 1 or 5: that is, every number greater than 3, is one of the forms 6n + 1, or 6n - 1.

18. The number of prime numbers is infinite.

19. A square number cannot terminate with an odd number of cyphers.

20. If a square number terminate with 4, the last figure but one

will be an even number.

21. If a square number terminate with 5, it will terminate with 25.
22. No square number can terminate with two equal digits, except two cyphers, or two fours.

23. No number whose last digit is 2, 3, 7, or 8, is a square number.
24. If a cube number be divisible by 7, it is also divisible by the

cube of 7.

25. The difference between any integral cube and its root is always divisible by 6.

26. Neither the sum nor the difference of two cubes can be a

cube.

27. A cube number may end with any of the natural numbers.
28. All the powers of any number that end with 6, will terminate with 6; so with the numeral 5.

TABLE

Of the first Nine Powers of the first Nine Numbers.

lst	2d	3d .	4th	5th	6th	7th	8th	9th
1	1	1	1	- 1	1	1.	1	1
2	4	.8	16	- 32	64	128	256	512
3	9	27	81	243	729	2187	6561	19683
4	16	64	256	1024	4096	16384	65536	262144
5	25	125	625	3125	15625	78125	390625	1953125
6	36	216	1296	7776	46656	279936	1679616	10077696
7	49	343	2401	16807	117649	823543	5764801	40353607
8	64	512	4096	32768	262144	2097152	16777216	134217728
9	81	729	6561	59049	531441	4782969	43046721	387420489

## TABLE Of Useful Numbers. . = 3.1415927 . 0.4971499 . 0.7071068 . 1.1447299 . 0.3183099 . 2.2214415 9.8696044 . 0.4501582 . 0.1013212 . 1.7724538 . 0.5641896 = 2.71828180.4342945 Modulus of common logarithms . . 434294482 Log. of ditto . . . . . 9.6377843 32.19084 5.67363 1.5077222 Log. q. Inches in a French mêtre . . . . . . 39.37079 Loz. of ditto . . . . . . . . . . 1.5951741 3.2808992 Log. of ditto . . . . . . . 0.5159929 10 764297 0.024711 2.20548 0.3435031 0.2200967 12.7 0.5235988 0.017453293 0.000290888 Arc of 1" to rad. 1 0.000004848 Degrees in an arc whose length is 1 57.295780°

Grains in 1 lb. ditto	. 7000
Grains in a cubic inch of distilled water, Bar. 3	0 959:459
Cubic inches in an ounce of water	1.79000
in., Th. 62°	077.076
Cubic inches in the imperial ganon	. 217210
reet in a geographical fine	. 6075'6
Feet in a geographical mile Log. of ditto Feet in a statute mile	3.7835892
reet in a statute mile	. 5280
Log. of ditto	3.7226339
Length of seconds' pendulum in inches	. 39.19084
Length of seconds' pendulum in inches Cubic inches in 1 cwt. of cast iron  " Bar iron  " Cast brass  " Cast copper	. 430.25
" Bar iron	. 397.60
" Cast brass	. 368.88
" Cast copper	. 352.41
" Cast lead	. 272.80
" Cast lead Cubic feet in 1 ton of paving stone	. 14.835
Granite.	. 13.505
" Marble	. 13.070
" " Chalk	. 12.874
" Limestone	. 11.273
Elm .	. 64.460
" Honduras mahogany	. 64.000
" " Honduras mahogany	. 51.650
" Beech	. 51.494
" Riga fir	47.762
" Ash and Dantzic oak	47.158
" " Spanish mahogany	42.066
" " English oak	. 36.205
To find the weight in lbs. of 1 foot of common	n
rope, multiply the square of its circumference	Α
in inches by	044
In Inches by	to .046
Ditto for a cable	•097

TABLE
Surface of Boilers' Tubes of Different Lengths and Diameters.

Diameter.	Length.	Surface.	Diameter.	Length.	Surface.		
In. 2½ "	Ft. in. 5 0	Sq. ft. 3.27	In.	Ft. in. 6 6	Sq. ft. 5·1		
	5 3 5 6	3·42 3·6	"	6 8 7 0	5·2 5·5		
3	5 9 6 0 6 0	3·75 3·9 4·7	"	7 6 8 0 8 6	5·89 6·28 6·67		
"	6 3	4.9	- 11-90	0 0 0	0.01		

## RECIPES FOR MAKING DIFFERENT KINDS OF GLASS.

1. Bottle Glass.—1. Dry glauber salts, 11 pounds; soaper salts, 12 pounds; half a bushel of waste soap ashes; sand, 56 pounds; glass skimmings, 22 pounds; green broken glass, 1 cwt.; basalt, 25

pounds. This mixture affords a dark green glass.

2. Yellow or white sand, 100 parts; kelp, 30 to 40; lixiviated wood ashes, from 160 to 170 parts; fresh wood ashes, 30 to 40 parts: potter's clay, 80 to 100 parts; cullet, or broken glass, 100. If basalt be used, the proportion of kelp may be diminished.

2. Green Window, or Broad Glass.—Dry glauber salts, 11 pounds: soaper salts, 10 pounds; half a bushel of lixiviated soap waste; 50 pounds of sand; 22 pounds of glass pot skimmings; 1 cwt. of

broken green glass.

3. Crown Glass.—300 parts of fine sand; 200 of good soda ash; 33 of lime; from 250 to 300 of broken glass; 60 of white sand; 30 of purified potash; 15 of saltpetre; (1 of borax;) 1 of arsenious acid.

4. Nearly White Table Glass.—1. 20 pounds of potashes; 11 pounds of dry glauber salts; 16 of soaper salt; 55 of sand; 140 of cullet

of the same kind.

2. 100 parts of sand; 235 of kelp; 60 of wood ashes;  $1\frac{1}{3}$  of manganese; 100 of broken glass.

5. White Table Glass. - 1. 40 pounds of potashes; 11 of chalk;

76 of sand; 1 of manganese; 95 of white cullet.

2. 50 of purified potashes; 100 of sand; 20 of chalk, and 2 of saltpetre.

6. Crystal Glass.—1. 60 parts of purified potashes; 120 of sand; 24 of chalk; 2 of saltpetre; 2 of arsenious acid; 1 of manga-

2. Purified pearlashes, 70 parts; white sand, 120; saltpetre, 10;

1 of arsenious acid; 1 of manganese.

3. 67 of sand: 23 of purified pearlashes; 10 of sifted slaked lime; 1/4 of manganese; 5 to 8 of red lead.

4. 120 of white sand; 50 of red lead; 40 of purified pearlash;

20 of saltpetre; & of manganese.

5. 120 of white sand; 40 of pearlash purified; 35 of red lead; 13 of saltpetre;  $\frac{1}{10}$  of manganese.

6. 30 of the finest sand; 20 of red lead; 8 of pearlash purified; 2 of saltpetre; a little arsenious acid and manganese.

7. 100 of sand; 45 of red lead; 35 of purified pearlashes; \frac{1}{7} of

manganese; 1 of arsenious acid.

7. Plate Glass —1. Very white sand, 300 parts; dry purified soda, 100 parts; carbonate of lime, 43 parts; manganese, 1; cullet, 300.

2. Finest sand, 720 parts; purified soda, 450; quicklime, 80;

saltpetre, 25; cullet, 425.

A little borax has also been prescribed; much of it communicates an exfoliating property to glass.

TABLE

Of Prime Numbers to 5000.

				Inid	100	
2	197	461	751	1051	1381	1697
3	199	463	757	1061	1399	1699
5	211	467	761	1063	1409	1709
7	223	479	769	1069	1423	1721
11	227	487	773	1087	1427	1723
13	229	491	787	1091	1429	1733
17	233	499	797	1093	1433	1741
19	239	503	809	1097	1439	1747
23	241	509	811	1103	1447	1753
29	251	521	821	1109	1451	1759
31	257	523	823	1117	1453	1777
37	263	541	827	1123	1459	1783
41	269	547	829	1123	1471	1787
43	271	557			1481	1789
47	277	563	839	1151		
53	281		853	1153	1483	1801
59	283	569	857	1163	1487	1811
61	283	571	859	1171	1489	1823
		577	863	1181	1493	1831
67	307	587	877	1187	1499	1847
71	311	593	881	1193	1511	1861
73	313	599	883	1201	1523	1867
79	317	601	887	1213	1531	1871
83	331	607	907	1217	1543	1873
89	337	613	911	1223	1549	1877
97	347	617	919	1229	1553	1879
101	349	619	929	1231	1559	1889
103	353	631	937	1237	1567	1901
107	359	641	941	1249	1571	1907
109	367	643	947	1259	1579	1913
113	373	647	953	1277	1583	1931
127	379	653	967	1279	1597	1933
131	383	659	971	1283	1601	1949
137	389	661	977	1289	1607	1951
139	397	673	983	1291	1609	1973
149	401	677	991	1297	1613	1979
151	409	683	997	1301	1619	1987
157	419	691	1009	1303	1621	1993
163	421	701	1013	1307	1627	1997
167	431	709	1019	1319	1637	1999
173	433	719	1021	1321	1657	2003
179	439	727	1031	1327	1663	2011
181	443	733	1033	1361	1667	2017
191	449	739	1039	1367	1669	2027
193	457	743	1049	1373	1693	2029
	101	170	1049	1919	1050	2029
	1	1		!		

0000	0000	2500	0000			1000
2039	2399	2789	3203	3581	3967	4371
2053	2411	2791	3209	3583	3989	4391
2063	2417	2797	3217	3593	4001	4397
2069	2423	2801	3221	3607	4003	4409
2081	2437	2803	3229	3613	4007	4421
2083	2441	2819	3251	3617	4013	4423
2087	2447	2833	3253	3623	4019	4441
2089	2459	2837	3257	3631	4021	4447
2099	2467	2843	3259	3637	4027	4451
2111	2473	2851	3271	3643	4049	4457
2113	2477	2857	3299	3659	4051	4463
2129	2503	2861	3301	3671	4057	4481
2131	2521	2879	3307	3673	4073	4483
2137	2531	2887	3313	3677	4079	4493
2141	2539	2897	3319	3691	4091	4507
2143	2543	2903	3323	3697	4093	4513
2153	2549	2909	3329	3701	4099	4517
2161	2551	2917	3331	3709	4111	4519
2179	2557	2927	3343	3719	4127	4523
2203	2579	2939	3347	3727	4129	4547
2207	2591	2953	3359	3733	4133	4549
2213	2593	2957	3361	3739	4139	4561
2221	2609	2963	3371	3761	4153	4567
2237	2617	2969	3373	3767	4157	4583
2239	2621	2971	3389	3769	4159	4591
2243	2633	2999	3391	3779	4177	4597
2251	2647	3001	3407	3793	4201	4603
2267	2657	3011	3413	3797	4211	4621
2269	2659	3019	3433	3803	4217	4637
2273	2663	3023	3449	3821	4219	4639
2281	2671	3037	3457	3823	4229	4643
2287	2677	3041	3461	3833	4231	4649
2293	2683	3049	3463	3847	4241	4651
2297	2687	3061	3467	3851	4243	4657
2309	2689	3067	3469	3853	4253	4663
2311	2693	3079	3491	3863	4259	4673
2333	2699	3083	3499	3877	4261	4679
2339	2707	3089	3511	3881	4271	4691
2341	2711	3109	3517	3889	4273	4703
2347	2713	3119	3527	3907	4283	4721
2351	2719	3121	3529	3911	4289	4723
2357	2729	3137	3533	3917	4297	4729
2371	2731	3163	3539	3919	4327	4733
2377	2741	3167	3541	3923	4337	4751
2381	2749	3169	3547	3929	4339	4759
2383	2753	3181	3557	3931	4349	4783
2389	2767	3187	3559	3943	4357	4787
2393	2777	3191	3571	3947	4363	4789

100	Author Park	TOW AT YOUR	1 - 1 - 1	1 7 10 1	La Principal	100
4793	4817	4877	4919	4943	4969	4999
4799	4831	4889	4931	4951	4973	5003
4801	4861	4903	4933	4957	4987	5009
4813	4871	4909	4937	4967	4993	

TABLE Of Solid Inches and Solid Feet.

7-			-	1 -	100 July 1		
Feet.	Inches.	Feet.	Inches.	Feet.	Inches.	Feet.	Inches.
MM 1=	= 1728	26=	=44928	51=	88128	76=	=131328
2	3456	27	46656	52	88956	77	133056
3	5184	28	48384	53	91584	78	134784
4	6912	29	50112	54	93312	79	136512
5	8640	30	51840	55	95040	80	138240
6	10368	31	53568	56	96768	81	139968
7	12096	32	55296	57	98496	82	141696
8	13824	33	57024	58	100224	83	143424
- 9	15552	34	58752	59	101952	84	145152
10	17280	35	60480	60	103680	85	146880
11	19008	36	62208	61	105408	86	148608
12	20736	37	63936	62	107136	87	150336
13	22464	38	65664	63	108864	88	152064
14	24192	39	67392	64	110592	89	153792
15	25920	40	69120	65	112320	90	155520
16	27648	41	70848	66	114048	91	157248
17	29376	42	72576	67	115776	92	158976
18	31104	43	74304	68	117504	93	160704
19	32832	44	76032	69	119232	94	162432
20	34560	45	77760	1	120960	95	164160
21	36288	46	79488	71	122688	96	165888
22	38016	47	81216	72	124416	97	167616
23	39744	48	82944		126144	98	169344
24	41472	49	84672		127872	99	171072
25	43200	50	86400	75	129600	100	172800
		1 90		310			

TABLE
Showing the Weight of Cast-Iron Plates, 12 inches square, and from \(^1\)s of an inch to 1 inch thick.

Width in Inches.		$\frac{1}{8}$ 125		$rac{1}{25}$	37 ——	5		<del>1</del> •5	.6	$\frac{1}{25}$	- A	5	-{	<del>7</del> 875		ne ch.
	lbs.	oz.	lbs.	oz.	lbs.	oz.	lbs.	oz.	lbs.	oz	lbs.	oz	lbs.	oz.	lbs.	oz.
12	4	138	9	105	14	8	19	58	24	24	29	0	33	138	38	10%

## To find the Horse Power that a Cast-Iron Wheel is capable of transmitting.

Multiply the breadth of the teeth or face of the wheel in inches by the square of the thickness of one tooth, and divide by the length of the teeth, for the strength at a velocity of 136 feet per minute.

Thus a wheel with the breadth of teeth  $= 7\frac{1}{2}$  inches, thickness=1.4, and length = 2, ought to transmit 7.35 horse power. For

$$1.4^2 = 1.96$$
, and  $\frac{7.5 \times 1.96}{2} = 7.35$ .

The strength at any other velocity is found by multiplying the power so obtained by any other required velocity, and by '0044.

Thus, the wheel as above, at the velocity of 320 feet per minute, would be capable of transmitting 10:3488 horse power.

TABLE

Of the Dimensions of Wheels in Actual Use.

Pitch in inches.	Character of Wheel.	Number of teeth.	Bre'dth in inches.	No. of revolu- tions per minute.	Hors	se Power.			
- 1	MERCIZ INC. ENGIN	1 10	300	11 15	-71	50 41			
$1\frac{1}{2}$	Spur Wheel,	72	41/2	120	8	7.5			
$2\frac{1}{4}$	Spur Wheel,	95	6	25	11/2	1.676			
31	Bevil Wheel,	40	7	$30\frac{1}{2}$	20	24.34			
$2\frac{5}{8}$	Cog Wheel,	60	6	40	12	15.82			
51	Bevil Wheel,	70	12	10	60	67.396			
$2\frac{1}{2}$	Spur Wheel,	90	8	12	6	9.72			
384	Internal,	80	9	20	41	48.8			
3	Cog Spur Wheel, .	60	8	30	121	.177			
3 6	Spur Wheel,	30	14	7	21	•261			
4	Spur Wheel,	100	10	8	25	29.6			
27/8	Spur Wheel,	33	70.0	55	23	.25			
$2\frac{8}{4}$	Spur Wheel, . ,	108	7	20	25	.26			
$2\frac{1}{2}$	Internal,	100	7	10	87	90.4			
5	Internal,	60	12	12	55	53.5			
5	Spur,	41	10	20	61	•50			
476	Spur,	50	12	23	65	71.3			
3%	Bevil Wheel,	35	10	24	26	25.6			
4	Cog Bevil Wheel,.	50	10	28	33	32:6			
4	Cog Spur Wheel, .	35	9	20	18	16.3			
6	On Water Wheel, .	112	14	12	110	·168			
48	Spur Wheel,	55	10	16	56	54.56			
	10 10 10 10 10		- T		110, 100	25			
BULL	COLUMN TO THE RESIDENCE OF THE PARTY OF THE								

### TABLE

Showing the Circumference of a Rope equal to a Chain made of Iron of a given Diameter, and the Weight in Tons that each is proved to carry; also the weight of a Foot of Chain made from Iron of that dimension.

	34 = -			
Rope's circum- ference in inches.	Chain Diameter in inches.	Proved to carry in tons.	Weight of a linear foot in lbs. avoir.	
3	1 & 1 6	1	1.08	
4		2	1.2	
484	8 d 1 1 6	3	2	
51/4	$\frac{1}{2}$	4	2.7	
6	½ & 1/6	<b>5</b>	3.3	
$6\frac{1}{2}$	58	6	4	
7	5 & 1 16	8	4.6	
71/2	<u>8</u>	92	5.2	
8	\$ & 1 16	1114	6.1	
9	7/8	13	7.2	
$9\frac{1}{2}$	7 & 1 1 6	15	8.4	
101	1 inch.	18	9.4	
	AND THE PROPERTY OF THE PARTY O	1007		

The Transverse Strength of a body is that power which it exerts in opposing any force acting in a perpendicular direction to its length, as in the case of beams, levers, &c., it is inversely as their lengths, and directly as their breadths, and the square of their depths. But, if cylindrical, as the cubes of their diameters.

That is, if a beam 5 feet long, 2 inches broad, and 3 inches deep, can carry 1798 lbs., another beam of the same material, 10 feet long, 2 inches broad, and 3 inches deep, will only carry 899 lbs.,

being inversely as their lengths.

Again, if a beam 5 feet long, 2 inches broad, and 3 inches deep, can support 1798 lbs., another beam of the same material, 4 inches broad, and 3 inches deep, will support double that weight, being directly as their breadths.

A beam of the same material, 5 feet long, 2 inches broad, and 6 inches deep, will sustain 7192 lbs., being as the square of their

depths.

TABLE

Showing the Equivalents and Specific Gravities of sixty-two Simple
Substances.

Name of Substance.	Symbol.	Equivalent or Atomic Weight,	Specific Gravity.	Name of Substance.	Symbol.	Equivalent or Atomic Weight.	Specific Gravity.
Hydrogen, .	H.	1	.0689	METALS			
Oxygen,	Oor.	8	1.026	Continued.			
Nitrogen, .	N.	14.2	1.529				
Chlorine, .	Cl.	35.5	2.444	Chromium,	Cr.	28.19	
Carbon,	C.	6.12		Mercury, .	Hg.	203	13.5
Iodine,	I.	126.5	4.948	Silver,	Ag.	108.3	10.5
Sulphur,	S.	16.1	1.99	Gold,	Au.		19.3
Phosphorus,	P.	18.7	1.4	Platinum, .	Pt. Sn.	98·84 58·9	21.5
Fluorine, Bromine, .	F. Br.	78.4	3.	Tin, Cobalt,	Co.	29.5	7.83
Boron,	В.	11	J	Manganese,	Mn.	$\frac{29}{27 \cdot 7}$	8.0
Selenium,	Se.	40	4.5	Nickel,	Ni.	29.5	8.8
Scientum, .	200.	10	T 0	Antimony,	Sb.	64.6	
3.0				Arsenic, .	As.	37.7	5.7
METALS.				Palladium,	Pd.	53.35	
2.13				Rhodium, .	R.	52.2	11
Potassium, .	K.	39.2	.865	Asmium, .	Os.	99.7	10
Sodium,	Na.	23.5	.972	Iridium, .	Ir.	99.8	18.68
Lithium,	L.	10		Cadmium, .	Cd.	55.8	8.6
Calcium,	Ca.	20.5		Molybde-			
Magnesium,	Mg.	12.7	OU III VI	num,	Mo.	47.9	8:6
Silicon,	Si.	22	0.00	Tungsten, or	0. 11		-0.00
Aluminum, .	Al.	13.7	S. French	Wolfram,	W.	94.8	17
Iron,	Fe.	28	7.7	Vanadium,	V.	68.5	
Lead,	Pb.	103.7	11.35	Uranium, .	U.	217 · 2	
Copper,	Cu	31.7	8.8	Titanium, .	Ti.	24.5	· will
Columbium,	Cm. G.	184·8 26	10 TO DE	Cerium, .	Ce. Nr.	46	ARCH, DEC.
Glucinum, . Yltrium,	Y.	32	900-1-10	Niobium, . Pelopium, .	Pe.	mob ni	
Zirconium, .	Zr.	34		Norium, .	No.	Tarian.	
Thorinum, .	Th.	60	900	Didymium,	D.	15 11 11	LEGA
Strontium, .	Sr.	43.8	NT 30 100	Lantanum,	Ln.	48	Walley.
Barium,	Ba.	68.6	10. 10.	Jerbium, .	Tb,	1-10	ALL THE REAL PROPERTY.
Bismuth	Bi.	71.5	1 1 1 1	Erbium, .	Ē.	ST. LAC.	10000
Tellurium, .	Te.	64.2	- 1000	Rutnheium,	Ru.	52	100
Zine,	Z.	32.3	From	2010 01000		12 Labour	100
			6.8 to				
			7.1				

## The Feeding Properties of different Vegetables.

In comparison with 10 lbs. of hay.

Hay,		10	Carrots, 35
Clover hay, .		8	Cabbage, 30 to 40
Vetch hay, .		4	Pease and beans, . 2 to 3
Wheat straw,	•	52	Wheat, 5
Barley straw,		52	Barley, 6
Oat straw, .		55	Oats, 5
Pea straw, .		6	Rye, 5
Potatoes, .	-	- 28	Indian corn, 6
Old potatoes,	Ξ.	40	Bran, 5
Turnips, .		60	Oil-cake, 2

Thus 2 lbs. of oil-cake is worth as much as 55 lbs. of oat straw.

## PENDULUMS.

A pendulum that vibrates seconds, or 60 in the latitude of London, is  $39\cdot1393$  inches long; and  $\sqrt{39\cdot1393}\times60=375\cdot36$ , which serves as a constant number for other pendulums; thus,  $375\cdot36$  divided by the square root of the pendulum's length, gives the number of vibrations per minute; and divided by the vibrations per minute, gives the square root of the length of pendulums.

EXAMPLE 1.—Required the number of vibrations a pendulum of 25 inches long will make per minute.

$$\frac{375\cdot36}{\sqrt{25}} = 75\cdot072 \text{ vibrations per minute.}$$

EXAMPLE 2.—Required the length of a pendulum to make 80 vibrations per minute.

$$\frac{375\cdot36}{80}$$
 =  $4\cdot692^2$  = 22·014864 inches long.

Table containing the Length of Pendulums to vibrate Seconds in various parts of the World.

	I	•	i
	Inches.	520 0	Inches.
At Sierra Leone, .	39.01954	At New York,	39.10153
" Trinidad,	. 39 01879	" Bordeaux,	39.11282
" Madras,	39.02630	" Paris,	39 12843
" Jamaica,	00 00 00	" Edinburgh,	39.15540
" Rio Janeiro, .	. 39.01206	" Greenland,	39.20328

A pendulum vibrating half seconds in the latitude of London is 9.8 inches in length; and for quarter seconds, 2.5 inches.

## ${ m TABLE}$ Showing the Symbols and Equivalents of Binary Compounds.

	DINARI COMPOUNDS.
Remarks.	Easily decomposed by the metals and metallic oxides. Supports combustion; its taste is sweet and pleasant. Transparent and color-less, produces orange red vapors in the atmospheric air and oxygen.  It is color-less at 0 degrees, but green at common temperatures. Called cyanogen, cannot support combustion.  Its vapor is a deep red color, and is rapidly absorbed by water. Extremely acid and caustic, emits suffocating fumes. Sometimes called spirits of hartshorn, or volatile alkali. Does not support respiration or combustion. Used in bleaching and diseases of the skin.  Sometimes called oil of vitriol. Very acid and corrosive. Inflammable, transparent, colorless. Burns with a blue flame. Non-supporter of combustion or respiration. Transparent and color-less.  Sometimes called olefant gas. Burns with a rich yellow flame. Fire-damp, which causes the explosions in coal mines.
Equiva- lent.	9 17 22.2 30.2 38.2 26.44 46.3 17 17 82.1 22.12 22.12 8*12 8*12 8*12 8*12 8*12
Symbol.	SHHCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
Name of Compound.	Water,

	BINARY COMPOUNDS.	251
Easily fused. Much used with soda as a flux.  Explodes at a low temperature, dangerous to obtain. The fumes with phosphorus to be carefully avoided.  Dissolves zinc and iron.  Muriatic acid. Great affinity for water. Possesses an acrid, pungent, suffocating odor.	Detonates with violence when exposed to heat. Its odor is penetrating and insupportable. Composed of chlorine 1, water 1, and nitrous acid 1. Known by the name of Aqua Regia, from its power of dissolving gold. Obtained from iodine and nitric acid. Detonates by a slight pressure. Acts powerfully upon mercury. Its vapors highly irritating. Froduces ulceration on the skin. Powerful taste, and a disagreeable fætid smell. It is a powerful deoxidating agent. Precipitates gold, silver, mercury, and platinum in the metallic form. Transparent and colorless. It detonates with oxygen when heated to 300°, or when the electric spark passes through it.	Bears a great resemblance to sulphuric acid.  Or sesquioxide. The brown rust of iron consists of this oxide.  The color is red.
35 67.5 75.5 36.5	156.2 197.5 197.7 119.7 711.4 55.4 34.4	64 41 36 80
С. В	014 O 11 O b 11 N 11 H 11 H 12 O b 12 O b	O. Se O. Fe O. Fe <sup>2</sup>
Bicarburetted hydrogen, Boracie acid,	gen,  Nitro-muriatic acid,  Iodic acid,  Teriodide of nitrogen,  Hydrofluoric acid,  Phosphoric acid,  Phosphoreacid,  Phosphoreacid,  Phosphoreacid,  Phosphoreacid,  Selenious acid,	Selenic acid, Selentreted hydrogen, Protoxide of iron,

TABLE Showing the Symbols and Equivalents of Binary Compounds. (Continued.)

	A THE	air, or	DIA.		Found in	00.00			on for	nish a	2
		ted in the	ure. ass.	ent.		k	e know.	gether.	at attracti	ide of iron. arts to fur	
	dies of	on is oxide	in contact with water at a high temperature, ommonly called litharge. Used in flint glass.	l as a pign	tive produ	copper blac	and zine w oxide of A	ng them to	f tin; gre	ed with oxi	
	. Remarks.	ed when is	er at a high	h employed	illed red oxide of copper. Native proportions in overtals of a red colon	opper, or	of oxygen	ies by fusi	k oxide o	ly associate gold. U	bronze, termed bronze powder.
		nd is form	with wate	ead. Muc	oxide of c	oxide of c	nbination e; commo	with alkal	alled blac	e, generall	rmed bron
		This compound is formed when iron is oxidated in the air, or	in contact with water at a high temperature Commonly called litharge. Used in flint glass.	Called red lead. Much employed as a pigment.	called red oxide of copper. Native production.	Called black oxide of copper, or copper black.	The only combination of oxygen and zine we know. Occurs native; commonly called oxide of Antimony.	It combines with alkalies by fusing them together.	Sometimes called black oxide of tin; great attraction for	Oxen's native, generally associated with oxide of iron. Formerly called mosaic gold. Used in the arts to furnish	bronze, te
	Equiva- lent.	116		343.1		39.7		161-2 169-2	6.99	74.9 ( 91.1 E	-
	Symbol.	O4 Fe3	O Pb	O Pbs	O Cu2	0 Cu	0 Sb2	Of Sb2	O Sn	O <sup>2</sup> Sn S <sup>2</sup> Sn	Calif
1	und.	on,		f lead, .	er,	er,	timony,		or stan-		Bearing.
Sales Later	Name of Compound.	Black oxide of iron,	Protoxide of lead,	Onoxide of lead,	Dinoxide of copper,	Protoxide of copper, Binoxide of copper	Protoxide of zinc, Sesquioxide of antimony,	Antimonious acid, Antimonic acid,	num,	Binoxide of tin, . Bisulphuret of tin,	
Delguera	Nar	Black	Protox	Quadre	Dinoxi	Protox	Protox Sesquic	Antime	rrotoxide num,	Binoxi Bisulpl	

BINARY COMPOUNDS.	253
Powerful deoxidating agent. Used in calico printing, and as a mordant fixing colors.  Called permuriate. Used in dyeing and calico printing.  It was formerly called butter of bismuth.  It occurs native; pure, and as a hydrate.  Used in the preparation of oxygen and chlorine. It is used to give a dark coating to earthenware.  Commonly called smalt when combined with a little silica and potassa. In this state it is much employed in coloring glass and glazing of earthenware.  Extremely poisonous, either internally or externally.  Considered as noxious as arsenious acid, or more so.  Delecirious. Killed Gehlen in 1815. It has an offensive odor. Burns with a blue flame.  It occurs native. Called realgar; used as a pigment, known as "King's yellow." Used in calico printing to deoxidate indigo.  Artificial Cinnabar. When powdered it is vermillion.	Exposed to the sun becomes purple. It occurs native, and much formed in chemical operations. It has a dark green color. Sometimes called suric acid.
4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	116.3 143.8 208 216 224
Cl'Sn O'Bi: O'Mn O'Mn O'Mn O'As' H'As' SAs SAs SAB SAB Cl'Hg	O Ag Cl Ag O Au O³ Au
Chloride of tin, Biehloride of tin, Protoxide of bismuth, Protoxide of bismuth, Protoxide of manganese, . Sesquioxide of manganese, . Binoxide of manganese,	Protoxide of silver, Prochloride of silver, Protoxide of gold, Binoxide of gold, Teroxide of gold,

# TABLE Showing the Symbols and Equivalents of Binary Compounds. (Continued.) VEGETABLE ACIDS AND SALTS.

Remarks.	51.48 Pungent and agreeable odor; crystallizes at a low temperature; blisters the skin.	Solution in water very sour; erystallizes in prisms.  Nearly like tartaric acid.	4 Powerful poison; two or three drachms produce deads. It is like Epson salts in appearance.  S Is very white: its odor is fractant and peculiar. Burns				00		At
Equiva- lent.			C <sup>2</sup> 36·24		2N 27.44	N Fe 109.32	H <sup>6</sup> 37.48 O Fe 90.2		- O Fe 58.12
Symbol.	O3 C4 H3	Ob C4 H2 O4 C4 H2	O C C	O'C'H3	H C'N	C'H'N Fe	0°N+01	. 03S + OFe	. 0°C+OFe
Name of Compound.	Acetic acid,	Tartaric acid,	Oxalic acid,	Gallic acid,	Hydrocyanic acid, Cvanic acid,	Ferrocyanic acid, Ethers	Sulphuric ether,	Sulphate of iron,	Carbonate of iron,

			·s		
	Called Goulard's extract. Patent yellow; is a mixture of chloride and oxide of lead. Deliquescent, and kept in close vessels. Blue vitriol, employed as an escharotic.	MILL	Vital shining Justice.  Common marking ink is	ALTERNATE .	
	le le		o 50		
	of	80 1 100			
ğ	de		E. P.		
g.	OX	ent	m ag		
ii.	जू	sec			91
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ico	lor sse rro	ĂŽ i	Ş 0	ne	
cal	chi	olo olo	t is	E	
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in orin wh sec	is is	dis nor	na na l		
ollo,	rd', an	E TE	n Plin	F 1 0 7 7 10	
loy lie lle ad	lov lov	s ioi	sul sul	5	
es es l'	yel yel sce	of ize	1ze	ose	2.4
in	d C	als all e v	all siv	<u>Č</u>	
Much employed in dyeing and calico printing. Used in calico printing. Insoluble. Usually called white lead. Sugar of lead, used in dyeing and calico printing.	Called Goulard's extract.  Patent yellow; is a mixture of chloride Deliquescent, and kept in close vessels.  Blue vitriol, employed as an escharotic.	Crystals of a bluish green color. Crystallizes in four-sided prisms. Deliquescent. White vitriol, rhombic prisms colorless.	Crystatizes in rhomboldat prisms with sliming justre.  Corrosive sublimate—dangerous.  Darkens when exposed to light.  The state of the	composed of this and a fittle muchage.	
Mr. Us. Us. Su. Su.	Ca De Da	40°C	වී පීති	arming the self-	orester
The state of the s	a per atten		J		
82 82	88 6 8	91.18 94.5 80.4 62.42	0, 11.10	42 444	91·12 60·64
165.9 151.8 133.82 163.18	93.9 79.8	91.18 94.5 80.4 62.49	265 2 251 1 274 170 5	152.54 23.24 172.44 199.44	91·12 60·64
	01		0101011		
- Andrea of Imp	a		0.5 0.5 0.5	80 80	
44 42	200	A + 0 Cu Ob N + 0 Z Ob N + 0 Z Ob N + 0 Z	HIT Y	<sup>3</sup> N + O Ag <sup>5</sup> P <sup>2</sup> + O Ag O C <sup>2</sup> H <sup>3</sup> O <sup>11</sup> C <sup>12</sup> H <sup>11</sup> O <sup>4</sup> C <sup>12</sup> H <sup>12</sup>	Os Cs H N2 (H2 O C N
00 00	00	0 7 7 7	000 800	のの日日日	HO
++ ++	+ ++	1555 T	++++	++5555	
AC DA	ZZ	1000	KOKK	NO. O = 4	_ H
		4000	, m , ,	7700	~
$ \begin{array}{c} 0^6 N + 0 Pb \\ 0^8 N + 0 Pb \\ 0^2 C + 0 Pb \\ A + 0 Pb \end{array} $	$A + O^{2} Pb^{3}$ $O^{5} N + O Cu$ $O^{5} N + O Cu$	<b>₹</b> 000	$0^{6}N + 0.2$ $0^{6}N + 0.Hg$ $0^{3}N + 0.Hg$ $0^{1}Hg$ $0^{6}N + 0.Ag$	000	$0^{8}  \mathrm{C}^{6}  \mathrm{H}  \mathrm{N}^{2}$ $2  \mathrm{(H}^{2}  \mathrm{O}  \mathrm{C}  \mathrm{N)}$
0 00		4000	000	0.0 N + 0 Ag 0.0 P <sup>2</sup> + 0 Ag 0.0 C <sup>2</sup> H <sup>3</sup> 0.1 C <sup>12</sup> H <sup>11</sup> 0.4 C <sup>12</sup> H <sup>12</sup>	
0 00		<b>4000</b>			
0 0 0	0.00	**************************************			
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	of our con			140001	
	of our con			140001	
	of our con			140001	
	of our con			140001	
	of our con			140001	
Acetate of iron, Obligate of lead, Obligate of lead, Obligate of lead, Carbonate of lead, Obligate of lead, Obligate of lead, Obligate of lead,	Chloride of lead, Chloride of lead,		Acetate of zinc,	Sulphate of silver, O <sup>9</sup> J Phosphate of silver, O <sup>6</sup> J Alcohol,	

## RECIPE FOR DYEING HATS.

The bath for dyeing hats, employed by the London manufacturers, consists, for 12 dozen, of

144 Pounds of logwood;

12 " green sulphate of iron or copperas, 7# " verdigris.

The copper is made of a semi-cylindrical shape, and should be surrounded with an iron jacket, or case, into which steam may be admitted, so as to raise the temperature of the interior bath to 190° Fah., but no higher; otherwise the heat is apt to affect the stiffening varnish, called the gum, with which the body of the hat has been imbued. The logwood having been introduced and digested for some time, the copperas and verdigris are added in successive quantities, and in the above proportions, along with every successive two or three dozen of hats suspended upon the dipping machine. Each set of hats, after being exposed to the bath, with occasional airings, during 40 minutes, is taken off the pegs, and laid out upon the ground to be more completely blackened by the peroxydizement of the iron with the atmospheric oxygen. In 3 or 4 hours the dyeing is completed. When fully dyed, the hats are well washed in running water.

A skilful operator furnishes the following valuable information

relative to the stiffening of hats. He says:

All the solutions of gums which I have hitherto seen prepared by hatters, have not been perfect, but in a certain degree a mixture, more or less, of the gums, which are merely suspended, owing to the consistency of the composition. When this is thinned by the addition of spirit, and allowed to stand, it lets fall a curdy-looking sediment, and to this circumstance may be ascribed the frequent breaking of hats. My method of proceeding is, first, to dissolve the gums, by agitation, in twice the due quantity of spirits, whether of wood or wine, and then, after complete solution, draw off one half the spirit in a still, so as to bring the stiffening to a proper consistency. No sediment subsequently appears on diluting this solution, however much it may be done. Both the spirit and alkali stiffenings for hats made by the following recipes, have been tried by some of the first houses in the trade, and have been much approved of:

Spirit Stiffening.—7 pounds of orange shellac; 2 pounds of gum sandarac; 4 oz. of gum mastic; ½ pound of amber resin; 1 pint of solution of copal; 1 gallon of spirit of wine, or wood naphtha.

The shellac, sandarac, mastic, and resin, are dissolved in the

spirit, and the solution of copal is added last.

Alkali stiffening.—7 Pounds of common block shellac; 1 pound of amber resin; 4 oz. gum thus; 4 oz. gum mastic; 6 oz. borax; ‡ pint of solution of copal.

The borax is first dissolved in a little warm water (say 1 gallon); this alkaline liquor is now put into a copper pan (heated by steam), together with the shellac, resin, thus, and mastic, and allowed to boil for some time, more warm water being added occasionally until it is of a proper consistence; this may be known by pouring a little on a cold slab, somewhat inclined, and if the liquor runs off at the lower end, it is sufficiently fluid. If, on the contrary, it sets before it reaches the bottom, it requires more water. When the whole of the gums seem dissolved, half a pint of wood naphtha must be introduced, with the solution of copal; then the liquor must be passed through a fine sieve, and it will be perfectly clear and ready for use. This stiffening is used hot. The hat bodies, before they are stiffened, should be steeped in a weak solution of soda in water. to destroy any acid that may have been left in them (as sulphuric acid is used in the making of the bodies). If this is not attended to, should the hat body contain any acid when it is dipped into the stiffening, the alkali is neutralised, and the gums consequently precipitated. After the body has been steeped in the alkaline solution, it must be perfectly dried in the stove before the stiffening is applied; when stiffened and stoved, it must be steeped all night in water to which a small quantity of the sulphuric acid has been added; this sets the stiffening in the hat body, and finishes the pro-A good workman will stiffen 15 or 16 hats a day. If the proof is required cheaper, more shellac and resin must be introduced.

## TABLE

## Of Pressures at which certain Gases are Liquified.

Gas is the name given to those elastic fluids which are permanent under a considerable pressure, and at the temperature zero.

Name of Gas.	Ве	ecomes liquid.	Calculated boiling point, barometer == 80 inches.	
vame of Gas.	Λt	Under a pressure of		
Sulphurous Acid, Chlorine, Anmonia, Sulphuretted Hydrog. Carbonic Acid,	59 F. 60 50 50 50 32 50 45	3 atmospheres 4 " 6.5 " 17 " 36 " 50 "	4° Fahr. 22 64 142 220 249 254	

TABLE

Showing the Proportionate Strength of Wheels in Horse Power, with a Velocity of 2.27 Feet per Second.

municipal to the following		Formula $\frac{3^{2}\cdot26\times43.5}{3\cdot9}=117\cdot60$ strength, at 2.27 feet per second Ft. per. Strength Ft. per. Then as 2.27: 117·60::5:259·9 h. p.  The thickness of cog multiplied by 2.1 equals the pitch, and the thickness of cog multiplied by 1.2 equals the length.
	H. P. at 30 feet per second.	1558.6 1466.7 1352.2 1134.84 975.42 984.74
	H.P. at 25 feet per second.	12954 11221-9 1126-00 1016-5 945-79 848-95 708-90 633-19 594-71
	H.P. at 20 feet per second.	1031.27 977.00 900.00 848.4 756.5 672.26 562.00 506.60 474.77 349.40 349.40 346.70
	H. P. at 15 feet per second.	776.2 732.7 675.66 636.34 572.26 675.66 422.15 357.11 357.26 259.50 259.
C ank	H. P at 10 feet per second.	48876 45938 42422 339-65 329-65 329-65 329-24 1199-25 11733-34 1152-42 1152-42 1152-42 1152-42 1152-42 1152-42 1152-42 1152-62 117-62 1
200	H. P. at 5 feet per second.	259.9 225.34 225.34 225.34 212.00 185.11 140.70 118.94 99.84 86.66 76.16 67.32 56.80 56.80 86.70 76.16 87.32 88.10
L	H.P.at 2°27 feet per second.	1117.60 110.95 102.25 96.80 87.87 77.14 7141 7141 7141 7141 7141 7141 71
1	Length in inches.	2
6	Breadth in inches.	483.5 890.9 890.9 834.8 824.8 825.2 827.2 827.2 827.2 827.2 827.2 836.6 83
	Thickness in -	33.55 33.125 33.125 33.125 35.
	Pitch in inches.	6.425 3.125 6.66 6.30 5.125 6.66 6.30 5.125 6.00 5.425 6.30 6.00 2.877 6.55 6.56 6.56 6.30 5.425 6.35 6.35 6.35 6.35 6.35 6.35 6.35 6.3

KNOT TABLE.

The minutes and seconds of time in which a vessel passes over the measured knot being known, look for the corresponding number in this table, which will be the rate of the vessel in knots per hour.

							ZN	O L	/ 1	.AI	LE	•											.0.
	14m.	4 285	4.280	4.275	4-270	4.265	4.260	4.255	4.950	4.245	4.240	4.935	4.230	4.225	4.220	4.215	4.210	4.206	4.201	4.196	4.191	4.186	
-	13m.	4.615	4.609	4.603	4.597	4.591	4.585	1.580	4.24	4.568	4.562	4.556	4.551	4.545	4.539	4.534	4.528	4.522	4.516	4.511	4.505	4.500	_
	12m.	2.000	4.993	4.986	4.979	4.972	4.965	4.958	4.951	4.945	4.938	4.931	4 924	4.918	4.911	4.904	4.897	4.891	4.884	4.878	4.871	4.864	
Di Di	11m.	5.454	5.446	5.438	5 429	5.451	5.413	5.405	5.397	5.389	5.381	5.373	5.365	5.357	5.349	5.341	5.333	5.325	5.317	5.309	5.301	5.504	_
	10m.	000.9	2.990	2.980	2.620	2.960	5.950	5.940	5.930	5 921	5.911	5.901	5.891	5.885	5.872	5.863	5.853	5.844	5.834	5.855	5.815	5.806	
	9m.	999.9	6.654	6.642	6.629	6.617	6.605	6.293	6.581	6.269	6.557	6.545	6.533	6.521	6.203	6.498	6.486	6.474	6.463	6.451	6.440	6.458	_
	8m.	7.500	7.484	7.468	7.453	7.438	7.422	7.407	7.392	7.377	7.362	7.346	7.331	7.317	7.302	7.287	7.272	7.258	7.243	7.229	7.214	7.200	
	7 m.	8.571	8.551	8.530	8.510	8.490	8.410	8.450	8.430	8.413	8.331	8.372	8.352	8.333	8.314	8-295	8.275	8.556	8.238	8.219	8.200	8.181	
	6m.	10.000	9.975	9.944	9.917	068.6	898.6	088.6	608.6	9.783	9.756	9.729	9 703	249.6	9.651	9.625	009.6	9.574	9.549	9.524	9.490	9.473	
	5m.	12.000	11.960	11.920	11.880	11.841	11.803	11.764	11.726	11.688	11.650	11.613	11.575	11.538-	11.501	11.465	11.428	11.392	11.356	11.323	11.285	11.250	
	4m.	15.000	14.938	14.876	14.815	14.754	14.694	14.634	14.575	14.516	14.457	14 400	14.342	14.285	14.220	14.173	14.118	14.063	14.008	13.953	13.900	13.846	_
	3m.	20.000	19.890	19.780	19.672	19.564	19.460	19.355	19.521	19.150	19.047	18-947	18.848	18.720	18.652	18.556	18.481	18.367	18.274	18.181	18.080	18.000	_
	Sec.	0	-	01	အ	4	2	9	-	00	6	10	11	12	13	14	15	16	17	18	19	20	-

KNOT TABLE—(Continued).

								K	N	10	T	AB	LE												
	14m.	4.101	4.176	4.17.1	4.166	4.161	4.157	4.152	4.147	4.149	4.137	4.133	4.198	4.193	4.118	4.114	4.110	4-105	4.100	4.095	4-090	4.086	4.081	,	
200	13m.	4.404	4.488	4.483	4.477	4.479	4.466	4.460	4.455	4.449	4.444	4.438	4.433	4.428	4.422	4.417	4.411	4.406	4.400	4.395	4.390	4.384	4.379		
	12m.	4.858	4.851	4.845	4.838	4.832	4.825	4.819	4.812	4.806	4.800	4.793	4.787	4.780	4774	4.768	4.761	4.755	4.749	4 743	4.738	4.730	4.7.94		
1	11m.	5.286	5.278	5.270	5.263	5.255	5.247	5.540	5.232	5.224	5.217	5.210	5.202	5.195	5.187	5.179	5.172	5 164	5.157	5.150	5.142	5.1.50	5.128		
01111	10m.	5.7.97	5.787	5.778	69.49	5.760	5.750	5.741	5.732	5.723	5.714	5.705	5.696	2.687	5.678	5.669	5 666	5.651	5.642	5.633	5.625	5.616	2.607		
	9m.	6.417	6.405	6.394	6.383	6.871	0989	6.349	6.338	6.327	6.315	6.304	6.593	6.282	6.271	6.260	6.250	6.239	6.228	6.217	6 207	6.196	6.185	18	
	8m.	7.185	7.171	7.157	7.142	7.128	7.114	7.100	7.086	7.072	7.059	7.045	7.031	7.017	7.004	066.9	246.9	6.963	6.950	6.936	6.923	606.9	968.9	Ok arts	
100	7 m.	8.163	8.144	8.127	8.108	8.090	8.071	8.053	8 035	8.017	8.000	7.982	7.964	7.947	7.929	7.912	7.895	7.877	7.860	7.843	7.826	608.4	7.792	8.8	
_	6m.	9.418	9.424	9.399	9.375	9.350	9.356	9.305	9.278	9.254	9.230	9.507	9.183	091.6	9.137	9.113	060.6	890.6	9.045	9.055	000.6	8.977	8-955		
	5m.	11.214	11.180	11.145	11.111	11.077	11.043	11.009	10.975	10.045	10 909	10.876	10.843	10.810	10.778	10.764	10.714	10.682	10.021	10.619	10.588	10.221	10:526		
	4m.	13.793	13.740	13.688	13.636	13 584	13.533	13.483	13.432	13.383	18.333	13.284	13.235	13.186	13.138	18.091	13.043	12.996	12.950	12.903	12.857	12.811	12.766		
	3m.	17-910	17-823	17.734	17.647	17.560	17.475	12.391	17.307	17.225	17.143	190.11	16.981	106.91	16.822	16.744	199.91	16.230	16.514	16.438	16.363	16.289	16.216		
000	Sec.	21	2.7	23	54	25	26	22	28	53	30	120	35	33	34	35	36	37	300	39	40	41	42		

## KNOT TABLE—(Concluded).

								K:	NO1		LA	BLI	E.							
	14m.	4.077	4 072	4.067	4.063	4.058	4 054	4.049	4.044	4.040	4.035	4.031	4.026	4 022	4.017	4.013	4.008	4.004		
	13m.	4.374	4.368	4.368	4.358	4.353	4.347	4.342	4.337	4.332	4.326	4.321	4.316	4.311	4.306	4.301	4.595	4.290		-
	12m,	4.718	4.712	4.706	4.700	4.693	4.687	4.681	4.675	4.669	4.663	4.657	4.651	4.645	4.639	4.633	4.627	4.621		
	11m.	5.121	5.114	5.106	660.9	5.091	5.084	5.077	5.070	5.063	5.056	5.049	5 042	5.035	5.028	5.020	5.013	5.006		
	10m.	5.598	5.590	5.581	5.572	5.564	5.555	5.547	5.538	5.530	5.521	5.513	5.504	5.496	5.487	5.479	5.471	5.463		
	9m.	6.174	6.164	6.153	6.143	6.132	6.122	6.112	6.101	6 091	180.9	6.071	090.9	6.050	6.040	080.9	6.020	0.009		
	8m.	6.883	0.28.9	6.857	6.844	6.831	6.818	6.805	6.792	6-4-19	994.9	6.754	6.741	6.729	6.716	6.704	6.691	6.679		The state of the s
	7m.	7.775	7.758	7.741	7.725	7 708	7 693	2.49.4	4.659	7.643	7.627	7.611	7.595	616.1	7.563	7.547	7.531	7.515		
1	6m.	8.933	8.911	8.889	8.867	8.845	8.823	8.801	8.780	8.759	8.737	8.716	8.695	8.675	8.654	8.633	8 612	8.591	0000	
	5m.	10.495	10.465	10.434	10.404	10.375	10.345	10.315	10.586	10.256	10-227	10.198	10.169	10.140	10.412	10.084	10.022	10.021		
	4m.	12.711	12.676	12.631	12.587	12.543	12.200	12.456	12.413	12.871	12.329	12-287	12.245	12.203	12.162	12.121	12.080	12 040		
	3m.	16.143	16.071	16.000	15.929	15.859	15.789	15.721	15.652	15.584	15.517	15.450	15.384	15.319	15.254	15.190	15.125	15.062	31	-
	Sec.	43	41	45	46	47	48	49	00	51	55	53	54	55	56	57	58	59	41	-

## CEMENTS.

Shell-lac Cement, or Liquid Gluc.—Fine orange shell-lac, bruised, 4 oz.; highly rectified spirit, 3 oz. Digest in a warm place, frequently shaking, till the shell-lac is dissolved. Rectified wood naphtha may be substituted for spirit of wine, where the smell is not objectionable. This is a most useful cement for joining almost any material.

Shell-lac Cement, without Spirit.—Boil 1 oz. of borax in 16 oz. water; add 2 oz. powdered shell-lac, and boil in a covered vessel till the lac is dissolved. This is cheaper than the above, and for many purposes, answers very well. Both are useful in fixing paper labels to tin, and to glass when exposed to damp.

Keller's Armenian Cement, for Glass, China, &c.—Soak 2 dr. of cut isinglass in 2 oz. of water for 24 hours; boil to 1 oz.; add 1 oz. of spirit of wine, and strain through linen. Mix this, while hot, with a solution of 1 dr. of mastic in 1 oz. of rectified spirit, and triturate with ½ dr. powdered gum ammoniae, till perfectly homogeneous.

Dr. Ure's Diamond Cement.—Isinglass, 1 oz.; distilled water, 6 oz.; boil to 3 oz., and add 1½ oz. of rectified spirit. Boil for a minute or two, strain, and add, while hot. first, ½ oz. of a milky emulsion of ammoniae, and then 5 dr. of tineture of mastic.

Hoenle's Cement, for Glass or Earthenware.—Shell-lae, 2 parts; Venice turpentine, 1 part. Fuse together, and form into sticks.

Cheese Cement, for Earthenware, &c — Mix together white of egg, beaten to a froth, quick-lime, and grated cheese. Beat them to a paste, which forms an excellent cement.

Curd Cement.—Add  $\frac{1}{2}$  pint of vinegar to  $\frac{1}{2}$  pint of skimmed milk. Mix the curd with the whites of 5 eggs well beaten, and sufficient powdered quick-lime to form a paste. It resists water, and a moderate degree of heat.

Cement for joining Spar and Marble Ornaments, &c.—Melt together 8 parts of resin, 1 of wax, and stir in 4 parts, or as much as may be required, of Paris plaster. The pieces to be made hot.

Hensler's, Cement.—Grind 3 parts of litharge, 2 of recently burnt lime, and 1 of white bole, with linseed oil varnish. This is a very tenacious cement, but it takes considerable time to dry.

Singer's Cement, for Electrical Machines and Galvanic Troughs.— Melt together 5 lbs. of resin, and 1 lb. of beeswax, and stir in 1 lb of red ochre (highly dried, and still warm), and 4 oz. of Paris plaster, continuing the heat a little above 212°, and stirring constantly till all frothing ceases. Or (for troughs), resin, 6 lbs; dried red ochre, 1 lb.; calcined plaster of Paris, ½ lb.; linseed oil, ½ lb.

CEMENTS.

Composition for welding Cast Steel.—Take of borax, 10 parts, sal ammoniae, 1 part; grind or pound them roughly together: then fuse them in a metal pot over a clear fire, taking care to continue the heat until all spume has disappeared from the surface. When the liquid appears clear, the composition is ready to be poured out to cool and concrete; afterwards, being ground to a fine powder, it is ready for use. \* \* \* To use this composition. The steel to be welded is first raised to a "bright yellow" heat, it is then dipped among the welding powder, and again placed in the fire, until it attains the same degree of heat as before; it is then ready to be placed under the hammer.

Cast-Iron Cement.—Take of clean iron borings, or turnings, 1 ewt.; of sal-ammoniac 8 oz.; and 1 oz. of flour of sulphur. Mix them thoroughly, and add sufficient water. If the cement is not to be immediately used, care should be taken to keep the mixture soaked in water; if left dry, the cement will heat, and be spoiled.

Cement for Steam Pipe Joints, &c., with Faced Flanges—To 2 parts of white lead mixed, add 1 part of red lead dry; grind, or otherwise mix them, to a consistence of thin putty; apply interposed layers, with one or two thicknesses of canvas or gauze wire, as the necessity of the case may require.

Glues.—1. A very strong glue is formed by throwing a small quantity of powdered chalk into melted common glue.

2. To make a glue which will resist the action of water—boil one pound of common glue in two quarts of skimmed milk.

Botany Bay Cement.—Take 1 part of Botany Bay gum, and melt and mix it with 1 part of brickdust.

Cap Cement.—As Singer's; but 1 pound of dried Venetian red may be substituted for the red ochre and Paris plaster.

Bottle Cement.—Resin 15 parts; tallow 4 (or wax 3) parts; highly dried red ochre 5 parts. The common kinds of sealing-wax are also used.

Turner's Cement.—Beeswax 1 oz.; resin  $\frac{1}{2}$  oz.; pitch  $\frac{1}{2}$  oz. Melt, and stir in fine brickdust.

Coppersmith's Cement.—Powdered quick-lime, mixed with bullock's blood, and applied immediately.

Engineers' Cement.—Equal weights of red and white lead, with drying oil, spread on tow or canvas. This is an admirable composition for uniting large stones in cisterns, &c.

Iron Cement for Closing the Joints of Iron Pipes.—Take of iron borings, coarsely powdered, 5 lbs.; of powdered sal-ammoniac 2 oz.; of sulphur 1 oz.; and water sufficient to moisten it. This composition hardens rapidly; but if time can be allowed it sets more firmly without the sulphur. It must be used as soon as mixed, and rammed tightly into the joints.

Cement for Steam Pipes.—Good linseed oil varnish ground, with equal weights of white lead, oxide of manganese, and pipeclay.

Gad's Hydraulic Cement.—Powdered clay 3 lbs.; oxide of iron 1 lb; and boiled oil to form a stiff paste.

Cements for Masonry of Chambers of Chlorine, &c.—Equal parts of pitch, rosin, and plaster of Paris.

Roman Cement.—1 bushel of slacked lime; 3½ lbs. of green copperas; and ½ bushel of fine gravel sand. The copperas should be dissolved in hot water. It must be stirred with a stick, and kept stirred continually while in use. Care should be taken to mix at once as much as may be requisite for one entire front, as it is very difficult to obtain the same shade or color a second time. It ought to be mixed the same day it is used. This is the English Roman cement.

The genuine Roman cement consists of the pulvis puteolanus, or puzzolene, a ferruginous clay from Puteoli, calcined by the fires of Vesuvius, lime, and sand, mixed with soft water. The only preparation which the puzzolene undergoes is that of pounding and sifting; but the ingredients are occasionally mixed with bullock's blood and suet, to give the composition greater tenacity.

Seal Engravers' Cement.—Resin 1 part; brickdust 1 part. Mix, with heat.

Marine Cement, commonly called Marine Gluc.—Cut eaoutehoue into small pieces, and dissolve it, by heat and agitation, in coal naphtha. Add to this solution powdered shell-lac, and heat the whole, with constant stirring, until combination takes place; then pour it, while hot, on metal plates, to form sheets. When used, it must be heated to 280° Fah., and applied with a brush.

Liquid Gluc.—Dissolve bruised orange shell-lac in 3 of its weight of rectified spirit, or of rectified wood naphtha, by a gentle heat. It is very useful as a general cement and substitute for glue. Another kind may be made by dissolving 1 oz of borax in 12 oz of soft water, adding 2 oz. of bruised shell-lac, and boiling till dissolved, stirring it constantly.

Bank Note Glue.—Dissolve 1 lb. of fine glue, or gelatine, in water; evaporate it till most of the water is expelled; add  $\frac{1}{2}$  lb. of brown sugar, and pour it into moulds. Some add a little lemon juice. It is also made with 2 parts of dextrine, 2 of water, and 1 of spirit.

Maissial's Cement, as an Air-Tight Covering for Bottles, &c.—Melt india-rubber (to which 15 per cent. of wax or tallow may be added), and gradually add finely powdered quick-lime, till a change of odor shows that combination has taken place, and a proper consistence is obtained.

Cement for Attaching Metal Letters on Plate Glass.—Copal varnish 15 parts; drying oil 5 parts; turpentine 3 parts; oil of turpentine CEMENTS. 265

2 parts; liquified glue 5 parts. Melt in a water bath, and add 10 parts of slacked lime.

Japan'se Cement.—Mix rice flour intimately with cold water, and boil gently.

French Cement.—Mix thick mucilage of gum arabic with powdered starch.

Store Cement.—River sand 20 parts; litharge 2 parts; quick-lime 1 part. Mix, with linseed oil.

Plumbers' Cement.—Resin 1 part; brick-dust 2 parts. Mix, with heat.

Parisian Cement.—Gum arabic 1 oz.; water 2 oz.; sufficient starch to thicken.

Coment for Floors.—The following style of floor is well adapted for plain country dwellings: Take two thirds of lime, and one of coal ashes, well sifted, with a small quantity of loam clay; mix the whole together, temper it well with water, and make it up into a heap; let it lie six or seven days, and then temper it again. After this, heap it up for three or four days, and repeat the tempering very high, till it becomes smooth, yielding, tough, and gluey. The ground being then levelled, lay the floor therewith about  $2\frac{1}{2}$  or 3 inches thick, making it smooth with a trowel. The hotter the season is the better; when thoroughly dried it makes a capital floor. Should a better looking floor be desired, take lime of rag stones, well tempered with white of eggs, and cover the floor half an inch thick with it, before the under flooring is too dry. If this be well done, and the floor thoroughly dried, it will look, when rubbed with a little oil, as transparent as metal, or glass.

Common Paste.—To a table-spoonful of flour add gradually half a pint of cold water, and mix till quite smooth; add a pinch of powdered alum (some add a small pinch of powdered rosin), and boil for a few moments, stirring constantly. The addition of a little brown sugar, and a few grains of corrosive sublimate, will, it is said by practical chemists, preserve it for years.

Soft Cement.—Melt yellow wax with half its weight of common turpentine, and stir in a little Venetian red, previously well dried and finely powdered. This cement does very well as temporary stopping for joints and openings in glass and other apparatus, where the heat and pressure are not great.

Lutes, or Cements, for Closing the Joints of Apparatus.—Mix Paris plaster with water to a soft paste, and apply it immediately. It bears nearly a red heat. It may be rendered impervious by rubbing it over with wax and oil.

Another.—Slacked lime, made into a paste with white of egg, or a solution of gelatine.

Another. Fat Lute.—Finely powdered clay, moistened with water, and beaten up with boiled linseed oil. Roll it into cylinders,

and press it on the joints of the vessels, which must be perfectly dry. It is rendered more secure by binding it with strips of linen moistened with white of egg.

Another.-Linseed meal beaten to a paste with water.

Another.—Slips of moistened bladder, smeared with white of egg.

Fire and Waterproof Cement.—To half a pint of milk put an equal quantity of vinegar, in order to curdle it; then separate the curd from the whey, and mix the latter with four or five eggs, beating the whole well together. When it is well mixed add a little lime through a sieve, until it has acquired the consistence of a thick paste. With this cement broken vessels may be united. It resists water, and, to a certain extent, fire.

Fire Lutes.—The following composition will enable glass vessels to sustain an incredible degree of heat: Take fragments of porcelain, pulverize, and sift them well, and add an equal quantity of fine clay, previously softened with as much of a saturated solution of muriate of soda as is requisite to give the whole a proper constance. Apply a thin and uniform coat of this composition to the glass vessels, and allow it to dry slowly before they are put into the fire.

Another.—Equal parts of coarse and refractory clay, mixed with a little hair, form a good lute.

A Cement for Stopping the Fissures of Iron Vessels.—Take two ounces of muriate of ammonia, 1 ounce of flour of sulphur, and 16 ounces of cast-iron filings, or turnings. Mix them well in a mortar, and keep the powder dry. When the cement is wanted take one part of this and twenty parts of clean iron filings, or borings; grind them together in a mortar, mix them with water to a proper consistence, and apply them between the joints. This cement answers for flanges of pipes, &c., about steam-engines.

Genuine Armenian Cement - "The jewellers of Turkey, who are mostly Armenians," says Mr. Eton, a very intelligent traveller, and at one time a resident and consul in that country, "have a singular method of ornamenting watch cases, &c., with diamonds and other precious stones, by simply glueing or cementing them on. The stone is set in silver or gold, and the lower part of the metal made flat, or to correspond with the part to which it is to be fixed. It is then warmed gently, and the glue applied, which is so very strong that the parts thus cemented never separate. This glue, which will firmly unite bits of glass, and even polished steel, and may of course be applied to a vast variety of useful purposes, is thus made: - Dissolve five or six bits of gum mastic, each the size of a large pea, in as much spirits of wine as will suffice to render it liquid; in another vessel dissolve as much isinglass, previously a little softened in water (though none of the water must be used), in French brandy, or good rum, as will make a two ounce phial of

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very strong glue, adding two small bits of gum galbanum, or ammoniacum, which must be rubbed or ground till they are dissolved. Then mix the whole with a sufficient heat, keep the glue in a phial closely stopped, and when it is to be used set the phial in boiling water."

Another.—Thick isinglass glue 1 part; thick mastic varnish 1 part. Melt the glue, mix, and keep it in a closely corked phial. For use, put the phial in hot water.

Elastic Cement for Bells.—Dissolve in good brandy a sufficient quantity of isinglass, so as to be as thick as molasses.

A very strong Carpenters' Glue.—Dissolve an ounce of the best isinglass, with a moderate heat, in a pint of water. Take this solution, and strain it through a piece of cloth, and add to it a proportionate quantity of the best glue, which has been previously soaked for about twenty-four hours, and a gill of vinegar. After the whole of the materials have been brought into a solution, let it once boil up, and strain off the impurities. This glue is well adapted for any work which requires particular strength, and where the joints themselves do not contribute towards the combination of the work; or in small fillets and mouldings, and carved paters, that are held on the surface by the glue.

A Glue for Inlaying Brass or Silver Strings, &c.—Melt your glue as usual, and to every pint add of finely powdered rosin and finely powdered brickdust two spoonfuls each; incorporate the whole together, and it will hold the metal much faster than any common glue.

A strong Glue that will resist Moisture.—Dissolve gum sandarae and mastic, of each \( \frac{1}{2} \) of an ounce, in \( \frac{1}{2} \) of a pint of spirit of wine, to which add \( \frac{1}{2} \) of an ounce of clear turpentine. Now take strong glue, or that in which isinglass has been dissolved; then, putting the gums into a double glue-pot, add by degrees the glue, constantly stirring it over the fire till the whole is well mixed; then strain it through a cloth, and it is ready for use. You may now return it into the glue-pot, and add \( \frac{1}{2} \) an ounce of very finely powdered glass; use it quite hot. If you join two pieces of wood together with it you may, when perfectly hard and dry, immerse it in water and the joint will not separate.

A Paste for laying Cloth or Leather on Table Tops.—To a pint of the best wheaten flour add two table spoonfuls of finely powdered rosin, and one spoonful of powdered alum. Mix them well together, put them into a pan, and add by degrees rain water, carefully stirring it till it is of the consistence of thinnish cream; put it into a saucepan over a clear fire, keeping it constantly stirred, that it may not get lumpy. When it is of a stiff consistence, so that the spoon will stand upright in it, it is done enough. Be careful to stir it well from the bottom, for it will burn if not well attended to. Empty it out into a pan, and cover it over till cold, to prevent a

skin forming on the top, which would make it lumpy. This paste is very superior for the purpose, and adhesive. To use it for cloth or baize spread the paste evenly and smoothly on the top of the table, and lay your cloth on it, pressing and smoothing it with a flat piece of wood; let it remain till dry; then trim the edges close to the cross-banding. If you cut it close at first it will, in drying, shrink and look bad where it meets the banding all round. If used for leather, the leather must be first previously dampened, and the paste then spread over it; then lay it on the table, and rub it smooth and level with a linen cloth, and cut the edges close to the banding with a short knife. Some lay their table-cover with glue instead of paste, and for cloth perhaps it is the best method: but for leather it is not proper, as glue is apt to run through. In using it for cloth, great care must be taken that your glue is not too thin, and that you rub the cloth well down with a thick piece of wood made hot at the fire, for the glue soon chills. You may by this method cut off the edges close to the border at once.

Cement Stopping.—Mix equal quantities of sawdust, of the same wood required to be stopped, and clear glue; and with this stop up the holes or defects of the wood. Where the surface is to be japanned or painted, whiting may be used instead of sawdust. Be sure to let the stopping dry before you attempt to finish the surface.

Mahogany-colored Cement.—Melt two ounces of beeswax, and half an ounce of rosin, together; then add half an ounce of Indian red, and a small quantity of yellow ochre to bring the cement to the desired color. Keep it in a pipkin for use.

A Cement to stop Flaws or Cracks in Wood of any Color.—Put any quantity of fine sawdust, of the same wood your work is made with, into an earthen pan, and pour boiling water on it, stir it well, and let it remain for a week or ten days, occasionally stirring it; then boil it for some time, and it will be of the consistence of pulp or paste; put it into a coarse cloth, and squeeze all the moisture from it. Keep for use, and when wanted mix a sufficient quantity of thin glue to make it into a paste; rub it well into the cracks, or fill up the holes in your work with it. When quite hard and dry, clean your work off, and, if carefully done, you will scarcely discover the imperfection.

Fireproof Stucco for Wood, &c.—Take moist gravelly earth (previously washed), and make it into stucco with the following composition: Pearlashes two parts; water five parts; common clay one part. It has been tried on a large scale and found to answer.

Terra Cotta—Potter's clay, Ryegate sand, and water, each a sufficient quantity. Model and bake.

Pew's Composition for covering Buildings.—Take the hardest and purest limestone (white marble is to be preferred), free from sand, clay, or other matter; calcine it in a reverberatory furnace, pulverize and pass it through a sieve. One part, by weight, is to be mixed

with two parts of clay well baked and similarly pulverized, conducting the whole operation with great care. This forms the first powder. The second is to be made of one part of calcined and pulverized gypsum, to which is added two parts of clay, baked and pulverized. These two powders are to be combined, and intimated incorporated, so as to form a perfect mixture. When it is to be used, mix it with about a fourth part of its weight of water, added gradually, stirring the mass well the whole time, until it forms a thick paste, in which state it is to be spread like mortar upon the desired surface. It becomes in time as hard as stone, allows no moisture to penetrate, and is not cracked by heat. When well prepared it will last any length of time. When in its plastic or soft state, it may be colored of any desired tint.

TABLE

Of Analysis of certain Organic Substances, from the best authorities.

	Carbon.	Hydrogen.	Oxygen.	Nitrogen.	Total
Sugar,	42.225	6.600	51.175	1.13	100
Starch,	44.250	6.674	49.076	10 1019	100
Gum,	42.682	6.374	50.944	70 1 3	100
Lignin,	52.53	5.69	41.78	WELLIAM.	100
Tonnin	59.500	3.825	43.585	11/19/19	100
Indigo,	73.260	2.500	10.43	13.81	100
Camphor,	73.38	10.67	14.61	•34	100
Caoutehoue,	87.2	12.8	_		100
Albumen,	52.883	7.540	23.872	15.705	100
Fibrin,	53.36	7.021	19.685	19 934	100
Casein,	59.781	7.429	11.409	21.381	100
Urea,	18.9	9.7	26.2	45.2	100
Gelatine,	47.881	7.914	27 207	16.998	100
Picromel,	54.53	1.82	43.65	=0)	100
Hordein,	44.2	6.4	47.6	1.8	100
Emelin,	64.57	7.77	22.95	4.3	100
Veratrin,	66.75	8.54	19.60	5.04	100
Cinchonin,	77.81	7.37	5.93	8.89	100
Quinin,	75.76	7.52	8.61	8.11	100
Bruein,	70.88	6.66	17:39	5.07	100
Strychnin,	76.43	6.70	11.06	5.81	100
Narcotin,	65.00	5.20	26.99	2.51	100
Morphin	72.340	6.366	16.299	4.995	100

TABLE

To Calculate the Pitch of a Toothed Wheel, when the radius and number of teeth are given; and the RADIUS, when the pitch and number of teeth are given, from 10 to 159 teeth.

No. of Teeth.	Radius.	No. of Teeth.	Radius.	No. of Teeth.	Radius.	No. of Teeth.	Radius.	No. of Teeth.	Radius.
B07		1-2		177	11 Lm 1 3	-	1	U S B	TARRE
-			a hand			10000	THE P.		3.0.1
10	1.618	40	6.373	70	11'144	100	15.918	130	20.692
11	1.774	41	6.532	71	11.303	101	16.077	131	20.851
12	1.932	42	6.691	72	11.463	102	16.236	132	21.010
13	2.089	43	6.850	73	11.622	103	16.395	133	21.169
14	2.247	44	7.009	74	11.781	104	16.554	134	21.328
15	2.405	45	7.168	75	11.940	105	16.713	135	21.488
16	2.563	46	7:327	76	12.099	106	16.873	136	21.647
17	2.721	47	7.486	77	12.258	107	17.032	137	21.806
18	2.879	48	7.645	78	12.417	108	17.191	138	21.965
19	3.038	49	7.804	79	12:576	109	17:350	139	22.124
20	3.196	50	7.963	80	12.735	110	17.509	140	22.283
21	3.355	51	8.122	81	12.895	111	17.668	141	22.442
22	3.513	52	8 281	82	13.054	112	17.827	142	22.602
23	3.672	53	8.440	83	13.213	113	17.987	143	22.761
24	3.830	54	8.599	84	13.370	114	18.146	144	22.920
25	3.989	55	8 758	85	13.531	115	18.305	145	23.079
26	4.148	56	8.917	86	13.690	116	18:464	146	23.238
27	4.307	57	9.076	87	13.849	117	18.623	147	23 397
28	4.465	58	9.235	88	14:008	118	18.782	148	23.556
29	4.624	59	9:394	89	14.168	119	18.941	149	23.716
30	4.788	60	9.553	90	14·327 14·486	120	19·101 19·260	150	23.875 $24.034$
31 32	4·942 5·101	62	$9.712 \\ 9.872$	91 <sup>-</sup> 92	14.645	$\begin{array}{c c} 121 \\ 122 \end{array}$	19.260	151 152	24.193
33	5.260	63	10.031	93	14.804	123	19.578	153	24.193
34	5.419	64	10.031	93	14.963	$\frac{123}{124}$	19.737	154	24.511
35	5.578	65	10.349	94	15.122	124	19 896	155	24.620
36	5.737	66	10 508	96	15.281	125	20.055	156	24.830
37	5.896	67	10.667	96	15.440	126	20.033	157	24.989
38	6.055	68	10.826	98	15.440	127	20.374	158	25.148
39	6.214	69	10.985	99	15.759	128	20.533	159	25.307
99	0 214	09	10 909	99	10 109	1.29	20 333	109	20 501
00	1		100 ==	577	Total II	2.2.3		Dily	100

RULE 1.—Divide the required radius by the radius opposite the given number of teeth in the table; the quotient will be the required pitch of the wheel.

Example. To find the pitch of a wheel whose radius is 43 inches, that shall contain 90 teeth:

Required radius 43 ÷ 14.327 = 3-inch pitch.

Rule 2.—Multiply the radius opposite the given number of

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teeth in the table, by the pitch required; the product will be the required radius of the wheel.

Example. To find the radius of a wheel that shall contain 48 teeth of 2½-inch pitch:

In the Table, radius  $7.645 \times 2.5 = 19\frac{1}{10}$  inches nearly.

# CABLES.

#### TABLE

For finding the Strain that may safely be applied to a good Hempen Cable.

Circum.	Pounds.	Circumfer.	Pounds.	Circumfer.	Pounds.
9127	- 22		17 33		7
4 4 70 4	-03	23.2	16 3	1	E 1001
6.	4320	10.25	12607.5	14.50	25230
6.25	4687.5	10.50	13230	14.75	26107.5
6.50	5070	10.75	13867.5	15.	27000
6.75	5467.5	11.	14520	15.25	$27907 \cdot 5$
7.	5880.	11.25	15187.5	15.50	28830
7:25	6307.5	11.50	15870	15.75	29767.5
7.50	6750	11.75	16567.5	16.	30720
7.75	7207 · 5	12.	17280	16.25	31687.5
8.	7680	12.25	18007.5	16.50	32670
8.25	8167.5	12.50	18750	16.75	33667.5
8.50	8670	12.75	19507.5	17.	34680
8.75	9187.5	13.	20280	17.25	35707.5
9.	9720	13.25	21067.5	17.50	36750
9.25	10267.5	13.50	21870	17.75	37807.5
9.50	10830	13.75	22687 . 5	18.	38880.
9.75	11407.5	14.	23520	18.25	39967 · 5
10.	12000	14.25	24367.5	1 4	AL SIL
Q180	X (6)	11.5	0		All the

To ascertain the Strength of Cables.—Multiply the square of the circumference in inches by 120, and the product is the weight the cable will bear in pounds, with safety.

To ascertain the Strength of Ropes.—Multiply the square of the circumference in inches by 200, and it gives the weight the rope will bear in pounds, with safety.

To ascertain the Weight of Manilla Ropes and Hawsers.—Multiply the square of the circumference in inches by '03, and the product is the weight in pounds of a foot in length.

This is but an approximation, sufficiently correct for many purposes.

TABLE
Showing the Size of Cables and Anchors proportional to the Tonnage of Vessels.

Tonnage of vessels.	Cables. Circumfer. in inches.	Chain Ca- bles. Diam. in inches.	Proof in tons.	Weight of Anchor in pounds.	Weight of a fathom of chain.	Weight of a fathom of Cable.
5	3.	• 5	• 84	56	5.7	2.1
8	4.	• 3	1.8	84	8.	4.
10	4.1	· 18	$2 \cdot \frac{1}{2}$	112	11.	4.6
15	5.7	• 1/2	4.	168	14.	6.5
25	6.	· 9	5.	224	17.	8.4
40	$6 \cdot \frac{1}{2}$	· <u>5</u>	6.	336	24.	9.8
60	7.	· 11/6	7.	392	27.	11.4
75	$7 \cdot \frac{1}{2}$	· 84	9.	532	30.	13 ·
100	8.	· 13	10.	616	36.	15.
130	9.	- 78	12.	700	42.	18.9
150	$9\cdot\frac{1}{2}$	· 15	14.	840	50.	21 ·
180	10.1	1.	16.	952	56.	25.7
200	11.	$1 \cdot \frac{1}{16}$	18.	1176	60.	28.2
240	12.	1.1	20.	1400	70.	33.6
270	12.1	$1 \cdot \frac{3}{16}$	21.	1456	78.	36.4
320	13.7	1.4	22.1	1680	86.	42-5
360	14.	$1 \cdot \frac{5}{16}$	25.	1904	96	45.7
400	14.1	1.8	27	2072	104.	49.
440	15.4	1.7	30.	2240	115.	56.
480	16.	$1 \cdot \frac{1}{2}$	33.	2408	125	59.5
520	16:1	$1\cdot\frac{9}{16}$	36.	2800	136	63.4
570	17.	1.5	39.	3360	144	67 · 2
620	17 · ½	1.11	42.	3920	152	71.1
680	18.	1.8	45.	4200	161	75.6
740	19.	$1 \cdot \frac{13}{16}$	49:	4480	172	84.2
820	20.	1 · 7/8	52.	5600	184	93.3
900	22.	$1 \cdot \frac{15}{16}$	56.	6720	196	112.9
1000	24.	1.	60.	7168	208 · ·	134.6

TABLE

For finding the Strain that may be applied to a Hempen Rope with safety.

Circum.	Pounds.	Circumfer.	Pounds.	Circumfer.	Pounds.
1· 1·25 1·50 1·75 2· 2·25 2·50 2·75 3·	200° 312°5 450° 612°5 800° 1012°5 1250° 1512°5 1800° 2112°5	3·50 3·75 4·25 4·50 4·75 5·25 5·50 5·75	2450· 2812·5 3200· 3612·5 4050· 4512·5 5000· 5512·5 6050· 6612·5	6. 6.25 6.50 6.75 7. 7.25 7.50 7.75 8.	7200 · 7812 · 5 8450 · 9112 · 5 9800 · 10512 · 5 11250 · 12012 · 5 12800 ·

TABLE

Of Weight of Copper Rods or Bolts, from \(\frac{1}{4}\) to 4 inches in diameter, and 1 foot in length.

Diam	Pounds.	Diameter.	Pounds.	Diameter.	Pounds.
•1	1892	1:1	3.8312	$2\cdot\frac{3}{8}$	17:0750
. 5	2956	$1 \cdot \frac{3}{16}$	4.2688	$2\cdot\frac{1}{2}$	18.9161
• <u>3</u>	·4256	1.4	4.7298	2.5	20.8562
1 7	•5794	1:5	5.2140	2.3	22.8913
•1	.7567	1.3	5.7228	2.7	25.0188
16	.9578	1:7	6.2547	3.	27.2435
* <u>5</u>	1.1824	1:1/2	6.8109	3.1	29.5594
·11	1.4307	1:9	7.3898	3.4	31.9722
• <u>8</u>	1.7027	1.5	7.9931	3.8	34.4815
13	1.9982	1.8	9.2702	3.1	37.0808
* <del>7</del>	2.3176	1.4	10.6420	3.5	39.7774
·15	2.6605	2.	12.1082	3.₹	42.5680
1.	3.0270	2.1	13.6677	3.4	45.4550
1:16	3.4170	2.4	15.3251	4.	48.4330
THE STATE OF	11 AL	LUL CA	1 159		Service at

Weight of a copper rod 12 inches long and 1 in. diameter = 3.039 lbs.

Weight of a brass rod 12 inches long and 1 inch diameter = 2.86 lbs.

TABLE

Of the Weight of Riveted Copper Pipes, from 5 to 30 inches in diameter, from 3 to  $\frac{5}{15}$  thick, and 1 foot in length.

				10	, ,		9	3 1
Diameter in inches.	Thickness in 16ths.	Weight in pounds.	Diameter in inches.	Thickness in 16ths.	Weight in pounds.	Diameter in inches.	Thickness in 16ths.	Weight in pounds.
5. 5. 5. 2. 2. 5. 6. 6. 6. 6. 7. 7. 2. 8. 9.	\$ 4 3 4 3 4 5 4 4 4 4 4 4 4 4 4 4 4 4 4 4	12:497 16:880 13:628 18:395 14:765 19:908 15:897 21:415 17:034 22:932 24:447 25:961 27:471 28:985	9·½ 10· 11· 12· 18· 14· 15· 16· 16· 17· 17· 18· 18·	4 4 4 4 4 4 5 4 5 4 5 4 5	30·598 32·208 35·200 38·456 41·456 44·640 47·646 59·588 50·752 63·470 53·856 67·344 57·037 71·258	19· 19· 20· 21· 22· 23· 24· 25· 26· 27· 28· 29· 30·	4 5 5 5 5 5 5 5 5 5 5 5	60·142 75·233 78·208 82·984 86·771 90·571 94·308 98·122 101·897 105·700 109·446 113·221 116·997

The above weights include the laps on the sheets for riveting and caulking.

The weights of the rivets are not added; the *number* per linear foot of pipe depends upon the distance they are placed apart, and their *size* upon the diameter of the pipe.

TABLE
Showing the Capacity of Cisterns in Gallons.
For each 10 Inches in Depth.

Feet Diam.		Feet Diam.	DIO:	Feet Diam.	01 ·	Feet Diam.	40
2	19:5	5	122:40	8	313.33	12	705
$2\frac{1}{2}$	30.6	51/2	148.10	81/2	353.72	13	827.4
3	44.06	6	176.25	9	396.56	14	959.6
31	59.97	61	206.85	91	461.40	15	1101.6
4	78.33	7	239.88	10	489.20	20	1958.4
41	99.14	71	275.40	11	592.40	25	3059.9

TABLE

Containing the weight of a Square Foot of Copper and Lead in lbs. avoirdupois, from  $\frac{1}{3}$  to  $\frac{1}{2}$  an inch in thickness, advancing by  $\frac{1}{3}$ .

Thickness.	Copper.	Lead.	Thickness.	Copper.	Lead.	
$\frac{1}{3}\frac{1}{2}$	1.45	1.85	$\frac{1}{4}$ and $\frac{1}{32}$	13.07	16.62	
	2.90	3.70	$\frac{1}{4}$ " $\frac{1}{16}$	14.52	18:47	
$\frac{\frac{1}{16}}{\frac{3}{32}}$	4.35	5.54	$\frac{1}{4}$ " $\frac{3}{32}$	15.97	20.31	
18	5.80	7:39	<u>3</u>	17.41	22 16	
1/8 and 1/3 2	7.26	9.24	$\frac{3}{8}$ " $\frac{1}{32}$	18:57	24.00	
½ " ½	8.71	11.08	\$ " 1 1 6	20.32	25.85	
$\frac{1}{8}$ " $\frac{3}{32}$	10.16	12.93	8 " 3 2	21.77	27.70	
1/4	11.61	14.77	$\frac{1}{2}$ .	23.22	29.55	
63	200		1000			

#### TABLE

Of the Weight of a Square Foot of Sheet Iron in lbs. avoirdupois, the thickness being the number on the wire gauge.—No. 1 is  $\frac{5}{16}$  of an inch; No. 4,  $\frac{1}{4}$ ; No. 11,  $\frac{1}{8}$ , &c.

No. on wire gauge, .	1	2	3	4	5	6	7	8
Pounds avoirdu.,	12.5	12	11	10	9	8	7.5	7
No. on wire gauge, .	9	10	11	12	13	14	15	16
Pounds avoirdu.,	6	5.68	5	4.62	4:31	4	3.95	-3
No. on wire gauge, .	17	18	19	20	21	22	1	j
Pounds avoirdu.,	2.5	2.18	1.93	1.62	1.5	1.37		

TABLE

Of the Weight of a Square Foot of Boiler Plate Iron, from \frac{1}{8} to 1 inch thick, in lbs. avoirdupois.

1/8	$\frac{3}{16}$	14	16	8	7 16	$\frac{1}{2}$	$\frac{9}{16}$	8	$\frac{\frac{1}{1}\frac{1}{6}}{}$	4	13	78	$\frac{1}{1}\frac{5}{6}$	1 in.
		-		-	-	_		-	-	-		-	-	
5	7.5	10	12.5	15	17.5	20	22.5	25	27.5	30	32.5	35	37.5	40

TABLE

Showing the Quantity of Water per Linear Foot in Pumps, or Vertical Pipes of different Diameters.

Diameter of pump in inches.	Number of gallons per linear foot.	Number of cubic feet per linear foot.	Diameter of pump in inches.	Number of gallons per linear foot.	Number of cubic feet per linear foot.
2	.136	.0218	8	2.176	·3490
$\frac{1}{2\frac{1}{4}}$	.172	0276	81	2.314	.3712
$-\frac{2\frac{4}{2}}{2\frac{1}{2}}$	212	.0340	81	2.456	3940
$2\frac{3}{4}$	.257	.0412	884	2.603	4175
3	.306	.0490	9	2.754	•4417
31	.359	.0576	91	2.909	.4666
$3\frac{1}{2}$	416	.0668	91	3.068	•4923
$3\frac{\tilde{3}}{4}$	.478	.0766	93	3:232	5184
4	.544	0872	10	3.400	•5454
41/4	.614	.0985	101	3.572	•5730
$4\frac{1}{2}$	.688	·1104	10i	3.748	·6013
484	.767	·1230	103	3.929	.6302
5	.850	·1363	11	4.114	.6599
$5\frac{1}{4}$	•937	1503	1114	4.303	.6902
$5\frac{1}{2}$	1.028	.1649	111	4.496	.7212
53	1.124	·1803	113	4.694	·7529
6	1.224	·1963	12	4.896	·7853
61/4	1.328	2130	$12\frac{1}{2}$	5:312	·8521
$6\frac{1}{2}$	1.436	2304	13	5.746	·9217
684	1.549	•2489	$13\frac{1}{2}$	6.196	.9939
7 -	1.666	.2672	14	6.664	1.0689
$7\frac{1}{4}$	1.787	2866	15	7.650	1.2271
71	1.912	3067	16	8.704	1.3962
74	2.042	3275	18	11.016	1.7670

#### Examples illustrative of the Utility of the Table.

1. Required the quantity of water lifted by each stroke of the bucket of a  $9\frac{1}{2}$ -inch pump, the length of the stroke being  $2\frac{1}{4}$  feet.

 $3.068 \times 2.25 = 6.903$  gallons, each stroke.

2 What length of stroke with a 6-inch pump will be necessary to discharge 44 gallons of water per minute, the number of strokes being 18 in the given time?

$$\frac{44}{1.224 \times 18} = 2$$
 feet, the length of stroke.

3. What must be the diameter capable of raising 25 cubic feet of water per minute, the length of the stroke being 2½ feet, and making 16 effective strokes per minute?

$$\frac{25}{2.5 \times 16} = .625$$
, or  $10\frac{3}{4}$  inches, nearly.

Properties of Atmospheric Air.—It is by the oxygen of the atmosphere that combustion is supported. The common combustibles of nature are chiefly compounds of carbon and hydrogen, which, during combustion, combine with the oxygen of the atmosphere, and are converted into carbonic acid and watery vapor, different species of fuel requiring different quantities of oxygen. The quantity required for the combustion of a pound of coal varies from two to three lbs. Sixty cubic feet of atmospheric air will produce 1 lb. of oxygen.

The pressure or fluid properties of the atmosphere oppose bodies in passing through it, the opposing resistance increasing as the square of the velocity of the body, and the resistance per square foot in lbs. as its velocity in feet per second, multiplied into 002288. Thus, suppose a locomotive engine in a still atmosphere, at a velocity of 25 miles per hour, presents a resisting frontage of 20 feet; required the amount of opposing resistance at that velocity.

25 miles per hour equal 36 67 feet per second. Then  $36.67^2 \times .002288 \times 20 = 61.5$  lbs., constant opposing force.

TABLE

Showing the Number of Threads to an Inch in V-thread Screws.

Diam. in inches, No. of threads,	1	5 16	<u>3</u>	7 16	1/2	58	84	78	1	11/8	11	18
No. of threads,	20	18	16	14	12	11	10	9	8	7	7	6
			10	411	2 9	8						
Diam. in inches, No. of threads,	$1\frac{1}{2}$	15	184	17	2	21	$2\frac{1}{2}$	28	3	31	31/2	
No. of threads,	6	5	5	41/2	$4\frac{1}{2}$	4	4	31/2	31/2	31	31	
Diam. in inches,	38	4	41	41/2	484	5	54	$ 5\frac{1}{2} $	54	6		
Diam. in inches, No. of threads,	3-	3	27	27/8	$2\frac{3}{4}$	28	25	25/8	21/2	21/2		

The depth of the threads should be half their pitch. The diameter of a screw, to work in the teeth of a wheel, should be such that the angle of the threads does not exceed 10°.

TABLE

Of the component parts of one English pound avoirdupois of 7000 grains of the following varieties of Wood. [Mushet.]

Description of Wood.	Water, Hyd. gas, Carb. acid.	Carbon.	Ashes.	Color and degree of saturation of the alkalme principle:
Oak	5382.6	1587.8	29.6	grov shapply allyaling
Oak,	5688.2	1258.0		grey, sharply alkaline.
Ash,	5650.2	1224.4	125.4	whitish blue, shrp. alk.
Birch,	5630.9	1344.3		brownish red, shrp. alk.
Norway Pine, .	5147.0		24.8	brown, not at all alk.
Mahogany,		1784.4	68.6	grey, sharply alkaline.
Sycamore,	5544.0	1381.4	74.6	pure white, weakly alk.
Holly,	5524.4	1394.3	81.3	pure white, sharply alk.
Scotch pine, .	5816.7	1151.9	31.4	brown, perceptibly alk.
Beech,	5737.3	1395.9	66.8	greyish white, shrp. alk.
Elm,	5576.6	1370.2	53.2	grey, partially alkaline.
Walnut,	5496.5	1446.4	57.1	f pure white, light as down, weakly alk.
American Maple	5553.2	1393.1	53.7	dark grey, sharply alk.
Do. Black ) Beech, .	5425.9	1301.8	72.3	brown, sharply alkaline.
Laburnum,	5196.4	1721.0	82.6	white & grey, partly alk.
Lignum Vitæ, .	5083.0	1880.0	35.0	grey, sharply alkaline.
Sallow,	5626.0	1294.8	79.2	light grey, sharply alk.
Chestnut,	5341.3	1629.6	29.1	grey, sharply alkaline.
7				

TABLE
Of Properties of Gases.

Atmospheric air being the standard of comparison, or 1000.

Names.	Specific gravity.	Names.	Specific gravity.
Hydriodic acid gas, . Chlorine " " . Carbonic " " . Nitrous oxide " . Cyanogen " . Oxygen " .	4340 2500 1527 1527 1805 1111	Carbonic oxide gas, . Carburetted hydrogen ". Prussie acid ". Ammoniacal ". Steam of water ". Hydrogen ".	972 972 937 590 623 69

TABLE

Of Change Wheels for Screw-cutting; the leading Screw being of ½ inch pitch, or containing 2 threads in an inch.

-	Number of											
Number of threads in inch of screw.	Nun	th in	Number of threads in inch of screw.	N	umber	of teet	h in	ii ii	Number of threads in inch of screw.  Lathe spindle- wheel.  Wheel in contact with spindle-wh. Pinnon in contact with screw-wheel Leading screw- wheel.			
iber of thread	ads w.			-	1 5	: t=	1.	nds w.	-	1 5 4	। उड़	1.
of sc	Lathe spindle wheel.	Leading screw wheel.	of thread of screw.	Lathe spindle- wheel.	Wheel in contact with spindle-wh.	Pinion in contact with spindle-wh.	Leading screw- wheel.	of threads	Lathe spindle- wheel.	Wheei in contact with spindle-wh,	Pinion in contact with screw-wheel	Leading screw- wheel.
oer ich	ne spine wheel.	ling sci wheel.	of	ne spin wheel.	ing	ind ind	ling scr wheel.	of	ne spir wheel.	indi	ew-	ling scr wheel.
umir	the	w	ppe	the	eel	ion gs t	wk	aper	the	sei i	on scr	din X
Z	La	Le	Nun	្ន	Wh	Pin	Let	Nun	La	Why	Pin	Lei
-	-	10		5.1		į		3	i	-	2	
1	80	40	81	40	55	20	60	19	50	95	20	100
$ \begin{array}{c c} 1\frac{1}{4} \\ 1\frac{1}{2} \\ 1\frac{8}{4} \\ 2 \end{array} $	80	50	81/2 81/2 82/4 91/2 92/4	90	85	20	90 75	$19\frac{1}{2}$	80	120	20	130
$1\frac{1}{2}$	80	60	83	60	70	20	75	20	60	100	-20	120
184	80	70	$9\frac{1}{2}$	90	90	20	95	$20\frac{1}{4}$	40	90	20	90
2	80	90	93	40	60	20	65	21 22	80	120	20	140
$2\frac{1}{4}$ $2\frac{1}{2}$ $2\frac{8}{4}$	80	90	10	60	75	20	80	22	60	110	20	120
$2\frac{1}{2}$	80	100	$10\frac{1}{2}$	50	70	20	75	$22\frac{1}{2}$	80	120	20	150
$2\frac{8}{4}$	80	110	11	60	55	20	120	$22\frac{1}{2}$ $22\frac{3}{4}$	80	130	20	140
3	80	120	12	90	90	20	120	$23\frac{3}{4}$	40	95	20	100
314 312 384	80	130	123	60	85	20	90	24	65	120	20	130
$3\frac{1}{2}$	80	140	13	90	90	20	130	25	60	100	20	150
33	80	150	$13\frac{1}{2}$	60	90	20	90	$25\frac{1}{2}$	30	85	20	90
4	40	80	$13\frac{1}{2}$ $13\frac{3}{4}$	80	100	20 !	110	26	70	130	20	140
41/4	40	85	14	90	90	20	140	27	40	90	20	120
$4\frac{1}{2}$	40	90	144	60	90	20	95	271	40	100	20	110
4½ 4½ 4¾	40	95	15	90	90	20	150	28	75	140	20	150
5 5½	40	100	16	60	80	20	120	$28\frac{1}{2}$	30	90	20	95
$5\frac{1}{2}$	40	110	$16\frac{1}{4}$	80	100	20	130	30	70	140	20	150
6	40	120	$16\frac{1}{2}$	80	110	20	120	32	30	80	20	120
$\frac{6\frac{1}{2}}{7}$	40	130	17	45	85	20	90	33	40	110	20	120
7	40	140	$17\frac{1}{2}$	80	100	20	140	34	30	85	20	120
71	40	150	18	40	60	20	120	35	60	140	20	150
8	30	120	183	80	100	20	150	36	30	90	20	120
-dier	1014 3	CONT. P.	2 77		10	1- 1	1 1	- 11-1	Lit		1	20107

Temperature and Weight of the Atmosphere at various heights.

Height.	Temperature.	Water heavier than the
Level of the sea,	60°	860 times.
One mile above,	. 43	1,083 "
Two miles above,	26	1,363 "
Three miles above,	9	1,716 "
Four miles above,	-8	2,160 "
Five miles above,	-25	2,719 "

TABLE

Showing how to discover the Quantity and Weight of Water in Pipes of any given size.

Diameter in inches.	Quantity in cubic inches.	Quantity in imperial gallons.	Weight in lbs, avoirdupois.		
$1 \\ 1 \\ 1 \\ 2$	14·14	0.051	0·51		
	56·55	0.205	2·05		
	127·23	0.460	4·60		
	226·19	0.818	8·18		
$rac{2rac{1}{2}}{3}$ $3rac{1}{2}$	353·43	1·278	12.78		
	508 94	1·841	18:41		
	692·72	2·506	25:06		
$egin{array}{c} 4 \ 4rac{1}{2} \ 5 \ 5rac{1}{2} \end{array}$	904·78 1145·11 1413·72 1710·60	3.272 $4.142$ $5.113$ $6.187$	32·72 41·42 51·13 61·87		
$\begin{array}{c} 6 \\ 6\frac{1}{2} \\ 7 \end{array}$	2035·75	7:363	73.63		
	2389·18	8:641	86.41		
	2770·88	10:022	100.22		
$egin{array}{c} 7rac{1}{2} \ 8 \ 8rac{1}{2} \ 9 \end{array}$	3180·86	11·505	115·05		
	3619·11	13·090	-130·90		
	4085·64	14·777	147·77		
	4580·44	16·567	165·67		
$\frac{9\frac{1}{2}}{10}$ $\frac{10\frac{1}{2}}{11}$	5103·52	18·459	184·59		
	5654·87	20·453	204·53		
	6234·49	22·550	225·50		
	6842·39	24·748	247·48		
$\begin{array}{c c} & 11 \\ 11\frac{1}{2} \\ 12 \end{array}$	7478·56 8143·01	27·049 29·452	241 48 270:49 294:52		

This table shows the quantity and weight of water contained in one fathom of length of pipes of different bores from 1 inch to 12 inches in diameter, advancing by half inch. The weight of a cubic foot of water is taken at 1000 ounces avoirdupois, and the imperial gallon at 10 lbs.

Multipliers used for ascertaining the quantity of Tallow, Oakum, and Oil that can be contained in Tanks for use of Steam-vessels.

Tallow,			59 lbs. in a cubic foot.
Oakum,		13	11 lbs. in a cubic foot.
Oil, .		0.00	6.23 galls. in a cubic foot.
Coal, .			45 cubic feet to a ton.

1	SPECI	J.T.	U K.	AVII	LIES	AN	1/ (	7111	EK	1	ROI EN	TIES OF DODIES.		201
Tin, cast, Zine, cast,	" hard,	PPO I	Iron, east,	" sheet,	Brass, cast,	" wrought,	Copper, cast,	Bismuth	Lead,	Mercury,	Pure gold,	Names.		Tables, combining the Specific
• • •	• •	•	•	•	•	•	• •	•	•	-	• •			he
7291 7190	7816	7700	7264	8396	7824	8910	8788	0893	1352	3500	9500 9258	Specific gravity.	Bd	Speci
442 773	1-1	1	2786	1	1900		_	18/3	612	1	3280 2016	Melting points in degrees of Fah.	PROPERTIES	he Gr
-278 -329	1 33	.137	125	L	-210	1	193	·156	-319	The state of	11	Contraction in parts of an inch per linear foot from the fluid to the average temp. in solid state.	30	PROPERTIES OF BODI Gravities and other Properties of Bodies.
2 11 5.06	- 58.91	25.00	7.87	12.23	8.01	15.08	8:51	-	· 81	1	11	Ultimate cohesive strength of an in. sq. prism in tons	METALS.	PROI l other
-700	1 1	4	1	6	1	07	1 1	N	000	1	- 00	Scale of wire-	19	PEE
40		00	1	6	1	లు	1 1	М	-7	i	<b>–</b> 5	drawing ductility.   Scale of laminable   ductility		ROPERTIES ther Propert
( degree 1.2 1.6	to any	4.7	to any	Great	to any	2.8	1 6	2.4	1.0	1	1.8	Ratio of hardness.		ies of Bo
701	1-1	4	1 1	100	I	_		K	6	1	သ	Scale as conduc-	71	)D]
	lind.	3.7	1	8.6	i	8 9	1 1	9.7	100	j	3.8	Ratio of power in the conduction of heat.	-	ES.
29 (11)	" Cannel, .	" Staffordsh.	" Newcastle	Brick,	- Oi	Craigleith do.,	Paving stone.	Millstone .	Portland do., .	Purbeck stone,	Marble, average Granite, do.	Names.	PROPERTIES OF	Water the standard of Comparison, or 1000
or ylan	1238	1240	1300	2000	2143	2362	2415	2554	2570	2601	2720 2651	Specific gravity.	STONES	of Con
=1-1-	77.37	77.50	81.15	125.00	133.98	147.62	150.93	159.62	160.62		170.00	Weight of a cubic foot in lbs.	ES, EARTHS,	npariso
400	29		27	17		15	14				13	Cubic feet in a ton.	THIS	n,
	21 10	4	H coh	0	000		           	-	4		9-0	10 11 0 0 1	0.01	70
	1	1		တ်င	, S	0.	1	1	Öi	•	20.5	Tons required to crush 1½ in. cubes	&c.	000

## Properties of Woods.

BILLIN		Port	co oj	11 000				
	NO. OF	vity,	of a	ina	Ultimate cohesive strength of an inch square prism in lbs.	Cor	nparat	ive
Names.		Specific gravity, water, 1000.	Average wt. of a cubic foot in lbs.	Cubic feet in a tou.	e coh mare n lbs.	ess.	Ē.	nce.
		wate	vera	ubic	imat treng h sq	Stiffness.	Strength.	Resilience.
5		σ <u>Ω</u> -	A D	0	D ani	. 02	Ī.	a -
	,-	1	-	-		-	1111	- 1
English oak,	ŭ	934	58	381	11880	100	100	100
Riga do,	-	872	-54	413	12888	93	108	125
Dantzie do.,	6	756	47	48	12780	117	107	99
American do.,		672	42	53	10253	114	86	64
Beech,		852	48	45	12225	77	103	138
Alder,		800	46	$48\frac{1}{2}$	9540	63	80	101
Plane,		640	40	55	10935	78	92	108
Sycamore,		604	38	59	9630	59	81	111
Chestnut,		610	38	59	10656	67	89	118
Ash,		845	52	43	14130	89	119	160
Elm,		673	42	53	9720	78.	82	86
Mahogany, Spanish, .		800	50	45	7560	73.	67	.61
" Honduras,	-	637	40	55	11475	93	96	99
Walnut,		671	42	53	8800	49	74	111
Teak,		750	46	481	12915	126	109	94
Poona,		640	40	55	12350	99	104	82
African oak,		944	_59	38	17200	101	144	138
Poplar,		383	34	66	5928	44	50	57
Cedar,		561	33	68	7420	28	62	106
Riga fir		753	47	48	9540	98	80	64
Memel do.,		546	34	66	9540	114	80	56
Scotch do.,		528	33	68	7110	55	60	65
Christ. white deal, .		590	37	60	12346	104	104	104
American white spruce		551	34	66	10296	72	86	102
Yellow pine,	-	461	28	80	11853	95	99	103
Pitch pine,	5	660	41	$54\frac{1}{2}$	_9796	73	82	92
Larch,		530	31	72	12240	79	103	134
Cork,	H	240	15	149	38 14	1 9		
***************************************	6		-	33	100 1	1 73		

#### Fusing Point of various Metals.

The fusing points of the more refractory substances are only to be ascertained approximately, on account of the doubtful accuracy of the indications given by the *pyrometers* at very high temperatures.

The pyrometer constructed of platinum is the most delicate, although the rate of its expansion must be uncertain as it approaches its own fusing point. The following are considered to be the fusing points of metals:

	Fahr.	Fahr.
Platinum,	3080°	Silver, 1830°
Wrought iron,		Zinc, 700
Steel,		Lead, 590
Gold,	2190	Bismuth, 500
Cast iron,	2100	Tin, 450
Conner	1920	

A dull red heat is estimated as 1480°; a bright red heat as 1830°; and a white heat as 2370° to 2910°, Fah.

#### Table of Properties of Liquids.

Names.	Specific grav. water, 1000.	Weight of an imp. gallon in lbs.	Names.	Specific grav. water, 1000.	Weight of an imp gallon in lbs.
100 100		400		. 1000	100-
Acid, sulphuric, .	1850	18.5	Oils, expressed:		- William
" nitric,	1271	12.7	linseed,	940	9.4
" muriatic, .	1200	12.0	sweet almond, .	932	9.3
" fluoric,	1060	10.6	whale,	923	9.2
" citric,	1034	10.3	hempseed,	926	9.3
" acetic,	1062	10.6	olive,	915	9.2
Water from the	March 1	1 1 1 2	Oils, essential:	-20010	dana-
Baltic,	1015	10.2	cinnamon,	1043	10.4
Water from the	200	7	lavender,	894	8.9
Dead Sea,	1240	12.4	turpentine,	870	8.7
Water from the			amber,	868	8.7
Mediterranean, .	1029	10.3	Alcohol,	825	8.2
Water, distilled, .	1000	10.0	Ether, nitric,	908	9.1
,			Proof spirit,	922	9.2
	7-10-0	100	Vinegar,	1009	10.1
January 1	1 300	100	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1000	10 1

Axle Grease.

1. The popular axle grease of the celebrated Mr. Booth is made as follows:

Dissolve ½ lb. common soda in 1 gallon of water, add 3 lbs. of tallow and 6 lbs. of palm oil (or 10 lbs. of palm oil only). Heat them together to 200° or 210° Fah.; mix, and keep the mixture constantly stirred till the composition is cooled down to 60° or 70°.

2. Another and thinner composition is made with  $\frac{1}{2}$  lb. of soda, 1 gallon of water, 1 gallon of rape oil, and  $\frac{1}{4}$  lb. of tallow, or palm oil.

3. The French compound, called Liard, is thus made:—Into 50 parts of finest rape oil put 1 part of caoutchouc, cut small. Apply heat, until it is nearly all dissolved.

4. Mankettrick's Jubricating compound consists of 4 lbs, of caoutchouc (dissolved in spirits of turpentine), 10 lbs, of common

soda, 1 lb. of glue, 10 gallons of oil, and 10 gallons of water. Dissolve the soda and glue in the water by heat, then add the oil, and lastly the caoutchouc, stirring them until perfectly incorporated.

5. The following is the ordinary kind of axle-grease in common use:—1 part of fine black lead, ground perfectly smooth, with 4

parts of lard. Some recipes add a little camphor.

#### TABLE

Of Fusibility of Metals.

As given by M. Thenard.

1.—Fusible below a red heat.

#### CENTIGRADE.

Mercury, .		-39~	
Potassium,.		+58	Gay Lussac and Thenard.
Sodium, .		90	Do. do.
Tin,		210	Newton.
Bismuth, .			Do.
Lead,		260	Biot.
Tellurium, .		a little less fus, than lead	Klaproth.
		undetermined	addition -
Zine,		370	Brongniart.
		a little below a red heat	all and more
1101	9_	Infusible below a med heat	4310

# 2.—Infusible below a red heat.

PYROMETER OF WEDGWOOD.								
Silver,	200	Kennedy.						
Copper,	27	Wedgwood.						
Gold,	32	Do.						
Cobalt,	( a little less difficult )							
Cobart,	to melt than iron							
Iron,	130	Wedgwood.						
46	158	Sir G. McKenzie.						
Manganese,	160	Guyon.						
Nickel,	160	Richter						
Palladium,	Nearly infusible, and to							
Molybdenum,	be obtained at a forge							
Uranium,								
Tungsten,								
Chromium,								
Titanium,	The bear like arms for setting	I would be seen as						
Cerium,	Infusible at the forge							
Osmium,	77 11							
Iridium,	the oxy - hydrogen							
Rhodium,	1 11 11							
Platinum,	100							
Columbium,	I was you also be a look							

#### TABLE

Containing the Quantities of Water, in cubic feet, that will be discharged over a Weir per minute, for every inch in its breadth, when the depths of the Water from the surface to the top edge of the wasteboard do not exceed eighteen inches.

Depth of the Wa- ter in inches.	Cubic feet per minute, according to Du Buat's formula.	Cubic feet per minute, according to experiments made in Scotland.	Depth of the Wa- ter in inches.	Cubic feet per minute, according to Du Bnat's formula.	Cubic feet per minute, according to experiments made in Scotland.
1 2 3 4 5 6 7 8	0·403 1·140 2·095 3·225 4·507 5·925 7·466 9·122 11·884	0.428 $1.211$ $2.226$ $3.427$ $4.789$ $6.295$ $7.933$ $9.692$ $10.564$	10 11 12 13 14 15 16 17 18	12·748 14·707 16·758 18·895 21·117 23·419 25·800 28·258 30·786	13·535 15·632 17·805 20·076 22·437 24·883 27·413 30·024 32·710

TABLE

Of the Composition of different Gunpowders.

2			
KINDS.	Nitre.	Charcoal.	Sulphur.
Royal Mills at Waltham Ab-			
bey, England,	75	15	10
France, national establishm't.	75	12.5	12.5
French, for sportsmen,	78	12	10
French, for mining,	65	15	20
United States of America,	75	12.5	12.5
Prussia,	75	13.5	11.5
Russia,	73.78	13.59	12.63
Austria (musket),	72	17	16
Spain,	76.47	10.78	12.75
Sweden,	76	15	9
Switzerland (a round powder)	76	14	10
Chinese,	75	14.4	9.9
Theoretical propor. (as above)	75	13.23	11.77
1		1	101

## Alloys.

Alloys having a Density greater than the	Alloys having a Density less than the
Mean of their Constituents.	Mean of their Constituents.
Gold and zinc. Gold and tin. Gold and bismuth. Gold and antimony. Gold and cobalt. Silver and zinc. Silver and lead. Silver and bismuth. Silver and antimony. Copper and zinc. Copper and zinc. Copper and tin. Copper and palladium. Copper and bismuth. Lead and antimony. Platinum and molybdenum. Palladium and bismuth.	Gold and silver. Gold and iron. Gold and lead. Gold and copper. Gold and iridium. Gold and nickel. Silver and copper. Silver and iron. Iron and bismuth. Iron and antimony. Iron and lead. Tin and lead. Tin and palladium. Tin and antimony. Nickel and arsenic. Zine and antimony.

TABLE
Showing the estimated Power of Man or Horse as applied to
Machinery.

Application of the Power.	Lbs. avr. at the rate of 220 feet per minute.	Lbs. avr. at the rate of one foot per minute.
A man is supposed to be capable of lifting or carrying	27.273	6000
When the united efforts of two men are applied to the winch of a crane, the han-	28.637	6300
dles being at right angles, each man exerts a force equal to	33:499	7350
pumping equal to	17:335 38:955 40:955 150	3814 8570 9010 33000

TABLE
Of the Speed and Force of Wind, at different velocities.

Velocity of the Wind in		Force in lbs. avoir- dupois per square	Common Appellations given to	
Miles per hour.	Feet per second.	foot.	the Wind.	
1 2 3 4 5 10 15 20 25 30 35 40 45 50 60 80 100	1·47 2·93 4·40 5·87 7·33 14·67 22·00 29·34 36·67 44·01 51·34 58·68 66·01 73·35 88·02 117·36 146·70	0005 020 044 079 123 492 1:107 1:968 3:075 4:429 6:027 7:873 9:963 12:300 17:715 31:490 49:200	Hardly perceptible.  Just perceptible.  Gentle, pleasant wind.  Pleasant, brisk gale.  Very brisk.  High winds.  Very high  A storm or tempest.  A great storm.  A hurricane.  A violent hurricane, which wrenches and tears up trees, forces dwellings and minor buildings from their foundations, and drives them before it.	

Note.—The following rule is used to find the force of wind acting perpendicularly upon a surface:—Multiply the surface in feet by the square of the velocity in feet, and the product by '002238. The result is the force in pounds avoirdupois.

Table showing the Height of the Boiling Point, Fah., at different Heights of the Barometer.

Barometer.	Boiling Point.	Barometer.	Boiling Point.
Inches.	Degrees.	Inches.	· Degrees.
31	213.57	281	209.55
301	212.79	28	208.69
30	212.00	271	207.84
291	211.20	27	206.96
20	210.38		

In a vacuum water boils at 98° to 100°, according as the vacuum is more or less perfect.

TABLE

Of the sizes of Nuts, equal in strength to their Bolts.

Diam. of bolt in in.	Short diameter of nut in in.	Diam. of bolt in in.	Short diameter of nut in inches.	Diam. of bolt in in.	Short diameter of nut in in.
$\frac{1}{2}$ $\frac{3}{4}$	55 55	1 <del>8</del> 1½	$\begin{array}{c} 2\frac{7}{16} \\ 2\frac{11}{16} \end{array}$	$2\frac{1}{2}$ $2\frac{5}{8}$	47
1 2 5 8	$1\frac{1}{16}$	15 15 14	$2\frac{7}{8}$ $3\frac{1}{8}$	28 28 28 27	4 <sup>8</sup> / <sub>1</sub> 4 <sup>15</sup> / <sub>16</sub>
8 24 78	$1\frac{5}{16}$ $1\frac{9}{16}$	$1\frac{7}{8}$	$3\frac{8}{8}$ $3\frac{9}{16}$	2 to 3 to	5 <del>8</del> 5 <del>8</del> 5 <del>8</del>
1 1 <del>1</del>	$1\frac{8}{4}$	2 <del>1</del> 2 <del>1</del> 2 <del>1</del>	$\begin{array}{c} 3\frac{3}{4} \\ 4 \end{array}$	3½ 3½ 3¾	$6\frac{5}{16}$ $6\frac{3}{4}$
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2 <del>1</del>	2 <u>8</u>	$4\frac{1}{4}$	4	71

Note.—The depth of the head should equal the diameter of the bolt; the depth of the nut should exceed it, in the proportion of 9 or 10 to 8.

TABLE

Showing the Power of various Species of Fuel.

Species of Fuel.	Effect in lbs of water heated 1° by one lb. of fuel.	Effect in lbs. of water con- verted into- steam of 220°.	Quantity to convert a cubic foot of water into low pres- sure steam.	Quantity to conver a cubic foot of water into steam, al- lowing 10 per cent. for loss.
	lbs.	lbs.	lbs.	lbs.
Caking coal,	9800	8.4	7.45	8.22
Coke,	9000	7.7	8.1	9.00
Splint coal,	7900	6.75	9.25	10.28
Oak wood, dry,	6000	5.13	12.2	13.6
Ordinary oak,	3600	3.07	20.31	22 6
Peat compact, of ordinary dryness, . }	3250	2-8	22.5	25.0

TABLE

Of the Ratios of the Successive Hardnesses of Bodies.

Substances.	Hardness.	Specific Gravity.	Substances.	Hardness.	Specific Gravity.
Diamond from Ormus,	20	3.7	Sardonyx,	12	2.6
Pink Diamond,	19	3.4	Occidental amethyst,	11	2.7
Bluish Diamond,	19	3.3	Crystal,	11	2.6
Yellowish Diamond, .	19	3.3	Cornelian,	11	2.7
Cubic Diamond,	18	3.2	Green Jasper,	11	2.7
Ruby,	17	4.2	Reddish yellow do	9	2.6
Pale ruby, from Brazil,	16	3.5	Schoerl,	10	3.6
Deep blue sapphire, .	16	3.8	Tourmaline,	10	3.0
Do., paler,	17	3.8	Quartz,	10	2.7
Topaz,	15	4:2	Opal,	10	2.6
Whitish topaz,	14	3.2	Chrysolite,	10	3.7
Ruby spinell,	13	3.4	Zeolite,	8	2.1
Bohemian topaz,	11	2.8	Fluor,	7	3.2
Emerald,	12	2.8	Calcareous spar,	6	2.7
Garnet,	12	4.4	Gypsum,	5	2.3
Agate,	12	2.6	Chalk,	3	2.7
Onyx,	12	2.6		20	

#### Ductility and Malleability of Metals.

Ductility is the property of being drawn out in length without breaking. This property is possessed in a pre-eminent degree by gold and silver, as also by many other metals, by glass in the liquid state, and by many semi-fluid resinous and gummy substances. The spider and the silkworm exhibit the finest natural exercise of ductility, upon the peculiar viscid secretions from which they spin their threads. When a body can be readily extended in all directions under the hammer it is said to be malleable; and when into fillets, under the rolling press, it is said to be laminable.

There appears, therefore, to be a real difference between ductility and malleability; for the metals which draw into the finest wire are not those which afford the thinnest leaves under the hammer, or in the rolling press. Of this fact iron affords a good illustration. Among the metals permanent in the air seventeen are ductile and sixteen are brittle. But the most ductile cannot be wire-drawn or laminated to any considerable extent without being annealed from time to time during the progress of the extension, or rather the sliding of the particles alongside of each other, so as to

loosen their lateral cohesion.

# TABLE Of the Ratio of the Ductility and Malleability of Metals.

Metals ductile and malleable, in alpha- betical order.	Brittle metals in alphabetical order.	Metals in the order of their wire-drawing ductility.	Metals in the order of their laminable ductility
Cadmium. Copper. Gold. Iron. Iridium. Lead. Magnesium. Mercury. Nickel. Osmium. Palladium. Platinum. Potassium. Silver.	Antimony. Arsenic. Bismuth. Cerium? Chromium. Cobalt. Columbium. Iridium. Manganese. Molybdenum. Osmium. Rhodium. Tellurium. Titanium.	Gold. Silver. Platinum. Iron. Copper. Zinc. Tin. Lead. Nickel. Palladium? Cadmium?	Gold. Silver. Copper. Tin. Platinum. Lead. Zinc. Iron. Nickel. Palladium? Cadmium?
Sodium. Tin. Zinc.	Tungsten. Uranium.		Agenta - I

Conducting Powers of Various Substances.

The conducting power of wood is very low; the softer woods being lower in this respect than those which are harder. Of metals, and some other substances, the following is the order, according to Despretz:

CS DI CUZ .	The second secon
Gold, 1000	Tin, 304
Silver, 973	
Copper, 898	Marble, 24
Platinum, 381	Porcelain, 12
Iron, 374	Tile, 11
Zinc, 363	The state of the s

Radiating Power of Various Substances.

Bodies that have polished surfaces radiate heat less than those that are roughened, and metallic surfaces less than those of more imperfect conductors. The following are the proportions of some of each according to Leslie:

f each, according to Leslie:	armine of in the telling port
Lamp-black, 100	Rough lead, 45
Water, 100	Mercury, 20
Writing-paper, 98	Polished lead, 19
Glass, 90	Polished iron,
Tissue-paper, 88	Tin, silver, copper, and gold, 12
Too SK	and the land of th

#### Reflecting Powers of Various Substances.

Heat is reflected from the surface on which its rays fall, in the same manner as light; the angle of reflection being opposite and equal to that of incidence. The metals are the strongest reflectors of heat, in the following order, according to Leslie:

UI.	neat, in th	He forto with	g order, a	ccolding to heart.	
1	Brass, .	proper sort	. 100	Lead,	
5	Silver, .	out unit office	. 90	Tinfoil rubbed with mer.,	10
1	Tinfoil, .	paradot by D	. 85	Glass,	10
]	Block-tin,		. 85	Glass, waxed or oiled, .	5
5	Steel .	o. However,	70	Date - Alleran - Landau of	

Power of Various Substances to Transmit Heat.

All bodies capable of transmitting heat are, more or less, transparent, though their powers of transmitting heat and light are not in the same relative proportions; as the following list of the relative powers of equal masses, determined by Melloni, will show:

Air, 100	Rape-seed Oil, 2
Rock salt, transparent, . 92	Tourmaline, green, 7
Flint-glass, 67	Sulphuric Ether, 21
Bisulphuret of Carbon, . 63	Gypsum, 20
Calcareous spar, transparent, 62	Sulphurie Acid, 17
Rock-crystal, 62	Nitric Acid, 15
Topaz, brown, 57	Alcohol, 15
Crown-glass, 49	Alum, in crystals, 12
Oil of turpentine, 31	Water,

#### TABLE

Showing the Scale of Proofs for Chain Rigging close-linked, &c.; the extreme Length of Links not to exceed five diameters of their size in Iron.

Diam. of Links.	Testing Weight.	Max. Strain.	Minimum Strain.	Diam. of Links.	Test. Wght.	Maximum Strain.	Minimum Strain.	
Inches.	Tons.	Tons.	Tons. Cwt	Inches.	Tons	Tons.	Tons. Cwt.	
15/8	315	75	68 0	$\frac{11}{16}$	$5\frac{5}{8}$	14	13 10	
$1\frac{1}{2}$	27	64	58 0	58	45	12	10 15	
18	225	54	49 0	9 16	384	10	8\frac{8}{4} nearly.	
1‡	183	45	41 0	1/2	3	7.	_6_18	
11/8	$15\frac{1}{4}$	37	34 0	7 16	21	_6 _	.5 2	
1	12	30	28 0	8	15	4	3 0	
$\frac{15}{16}$	$10\frac{1}{2}$	26	25 0	$\frac{5}{16}$	11/8	3	2 14	
78	91	23	22 0	$\frac{9}{32}$	7 8	none broken.	none broken.	
$\frac{13}{16}$	77	20	20 0	1	3	184	1 14	
84	6 <u>8</u>	17	16 0	3 16	$\frac{13}{34}$	$1\frac{1}{10}$	0 19	

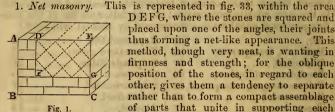
## MASONRY.

## Of the different kinds of Masonry.

Masonry, in the general acceptation of the term, is the art of cutting or squaring stones, to be applied to the purposes of build ing; or, in a more limited sense, it is the art of joining stones toge ther with mortar, or otherwise.

The ancients enumerate seven different methods in which they arranged the stones of their buildings. Vitruvius thus classes them: three of hewn or squared stones, threw of unhewn, and one

a mixture of both methods.

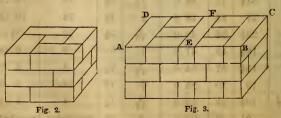


DEFG, where the stones are squared and placed upon one of the angles, their joints thus forming a net-like appearance. This method, though very neat, is wanting in firmness and strength; for the oblique position of the stones, in regard to each other, gives them a tendency to separate rather than to form a compact assemblage

of parts that unite in supporting each other. Whenever this form of masonry is employed, it is consequently necessary to keep the work together by a border of stones, having some other arrangement, one that is not only capable of supporting itself, but of overcoming the resistance of the net-like form. This is shown in the same figure at ABC; and where the network is merely a casing of stone to the brickwork of a wall, it will be found to answer tolerably well, and looks very neat.

2. Bound masonry is that represented in fig. 2, and is remarkably strong. The perpendicular joints in each course fall directly in the middle of the stones composing the course below and above it; and while it has every requisite of solidity, the joints have, at

the same time, a regular and pleasing appearance.

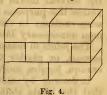


Greek masonry is that represented in fig. 3, where every alternate stone, as shown at AD, EF, and BC, is made of the whole thickness of the wall, and serves to bind together the stones

which compose the external and internal faces of the building; and this may be called double binding, as from the perpendicular joints being somewhat similarly situated to that in bound masonry, it has also an additional binding, by extending to the courses above and below it, thus forming a compact and durable wall, which resists every effort to separate in any direction.

4. Masonry by equal courses. This method of uniting stones is shown in fig. 4, and only differs from the bound masonry in its

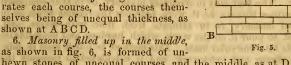
snown in 1g. 4, and only differs from the being composed of unhewn stones, or rather in being formed of stones that are not so accurately cut, nor the edges so perfectly squared; it being only necessary that the external face should be level, and the horizontal joints at equal distances from each other, care being taken at the same time that the perpendiculars are so situated as to bind the courses above and below them.



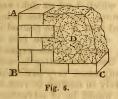
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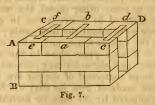
5. Masonry by unequal courses. This is represented in fig. 5, and is, like the last, formed of unhewn stones, without any regularity

as to their size, it being sufficient that each course is made to bind with the preceding, and the only regularity observed is in the joining which separates each course, the courses themselves being of unequal thickness, as shown at ABCD.



hewn stones of unequal courses, and the middle, as at D, is filled up with stones thrown in at random among the mortar.





7. Compound masonry is, as its name imports, a mixture of the other kinds. It is represented in fig. 7, where the external course AB is formed of bound masonry, and the corresponding internal course is at some distance from it, but held to the former by means of iron cramps, as shown at a, b, c, d, c, f, the space between being filled in with small stones or flints thrown into the mortar.

## The Methods of Joining Stone.

As the strength and durability of masonry depend as much on the method employed, and the care taken in making all the joints to correspond accurately with each other, as in the quality of the material employed, some remarks will be required in explanation of the methods of joining stone. We shall, therefore, enumerate the several means adopted by workmen, and, where necessary notice the purposes to which each method is best adapted, giving some cautions to secure success in practice, and to save the workman unnecessary labor and trouble.

The joints in masonry are either secured by the means of mortar, cement, or plaster of Paris, or the courses are held together by

cramps, joggles, mortice, and tenoning, or dovetailing.

1. Joining by mortar, or cements. It is absolutely necessary that the joints should be perfectly smooth, and touch in every part; and the stones must be so square as to bed well on each other, that is to say, they must not have such irregular faces as to roll, or, in technical terms, be winding to each other. The greatest care must be taken by the workman to have his mortar of a proper consistence—not too thin, as in drying it would shrink from the work, nor too thick, for that would prevent the stones from bedding properly. The best way in irregular masonry, or in that composed of small stones thrown, as it were, between the regular work, as in compound masonry, is to saturate fresh lime with water, and, while hot, to pour it on the work, which hardens and consolidates the whole into one solid mass. This method is much used in joining soft stones and brickwork, and is calculated to promote the strength and solidity of the work.

2. Joining by cramps. Cramping is performed by inserting into the two pieces of stone, which are to be bound together, a piece of iron or some other metal, the ends of which, bent at right angles, are inserted in a cavity cut in each stone, the cavities being so large as to admit the iron easily; melted lead is then poured in to fill the vacant space, and, when cold, a chisel is driven into it, so that it may press close to the work; for all metals expand by fusion, and obstacles may prevent them from contracting in cooling. Cramps composed of copper are, in many cases, very preferable to those made of iron, for they are less likely to oxidize, or rust, or to be affected by the lime or mortar. It would be of advantage to coat the cramps, if made of iron, with some substance that would defend them from the effects of damp. We may here remark, that the channel made to receive the cramp should be dovetailed, to prevent the lead from coming out, which it is otherwise apt to do, in the course of time. The only objection to the use of copper cramps, in preference to iron, is their expense, which in large public works is not of any importance, and, for common purposes, iron answers very well; but the more malleable or tough the iron

the better it is, as it is more calculated to resist the different tem-

peratures to which the work may be exposed.

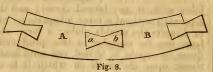
3. Joining by joggles. The method of securing the joints of masonry by means of joggles is chiefly adopted for securing the joints of columns or pillars; and consists in sinking a cavity in the two pieces in such a manner as to make them correspond with each other, and inserting in that cavity a piece of metal, stone, or even wood, so that any lateral thrust may not be able to separate them. This method may, with very great advantage, be applied in the construction of domes, and works of the same nature, where it is necessary to avoid the lateral thrust as much as possible.

We may here take the opportunity of mentioning a plan proposed by Dr. Hutton, in his edition of Oznamare's Mathematical Recreations, for taking away the lateral thrust of domes and cupolas. The following is the problem proposed, and the solution given:

"How to construct a hemispherical arch, or what the architects call an arc en cul-de-four, which shall have no thrust on its piers.

"Let A B, fig. 8, be two contiguous voussoirs, which we will suppose to be three feet in length, and eighteen inches in breadth.

Cut out on the contiguous sides two cavities, in the form of a dovetail, four inches in depth, with an aperture of the same extent, a, b, five or six



inches in length, and as much in breadth. This cavity will serve to receive a double key of cast-iron, as shown in fig. 9, or of common forged-iron, which is still more secure, as it

common forged-iron, which is still more secure, as it is not so brittle. These two voussoirs will thus be connected together in such a manner that they cannot be separated without breaking the dovetail at the re-entering angle; but, as each of its dimensions

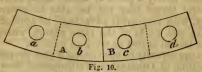


the re-entering angle; but, as each of its dimensions in this place will be four inches, it will be easily seen that an immense force would be required to produce that effect; for we are taught, by well-known experiments on the strength of iron, that it requires a force of four thousand five hundred pounds to break a bar of forged iron an inch square, by the arm of a lever of six inches; consequently, two hundred and eighty-eight thousand pounds would be necessary to break a bar of sixteen square inches, like that in question. Hence there is reason to conclude, that these voussoirs will be connected together by a force of two hundred and eighty-eight thousand pounds; and as they will never experience an effort to disjoin them nearly so great, as might easily be proved by calculation, it follows that they may be considered as one piece."

They might be still further strengthened in a very considerable degree, for the height of these dovetails might be made double, and

a cavity might be cut in the middle of the bed of the upper voussoir, fit to receive it entirely: the dovetail could not then be broken without breaking the upper voussoir also; but it may be easily seen that, to produce this effect, an immense force would be required.

The second method proposed by Dr. Hutton is more properly by



the aid of joggles. Let A and B, fig. 10, be two contiguous voussoirs, and C, fig. 11, the inverted voussoir of the next course, which ought to cover the

joint between A and B. Each of the voussoirs A and B being divided into two parts as ab and cd: then



divided into two parts, as ab and cd; then if at ab and cd we sink an hemispherical cavity, in which to introduce a globe of very hard marble, and in the upper voussoir, fig. 10, we sink similar cavities, bc; this, when laid on bc, fig. 11, will form a secure

joint without any lateral thrust; and the two courses cannot be separated without a force adequate to either break the solid stone, or disunite the marble globe; a force almost inconceivable, or at least one far superior to that produced by the arch; the whole dome, or cupola, is, in fact, one solid mass, and can exert no lateral thrust upon the walls on which it is raised. Marble globes are recommended, because iron is liable to rust; but, if the joggles were made of iron, and covered with pitch before they were placed in the cavities, there would be little to fear from rust; and particularly as the iron is inclosed in the substance of the stone, and quite excluded from the action of atmospheric causes.

Little need be said in this place as to morticing and tenoning, or dovetailing, except that they differ slightly from the same operations in joiners' work; for, as cement is used in the joining, they need not be so accurately cut, and are made shorter and thicker than those formed by the joiner, it being sufficient that the parts of each piece to be joined enter into each other at most five or six inches, even in large masses of stone. In small pieces, an inch or an inch and a half is sufficient; for, if the tenon or dovetail be too long, it will decrease the solidity of the joint. For greater security, a small channel is frequently cut in the shoulder of the joint, and melted lead is poured into it, which, filling up the space round the tenon or dovetail, makes the joint more secure, and the work firm and solid.

In laying some sorts of stones, it is desirable, as far as possible, to place them in the same direction as they had when in the quarry, or, as it is termed by workmen, bedways of the stone; for, if laid in other directions, they are liable to peel and split by the action of the atmosphere.

# BRICKLAYING.

#### Foundations.

The best soils for building upon are gravel, chalk, and stone rock.

Those most to be guarded against are sands, bog earth, clays, and made earth (no matter how hard). Where these occur, avoid piling (except in water works); plank the foundations through the centre of the walls, place long tassels in the piers, lay in chain bond, let the plates be stout, and in one piece, the whole length of each wall; all that is required is to so bind the building that it may settle altogether, and not partially.

In doubtful foundations, it is advisable to have a trench dug out to the depth of 2 feet to 3 feet below the footings of the brickwork, and about twice the width of the footings, which is to be filled up with concrete, composed of stone lime ground and ballast, or coarse gravel, to be mixed with water, in the proportion of one of lime to five or six of gravel; immediately that it is made up it must be shot into the trench from a stage, 6 feet above, which will cause it to fall in a solid mass; and in a few hours afterwards it will be as firm as a rock.

It is strongly recommended to have good plates; whatever may be slighted in other parts these should not be neglected—they are the soul and support of a building, and cannot, if put in too small, be taken out and replaced, as other timbers may; the difference in large houses will rarely amount to twenty-five dollars.

Bond the work—English bond—using all whole bricks, a course

of stretchers and headers alternately.

Particular care must be taken that all the internal joints of brickwork are well flushed up with mortar; too frequently the workmen are apt to neglect doing it; the consequence is, that all the interior joints are hollow, and allow the damp to penetrate to the inside, no matter how thick the wall may be. Another serious defect in brickwork is in not properly bonding the facing to the backing, particularly if the facing be malms or bricks, which cost an extra price; generally the headers are only bats or half bricks, instead of being a stretcher or a whole brick to bond in with the brickwork at the back; there ought to be at least one stretcher in every 3 feet to each course, if there be not the wall will split or divide into two thicknesses.

In building arches of a large span, it is advisable to build them in half brick rims, with vertical or radiating bond every 3 or 4 feet in the girt; if this latter precaution be not adopted, the consequence will be, that when the centre is struck, the rims will divide and weaken the arch, and perhaps cause a total failure.

In selecting bricks, clap them together-if they ring well, and,

when broken, show that they are burnt through, they will answer the purpose. A hard clamp burnt gray stock is all that is wanted for strength; for water-works and foundations use clinker burnt marl stocks. Avoid samnel or place bricks, and chuffy stocks, and

generally prefer hand tempering to pugging the clay.

In mixing of mortar, it is advisable to see that the laborer properly turns up the mortar, and that the lime is thoroughly incorporated with the sand throughout; avoid using too much water, as it drowns the lime and weakens it; in large works it is best to mix the lime and sand in a mill—cement must be mixed in small quantities.

TABLE

Showing the Quantity of Earth to be removed, the Number of Bricks and Gallons in one foot in depth or length.

Diam.	1 I	Brick rin	1.	1,1	1.050		
in the clear.	e		Feet cube	Number of bricks.		Contents in gallons.	
ft, in.	digging.	laid dry.	in mortar	digging.	laid dry.	in mortar	of other
			a vent	of Louisian	0.0 -17	Jumedie	9/3/1
0 9	1 8	23	19	4 0	60	50	23/4
1 0	2 4	28	23	4 9	70	58	5
1 3	3 1	33	27	5 9	80	66	71
1 6	4 0	38	31	7 1	90	74	11
1 9	4 9	43	35 _	8 3	102	82	15
2 0	5 9	48	41	9 6	112	92	193
2 3	7 1	53	44	11 0	122	100	25
$\begin{array}{c c}2&6\\3&0\end{array}$	8 3	58	48	12 6	132	108	301
3 0	11 0	68	57	15 9	154	126	44
3 6	14 2	79	65	19 6	174	142	60
4 0	17 7	89	73	23 8	194	159	78
4 6	-21 6	100	82	28 3	214	176	100
5 0	26 0	110	90	33 2	234	192	122
5 6	30 7	120	98	38 5	254	209	149
6 0	35 8	130	107	44 2	276	226	176
6 6	41 3	140	115	50 3	296	242	206
7 0	47 2	150	123	56 7	316	260	239
7 6	53 5	160	131	63 6	336	276	275
8 0	60 1	170	140	70 9	358	292	313
8 6	67 2	180	148	78 5	378	308	354
9 0	74 7	191	156	86 6	398	326	396
10 0	90 8	212	174	103 9	438	360	489
3011 30	403.00	to Dance		adven la	1 1-15	tiv to Am	N Day

In the measurement of brickwork no allowance is to be made in quantity for small or difficult works.

Flues to be measured solid.

Timbers inserted in walls not to be deducted.

Two inches to be allowed for bedding plates, where no brick-work is over them.

All cuttings to be measured superficially, excepting to bird's mouths

and squint quoins, which are to be run.

The net quantity of brickwork being found, it is to be reduced to the standard thickness of a brick and a half, and brought into

statute rods of 5½ yards square, or 272 superficial.

Ovens, coppers, and solid walls, of irregular thickness, to be cubed and brought into the standard thickness, by multiplying by 8 (the number of  $1\frac{1}{2}$  inches in a foot), and dividing by 9 (the number of  $1\frac{1}{2}$  inches in a brick and a half, or  $13\frac{1}{2}$  inches, the standard thickness).

Facings of all descriptions to be measured and charged extra, per

foot superficial.

272 feet superficial is a rod of brickwork,  $1\frac{1}{2}$  brick, or  $13\frac{1}{2}$  inches thick, the standard thickness, to which all brickwork, of whatever thickness, is reduced.

306 cubic feet, or 111 cubic yards, equal to 1 rod of reduced

brickwork.

4352 stock bricks to 1 rod reduced, 4 courses 1 foot high.

4533 ditto, if the 4 courses measure 111 inches high.

These calculations are without allowing any waste, which is more than amply compensated in dwelling-houses, by not deducting flues and bond timber; in such work, 4300 stocks, or 4500 place, are sufficient.

5371 bricks laid dry to 1 rod.

4900 ditto in wells and circular cesspools.

A rod of brickwork contains 235 feet cube of bricks, and 71 feet of mortar (4 courses to a foot); which will weigh, upon an average

calculation, 15 tons.

A rod of brickwork requires 1½ cubic yard of chalk lime, and 3 single loads or yards of drift; or 1 cubic yard of stone lime, and 3½ single loads or yards of sand; or 36 bushels of cement, and 36 of sharp sand.

16 bricks to a foot of reduced brickwork.

7 ditto to a foot super of facing.

10 ditto to a foot super of gauged arches.

30 bricks on edge, and 45 bricks flat, to 1 yard of brick-nogging.

36 stocks laid flat, and 52 ditto on edge, to 1 yard of paving.

36 paving bricks laid flat, and 82 ditto on edge, ditto.

A load of mortar, 27 feet cube, requires 9 bushels of lime and 1 yard of sand. A hod contains 20 bricks.

Lime and sand loses one third of its bulk when made into mortar

-likewise cement and sand.

The proportion of mortar, or cement, when made up, to the lime, or cement and sand before made up, is as 2 to 3.

Lime, or cement and sand, to make mortar, require as much water as is equal to one third of their bulk, or about 5½ barrels for a rod of brickwork built with mortar.

## PLASTERING.

Thickness of Compo.	Inch yards.	% inch yards.	% inch yds.
1 bushel of cement will cover	$1\frac{1}{7}$	$1\frac{1}{2}$	. 21
1 do. and 1 of sand do.	$2\frac{1}{4}$	. 3	$4\frac{1}{2}$
1 do. and 2 do. do.	$3\frac{1}{3}$	$4\frac{1}{2}$	$6\frac{8}{4}$
1 do. and 3 do. do.	$4\frac{1}{2}$	. 6	. 9

(3 inch is the usual thickness.)

1 cwt. of mastic and 1 gallon of oil . . .  $1\frac{1}{2}$  . . .  $2\frac{1}{2}$ 

1 cubic yard of chalk lime, 2 yards of road drift or sand, and 3 bushels of hair, will cover 75 yards of render and set on brick, and 70 yards on lath, or 65 yards plaster and render 2 coats and set on brick, and 60 yards on lath; floated work will require about the same as 2 coats and set.

1 bundle of laths and 500 nails will cover about 4½ yards.

#### Mortar.

1 hundred of lime contains 25 striked bushels, or 100 pecks. It is a measure 3 feet square, and 3 feet 1 inch deep. 1 chaldron of lime is equivalent to 57.765 cubic feet, or rather more than 2 hundred.

18 heaped bushels, 22 striked bushels, or 1 yard cube, a single load of sand, mortar, &c.

1 double load is equal to 36 heaped bushels.

1 hod of mortar is equal to 1134 cubic inches, or 8 duodecimal inches, or  $9 \times 9$ , and 14 inches long.

2 hods of mortar make a bushel nearly.

#### Cement.

1 barrel of cement is 5 bushels, and weighs 3 cwt. 1 rod of brickwork, in cement, requires 36 bushels of cement and 36 bushels of sand.

1 yard, or 9 feet superficial of 14 inches, or 1½ brickwork, in cement, requires about 2½ bushels.

1 yard superficial of pointing to brickwork, in cement, requires

about one eighth of a bushel.

1 yard square of plastering, in cement, requires three fourths of a bushel.

Carpentry and Plastering are measured by the square foot or yard; or, in moulded and ornamental work, by the linear foot. In extensive work the square of 100 feet is also used.

Paving is measured by the square yard.

## Digging, &c.

 $23\frac{1}{2}$  cubic feet of sand,  $17\frac{1}{3}$  ditto clay, 18 ditto earth, 13 ditto chalk, equal to a ton.

A cubic yard of earth, before digging, will occupy about 11

cubic yard when dug.

27 cubic feet, or 1 cubic yard, contains 21 striked bushels, which is considered a single load, and double these quantities a double load.

18 cubic feet of night soil, 1 ton.

2½ tons of ditto is the quantity a cart contains; 6 feet long, 3 feet 3 inches wide, by 2 feet 4 inches deep, or 45 feet cube.

#### Coarse Stuff.

Coarse stuff, or lime and hair, as it is sometimes called, is prepared in the same way as common mortar, with the addition of hair procured from the tanner, which must be well mixed with the mortar by means of a three-pronged rake, until the hair is equally distributed throughout the composition. The mortar should be first formed, and when the lime and sand have been thoroughly mixed, the hair should be added by degrees, and the whole so thoroughly united that the hair shall appear to be equally distributed throughout.

## Fine Stuff.

This is made by slaking lime with a small portion of water, after which so much water is added as to give it the consistence of cream. It is then allowed to settle for some time, and the superfluous water is poured off, and the sediment is suffered to remain till evaporation reduces it to a proper thickness for use. For some kinds of work it is necessary to add a small portion of hair.

#### Stucco for Inside of Walls.

This stucco consists of fine stuff already described, and a portion of fine washed sand, in the proportion of one of sand to three of fine stuff. Those parts of interior walls are finished with this stucco which are intended to be painted. In using this material, great care must be taken that the surface be perfectly level, and to secure this it must be well worked with a floating tool or wooden trowel. This is done by sprinkling a little water occasionally on the stucco, and rubbing it in a circular direction with the float, till the surface has attained a high gloss. The durability of the work very much depends upon the care with which this process is done, for if it be not thoroughly worked it is apt to erack.

#### Gauge Stuff.

This is chiefly used for mouldings and cornices which are run or formed with a wooden mould. It consists of about one fifth of plaster of Paris, mixed gradually with four fifths of fine stuff. When the work is required to set very expeditiously, the proportion of plaster of Paris is increased. It is often necessary that the plaster to be used should have the property of setting immediately it is laid on, and in all such cases gauge stuff is used, and consequently it is extensively employed for cementing ornaments to walls or ceilings, as well as for casting the ornaments themselves.

## Higgins' Stucco.

To fifteen pounds of the best stone lime add fourteen pounds of bone ashes, finely powdered, and about ninety-five pounds of clean, washed sand, quite dry, either coarse or fine, according to the nature of the work in hand. These ingredients must be intimately mixed, and kept from the air till wanted. When required for use, it must be mixed up into a proper consistence for working with lime water, and used as speedily as possible.

#### Parker's Cement.

This cement, which is perhaps the best of all others for stucco, as it is not subject to crack or flake off, is now very commonly used, and is formed by burning argilfaceous clay in the same manner that lime is made; it is then reduced to powder, by the process described in a previous part of this work. The cement, as used by the plasterer, is sometimes employed alone, and sometimes it is mixed with sharp sand; and it has then the appearance, and almost the strength, of stone. As it is impervious to water, it is very proper for lining tanks and cisterns.

#### Hamelein's Cement.

This cement consists of earthy and other substances insoluble in water, or nearly so; and these may be either those which are in their natural state, or have been manufactured, such as earthenware and china; those being always preferred which are least soluble in water, and have the least color. When these are pulverized, some oxide of lead is added, such as litharge, gray oxide, or minium, reduced to a fine powder; and to the compound is added a quantity of pulverized glass or flint stones, the whole being thoroughly mixed and made into a proper consistence with some vegetable oil, as that of linseed. This makes a durable stucco or plaster, that is imprevious to wet, and has the appearance of stone.

The proportion of the several ingredients is as follows:—to every five hundred and sixty pounds of earth, or earths, such as pit sand, river sand, rock sand, pulverized earthenware or porcelain, add forty pounds of litharge, two pounds of pulverized glass or flint, one pound of minium, and two pounds of gray oxide of lead. Mix

the whole together, and sift it through sieves of different degrees of fineness, according to the purposes to which the cement is to be

applied.

The following is the method of using it:—To every thirty pounds' weight of the cement in powder add about one quart of oil, either linseed, walnut, or some other vegetable oil, and mix it in the same manner as any other mortar, pressing it gently together, either by treading on it, or with the trowel; it has then the appearance of moistened sand. Care must also be taken that no more is mixed at one time than is required for use, as it soon hardens into a solid mass. Before the cement is applied, the face of the wall to be plastered should be brushed over with oil, particularly if it be applied to brick, or any other substance that quickly imbibes the oil; if to wood, lead, or any substance of a similar nature, less oil may be used.

#### Maltha, or Greek Mastic.

This is made by mixing lime and sand in the manner of mortar, and making it into a proper consistency with milk or size, instead of water.

#### Plaster in imitation of Marble.

This species of work is exquisitely beautiful when done with taste and judgment, and is so like marble to the touch, as well as appearance, that it is scarcely possible to distinguish the one from the other. We shall endeavor to explain its composition, and the manner in which it is applied; but so much depends upon the workman's execution, that it is impossible for any one to succeed in an attempt to work with it without some practical experience.

Procure some of the purest gypsum, and calcine it until the large masses have lost the brilliant sparkling appearance by which they are characterized, and the whole mass appears uniformly opaque. This calcined gypsum is reduced to powder, and passed through a very fine sieve, and mixed up, as it is wanted for use, with Flanders glue, isinglass, or some other material of the same kind. This solution is colored with the tint required for the scagliola, but when a marble of various colors is to be imitated, the several colored compositions required by the artist must be placed in separate vessels, and they are then mingled together in nearly the same manner that the painter mixes his color on the pallet. Having the wall or column prepared with rough plaster, it is covered with the composition, and the colors intended to imitate the marble, of whatever kind it may be, are applied when the floating is going on.

It now only remains to polish the work, which, as soon as the composition is hard enough, is done by rubbing it with pumice-stone, the work being kept wet with water applied by a sponge. It is then polished with Tripoli and charcoal, with a piece of fine linen, and finished with a piece of felt, dipped in a mixture of oil

and Tripoli, and afterwards with pure oil.

#### Composition.

This is frequently used, instead of plaster of Paris, for the ornamental parts of buildings, as it is more durable, and becomes in time as hard as stone itself. It is of great use in the execution of the decorative parts of architecture, and also in the finishings of picture frames, being a cheaper method than carving, by nearly

eighty per cent.

It is made as follows: Two pounds of the beek whitening, one pound of glue, and half a pound of linseed oil are heated together, the composition being continually stirred until the different substances are thoroughly incorporated. Let the compound cool, and then lay it on a stone covered with powdered whitening, and heat it well until it becomes of a tough and firm consistence. It may then be put by for use, covered with wet cloths to keep it fresh. When wanted for use it must be cut into pieces, adapted to the size of the mould, into which it is forced by a screw press. The ornament, or cornice, is fixed to the frame or wall with glue, or with white lead.

## To make Glass Paper.

Take any quantity of broken glass (that with a greenish hue is the best), and pound it in an iron mortar. Then take several sheets of paper, and cover them evenly with a thin coat of glue, and, holding them to the fire, or placing them upon a hot piece of wood or plate of iron, sift the pounded glass over them. Let the several sheets remain till the glue is set, and shake off the superfluous powder, which will do again. Then hang up the papers to dry and harden. Paper made in this manner is much superior to that generally purchased at the shops, which chiefly consists of fine sand. To obtain different degrees of fineness, sieves of different degrees of fineness must be used.

#### To make Stone Paper.

As, in cleaning wood-work, particularly deal and other soft woods, one process is sometimes found to answer better than another, we may describe the manner of manufacturing a stone paper, which, in some cases, will be preferred to sand paper, as it produces a good face, and is less liable to scratch the work. Having prepared the paper as already described, take any quantity of powdered pumice-stone, and sift it over the paper through a sieve of moderate fineness. When the surface has hardened, repeat the process till a tolerably thick coat has been formed upon the paper, which, when dry, will be fit for use.

# WOODWORK, CARPENTRY, &c.

#### Decay of Wood.

Some woods decay much more rapidly than others; but they will all, in some situations, lose their fibrous texture, and with it their properties. To ascertain the causes which act upon woods, and effect their destruction, is an important object both to the builder and to the public.

## Cause of the Decay of Timber.

All vegetable as well as animal substances, when deprived of

life, are subject to decay.

If the trunk or branch of a tree be cut horizontally it will be seen that it consists of a series of concentric layers, differing from each other in color and tenacity. In distinct species of trees these layers present very different appearances, but in all cases the outer rings are more porous and softer than the interior. Wood is essentially made up of vessels and cells, and the only solid parts are those coats which form them. These vessels carry the sap which circulates through the tree, gives life and energy to its existence. and is the cause of the formation of leaves, flowers, and fruit. But when the tree is dead, and the sap is still in the wood, it becomes the cause of vegetable decomposition by the process of FERMENTATION. There are five distinct species of vegetable fermentation—the saccharine, the coloring, the vinous, the acetous, and the putrefactive. We are indebted to Mr. Kyan for the discovery that albumen is the cause of putrefactive fermentation, and the subsequent decomposition of vegetable matter.

#### Circumstances favorable to Vegetable Decomposition.

Wood is not equally liable to decay under all circumstances. When thoroughly dried it is not so quickly decomposed as when in its green state, for in the latter condition it has in itself all the elements of destruction, and it is scarcely possible to prevent the effect if it be then used in building. But supposing the timber to be perfectly seasoned, it is more liable to decay under some circumstances than in others. Timber is most durable when used in very

dry places.

When timber is constantly exposed to the action of water, the decomposition effected will depend upon the nature and chemical composition of the substance. A portion of wood may be soluble in water, but other parts are not; so that after a definite period, the continued action of water upon a piece of timber ceases, and it can sustain the influence of this cause until that period there is no termination to its endurance, except from those casualties which it might have been able to bear in its original state, but cannot after the removal of that portion of its substance soluble in water.

Should a piece of timber that has been for a long time exposed to water be brought into the air and dried, IT WILL BECOME BRITTLE AND USELESS.

When wood is alternately exposed to the influence of dryness and moisture it decays rapidly. It appears, from experiments, that after all the matter usually soluble in water has been removed, a fresh maceration and contact of the air produces a state of matter in that which is left which renders it capable of solution. A piece of timber may then in this manner be more and more decomposed, until at last the whole mass is destroyed. The builder is sometimes compelled to use wood in places where it will be exposed to alternate dryness and moisture; fencing, weather boarding, and other works, are thus exposed. In all these cases he may anticipate the destructive process, and provide against it. The wood used in such situations should be thoroughly seasoned, and then painted or tarred; but, if it be painted when not thoroughly seasoned, The DESTRUCTION WILL BE HASTENED, for the evaporation of the contained

vegetable juices is prevented.

There is one other circumstance to be considered—the influence of moisture associated with heat. Within certain limits the decomposition resulting from moisture increases with the temperature. The access of the air is not absolutely necessary to the carrying on of this process, but water is; and as it goes on, carbonic acid gas and hydrogen gas are given off. The woody fibre itself is not free from this decomposition, for, as the carbonaceous matter is abstracted by fermentation, it becomes more susceptible of this change. This statement is proved by the circumstance, that when quicklime is added to the moisture the decomposition is accelerated, for it abstracts carbon; but the carbonate of lime produces no such effect: a practical lesson may be learnt from this fact; if timbers be bedded in mortar, decomposition must follow, for it is a long time before it can absorb sufficient carbonic acid to neutralize the effect, and the dampness which is collected by contact with the wet mortar increases the effect. When the wood and the lime are both in a dry state no injury results, and it is well known that lime protects wood from worms.

When the destructive process first becomes visible it is by the swelling of the timber, and the formation of a mould or fungus upon its surface. This fungus or cryptogamic plant rapidly increases, and soon covers over the whole surface of a piece of timber, having a white, grayish-white, or brownish hue. When the seeds of destruction are thus once sown they cannot be readily eradicated. Heat and moisture may be considered the prominent causes of the rapid decomposition of vegetable substances. When wood is completely and constantly covered with water this effect is not produced; and we have an example in the fact, that, although those parts of a vessel which are subject to an occasional moisture are liable to dry rot, yet those parts which are constantly beneath the water are not ever thus affected; and although the head of a pile, which may be now and then wetted by the casual rise of the tide,

and is then dried again by the sun, may be decomposed, yet those parts which are always covered with water have been found in a solid state after CENTURIES of immersion.

## Means of Preventing Decay.

Something may be done towards the prevention of decay by felling the timber at a proper season. A tree may be felled too soon or too late, in relation to its age and to the period of the year. A tree may be so young that no part of it shall have the proper degree of hardness, and even its heart-wood may be no better than sap-wood; or a tree may be felled when it is so old that the wood, if not decayed, may have become brittle, losing all the elasticity of maturity. The time required to bring the several kinds of trees to maturity varies according to the nature of the tree and the situation in which it may be growing. Authors differ a century as to the age at which oak should be felled, some say one hundred, and others two hundred years; it must, then, be regulated according to circumstances.

But it is also necessary that the timber trees should be felled at a proper season of the year; that is to say, when their vessels are least loaded with those juices which are ready for the production of sap-wood and foliage. The timber of a tree felled in spring or in autumn would be especially liable to decay; for it would contain the element of decomposition. Midsummer and midwinter are the proper times for cutting, as the vegetative powers are then ex-

pended.

There are some trees, the bark of which is valuable, as well as the timber; and as the best time for felling is not the best for stripping the bark, it is customary to perform these labors at different periods. The oak-bark, for instance, is generally taken off in early spring, and the timber is felled as soon as the foliage is DEAD; and this method is found to be highly advantageous to the durability of the timber. The sap-wood is hardened, and all the available vegetable juices are expended in the production of foliage. Could this plan be adopted with other trees, it would be desirable; but the barks are not sufficiently valuable to pay the expense of stripping.

### Seasoning Timber.

Supposing all these precautions to be taken in felling timber, it is still necessary to season it; that is, to adopt some means by which it may be dried, so as to throw off all the juices which are still associated with the fibres of the wood. As soon as the timber is felled, it should be removed to some dry place; and, being piled in such a manner as to admit a circulation of air, remain in log for some time, as it has a tendency to prevent warping. The next process is to cut the timber into scantlings, and to place these upright in some dry situation, where there is a good current of air, avoiding the direct rays of the sun. The more gradually the

process of seasoning is carried on, the better will be the wood for all the purposes of building. Mr. Tredgeld says, "It is well known to chemists, that slow drying will render many bodies less easy to dissolve; while rapid drying, on the contrary, renders the same bodies more soluble. Besides, all wood, in drying, loses a portion of its carbon, and the more in proportion as the temperature is higher. There is in wood that has been properly seasoned a toughness and elasticity which is not to be found in rapidly dried wood. This is an evident proof that firm cohesion does not take place when the moisture is dissipated in a high heat. Also, seasoning by heat alone, produces a hard crust on the surface, which will scarcely permit the moisture to evaporate from the internal part, and is very injurious to the wood.

"For the general purposes of carpentry, timber should not be used in less than two years after it is felled; and this is the least time that ought to be allowed for seasoning. For joiners' work it requires four years, unless other methods be used; but, for carpentry, natural seasoning should have the preference, unless the

pressure of the air be removed."

Many artificial methods of seasoning timber have been proposed; and a brief notice of some of those which have been found most useful will be required.

## Seasoning by a Vacuum.

All the vegetable and animal juices are kept in their particular vessels by the pressure of the atmosphere: remove that pressure, and the animal fluids could no longer be retained by the veins and arteries; and the vegetable fluids would exude and appear on the surface of the plant. Place a small piece of wood beneath the receiver of an air-pump, and exhaust the air, and in a short time the wood will be covered with drops of the liquid which can no longer be retained, as the atmospheric pressure is removed. Mr. Langton thought that this might be applied to the extraction of those vegetable juices in timber, known to be the cause of its decay. An arrangement was therefore adopted, by which large masses of timber might be inclosed in a vessel having such machinery as would be necessary to exhaust the air, heat being at the same time employed so as to vaporize the exuded juices. vapor is conveyed away by pipes surrounded by cold water, and is condensed into liquid having a sweet taste. This process is deserving of more attention than has hitherto been given to it.

### Water Seasoning.

It has been stated, by various writers, that wood immersed in water for about a fortnight, and then dried, is better suited for all the purposes of the joiner. There can be no doubt that immersion in water tends to neutralize the effect of the saccharine matter, by dilution or an almost absolute removal. This process has also the effect of rendering the wood less liable to crack and warp; but, if

we judge by Duhamel's experiments, it injures the strength of the material, and should not, therefore, be adopted in any instance where the timber is to be employed by the carpenter. Evelyn recommends boards that are to be used for flooring to be seasoned in this way: "Lay your boards," he says, "a fortnight in water, (if running the better, as at a mill-pond head;) and then setting them upright in the sun and wind, so as it may pass freely through them, turn them daily; and thus treated, even newly-sawn boards will floor far better than those of a many years' dry seasoning, as they call it." Timber intended for ship building may be immersed in sea water; but that which is to be used for houses ought to be placed in fresh water; for if timber, or any other building material, be impregnated with salt, it will ever be wet, for salt attracts moisture so readily that it may be used approximately as a hygrometer. Plaster or mortar made with salt water will always sweat with a moist atmosphere; and timber intended for the house carpenter, if impregnated with salt, will always be damp, or covered with a crystallized efflorescence. Much injury, however, is sometimes done by not thoroughly immersing the timber; the carpenter should therefore be careful when he employs this method of seasoning, that the timber is entirely covered with water, and that it be not exposed to its action for too long a time.

## Seasoning by Smoking and Charring.

Authors who have written upon the seasoning of timber have spoken of the effects of smoke, and the carbonization of the surface. We have adopted the same arrangement, but it will be necessary to caution the reader against a misconception of a very inaccurate expression. Timber cannot be seasoned by either smoking or charring, but seasoned timbers may be made more capable of resisting the effects of certain situations by these processes. Should a piece of timber, containing the vegetable juices, be smoked or charred, it would be a means of accelerating decomposition; for preventing all means of evaporation, the common sources of protection would become sources of destruction. But when timber is to be used in situations where it is liable to be attacked by worms, or to produce fungi, it may be desirable to smoke or to char it.

## Seasoning by Boiling or Steaming.

Timber is sometimes seasoned by steaming or boiling, both of which means are frequently adopted by ship-builders. The strength of timber appears to be somewhat impaired by these processes, but it is generally less liable to shrink or crack. Duhamel states that he boiled a piece of wood, and then dried it upon a stove, but in drying it, it lost part of its substance, as well as the water contained, and, upon a repetition, he found that it had lost still more of its weight. Four hours' exposure to steam or boiling water is sufficient for timbers of ordinary dimensions, and the drying afterwards goes

on very rapidly, but it should be done as gradually as possible. The joiner frequently finds it necessary to steam or boil wood, to bend it into a particular curve, and also the ship-builder. It has been stated by writers on ship-building, that boiling increases the durability of timber; and, in proof of this, they inform us that the planks in the bow of a ship, which are bent in this way, are never

affected by the dry rot.

It may now be inquired whether, after the most perfect seasoning, timber is secured against the process of decay? To this question a negative answer must be given. However well the timber may be seasoned, it will certainly rot if placed in a damp situation. the rapidity of the decomposition depending upon the nature and state of the wood, and the activity of the destroying agent. As the builder seldom attempts any other seasoning than that which depends upon drying his timbers, it is absolutely necessary that he should carefully avoid the rise of damp, and adopt every means in his power to prevent this evil. Timbers are usually placed in contact with walls, but it must not be supposed that this is sufficient to keep them from the access of damp, for they are frequently the conducting media. Brickwork very readily absorbs moisture, and also throws it upwards, so that the ends of timbers are in contact with the very source of mischief. To prevent the rise of damp upwards, it is common to use, for a few feet above the foundations, cement, a substance impervious to water, instead of mortar, or to place between the courses zinc or slate. But that these plans may be effective, the basement walls should be surrounded with an open area, for, if in contact with the earth on their sides, they can be of no value. To prevent dampness from entering in front, the brickwork should be covered with compo, or some substance impermeable to water.

Another thing to be considered, for the security of timbers, is to arrange, in every plan of a building, for a perfect circulation of air. Ventilation is a most important requisite in the construction of a building, although it is generally a matter of very little importance in the consideration of those who have to plan or construct buildings. The ventilation of roofs is by no means difficult, but there are often so many obstacles to the ventilation of flooring that the designer will not give sufficient attention to his subject to provide against them. These things, however, are not matters of speculation, to be attended to by those who have no higher employment, but are absolutely necessary for the construction of a work that is

intended to survive the builder.

The attention of scientific men has been recently directed to the experiments made by Mr. Kyan. Having made a great number of experiments with a view to ascertain the primary cause of vegetable decomposition, he was at last convinced that albumen was that cause, and that to neutralize its effects would be to prevent decomposition. Some plan was required similar to that adopted in tanning. The gelatin in animal bodies is quite as liable to decom-

position as the albumen of vegetables; but when tannin, the infusion of oak bark, is combined with it, the destructive properties are lost, and the animal matter becomes durable, and almost incapable of decay. Reasoning upon this effect, Mr. Kyan imagined that it might be possible to prevent vegetable decomposition by causing the albumen to form a combination with some other substance; and, knowing the affinity of corrosive sublimate for the albumen, he entered upon a series of experiments, which led him to propose

the use of that substance as a protection for timber. Mr. Kyan inferred that, as wood consists of various successive layers, in which the albumen, or juices containing albumen, circulated freely, it is quite certain, as these juices within the wood, with the watery parts, fly off by the leaves, that the albumen remains behind, and it is probable that this albumen, which from its nature is peculiarly prone to enter into new combinations, is the thing in wood which begins the tendency to decomposition, and produces ultimate decay, whether that decomposition is attended with the formation of cryptogamic substances, or whether in the less organized form, the change occurs with the simple production of what has been called the dry rot. Mr. K. conceived, therefore, if albumen made a part of wood, the latter would be protected by converting that albumen into a compound of protochloride of mercury and albumen; and he proceeded to immerse pieces of wood in this solution, and obtained the same result as that which he had ascertained with regard to the vegetable decoctions. Having done so, it became necessary to employ various modes of experiment, as well as comparative experiments. Now it is not clear in what part of the wood the vegetable albumen may be found, though it exists more especially in that part of the tree which is denominated the alburnum or sap, and is found between the heart-wood and the innermost layer of bark. The experience of all practical men has confirmed the opinion, that this portion of wood is the first to decay.

It is probable that, as the alburnum becomes successive layers of wood, it loses a quantity of albumen; or that, in consequence of the pressure which takes place by the addition of each successive layer, it becomes so situated as to lose a part of its exposure to the vessels where a change may occur, and therefore becomes, in some measure, protected; for that which is one year alburnum or sap,

may be, and indeed generally is, proper wood the next.

The mode in which the application of the solution takes place is in tanks, which may be constructed of different dimensions, from twenty to eighty feet in length, six to ten in breadth, and three to eight in depth. The timber to be prepared is placed in the tank, and secured by a cross-beam to prevent its rising to the surface. The wood being thus secured, the solution is then admitted from the cistern above, and for a time all remains perfectly still. In the course of ten or twelve hours, the water is thrown into great agitation by the effervescence occasioned by the expulsion of the air

fixed in the wood, by the force with which the fluid is drawn in by chemical affinity, and by the escape of that portion of the chlorine, or muriatic acid gas, which is disengaged during the process. In the course of twelve hours this commotion ceases, and in the space of seven to fourteen days, varying according to the diameter of the wood, the change is complete, so that as the corrosive sublimate is not an expensive article, the albumen may be converted into an indecomposable substance at a very moderate rate, and the seasoning will take place in the course of two or three weeks."

Mr. Kyan's method of seasoning has been already tested, under circumstances so severe, that they may be said to have proved its efficiency. A piece of oak was five years in the fungus pit in Woolwich yard, London, a place notorious for the rapid and almost instantaneous destruction of vegetable matter, and it was as sound when taken out as when put in. This was the most severe test to which the method could be subjected, and its having sustained the trial is a proof of the value of the discovery. It has, however, been objected to the process, that the impregnation of timber with corrosive sublimate must unfit it for use in ship-building; but Mr. Kyan has furnished evidence to the contrary, and proves that salubrity is one advantage. We strongly recommend the builder to make experiments himself upon wood prepared by Mr. Kyan, by using it in places where decay is rapid.

## Framing of Timbers.

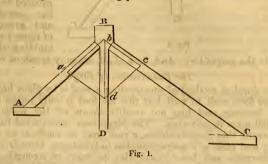
When timbers are framed together, it is with the intention of supporting some weight, or resisting the strains to which the materials may be exposed in the situations where they are to be placed. Horizontal or vertical timbers are not always of themselves sufficiently strong to sustain the pressure to which they may be subject, but they need assistance, and it then becomes a question, how can the materials intended to assist be best applied, and what are the smallest scantlings that can be adapted? Two things must be studied—stability and economy. It has been often stated that these two results cannot be accomplished by the same arrangement, but as the forces which are to be opposed have usually a direct application, so the system by which they are to be resisted may, usually, be of a simple construction.

## Composition and Resolution of Forces.

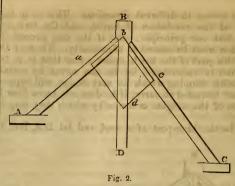
Two great mechanical principles lie at the base of all proper attempts to estimate the nature of the forces which may be exerted upon substances in particular situations; these principles are called the composition and the resolution of forces.

The resolution of forces is the means of finding any two or more forces which may resist or control the pressure of any one force. The composition of forces consists in finding the direction and amount of one force that is capable of producing the same effect as two or more forces acting in different directions. This is, in fact, only the reverse of the resolution of forces, and the two are, strictly speaking, but one principle; and if the one process be understood, the other must be almost so of necessity. Nor may the student pass over this part of the work, under a fear that it is too mathematical for him to understand, for he can never be certain that the roofs or other framing which he may design will support the weights they are intended to carry, if he does not know how to calculate the action of the weights or forces by which they may be pressed.

Let B D, fig. 1, be the king-post of a roof, and let B A, B C, be



the rafters: they are framed together for the purpose of carrying some weight; and the question is this-are they sufficiently strong to carry the weight which is to be placed upon them? To determine this we must refer to the resolution of forces. Let us suppose some determined weight to rest upon the point B. Then, by some scale of equal parts, draw a line B d, equal to the number of pounds, hundred weights, or tons, resting upon the point B, and draw da parallel to BC, and dc parallel to BA. Now measure the line a B by the same scale, and it will give the number of pounds, hundred weights, or tons, by which AB is strained, and cB will give the strain upon BC. But, in the drawing affixed, the rafter BC is longer than the rafter BA; but this does not at all affect the weight, for it remains the same, whatever may be the length of the beam which carries it; but it is necessary to remember that, by increasing the length of the beam, it is rendered less capable of supporting the weight, and a proportionate increase of dimensions must be allowed. But should the direction of the beam be changed, a very different result will be obtained, for in every case the pressure will be increased or decreased. The strain upon the beam BA, fig. 2, will now be measured by the line ab, and that upon B c by b c. In fact, a very slight alteration of position may, under certain circumstances, enormously increase or decrease a strain. It will be searcely necessary to explain how two or more



forces may be composed, and the single force, acting in a certain direction, be calculated.

Leaving the subject of the composition and resolution of forces, after a statement of the principle, we may proceed to explain the construction and arrangement of those parts of a building which be-

long to the carpenter. And, first of all, we may speak of roofs.

The Construction of Roofs.

The simplest method of constructing a roof is to place horizontal timbers from wall to wall, but this method is only suited to very short bearings, and does not readily throw off the water which may fall upon its covering. The Egyptians constructed flat roofs. To prevent this inconvenience, a roof may be made as an inclined plane; and such a construction has advantages, though its want of uniformity and beauty, and also its want of strength, proportioned to the amount of timber employed, are objections to its use; but still it is stronger than the flat roof, and readily carries off the water that may fall upon it. The best form for a roof is that in which there are two sides, equally inclined to the horizon, and resting in a line called the ridge of the roof. The angle which the inclined side forms with the horizon is called the pitch. In countries where there is a cold climate, and snow is apt to fall in large quantities, the roof is high; in warm countries the roof is low. In Gothic architecture the roof is generally high pitched, and it is so consonant with the style that it often forms a prominent feature in these buildings. There are not so many advantages in high pitched roofs as most persons suppose, and there are many disadvantages. The additional force of the wind upon a high roof is a serious objection, and when parapets are employed it is so far from preventing the effects of a heavy fall of rain or snow that the gutters are so filled that the pipes cannot carry off the water fast enough, or, being stopped by the dirt carried down by the velocity of the water, an overflow is occasioned. The height of roofs is now generally between one third and one sixth of the span.

It is the carpenter's business to frame the timbers of roofs, and sometimes he is required to design them, and he should therefore know how to obtain the strength and other qualities required, with

the smallest possible amount of timber.

A piece of timber, in whatever way it may be placed, except when vertical, will bend or sag, that is to say, its upper side will form itself into a concave surface. The more horizontal the timber is placed the more it will always sag, and as the distance between the points on which it rests is increased, so it has greater liabilities of bending. To prevent this effect as much as possible, arrangements must be made for the support of the beam in some intermediate points. Now, it may be supported from either above or below. If there should be any walls between those on which the ends of the timber rest, these will be sufficient for all the purposes required; if not, the same result must be produced by a system of framing.

The timbers which compose a roof are known by different names, according to the uses for which they are employed, and the situations in which they are placed. The principal timbers of a roof are the following, but they are not all used in every roof; the tiebeams, wall-plates, collar-beams, king-posts, queen-posts, struts, principal rafters, common rafters, ridge-piece, collar-beams, purlins,

and pole-plates.

The Tie-BEAM (A), fig. 3, is a horizontal piece of timber, which

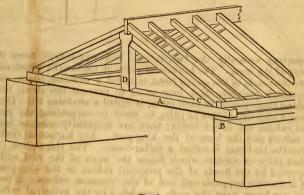
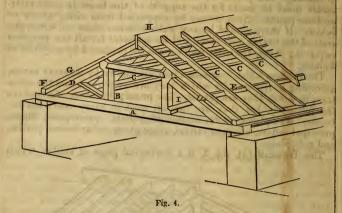


Fig. 3

extends from wall to wall, and rests upon the Wall-plates (B) at each end. It is employed for the purpose of connecting the feet of the principal rafters (C), which would otherwise have a tendency to push out the walls by their own weight, and the weight of the materials placed upon them. In roofs of large span, it is necessary that the tie-beam should be well supported in some point or points, between the ends on which it is supported, for if this be not done it will sag and draw either one or both of the principal rafters towards its centre, and thus destroy the stability of the framing. The King-post (D) is sometimes used for this purpose. It

is a piece of timber placed in a vertical position, connecting the point where the two principal rafters meet, and the centre of the tie-beam.

When the king-post is not thought to be sufficient to support the pressure which may be on the framing, Queen-posts (B), fig. 4, may be used, which are pieces of timber placed in an upright position,



supporting severally the two rafters, and equidistant from the centre of the truss. The horizontal piece of timber (C) which connects the heads of the queen-posts, is called a straining-beam; and that which connects their base, so as to prevent the struts from pushing them nearer to each other, is called a straining cill. Those pieces which are placed in pairs, to assist in supporting the principal rafters, are called struts; they are frequently used to unite the rafters and the base of the king-post. Any horizontal timber above the tie-beam is called a collar-beam. The ridge-piece (H) is that piece of timber which forms the apex of the roof, and is supported by the heads of the principal rafters or the king-posts, and in its turn supports one end of the common rafters. A poleplate is a beam over the walls, supported by the principal rafters or the tie-beam, and is intended to carry the lower ends of the common rafters. Purlins (E) are horizontal timbers, between the pole-plates and ridge-piece. The small spars (cc), which are parallel to the principal rafters, and are supported by the ridge-

## The Dimensions of Timbers used in a Roof.

plate, purlins, and pole-plates, are called common rafters.

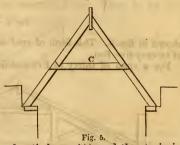
However accurately a roof may be designed, it is unfit for its purpose if the dimensions of the parts be not accurately proportioned. To accomplish this, some experience is required, and a

knowledge of the strength of timbers, under particular circumstances.

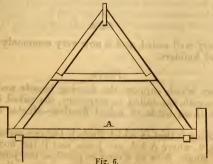
There are two things to be secured—a sufficient strength to support the weights to be carried without sagging, and to do that without burdening the walls or other parts of the building over which the roof is thrown. This is not always an easy task, for roofs are sometimes to be made in such forms as prevent the adoption of those means which would otherwise immediately accomplish the object. Sometimes a very large roof must be made flat, at other times a lantern-light must be provided in its centre; and, in a third case, it may be necessary to erect a dome. In designing for these and other roofs, attention should be paid to the character and success of similar works already executed, and the artist should study the points of similarity and difference between these and his own work, so as to provide against dangers, which may peculiarly affect his building.

## Examples of Roofs.

Fig. 5 is a roof, the rafters of which are only supported by a collar-beam (C). which acts in part as a tie; but this arrangement is so feeble, that it should never be used over a space where the span is more than fifteen feet.



In fig. 6 there is the addition of a tie-beam (A), and the strain is here thrown from the collar to the tie-beam; the former being compressed, the latter in a state of tension. As there is no arrange-



ment in this truss to support the tie-beam, and to prevent it from sagging, it is unfit for a span of more than twenty-five feet.

To prevent the inconveniences resulting from the sagging of the tie-beam, a king-post (P) and struts (SS) may be introduced, as

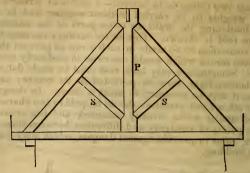


Fig. 7.

shown in fig. 7. This form of roof is very well adapted for a span of twenty-five feet.

For a span of thirty to five-and-forty feet, the truss represented

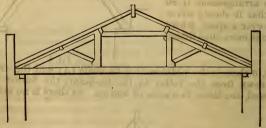


Fig. 8.

in fig. 8 is very well suited, and is now very commonly adopted by architects and builders.

#### Floors.

The timbers which support the flooring boards, and the ceiling of a room beneath, are called, in carpentry, the naked flooring.

There are three kinds of naked flooring—single, double, and framed.

Single flooring is that in which there is but one series of joists, as shown in fig. 9, where AAA are joists, and B the flooring-boards. To make a single floor as strong as possible, the joists should be thin but deep, sufficient thickness being always allowed for the nailing of the flooring boards. Two inches by six is the smallest

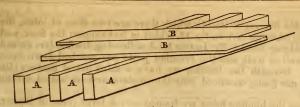


Fig. 9.

dimension for joists; for a length of twenty feet they should be about three inches thick, and twelve inches deep.

Sometimes the joists cannot have in a particular place a bearing upon the walls, and then a piece of timber is framed between the nearest joists. This is done where flues, fire-places, and stairs interfere. The timber thus used is called a trimmer, and the two joists on which it is supported are called trimming-joists, and should be made a little stronger than the common joists. Thus, in fig. 10,

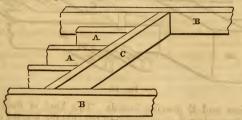
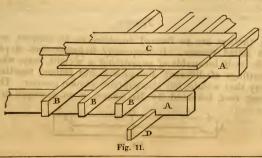


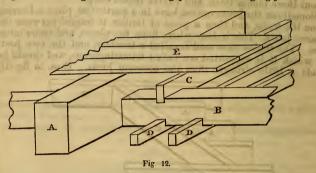
Fig. 10.

AA are common joists, BB trimming joists, and C a trimmer. When the bearing is more than seven or eight feet, the joists should be strutted; that is to say, short pieces of board should be fitted between the joists, so as to form a continued line from wall to wall. These struts greatly strengthen the floor, and prevent the joists from sinking; but it is not desirable to mortice them into the joists, as that process has the effect of weakening the joists themselves.



Double flooring is that in which there are two tiers of joists, the binding joists, as A A, in fig. 11, which in fact support the floor, and the bridging joists B B. In this kind of flooring, the binders extend from wall to wall, and the bridging joists are notched down upon them. Beneath the binders we have a third tier of timbers (D), which are pulley-morticed into the binders, and are called ceiling joists.

When the binding joists are framed into a large piece of timber, called a girder, the floor is said to be a double framed floor. Thus in fig. 12 A is the girder, B a binding joist, C a bridging joist, D D

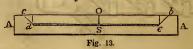


ceiling joists, and E flooring boards. This kind of floor is decidedly the best when it is necessary to provide for a good and even ceiling, for although single floors may be made very strong for a great bearing, yet the ceilings are always liable to crack.

It is not easy to obtain timber for girders of much more than twenty feet scantling, and they are therefore trussed. Trusses are used in both floors and roofs, but we have not thought it desirable to interrupt the course of explanation we have given, by a reference to any particulars concerning this branch of carpenter's work; yet it is necessary that we should now make a few remarks upon it.

## Trusses.

When timbers are so framed together as to support weights, they are called trusses. It frequently happens that a piece of timber, in itself incapable of supporting a weight, may, when cut into scantlings of different dimensions, and framed together, only carry that weight, but also support a much greater. The bow and string roof, invented by Mr. Smart, is an example in point.



Let A A, in fig. 13, be a piece of timber, which we will suppose to be insufficient of itself to carry a particular weight; from this cut the pieces o, s, e, b, and o, s, d, c. Then let these pieces be raised as in fig. 14, and a key be placed between them at the apex; and

it will form a very strong truss, which may be made still more capable of resisting a strain, by the application of struts.

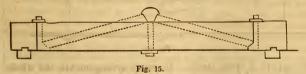


The principal rafters of a roof are so called because they are trussed. It is not necessary to truss all the rafters in a roof, and it would be very expensive to do so; and therefore trusses are placed at particular distances from each other, according to the weight to be carried; and they are formed in different ways, according to the span over which they are thrown.

It has been already stated, that girders are sometimes trussed, and should always be when their bearing is much more than twenty feet. We have often seen trusses which, so far from strengthening the girders, have decidedly weakened them. Large girders are sometimes sawn down the middle, and when reversed, are bolted together with slips of wood between them. It has been supposed that this strengthens, and is adopted for this purpose; but the supposition is erroneous, though the plan is certainly a good one, for it allows a free circulation of air between the pieces, and facilitates the emission of any dampness that may be in the timber.

A strong girder may be made as strong, in fact, as any truss of the same depth, by bolting two pieces of timber together, or by confining them with iron hoops, the ends of the girder being smaller than the centre, so as to allow the hoops to be driven tighter, and confine the beams.

In fig. 15 we have given a representation of a strong truss



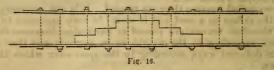
girder, the truss post and the abutment pieces being made of wrought iron.

# Of Connecting Timbers.

It is sometimes impossible to obtain timbers of the length required for the several parts of a building, and it is then necessary to join two or more pieces together, so as to form them into one piece, and to injure the stability as little as possible. This process is called scarfing, and the parts of the joints which come in contact are called scarfs, and are usually connected by iron bolts.

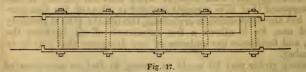
There are many ways of scarfing, every builder adopting that one which appears to him the best under the circumstances in which the timber is to be employed. Two or three different methods may be mentioned, leaving the workman to examine those which he may happen to meet with in practice, and the various designs which have been given by writers on the art of building.

Fig. 16 shows the means of scarfing without diminishing the



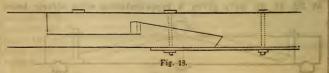
length of the pieces. This is done by the introduction of a third piece, having the form of steps, and all the pieces being united together by bolts and plates.

Fig. 17 is a representation of a scarfing, which is very simple, and frequently used, though there is a considerable loss of timber.



The pieces to be united are connected by iron bolts, an iron plate being placed on both sides.

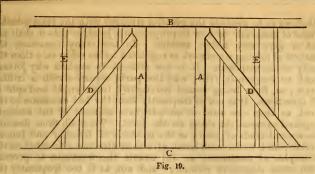
Fig. 18 represents a form of scarfing, adapted to a beam, which



has to support a cross strain. In many arrangements, the whole strain is supported by the straps and bolts, but in this they do not, in consequence of the indentation.

### Timber Partitions.

Rooms and passages are often separated by timber partitions, which are so formed as to be covered with lath and plaster. In fig. 19 we have given a design for the framing of a partition, with a door through it; AA are the door-posts, B the head, C the sill, DD are braces which support the quartering, and are assisted by



the struts, E.E. It will be quite evident from a glance at the drawing, that the door-posts help to sustain the braces and struts; while they in return prevent the fall of the door-posts. Braces may be introduced in various ways, but strength is the object for which they ought to be introduced, a circumstance which is very frequently entirely forgotten by carpenters. In some instances, it may be found desirable to introduce a simple truss into a design for partitions.

The carpenter usually connects his timbers either by notching, or by mortice and tenon. Dovetail joints are sometimes used in carpentry, but they ought never to be adopted, for they will always draw when the timber shrinks, and the oblique surface of the dovetail tends to force the timbers apart, acting as though it were a wedge.

### Gluing Joints.

In general, nothing more is necessary to glue a joint, after the joint is made perfectly straight, or, in technical terms, out of winding, than to glue both edges while the glue is quite hot, and rub them lengthwise until it has nearly set. When the wood is spongy, or sucks up the glue, another method must be adopted, one which strengthens the joints, while it does away with the necessity of using the glue too thick, which should always be avoided; for the less glue there is in contact with the joints, provided they touch, the better; and when the glue is thick, it chills quickly, and cannot be well rubbed out from between the joints. The method to which we refer is, to rub the joints on the edge with a piece of soft chalk, and, wiping it so as to take off any lumps, glue it in the usual manner; and it will be found, when the wood is porous, to hold much faster than if used without chalking.

# Of the different Methods of joining Woodwork.

Many workmen are not aware of the proportion which a piece made to fit into another should have towards that into which it is fitted, so as to produce the greatest strength with the least possible waste of material; or how to proportion a joint, so that it shall not fail or give way before another. In too many instances, the method of joining woodwork is regulated by no other rule than the fancy of the workman. It is not difficult to explain why joiners' work so frequently fails; why the parts separate with a triffing strain; or, from being bound too tightly together, fly and split in all directions. It is not so frequently from the bad execution of the work, as from the want of an adequate estimate of the strength required to resist the stress on the joint. We shall, then, describe the several kinds of joints, or the methods of framing and joining timber: and, under each head, give such directions, founded on the principles of mechanics, as will enable the workman to proceed with some degree of certainty; and not, as is too frequently the case with artisans, observe no other rules than those which custom has authorized, and practice made familiar.

## Dovetailing.

We have given, in the cuts, several examples of dovetailing. The parts which fit into each other are known by different names; the projecting piece, represented in fig. 20, is called the pin of the dovetail; and the aperture into which it is fitted, as shown in fig.

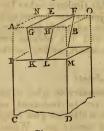


Fig. 20.

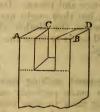
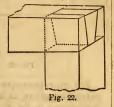


Fig. 21.

21, is called the socket. Now the strength of a dovetail depends upon so proportioning the pin and the socket as to enable them to support, rather than destroy, each other. Let ABCD, fig. 20, be a scantling, which is required to be joined to another, by means of a single dovetail. The strength of the joint depends on the form of the dovetail, as well as on the proportion it bears to the parts cut away. We shall endeavor to lay down the principle on which the greatest strength may be secured. Having squared the end of the scantling, and gauged it to the required thickness, AIKLM, divide IM into three equal parts, at K and L. Let KL be the small end of the dovetail, and make the angles IKG and MLH equal to about 75 and 80 degrees respectively; and make GE and IIF parallel to AN and BO. Then cut away the parts AIKGEN, and BMLHFO, and having formed the socket to correspond, by

marking the form of the dovetail on the top of the piece ABCD, fig. 21, and cutting away accordingly, the pieces may be fitted together, as shown in fig. 22. It may be here observed, that the

bevel of the dovetail, that is, the angle IK G, fig. 20, may be either more or less than has been mentioned, according to the texture of the wood. Hard, close-grained woods, not apt to rive or split, will admit of a greater bevel than those which are soft, or subject to split; thus the bevel of a dovetail in deal must be less than in hard oak, or in mahogany. It is a great fault to make a dovetail too beveling, for instead of adding



to the strength of the joint, as some persons suppose, it weakens it; for provided the bevel is sufficient to prevent the possibility of pulling the pieces apart, the less the bevel that is given the better. It must have been observed, that there is a great difference between the dovetail made by the cabinet-maker and by the joiner; the former has very little bevel, the latter very much; the former looks neat, and is at the same time strong; while the latter, appearing to aim at strength, looks clumsy, and is at the same time much the weaker of the two.

Fig. 23 represents the dovetail in common use for drawer-fronts. When it is required to hide the appearance of the joint in front, the board ABCD is cut with the pin, and AEFB with the socket. The pins in this sort of dovetail are in general from about three quarters of an inch to an inch apart, according to the size of the pieces to be joined.

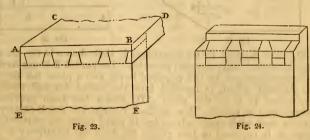


Fig. 24 represents the pin part of a lap dovetail, which, when put together, shows only a joint, as if the pieces were rebated together, as shown in fig. 25. ABCD represents the pin, EFGH the socket, and when put together the line HG is only seen as a joint; and if the corner AB is rounded to the joint GH, it will appear as if only mitred together. This kind of dovetail is very useful for many purposes where neatness is required, such as in making boxes.

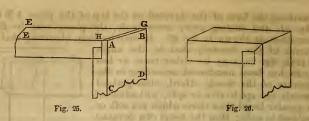
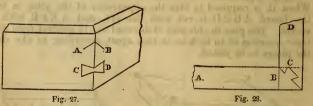


Fig. 26 represents a still neater dovetail; and, as the edges are mitred together, it is termed a mitred dovetail; and is the same as that shown in fig. 6, except that instead of the square shoulder, or rebat, in A B, it is cut into a mitre, and the other piece is made to

correspond.

Another very neat as well as expeditious method of joining pieces of wood, and it is somewhat analogous to dovetailing, is shown in fig. 27. The joint is first formed into a mitre, and the pieces are then keyed together, either by making a saw kerf in a slanting direction, as at A B, or by cutting out a piece, as at C D, in the form of a dovetail. The first method, A B, is called, amongst workmen, keying together; the second, C D, key-dovetailing.



The last method to be mentioned is that shown in fig. 28, and may be termed mitre dovetail grooving; the part A B being formed with shoulders cut to the required bevel, and a piece left for the pin dovetail, which is inserted into the socket dovetail, made to correspond to it in the piece CD, which has been previously formed into a mitre. This method, though not much employed, may be used with great advantage in many instances, particularly when it is required to join pieces together the lengthway of the grain.

### Mortice and Tenon.

Under this head, we shall endeavor to give some rules necessary to be observed in attempting to proportion the parts of the mortice and tenon, so that they may be equally strong, or that the tenon may not be more likely to give way than the checks of the mortice; for this is the principal thing to be avoided. The workman frequently allows too little substance for the tenon, lest he should weaken the mortice; and sometimes he falls into the opposite error; facts which clearly prove that he is not acquainted with a means of obtaining a maximum of strength with a given quantity of material.

Figs. 29 and 30 represent a simple mortice and tenon. The dotted

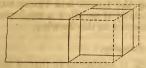


Fig. 29.

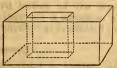
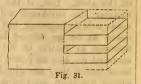


Fig. 30.

lines show the parts to be cut away. To show the thickness of the tenon, and consequently the width of the mortice, we have here one tenon and two shoulders, that is, three parts; one of which is to be allowed for the tenon, and two for the shoulders; and this will in general be found the best proportion, for if the tenon be more than that, it will weaken the shoulders of the mortice. Now if we have, as is frequently the case, two tenons in one piece, as represented in fig. 31, there will be five parts, two tenons, and three shoulders; so that each tenon will be one fifth of the thick-

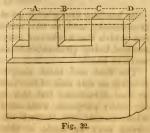
ness of the stuff, for the shoulders are all equal to the tenons. This rule may be generally observed, unless the tenon is at a considerable distance from the end of the stuff, and then something more may be allowed for its thickness, as the mortice is then not so liable to split; but it should in no case, however sound the timber, or tough the



material, be more than two out of four parts; that is to say, it can never be safe to make the tenon more than half the thickness of the stuff, and that only under particular circumstances, when the mortice is near the middle of the scantling, for the piece in which the mortice is cut would, in other cases, be considerably weakened.

There is frequently in joiners' work a shoulder at the bottom of

the tenon that fits into the piece in which the mortice is cut, as represented in fig. 32; and the tenon is divided into two parts, as there shown, which, when the stuff is wide, is a good method, as it strengthens the piece in which the mortice is cut, without weakening, in the same proportion, the mortice itself; and we would suggest, in this case, that the piece BC, cut out from between the tenons AB



and DC, be nearly, if not quite, one third of the distance AD; for if much less, the piece left between the mortice will add but very little to the strength of the piece in which the mortice is made; and the tenon would be stronger in proportion to the mortice-piece than necessary. It may be here observed, that if the width of the tenon be much more than four times its thickness, additional strength will be gained by dividing the tenons into two or more parts, as shown in the figure, particularly if we allow a small piece at the bottom of the tenon, as represented in the drawing.

# Grooving and Lapping.

This method of joining wood-work is analogous to that of morticing and tenoning. When it is required to join two boards together by means of a tongue and groove, the groove should never exceed one third of the thickness; and often, if the piece for the tongue be formed of hard wood and liable to split, one quarter of the thickness will be sufficient. When a panel is let into a groove in the style, the joiner is often guided by the thickness of the panel itself, which should never be less than one third the thickness of

the style.

In making a groove across the grain, as for partitions, it will be best, in most cases, to make it about a fifth or sixth of the substance of the stuff. But, if the groove be formed into a dovetail, one quarter the thickness will be better, and the dovetail should be made a little tapering, but not too much. It should, in fact, be so made as to go almost home without requiring a blow from a hammer or mallet to drive it into its place until it has nearly attained it; and all joints should be easily separated with a gentle blow before they are glued. In a lap-joint, that is, in lapping two pieces together, supposing them of equal thickness, half the substance of each should be cut away; and, if of unequal thickness, the lap should be made in the thinner piece, of about two thirds or three quarters of its thickness, according to the substance of the thicker piece; thus endeavoring in this, as in all other cases, to avoid weakening one piece more than another.

## Bending and Gluing-up.

In bending and gluing-up stuff for sweep-work, much judgment is necessary, and, as the methods are various, we shall mention a few which the workman may apply, as occasion may require, one method being preferable to another, according to the nature of the work in hand.

The first and most simple method is that of sawing kerfs or notches on one side of the board, thereby giving it liberty to bend in that direction; but this method, though very ready and useful for many purposes, weakens the work, and may cause it to break when strains are thrown on the piece. But a tolerably strong sweep may be made in this manner, if, after sawing the kerfs

(particular care being taken to make them regular and even, and to saw them at regular depths), some strong glue be rubbed into each kerf. When bent into the required sweep, a piece of strong canvas should be glued over the kerfs themselves, and the glue be left to harden in the position to which the stuff is bent.

Another method is to glue up the stuff in thin thicknesses, in a cawl or mould, made with two pieces of thick wood cut into the required sweep. This method, if done with eare, that is, making the several pieces of equal thickness throughout, of wood free from knots, is perhaps the best that can be devised for strength and accuracy. It is also a practice sometimes to glue up a sweep in three thicknesses, making the middle piece the contrary way of the grain to the outside and inside pieces, which run lengthwise. This method, though frequently used for expedition, is much inferior to the above, as the different pieces cannot shrink together, and consequently the joint between them is apt to give way.

A solid piece, if not too thick, may be sometimes bent into the form required. If a piece of timber be well soaked upon the intended outside of the curve, it may be bent into position, and if kept in that position till cold will retain the curvature that is given

to it.

The only other method of forming a curve, necessary for us to mention, is that of cutting out solid pieces to the required sweep, and gluing them upon one another till they have the thickness required, taking care that the joints are alternately in the centre of each piece below it, something in the manner of courses of bricks one above the other. In this case, it will be necessary, if the work be not painted, to veneer the whole with a thin piece, after it has been thoroughly dried and planed level, and then made somewhat rough with either a rasp or toothing-plane. But the joiner must adopt one plan or another, according to circumstances.

## Scribing.

Scribing is the operation by which a piece of wood-work is made to fit against an irregular surface. Thus, for instance, the plinth of a room is made to meet or correspond with the unevenness of the floor. To determine the portion which is to be cut off from a partition, or any wood-work where a floor or ceiling is irregular, it is only necessary to open the compasses to a width equal to the greatest distance between the plinth and the floor; and, passing one leg over the uneven surface, the other leg will leave a mark on the plinth. If the wood be cut away on that line, a surface will be obtained which will make a good joint with the floor or ceiling. But the chief use of the art of scribing is to enable the joiner so to connect the moulding of panels or cornices, that when placed together, they shall seem to form a regular mitre-joint. This method has certainly one advantage over the common method of mitring, for, if the stuff should shrink, little or no alteration will be made in the appearance, but, under the same circumstances, a mitre

would open, and the joint would be shown. The method adopted is this: To cut one piece of the moulding to the required mitre, and then, instead of cutting the other to correspond with it, cut away the parts of the first piece to the edge of the first moulding, which will then fit to the other moulding, and appear as a regular mitre.

# Finishing of Joiners' Work.

Joiners' work is generally intended to increase the beauty of a building. When a joiner works in wainscot, oak, or mahogany, his chief object must be to obtain a surface perfectly smooth and When the framing is glued together, the glue which oozes out, and may be spilt upon the work, must be allowed to remain a few minutes and chill, and may then be carefully scraped off with a chisel; and the parts which cannot be thus cleaned may be washed with a sponge dipped in hot water and squeezed nearly dry. This not only saves trouble in operations which follow, but prevents staining, always produced when glue is suffered to remain till quite hard, particularly on wainscot, which turns black in every joint or place where the glue is suffered to remain. After this operation, which, though it may appear tedious to some workmen, will be found a saving of time, the work should remain till perfectly dry; and, when the joints and other parts have been levelled with a smoothing plane, the whole surface may be passed under a smooth scraper, and finished with fine glass paper. It will be sometimes necessary, when the grain is particularly cross, to damp the entire surface with a sponge "to raise the grain," and then again to apply the glass-paper. The work will then be ready for polishing with wax, or varnishing, and the good appearance of the work will be in proportion to the time and trouble expended in

In cleaning pine, the same precautions must be taken for the removal of glue left upon the joints, or spilt upon the work, as already described. This being done, the work may be cleaned off with a piece of glass-paper that has been rubbed with chalk, or, in some cases, with a piece of hearthstone. The work is then ready for the painter; but as there are knots and other places where the turpentine contained in the wood is apt to ooze out, either with or without the increase of heat, and thus spoil the appearance of the finishing, those parts are done over with a composition, and the process is called priming. This is properly the painter's business; but it must sometimes be done by the joiner, for the sake of saving his work. The composition used for this purpose is made with red lead, size, and turpentine, to which is sometimes added a small quantity of linseed oil. Priming has also the advantage of preventing the knots from being seen through the paint. Some workmen omit in this composition the oil and the turpentine, but the size of itself is apt to peel off, and does not thoroughly unite itself

with the wood.

Another method of cleaning-off pine is sometimes adopted. When the surface has been made quite smooth with the plane, it is rubbed with a piece of chalk, and the whole is cleaned with a piece of fine pumice-stone, as in the former process it was done with glasspaper; but if the grain should be still rough, the work may be damped with a sponge, and the operation repeated when dry.

As, in finishing interior work, it is now customary to imitate the graining of different kinds of wood, it is necessary that the joiners' work should be well finished; for if a good even surface be not provided, it will be impossible for the painter to produce the effect he desires. Every defect in the ground will, in fact, be more visible under a delicate graining than when the surface is covered with successive coats of color; but, even in the latter case, work well prepared will not only look better, but the color will not be so apt to chip and peel off as when the surface is not properly levelled.

## TERMS USED IN BUILDING.

Abacus.—The upper member of the capital of a column, that on which the architrave rests. It has different forms in the several orders: In the Tuscan or Doric, it is a square tablet; in the Ionic, its edges are moulded; in the Corinthian, its sides are concave, and frequently enriched with carving.

Abutment.—That part of a pier from which the arch springs.

Acanthus.—A plant whose leaves are carved on the Corinthian and Composite capital. They are differently disposed, according to circumstances; and the leaves of the laurel and parsley are sometimes employed in their place.

Acroterium.—A pedestal on the angle or apex of a pediment,

intended as a base for sculpture.

Altitude.—The perpendicular height of anything in the direction of the plumb line. The length of a body is measured on the body itself, and remains constant, its altitude varies according to its inclination to or from the perpendicular.

Alto Relievo.—A sculpture, the figures of which project from the

surface on which they are carved.

Amphiprostylos — An order of Grecian temples, having columns

in the back as well as the front.

Amphitheatre.—A double theatre, employed by the ancients for public amusements. The colosseum at Rome, built by Vespasian, is one of these.

Annulet.—A small square moulding, used to separate others; the fillet which separates the flutings of a column is sometimes known by this term.

Ante.—Pilasters attached to a wall, receiving an entablature, and having bases and capitals differing according to the order employed, but always unlike those of the columns.

Antepagmenta. - A term in ancient architecture, the architraves

round doors.

Apophyge.—That part of a column which connects the upper fillet of the base and the under one of the capital with the cylindrical

part of the shaft.

Arœostylos —That style of building in which the columns are distant from one another from four to five diameters. Strictly speaking, the term should be limited to an intercolumniation of four diameters, which is only suited to the Tuscan order.

Arch.—Such an arrangement, in a concave form, of building materials, as enables them, supported by piers or abutments, to

carry weights and resist strains.

Arch-buttress. - Sometimes called a flying buttress; an arch

springing from a buttress or pier against a wall.

Architrave.—That part of the entablature which rests upon the capital of a column, and is beneath the frieze. It is supposed to

represent the principal beam of a timber building.

Area.—This term is applied to superficies, whether of timber, stone, or other material, and is the superficial measurement; that is, the length multiplied into the breadth. The word area sometimes signifies an open space.

Arris -The line in which two surfaces meet each other.

Ashler.—Common freestone, as it comes from the quarry, generally about nine inches thick, but of different superficial dimensions.

Ashtering. - Quartering, to which laths are nailed.

Astragal.—A small moulding with a semicircular profile, some-

times plain and sometimes ornamented.

Attic Order.—A term used to denote the low pilasters which are placed over orders of columns or pilasters, and frequently employed in the decorations of an attic.

### 10.1 B. I

Baluster.—A small pillar or pilaster, supporting a rail.

Balustradz.—A series of balusters connected by a rail.

Band.—A square member. To distinguish the situation in which it is placed, or the order in which it is used, an adjective is frequently prefixed; thus, a dentil or a modillion band.

Base.—The lower division of a column. The Grecian Doric has

no base, and the Tuscan has only a single torus on a plinth.

Bead.—A circular moulding, which lies level with the surface of the material in which it is formed. When the moulding projects, or several are joined, it is called reeding.

Beak .- A small fillet in the under edge of a projecting cornice,

intended to prevent the rain from passing between the cornice and fascia.

Beam.—A piece of timber in a building laid horizontally, and intended to support a weight, or to resist a strain.

Beam-filling.—The masonry, or brickwork, between beams or joists.

Bearer .- A vertical support.

Bearing.—The length between bearers, or walls; thus, if a beam rests on walls twenty feet apart, the bearing is said to be twenty feet.

Bed Mouldings.—Those mouldings between the corona and the frieze.

Bevil.—An instrument used by workmen for taking angles. In form it resembles a square, but the blade is moveable about a centre. When the two sides of any solid body have such an inclination to each other as to form an angle greater or less than a right angle, the body is said to be beviled.

Bond.—A term used to signify the connection between the parts of a piece of workmanship. In bricklaying and masonry, it is that connection between bricks, or pieces of stone, which prevents one

part of the building from separating itself from another.

Bond Timber.—Timber laid in walls to tie or bind them together.

Brace.—A piece of timber placed in an inclined position, and used in partitions or roofs, to strengthen the framing. When a brace is employed to support a rafter, it is called a strut.

Bressummer.—A beam, or iron tie, intended to carry an external

wall, and itself supported by piers or posts.

Bricknoggin.—Brickwork between quartering.

Buttress.—A mass of stone or brick-work intended to support a wall, or to assist it in sustaining the strain that may be upon it. Buttresses in Gothic architecture are used for ornament as well as strength.

C.

Cabling.—Cylindrical pieces filling up the lower part of the flutes of a column.

Camber.—To give a convexity to the upper surface of a beam.

Cantalivers.—Pieces of wood or stone beneath the eaves to support them, or mouldings above them.

Capital.—That part of a column or pilaster beneath the entablature; or, in other words, the uppermost member of a column or pilaster. The capital is variously formed, according to the order: Thus, we have the Tuscan, Doric, Ionic, Corinthian, and Composite capitals, and many others, that have been invented since the times of the Greeks and Romans.

Caryatides.-Figures of women, introduced to support an enta-

blature, instead of columns.

Casement.—Applied to a window which is hung upon hinges in

place of lines and weights.

Casting.—The warping or shrinking of timber or wood-work, occasioned by an insufficient strength, or by an unequal exposure to the weather, and want of proper seasoning.

Cavetto.—A concave moulding, the quadrant of a circle. Centering.—The framing upon which an arch is turned.

Clamping.—When one piece of wood is so fixed into the end of another as to prevent it from splitting or easting, it is said to be clamped. The pieces may be united with a mortice and tenon, or with a groove and tongue.

Collar Beam.—A beam framed between two principal rafters.

Console.—An ornament cut on the key-stone of an arch, sometimes in the form of a scroll, at other times to represent a human face.

Content.—The amount of any substance in rods, yards, feet, or

inches whether solid or superficial.

Coping.—The stone which covers the top of a wall or parapet.

Corbel.—A bracket, or piece of timber projecting from a wall: in

Gothic architecture, usually carved with some grotesque figure.

Cornice.—The combination of mouldings which finishes or crowns an entablature.—The term is also applied to the mouldings which finish the walls and ceiling of a room, hall, or passage, filling up the angle which they make.

Crown.—A term applied to the uppermost or highest part of an

arch, that in which the key-stone is fixed.

Cyma.—A moulding with a waved or crooked profile, partly convex, partly concave. It is called by workmen an ogee. When the hollow part of the moulding is uppermost, it is called a cymarecta; when the convex part is above, a cymareversa.

#### D.

Dado.—That flat part of the base of a column between the plinth and the cornice. It is of a cubical form, and from thence takes its name.

Dentils.—Square blocks introduced as ornaments into cornices of the Doric, Ionic, and Corinthian orders. A small circular piece is sometimes cut out, and at other times they are fluted.

Die.—A square cube.

Door Frame.—The case in which a door opens and shuts, consisting of two uprights and one horizontal piece, connected together by mortices and tenons.

Dormer.—A window made in the sloping part of a roof, or above

the entablature.

Dovetailed —When two pieces of wood are fastened together, by letting the pieces of one into apertures formed in the other, of a

shape somewhat resembling a fan or dovetail, they are said to be dovetailed.

Drops-Ornaments in the Doric entablature resembling bells

placed immediately under the triglyphs.

Dwarf Wall.—A wall that has a less height than that of the story in which it is used.

### E.

Eaves.—The edge of a roof or slating which overhangs a wall, and is designed to carry off the water, without flowing down the wall.

Echinus.—A moulding, the profile of which is the quadrant of a circle turned outwards, or in some instances a conic section. It is said to resemble the shell of the chestnut.

Ellipse.—That curve called by workmen an oval.

Entablature.—That assemblage of mouldings, &c., which are supported by the column. It consists of three parts—the architrave, frieze, and cornice.

Entasis.—The swelling of a column.

Eustylos-That intercolumniation in which the columns are

placed two diameters and a quarter from each other.

Eye.—A term sometimes used in architecture to denote a small window in a pediment. The middle of the Ionic volute, that is, the circle within which the different centres for drawing it are found, is known by the same name.

#### F.

Façade.—The face or front of a building; strictly speaking, the

principal front.

Fuscia.—A flat broad member, in architecture, but of small projection. It is used to denote the flat members into which the architrave is divided, and these are called fascia.

Feather-edged .- Boards or planks thicker at one edge than the

other.

Fillet.—A small square moulding, of slight projection. In carpentry, it means a piece of wood to which boards are nailed.

Flashings.—Pieces of lead so let into the wall as to lap over a

gutter.

Flatting .- Painting, which has no gloss on its surface, being

worked with turpentine. It is used for finishing.

Flutes.—Vertical channels cut in the shafts of columns and pilasters, sometimes meeting one another at a sharp edge, and at other times having a fillet between them.

Flyers.—Stairs which rise without winding.

Flue.—The aperture of a chimney.

Footings.—The courses of brick or stone at the foundation of a wall.

Frieze.—The flat member in an entablature, separating the architrave from the cornice.

Furring.—A means of restoring an irregular framing by the addition of small pieces of wood nailed to the framing itself.

Fust.—The shaft of a column.

G.

Gable.—The upright triangular end of a building at the ends of a roof.

Girder.—The largest piece of timber in a floor, that into which the joists are framed.

Groin.—The intersection of two arches.

Groove.—A rectangular channel cut in stone or timber; such as that which is cut in the stiles to receive the panel of a door.

Grounds.—Those pieces of wood imbedded in the plastering of walls to which skirting and other joiners' finishings are attached.

Guttæ.—See "Drops."

Gutter.—A valley between the parts of a roof, or between the roof and parapet, intended to carry off the rain.

П.

Half Round.—A moulding in a semicircular form, projecting from the surface.

Headers .- Bricks laid with their short face in front.

Hips.—Those pieces of timber placed in an inclined position at the corners or angles of a roof.

arch at La

Impost.—The combination of mouldings which form the capital of a pier.

Insulated.—A term applied to a column which is unconnected with a wall, or to a building, that stands detached from others.

Intercolumniation.—The space between two columns.

Intertie.—Small pieces of timber placed horizontally between, and framed into, vertical pieces to tie them together.

J.

Jambs.—The side pieces of an opening in a wall, such as doorposts, and the uprights at the side of window frames.

Joggle-piece.—A post to receive struts.

Joists.—Those pieces of timber which are framed into a girder, bressummer. or otherwise, to support a ceiling or a floor.

#### K.

Key-stone.—That stone in the top or crown of an arch which is in a perpendicular line with the centre.

King-post.—The centre post of a trussed framing, intended to

support the tie-beam and struts.

Knee.—A piece of timber bent to receive some weight, or to

#### T.

Lantern.—A frame in the dome or cupola of a building to give light. The term is applied to some kinds of fanlights, that is, the frame over a door to light a passage or corridor.

Lining.—That joiners' work which covers an interior surface.

Lintels.—The pieces of timber which lie horizontally over the jambs of windows and doors.

#### M.

Mantel.—The cross-piece which rests on the jamb of a chimney.

Metopa.—The interval between the triglyphs in the Doric order.

Minute.—The sixtieth part of the diameter of a column.

Modillion.—An ornament in the Ionic, Corinthian, and Composite orders. It is a sort of bracket, and should be placed under the corona.

Module.—The semi-diameter of a column, and is divided into thirty minutes. It is the measure by which the architect deter-

mines the proportions between the parts of an order.

Mortise.—A method of joining two pieces of wood; a hole being made in one of such a size as to receive the tenon or projecting

piece formed on the other.

Mosaic.—A term applied to pavements, and other work, when formed of various materials of different shapes and colors, laid in a kind of stucco, so as to present some pattern or device. The ancients were very successful in the execution of Mosaic, and many fine specimens remain to this day.

Mullion.—Upright posts or bars which divide the lights in a

Gothic window.

### N.

Naked.—This term is applied, in architecture, to a plain surface, or that which is unfinished; as the naked walls, the naked flooring—that is, uncovered. The word is sometimes applied to flat surfaces before the mouldings and other ornaments have been fixed.

Newel .- The centre round which the stairs wind in a circular

staircase.

Nosings.—The rounded and projecting edges of the treads of stairs.

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Obelisk .- A slender pyramid.

Ogee.—A moulding, consisting of a portion of two circles turned in contrary directions, so that it is partly concave and partly convex, and somewhat resembles the letter S.

Order.—An assemblage of parts having certain proportions to one another. There are five orders of architecture—Tuscan, Doric, Ionic, Corinthian, and Composite—all of which were invented by

the ancients, and are now employed by the moderns.

Oval.—A curve line, the two diameters of which are of unequal length, and is allied in form to the ellipse. An ellipse is that figure which is produced by cutting a cone or cylinder in a direction oblique to its axis, and passing through its sides. An oval may be formed by joining different segments of circles, so that their meeting shall not be perceived, but form a continuous curve line. All ellipses are ovals, but all ovals are not ellipses; for the term oval may be applied to all egg-shaped figures, those which are broader at one end than the other, as well as to those whose ends are equally curved.

Ovolo.—A convex projecting moulding whose profile is the qua-

drant of a circle.

#### p

Panel.—A compartment inclosed in a frame, into which it is framed or grooved.

Parapet.—A low wall generally about breast-high, on the top of

bridges or buildings.

Pargetting.—Rough plastering, commonly adopted for the inte-

rior surface of chimneys.

Pedestal.—That arrangement on which columns are sometimes placed: it is divided into three parts—the cornice, the die, and the base.

Pediment.—A low triangular crowning ornament in the front of a building, and over doors and windows. Pediments are sometimes

made in the form of a segment of a circle.

Pier.—A square, or other formed mass, used to strengthen or support a building; it sometimes signifies that mass of stone or brickwork between the arches of a bridge, and from which they spring, or against which they abut. But the term is usually employed to designate the solid part between the doors or windows of a building.

Pilaster.—A square pillar insulated, or engaged to the wall, and

is usually enriched with a capital and base.

Piles.—Large timbers, usually shod with pointed iron caps,

driven into the ground for the purpose of making a secure foundation.

Pillar.—An irregular, insulated column. It differs from a column in having no architectural proportion, being either too massive or too slender.

Pinnacle.—A small spire used to ornament Gothic buildings.

Pitch of a Roof.—The proportion obtained by dividing the span by the height; thus we speak of its being one half, one third, one fourth.

Plinth —The solid support of a column or pedestal.

Plumb-line.—An instrument to determine perpendiculars; it consists of a piece of lead attached to a string.

Porch.—The vestibule or entrance to a building.

Portico.—A kind of gallery or piazza, frequently erected in front of large buildings.

Posts.—Square timbers set on end; the term is especially applied to those which support the corners of a building, and are then framed into the bressummer or cross-beam, under the walls.

Pricking-up.—The first coat of plaster worked upon laths.

Profile. The outline; the contour of a part, or the parts compassing an order.

Pugging.—The stuff laid upon sound boarding to prevent the passage of sound from one story to another.

Puncheons.—Short pieces of timber employed to support a weight

when the bearing is too distant.

Purlines.—Those pieces of timber which lie across the rafters to

prevent them from sinking.

Putlogs.—Pieces of timber used in building a scaffold; they are those which lie at right angles to the line of wall, and rest on the scaffold poles or ledgers.

Pyramid.—A solid massive edifice which rises from a square or

rectangular base, and terminates in a point called the vertex.

#### Q.

Quarter Round.—See "Ovolo."

Quarters.—Pieces of timber used in an upright position for partitions. Quarters may be either single or double; the single are generally two inches thick, and four inches broad; the double are four inches square. The quarters are never placed at a greater distance than fourteen inches from each other.

Quirk.—A piece of ground taken out of a plot. The term is also applied to a particular form of moulding, one which has a sudden

convexity.

Quoins.—The corners of a building; they are called rustic quoins when they project from the wall, and have their edges chamfered off.

#### R.

Rabbet or Rebate.—A groove or channel in the edge of a board.

Rafters.—Those timbers which form the inclined sides of a roof.

Raking.—Means literally inclining, and is applied to those mouldings which, instead of maintaining the horizontal line, are suddenly bent out of their course.

Rails.—Those pieces in framing which lie in a horizontal position are called rails; those which are perpendicular are called stiles; hence two rails and two stiles inclose a panel. The term is also applied to those pieces in fences or paling which go from post to post.

Relief.—The projection which a figure has from the ground on

which it is carved.

Return.—That part of any work which falls away from the line in front.

Ridge.—The highest part of a roof, or the timber against which the rafters putch.

Riser —That board in stairs set on edge under the tread or step of the stair.

Rustic.—This term is applied to those courses of stone-work, the face of which is jagged or pecked so as to present a rough surface. That work also is called rustic in which horizontal and vertical channels are cut in the joinings of the stones, so that when placed together an angular channel is formed at each joint.

#### S

Sash.—The framework which holds the squares of glass in a window.

Sash-frame.—The frame which receives the sash.

Scantting.—The measure to which a material is to be or has been cut.

Scotia.—A semicircular concave moulding, chiefly used between the tori in the base of a column.

Scribing .- Fitting wood-work to an irregular surface.

Scroll.—A carved curvilinear ornament, somewhat resembling in

profile the turnings of a ram's horn.

Sill.—The horizontal piece of timber at the bottom of framing; the term is chiefly applied to those pieces of timber or stone at the bottom of doors or windows.

Shaft.—The body of a column; that part between the base and

eapital.

Shore.—A piece of timber placed in an oblique direction to support a building or wall.

Skirting.—The narrow boards placed round an apartment against

the walls, and standing vertically on the floor.

Sleepers.—Pieces of timber placed on the ground to support the ground-joists, or other woodwork.

Soffit.—A term applied to a frame or paneling overhead, or to a lining, such as that which is fixed in the underside of the tops of windows.

Stiles.—The upright pieces in framing or paneling. Struts.—Pieces of timber which support the rafters.

Summer.—A large piece of timber supported by piers or posts; when it supports a wall, it is called a breast-summer, or bressummer.

#### T.

Tenon.—A piece of wood so formed as to be received into a hole in another piece called a mortice.

Throat.—That hollow which terminates the upper end of the

shaft of a column.

Tongue.—That projecting piece at the end of a board which is formed to be inserted into a groove.

Torus.-A moulding that has a convex semicircular or semi-

elliptical profile.

Transom —  $\Lambda$  piece that is framed across a double window-light. Trellis.—An open framing, pieces crossing each other so as to form

diamond or lozenge-shaped openings.

Tryglyphs.—Ornaments in the Doric frieze consisting of a square projection with two angular channels, the edges of each forming half a channel. They are placed immediately over the centre of a column; their width is generally one module.

Trimmers.—Pieces of timber framed at right angles to the joist

for chimneys, and the well-holes of stairs.

Tympanum.—The space inclosed by the inclined and horizontal sides of a pediment.

### V.

Valley — The space between two inclined sides of a roof.

Vaults.—Underground buildings with arched ceilings, whether circular or elliptical.

Vertex.—The top or summit of a pointed body, as of a cone.

Volute.—The scroll in the capital of the Ionic order.

Voussoirs.—The stones which compose the face of an arch, having a somewhat wedge-shaped form.

#### W.

Wall-plates.—The timbers built up with a wall, to carry the joists.

Weather-boarding .- Weather-edge boards, fixed vertically, so as

to lap over one another.

Well-hole.—The aperture left in floors to bring up the stairs.

## GLUES.

### Parchment Glue.

Parchment shavings 1 pound; water 6 quarts. Boil until dissolved, then strain and evaporate slowly to the proper consistence. Use a water bath if you want it very light colored.

# Japanese Cement, or Rice Glue.

Rice flour; water, sufficient quantity. Mix together cold, then bring the mixture to a boil, stirring it all the time. Observe to boil it in a vessel that will not color it.

# Japanners' Gold Size.

Gum ammoniac 1 pound; boiled oil 8 ounces; spirits of turpentine 12 ounces. Melt the gum, then add the oil, and lastly the spirits of turpentine.

#### Gold Size.

Yellow ochre 1 part; copal varnish 2 parts; linseed oil 3 parts; turpentine 4 parts; boiled oil 5 parts. Mix. The ochre must be in the state of the finest powder, and ground with a little of the oil before mixing.

### Glue Liquid.

Glue, water, vinegar, each 2 parts. Dissolve in a water-bath, then add alcohol 1 part. An excellent cement.

## Transparent Liquid Japan for Metal.

Copal varnish 35 parts; camphor 1 part; boiled oil 2 parts. Mix.

### Portable Glue for Draughtsmen, &c.

Glue 5 parts; sugar 2 parts; water 8 parts. Melt in a water-bath, and cast it in moulds. For use, dissolve in warm water.

### Waterproof Glue.

1. Glue 1 part; skimmed milk 8 parts. Melt and evaporate in a

water-bath to the consistence of strong glue.

2. Glue 12 parts; water sufficient to dissolve. Then add yellow resin 3 parts, and when melted add turpentine 4 parts. Mix thoroughly together. This should be done in a water-bath.

# PAPERS.

## Fire-proof Paper.

Take a solution of alum and dip the paper into it, then throw it over a line to dry. This is suitable to all sorts of paper, whether plain or colored, as well as textile fabrics. You must try a slip of the paper in the flame of a candle, and if not sufficiently prepared dip and try it a second time.

#### Black Edge Paper.

Blacklead 11 parts; common ink 22 parts; dissolved gum-arabic 1 part. Mix. Then with a sponge lay the color on the edge of the paper, previously placed in the cutting-press, rub it in with a piece of cloth, and burnish. The edge of the paper must be rendered perfectly smooth before applying the black.

#### To Stain Paper or Parchment.

Red.—Brazil 12 parts; water 70 parts; alum 5 parts. Boil.

1. Blue.—Sulphate of indigo. Water to dilute.

Prussian blue 2 parts; muriatic acid 1 part. Water to dilute.
 Logwood 4 parts; water 30 parts; sulphate of copper 1 part.

Green.—Crystals of verdigris 2 parts; vinegar 1 part. Water to dilute.

Yellow.-French berries, water, and a little alum. Boil.

Purple.—Logwood 2 parts; alum 1 part; water 20 parts. Boil. The addition of a little gum to the above renders them suitable for coloring maps, &c.

#### Paper for Draughtsmen, &c.

Powdered tragacanth 1 part; water 10 parts. Dissolve and strain through clean gauze, then lay it smoothly with a painter's brush on the paper, previously stretched on a board. This paper will take either oil or water colors.

#### Copying Paper.

Lay open your quire of paper (clean white, of large size), take the brush and cover it with the following varnish, then hang it up on the line; take another sheet and repeat the operation, until you have finished your quantity. If not clear enough, give each sheet another coat when dry:—Canada balsam, turpentine, equal parts. Mix.

#### Liquid Gold, for Vellum, &c.

Take gold-leaf and grind it with gum-water; then add a small quantity of bichloride of mercury, and bottle for use.

#### Liquid Silver, for Vellum, &c.

Take silver-leaf and grind it, with gum-water or glair of egg.

#### Paper that Resists Moisture.

Take unsized paper, lay it flat on a clean surface, and brush it over with a solution of mastic in oil of turpentine; or plunge it into the solution and hang it up to dry. This paper possesses all the usual qualities of writing paper, with the advantage of resisting moisture.

#### To Detect the presence of Plaster in Paper.

Calcine the paper in a close vessel, and dilute the residue with

PAPERS.

vinegar, in a silver spoon; if sulphuretted hydrogen is disengaged, which blackens the spoon, the presence of a sulphate (plaster) will be shown. This adulteration has lately become very common among the paper-makers, with the view of increasing the weight.

#### Waxed Paper.

Take cartridge or other paper, place it on a hot iron and rub it with beeswax, or make a solution of the wax in turpentine, and apply it with a brush. Useful for making water or air-proof pipes, for chemical experiments, &c.

#### To extract Grease Spots from Paper.

Apply a little powdered pipe-clay, on which place a sheet of paper, then use a hot iron. Remove the adhering powder with a piece of India-rubber.

#### Papier Mâché.

Take paper, any quantity. Boil it well, then pound it to a paste, and mould. Used in making toys, snuff-boxes, &c.

#### To Gild the Edges of Paper.

Armenian bole 4 parts; sugar candy 1 part. White of egg to mix. Apply this composition to the edge of the leaves, previously firmly screwed in the cutting-press; when nearly dry smooth the surface with the burnisher; then take a damp sponge and pass over it, and with a piece of cotton-wool take the leaf from the cushion and apply it to the work; when quite dry burnish, observing to place a piece of silver or India paper between the gold and the agate.

#### Tracing Paper.

Nut oil 4 parts; turpentine 5 parts. Mix, and apply it to the paper, then rub it dry with wheat flour, and brush it over with oxgall. This will bear writing on.

#### Lithographic Paper.

Give the paper 3 coats of thin size, 1 of starch, and 1 of solution of gamboge. Each to be applied with a sponge, and allowed to dry before the next is applied.

#### Hydrographic Paper.

This name has been given to paper which may be written on with water. It may be made by rubbing paper over with a mixture of finely powdered galls and sulphate of iron heated till it becomes white. The powder may be pressed into the paper by passing it between rollers, or passing a heavy iron over it. A mixture of dried sulphate of iron and ferro-prussiate of potash may be used for blue writing. Or the paper may be imbued with a strong solution of one ingredient thoroughly dried, and the other applied in powder. Paper which has been wet with a solution of ferro-

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prussiate of potash also serves for writing on with a colorless solution of persulphate of iron.

#### Iridescent Paper.

Nut-galls 8 parts; sulphate of iron 5; sal-ammoniac 1; sulphate of indigo 1; gum-arabic & To be boiled in water, and the paper washed with it exposed to ammonia.

To give Paper the Appearance and Toughness of Parchment.

Dip white unsized paper for half a minute in strong sulphuric acid, and afterwards in water containing a little ammonia. When dried it will look like, and be as strong as parchment.

Photographic Papers.

The following papers should be the finest satin post, of uniform texture, free from the maker's mark, specks, and all imperfections. The papers must be prepared by candle-light, and kept in the dark till used.

- 1. Simple Nitrated Paper.—This is merely paper brushed over with a strong solution of nitrate of silver. In brushing over the paper it must be crossed. Its sensitiveness is increased by using spirit of wine instead of water. This paper only requires washing in water to fix the drawing.
- 2. Muriated Paper.—The paper is first soaked in solution of copper salt, pressed with a linen cloth or blotting paper, and dried. It is then brushed over on one side (which should be marked near the edge) with the solution of nitrate of silver, and dried at the fire. The stronger the solution the more sensitive the paper. If dipped in a solution consisting of 35 grains of chloride of barium and 2 oz. of distilled water, richer shades of color are obtained.
- 3. Iodized Paper.—Brush over the paper on one side (which should be marked) with strong solution of nitrate of silver (100 gr. to 1 oz); then dip it in a solution consisting of 100 gr. of iodide of potassium dissolved in 4 oz. of distilled water. Wash it in distilled water, drain, and dry it.
- 4. Bromide Paper.—Soak the paper in a solution composed of 40 gr. bromide of potassium dissolved in 1 oz. of distilled water; then brush it over with a strong solution of nitrate of silver, and dry in the dark.
- 5. Calotype Paper.—Dissolve 100 gr. of crystallized nitrate of silver in 2 oz. of distilled water, and add 2 fluid dr. and 40 minims of acetic acid. Mix these at the time of using with an equal measure of cold saturated recently prepared solution of gallic acid. Brush iodized paper with this solution, and mark the side; in half a minute dip it into water, and press it between blotting paper. It is then ready for the camera, where it remains from half a minute to 5 minutes. When removed from the camera dip it into water,

press it between blotting paper, and wash it with a solution of 100 gr. of bromide of potassium in 8 or 10 oz. of water.

- 6. Chromotype Paper.—Soak the paper in a solution of bichromate of potash (in which solution a little sulphate of indigo is sometimes added to vary the color), and dry it at a brisk fire. To fix the drawing careful immersion in warm water is all that is required. It is not sufficiently sensitive for the camera.
- 7. Compound Chromotype Paper.—Dissolve 10 gr. of bichromate of potash, and 20 gr. of sulphate of copper, in an ounce of water. Wash the paper in this solution, and dry it. After the paper has been exposed to the sun, with the article to be copied superposed upon it, it is washed over in the dark with a solution of nitrate of silver of moderate strength. A vivid picture makes its appearance, which is sufficiently fixed by washing in pure water. This is for copying engravings, &c. Another method is to brush writing paper over with a solution of 1 dr. of sulphate of copper in 1 oz. of water; and when dry with a strong, but not saturated, solution of bichromate of potash.
- 8. Cyanotype Paper.—Brush the paper over with a solution of ammonio-citrate of iron. Expose the paper in the usual way, then wash it over with a solution of ferro-cyanide of potassium.
- 9. Crysotype Paper.—Wash the paper with solution of ammoniocitrate of iron, dry it, and afterwards brush it over with a solution of ferro-cyanide of potassium. Dry it in a dark room. The image is brought out by brushing it over with a neutral solution of gold or silver.
- 10. Catalisotype.—Steep paper in water, with a drop or two of hydrochloric acid; absorb the superfluous moisture with blotting paper; brush over with a mixture of  $\frac{1}{2}$  dr. syrup of iodide of iron,  $2\frac{1}{2}$  dr. of water, and a drop or two of tincture of iodine. Dry with blotting paper, and brush over with a solution of 12 gr. of nitrate of silver to 1 oz. of distilled water. It is then ready for the camera. The picture is fixed by washing in water, and afterwards in a solution of 20 gr. of bromide to 1 oz. of potassium.
- 11. Paper for Positive Photographs.—Most of the preceding give negative pictures, the lights and shadows being reversed; in the following they are correct: Dissolve 40 gr. of muriate of ammonia in 4 oz. of water. Wash highly glazed paper in this solution, dry it, and brush it over with the following solution: Dissolve 120 gr. of crystallized nitrate of silver in  $1\frac{1}{2}$  oz. of distilled water; and add  $1\frac{1}{2}$  oz of alcohol; after it has stood a few hours filter it. Expose the paper thus washed to the sunshine, till it is darkened; if mottled, wash it a second time, and expose it again. Before using the paper make up the following solution: Hydriodate of barytes 40 gr.; water 1 oz.; pure sulphate of iron 5 gr. Mix, filter, add a drop or two of diluted sulphuric acid, and when settled decant the clear liquor for use. Wash the paper over in this solution, expose

it in the damp state, with the engraving or other object on it to the light, and fix the drawing by washing with water only.

#### Photographs.

To copy objects, lay them on a plate of clear glass, fixed in a frame; place the prepared paper over them; and fix a back, with a cushion attached to it, so as to press the paper closely on the glass. The glass is then exposed to the light, and the drawing afterwards fixed, as described above. For feathers, lace-work, and other objects which freely admit light through them, the nitrated paper and less sensitive muriated papers may be used. For copying engravings, leaves, and other botanical objects, or entomological specimens, the more sensitive muriated papers, or the bromide paper, or other sensitive kinds, may be used. Engravings should be wetted, and placed with their face to the prepared side of the paper, and kept in close contact with it. Leaves should have their under surface next the glass. For the camera, the most sensitive samples of the muriated papers, made with not less than 100 gr. of nitrate of silver to the ounce, are selected. The calotype is still more certain. The papers intended for the camera require to be very carefully prepared. Glass is used instead of paper, after being coated with white of egg, or collodion, with which the compounds of silver are mixed, or over which they are brushed.

#### BRONZING.

Bronzing Sculpture, Wood, &c.

Bronze of a good quality acquires, by oxidation, a fine green tint, called patina antiqua. Corinthian brass receives, in this way, a beautiful clear green color. This appearance is imitated by an artificial process, called bronzing. A solution of sal-ammoniac and salt of sorrel in vinegar is used for bronzing metals. Any number of layers may be applied, and the shade becomes deeper in proportion to the number applied. For bronzing sculptures of wood, plaster figures, &c., a composition of yellow ochre, Prussian blue, and lamp-black, dissolved in glue-water, is employed.

#### Bronze.

- 1. Copper 83 parts; zinc 11 parts; tin 4 parts; lead 2 parts. Mix.
  - 2. Copper 14 parts; melt, and add zinc 6 parts; tin 4 parts.

#### Ancient Bronze.

Copper 100 parts; lead and tin each 7 parts. Mix.

To give an Antique Appearance to Bronze Figures.

Salt of sorrel 1 part; sal ammoniac 4 parts; white vinegar 224 parts. Dissolve, and apply with a camel-hair peneil, just sufficient to damp the bronze, previously warmed. Repeat the operation if required.

#### Keller's Bronze.

Copper 91 parts; tin 2 parts; zinc 6 parts; lead 1 part. Mix.

#### Bronze Powder.

Bichloride of mercury 1 part; borax and nitre each 8 parts; tutty 16 parts; verdigris 32 parts; oil to make into a paste. Melt.

#### Beautiful Red Bronze Powder.

Sulphate of copper 100 parts; carbonate of soda 60 parts. Apply heat until they unite into a mass, then cool, powder, and add copper filings 15 parts. Well mix, and keep them at a white heat for twenty minutes, then cool, powder, and wash and dry.

#### Bronzing Fluid for Guns, &c.

Nitric acid sp. gr. 1.2, nitric ether, alcohol, muriate of iron, each 1 part. Mix, then add sulphate of copper 2 parts; dissolved in water 10 parts.

#### ENAMELS.

#### White Enamel.

Tin 2 parts; lead 1 part. Calcine, then take of the above oxides 1 part; crystal 2 parts; manganese a small portion. Grind well together, fuse, and pour the mass into cold water; dry, grind again to powder, and fuse; repeat the process four or five times, observing great care to prevent any contamination from smoke, or iron, or copper.

#### Another.

Arsenic 14 parts; potash 25 parts; nitre 12 parts; glass 13 parts; flint 5 parts; litharge 3 parts.

#### Blue Enamel.

Fine paste (not metallic) 10 parts; nitre 3 parts. Oxide of cobalt to color.

#### Green Enamel.

Frit 1 pound; oxide of copper 1 ounce; red oxide of iron 12 grains.

#### Fluxes of Enamel Colors.

1. Flint powder 1 part; calcined borax 1 part; flint glass 3 parts; red lead 4 parts. Keep them in a state of fusion, in a Hessian crucible, for three hours; then pour into cold water, dry, and powder.

2. Glass powder 11 parts; white arsenic 1 part; nitre 1 part.

Mix.

#### Yellow Enamel.

White oxide of antimony 1 part; white lead 2 parts; alum and sal-ammoniac each 1 part. Mix in fine powder, and apply just sufficient heat to decompose the ammoniac.

#### Black Enamel.

Clay 2 parts; protoxide of iron 1 part. Mix.

#### MARBLE STAINING.

#### To Stain Marble.

It is necessary to heat the marble hot, but not sufficiently so as to injure it, the proper heat being that at which the colors nearly boil.

Blue.—Alkaline indigo dye, or turnsole with alkali.

Red.—Dragon's blood in spirits of wine.

Yellow.—Gamboge in spirits of wine.

Gold Color.—Sal-ammoniac, sulphate of zinc, and verdigris, equal parts.

Green.—Sap green, in spirits, with potash.

Brown.—Tincture of logwood.

Crimson.—Alkanet root in turpentine.

The marble may be veined according to taste. To stain marble well is a tedious and difficult operation.

#### To Stain White Marble.

Apply with a brush a strong alcohol tineture, made from the root alkanet.

#### To Clean Marble.

Chalk (in fine powder) 1 part; pumice 1 part; common soda 2 parts. Mix. Wash the spots with this powder, mixed with a little water; then clean the whole of the stone, and wash off with soap and water.

#### To Extract Oil from Stone or Marble.

Soft soap 1 part; Fuller's earth 2 parts; potash 1 part; boiling water to mix. Lay it on the spots of grease, and let it remain for a few hours.

# COMPOUND COLORS IN DYEING,

Are produced by mixing together two simple ones; or, which is the same thing, by dyeing cloth first of the simple color, and then by another. These colors vary to infinity, according to the proportions of the ingredients employed. From blue, red, and yellow, red-olives, and greenish-greys are made.

From blue, red, and brown, olives are made from the lightest to the darkest shades; and by giving a greater shade of red, the

slated and lavender-grevs are made.

From blue, red, and black, greys of all shades are made, such as sage, pigeon, slate, and lead-greys. The king's or prince's color is duller than usual; this mixture produces a variety of hues or colors almost to infinity.

From yellow, blue, and brown, are made the goose-dung and

olives of all kinds.

From brown, blue, and black, are produced brown-olives, and

their shades.

From the red, yellow, and brown, are derived the orange, gold color, feuille-mort or faded leaf, dead carnations, cinnamon, fawn, and tobacco, by using two or three of the colors as required.

From yellow, red, and black, browns of every shade are made.

From blue and vellow, greens of all shades.

From red and blue, purples of all kinds are formed.

#### Dyer's Spirit.

Aquafortis 10 parts; sal-ammoniae 5 parts; tin 2 parts. Dissolve.

#### Japan Grounds.

Red.—Vermillion makes a fine scarlet, but its appearance in japanned work is much improved by glazing it with a thin coat of

lake, or even rose pink.

Yellow.—King's yellow, turpeth mineral, and Dutch pink, all form very bright yellows, and the latter is very cheap. Seed-lac varnish assimilates with yellow very well; and when they are required very bright, an improvement may be effected by infusing turneric in the varnish which covers the ground.

Green.—Distilled verdigris laid on a ground of leaf gold produces the brightest of all greens; other greens may be formed by mixing King's yellow and bright Prussian blue, or turpeth mineral

and Prussian blue, or Dutch pink and verdigris.

Blue.-Prussian blue, or verditer glazed with Prussian blue or

smalt.

White.—White grounds are obtained with greater difficulty than any other. One of the best is prepared by grinding up flock-white, or zinc-white, with one sixth of its weight of starch, and drying it; it is then tempered, like the other colors, using the mastic varnish for common uses; and that of the best copal for the finest. Par-

ticular care should be taken that the copal for this use be made of the clearest and whitest pieces. Seed-lac may be used as the uppermost coat, where a very delicate white is not required,

taking care to use such as is least colored.

Black.—Ivory-black, or lamp-black; but if the lamp-black be used it should be previously calcined in a closed crucible. Black grounds may be formed on metal, by drying linseed oil only, when mixed with a little lamp-black. The work is then exposed in a stove, to a heat which will render the oil black. The heat should be low at first, and increased very gradually, or it will blister. This kind of japan requires no polishing. It is extensively used for defending iron articles from rust.

# POLISHES.

#### To Polish Brass Inlaid Work.

File the brass very clean with a smooth file; then take some tripoli powdered very fine, and mix it with the linseed oil. Dip in this a rubber of hat, with which polish the work until the desired effect is obtained.

If the work is ebony, or black rosewood, take some elder-coal powdered very fine, and apply it dry after you have done with the

tripoli, and it will produce a superior polish.

The French mode of ornamenting with brass differs widely from ours, theirs being chiefly water-gilt (or molu), excepting the flutes of columns, &c., which are polished very high with rotten stone, and finished with elder-coal.

#### To Brass Plates of Copper.

The plates previously sufficiently heated, expose them to the fumes of zinc.

#### To Clean Brass.

1. Finely powdered sal-ammoniac; water to moisten.

2. Roche alum 1 part; water 16 parts. Mix. The articles to be cleaned must be made warm, then rubbed with either of the above mixtures, and finished with fine tripoli. This process will give them the brilliancy of gold.

#### To Brass Vessels of Copper.

Argol 1 part; amalgam of zine 1 part; muriatic acid 2 parts; water to fill the vessel. Boil.

#### Method of Cleaning Brass Ornaments.

Brass ornaments that have not been gilt or lacquered may be cleaned, and a very brilliant color given to them, by washing them

with alum boiled in strong ley, in the proportion of an ounce to a pint, and afterwards rubbing them with strong tripoli.

#### French Polish.

Alcohol 260 parts; copal varnish 13 parts; sandarach (powdered) 1 part; mastic (powdered) 1 part; shell-lac (powdered) 24 parts. Mix, and digest in a moderate heat, in a strong close vessel.

#### To French Polish.

The varnish being prepared (shell-lac), the article to be polished being finished off as smooth as possible with glass paper, and your rubber being prepared as directed below, proceed to the operations as follows: The varnish, in a narrow necked bottle, is to be applied to the middle of the flat face of the rubber, by laying the rubber on the mouth of the bottle and shaking up the varnish once, as by this means the rubber will imbibe the proper quantity to varnish a considerable extent of surface. The rubber is then to be inclosed in a soft linen cloth, doubled, the rest of the cloth being gathered up at the back of the rubber, to form a handle. Moisten the face of the linen with a little raw linseed oil, applied with the finger to the middle of it. Placing your work opposite the light, pass your rubber quickly and lightly over its surface until the varnish becomes dry, or nearly so; charge your rubber as before with varnish (omitting the oil), and repeat the rubbing, until three coats are laid on, when a little oil may be applied to the rubber, and two coats more given to it. Proceeding in this way, until the varnish has acquired some thickness, wet the inside of the linen cloth, before applying the varnish, with alcohol, and rub quickly, lightly, and uniformly the whole surface. Lastly, wet the linen cloth with a little oil and alcohol without varnish, and rub as before till dry.

To make the Rubber.—Roll up a strip of thick woollen cloth which has been torn off, so as to form a soft elastic edge. It should form a coil from one to three inches in diameter, according to the

size of the work.

#### BOOKBINDERS' RECIPES.

Japan Coloring, for Leather Book-Covers, &c.

After the book is covered and dry, color the cover with potashwater mixed with a little paste, give it two good coats of Brazil wash, and glair it. Put the book between wands, allowing the boards to slope a little. Dash on copperas water, then with a sponge full of red liquid, press out on the back and on different parts large drops, which will run down each board, and make a fine shaded red. When the cover is dry wash it over two or three times with Brazil wash, to give it a brighter color.

#### Blue Sprinkle for Bookbinders.

Strong sulphuric acid 8 ounces; Spanish indigo, powdered, 2 oz. Mix in a bottle that will hold a quart, and place it in a water-bath to promote solution. For use, dilute a little to the required color in a teacup.

#### Bine Marble for Books, &c.

Color the edges with King's yellow, and when dry tie the book between boards. Throw on blue spots in the gum trough, wave them with the iron pin, and apply the edges thereon.

#### Brown Color for Marbling or Sprinkling Books.

1. Logwood chips 1 part; annatto 1 part; boil in water 6 parts. If too light, add a piece of copperas about the size of a pea.

2. Umber, any quantity. Grind it on a slab with ox gall and a little lampblack. Dilute with ale.

#### Gold Sprinkle for Books.

Put into a marble mortar half an ounce of pure honey and one book of gold leaf, rub them well together until they are very fine, add half a pint of clear water, and mix them well together: when the water clears, pour it off, and put in more, till the honey is all extracted, and nothing remains but the gold. Mix one grain of corrosive sublimate in a teaspoonful of spirits of wine, and when dissolved, put the same, together with a little gum-water, to the gold, and bottle it close for use. The edges of the book may be sprinkled or colored very dark, with green, blue, or purple, and lastly with the gold liquid, in small or large spots, very regular, shaking the bottle before using. Burnish the edges when dry, and cover them with paper to prevent the dust falling thereon. This sprinkle will have a most beautiful appearance on extra work; ladies may use it for ornamenting their fancy work, by putting it on with a pen or camel's-hair brush, and when dry burnish it with a dog's tooth.

#### Marble for Leather Book-covers.

Wash the cover and glair it, take a sponge charged with water, having the book between wands, and drop the water from the sponge on the different parts of the cover, sprinkle very fine with vinegar black, then with brown, and lastly with vitriol water. Observe to sprinkle on the colors immediately after each other, and to wash the cover over with a clean sponge and water.

#### Chinese Edge for Books.

1. Color the edge with light liquid blue and dry; then take a sponge charged with vermillion, and dab on spots according to fancy; next throw on rice, and finish the edge with dark liquid blue.

2. Color light blue on different parts of the edge with a sponge; do the same where there are vacancies with yellow and Brazil red;

dry and dab on a little vermillion in spots; then throw on rice, and finish with a bold sprinkle of dark blue. Burnish.

#### Wax Marble for Leather Book-covers, &c.

This marbling must be done on the fore edge, before the back of the book is rounded, or becomes round, when in boards, and finished on the head and foot. Take beeswax and dissolve it over the fire in an earthen vessel; take quills stripped of their feathers, and tie them together; dip the quill-tops in the wax, and spot the edge, with large and small spots; take a sponge charged with blue, green, or red, and smear over the edge; when done, dash off the wax, and it will be marbled. This will be useful for stationery work, or for folios and quartos.

#### Egyptian Marble for Leather Book-covers.

1. Yellow.—Boil quercitron bark with water and a little powdered alum, over a slow fire, until it is a good strong yellow. Pour the liquid into a broad vessel, sufficiently large to contain the cover when extended. Before the liquid is cool, take the dry cover, and lay the grain side flat on the color; press it lightly that the whole may receive the liquid; let it soak some time, and then take it from the vessel. The book must be covered in the usual manner, and permitted to dry from the fire. Glair the book; when dry, place it between the wands; take a sponge and water, and press large spots thereon; dip a quill-top into the vinegar black, with it touch the water on the cover in different parts, which will have a fine effect when managed with care. Let it stand a few minutes, then take off the water with a clean sponge.

2.—Green.—Color the cover in a large vessel, as mentioned before, with Scott's liquid blue; when done, put it into a vessel of clear water for an hour. Take it out and press out the water, then cover the book. Glair the cover; when dry, place it between wands, and drop weak potash water from a sponge thereon; dip the quill-top into the strong black, and touch the water with it. This must be repeated till you have a good black. When dry,

clear it with a sponge and water.

3. Red.—Boil Brazil dust in rain-water on a slow fire, with a little powdered alum and a few drops of solution of tin, till a good color is produced. Dip a piece of calf leather into the liquid, and you may ascertain the color wanted. If too light, let it boil till it is reduced to one half of the quantity; take it from the fire, add a few more drops of the solution of tin, and pour it into a large vessel. Put the dry cover on the liquid, and let it remain for a quarter of an hour, then press out the water. Color it over with a sponge and the quercitron bark water, and cover the book. Glair the cover, place it between wands, dash on water with a brush, also potash water; and, lastly, finish it with the strong vinegar black, with the quill-top. Observe that too much black is not put

on; the intention of the marble is to show the red as transparently as possible.

#### French Marble for Books.

Provide a wooden trough, two inches deep, six inches wide, and the length of a super-royal sheet. Boil in a brass or copper pan any quantity of linseed and water, until a thick mucilage is formed; strain it into the trough and let it cool; then grind on a marble slab any of the following colors in small-beer: Prussian blue, king's yellow, rose pink, vermillion, flake white, lamp-black, brown umber, green, blue, and yellow, orange, red, and yellow, purple, red, and blue, brown, black, and yellow, or red.

The lamp-black and umber must be burnt over the fire to deprive

them of their greasy nature.

For each color you must have two cups, one for the color after grinding, the other to mix it with ox-gall, which must be used to thin the colors at discretion. If too much gall is used the colors will spread; when they keep their place on the surface of the trough, when moved with a quill, they are fit for use.

To prevent the water entering between the leaves of the book, tie it tight between cutting-boards of the same size, and place the trough in a steady situation, to prevent the colors from moving.

Having all things in perfect readiness for marbling, supposing you begin with the blue, throw on with the brush bold spots of blue, sprinkle very fine with the white on the blue spots, fill up the spaces with red and yellow, by dipping first the quill-top into the yellow, and touching the gum therewith, then with the red. The red and yellow may be waved or drawn round the blue spots with an iron pin, or as the marbler may think proper, according to fancy.

Hold the book with its edge downwards, and press it lightly on the colors so disposed on the gum, and the edge will be immediately marbled. The colors that may remain on the gum must be taken off, by applying paper thereon, before you prepare for marbling again. In this manner you may marble the edges to resemble the

end-papers, which will have a pleasing effect.

#### Chinese Marble for Leather Book-covers, &c.

Color the cover of the book dark brown, and when dry put it into the cutting-press, with the boards perfectly flat; mix whiting and water of a thick consistence and throw it on, in spots or streaks, some large and some small, which must remain till dry. Spot or sprinkle the cover with liquid blue, and lastly throw on large spots of liquid red. The colors must be dry before washing off the whiting.

#### Orange Sprinkle for Books.

Color the edge with King's yellow, mixed in weak gum-water, then spriakle with vermillion mixed in the same manner.

#### Green Sprinkle for Books.

1. Yellow the edge, then sprinkle with dark blue.

2. French berries 1 part; soft water 8 parts. Boil, and add a little powdered alum; then bring it to the required shade of green, by adding liquid blue.

#### Green Marble for Leather Book-covers, &c.

The edge must be marbled with a good bright green only. When the color is prepared with the ox-gall, and ready for use, a few drops of sweet oil must be mixed therein, the color thrown on with a brush, in large spots, till the gum is perfectly covered. The oil will make a light edge round each spot, and have a good effect.

Blue, green, and brown may be also used separately in like

manner

Sheets of paper may be done, having a trough large enough, and the sheets damped as for printing, before marbling.

Spirits of turpentine may be sprinkled on the colors, which will

make white spots.

#### Binder's Thread Marble.

Yellow the edge; when dry, cut pieces of thick thread over the edge, which will fall on different parts irregularly; give it a fine dark sprinkle, and shake off the thread.

#### Rice Marble, for Leather Book-covers, &c.

Color the cover with spirits of wine and turmeric, then place on rice in a regular manner; throw on a very fine sprinkle of copperas-water till the cover is nearly black, and let it remain till dry. The cover may be spotted with the red liquid or potash-water, very freely, before the rice is thrown off the boards.

#### Orange Color for Marbling or Sprinkling Books, &c.

Ground Brazil-wood 16 parts; annotto 4 parts; alum, sugar, and gum-arabic, each 1 part; water 70 parts. Boil, strain, and bottle.

#### Tree Marble, for Leather Book-covers ..

A marble in the form of trees may be done by bending the boards a little on the centre, using the same method as the common marble, having the cover previously prepared. The end of a candle may be rubbed on different parts of the boards, which will form knots.

#### Vinegar Black for Bookbinders, &c.

Steep iron filings or rusty iron in good vinegar for two or three days, then strain off the liquor.

#### To Sprinkle Books.

Take a stiff brush made of hogs' bristles, perfectly clean, dip it in the color; squeeze out the superfluous liquid; then rub a

folding-stick across the brush, and a fine sprinkle will fall on the edge of the book, which should be previously screwed tight in the cutting-press. Repeat the operation until the color is thrown equally on every part of the leaves. The brush should be held in the left hand, and the stick in the right.

#### Purple Sprinkle for Bookbinders.

Logwood chips 4 parts; powdered alum 1 part; soft water 24 parts. Boil until reduced to sixteen parts, and bottle for use.

2. Brazil dust (fine), and mix it with potash-water for use.

#### Soap Marble for Books.

This is applicable for marbling stationery, book edges, or sheets

of paper for ladies' fancy work.

Grind, on a marble slab, Prussian blue, with water, and a little brown soap, to a fine pliable consistence, that it may be thrown on with a small brush.

Grind King's yellow, in the same manner, with water and white

soap.

When green is intended for the ground color, grind it with brown soap, and King's yellow with white soap. Lake may be used for a ground color, and Prussian blue ground with white soap; brown umber for a ground color, and flake-white ground with white soap. Any color of a light substance may be ground for marbling.

#### Spotted Marble for Books, &c.

After the fore-edge of the book is cut, let it remain in the press, and throw on linseeds in a regular manner; sprinkle the edge with any dark color, till the white paper is covered, then shake off the seeds. Various colors may be used. The edge may be colored with yellow or red before throwing on the seeds and sprinkling with blue. The seeds will make a fine fancy edge when placed very thick on different parts, with a few slightly thrown on the spaces between.

Brown Sprinkle for Leather Book-covers, &c.

Pearlash or potash 1 part; soft water 4 parts. Dissolve and strain.

#### Red Sprinkle for Binders.

Brazil-wood (ground) 4 parts; alum 1 part; vinegar 4 parts; water 4 parts. Boil until reduced to seven parts, then add a small quantity of loaf-sugar and gum. Bottle for use.

Black Sprinkle for Leather Book-covers, &c.
Green copperas 1 part; soft water, hot, 6 parts. Dissolve.

Stone Marble for Leather Book-covers, &c.

Glair the cover, and when dry put the book into the cuttingpress, with the boards sloping, to cause the colors to run gently down. Throw on weak copperas-water with a brush; dip a sponge into the strong potash-water, and press out the color from the sponge on different parts of the back, so that the colors may run down each side from the back. Where the brown has left a vacancy apply vitriol-water in the same manner. The book must remain till perfectly dry before washing it.

# CRAYONS.

#### Lithographic Crayons.

1. Take white wax 4 parts; gum-lac 2 parts. Melt over a gentle fire, then add dry tallow soap in shavings 2 parts. Stir until dissolved. Next add white tallow 2 parts; copal varnish 1 part; lampblack 1 part. Mix well, and continue the heat and stirring until, on trial by cooling a little, it appears of a proper quality, which should be that it will bear cutting to a fine point, and trace delicate lines without breaking.

2. Take dry white tallow soap 6 parts; white wax 6 parts;

lampblack 1 part. Fuse in a covered vessel.

3. Take lampblack 1 part; tallow soap 2 parts; shell-lac 2

parts; wax 4 parts. Mix, with heat, and mould.

4. Take dried tallow soap 5 parts; wax 4 parts; lampblack 1 part. Mix as before.

#### Crayons.

1. Shell-lac 6 parts; spirit 4 parts; turpentine 2 parts; color 12 parts; pale clay 12 parts. Mix.

2. Pipe-clay, color as required, water to mix. Form into a stiff

paste, and roll it into crayons.

#### To Fix Crayon Colors.

Paste your paper on canvass, in a frame, in the usual way, then brush over the back two or three times with the following mixture, and when the last coat is dry give the face of the picture one or two coats in the same way. This will make it resemble an oil painting. Spirits of turpentine 10 parts; boiled oil 6 parts. Mix.

#### To render permanent Chalk or Pencil Drawings.

Lay the drawing on its face, and give the back two or three thin coats of the following (No. 1) mixture; let it dry, and turn it with the chalk upwards, and give that side one or two coats also; lastly, if you choose, give it one or two coats of No. 2.

1. Isinglass or gum-arabic 5 parts; water 12 parts. Mix.

2. Canada balsam 4 parts; turpentine 5 parts. Mix.

#### Wash to fix Blacklead Peneil Drawings.

1. Isinglass 1 part; water 50 parts. Dissolve with heat, and filter.

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2. Take skimmed milk, and strain. For use, pour the liquid on a surface sufficiently large, and take the drawing by the corners, lay it flat on the wash, then carefully remove it, and place it on a slanting surface to drain and dry. This will also answer for chalk drawings.

### GILDING.

#### To Gild or Silver Leather.

Finely powder resin, and dust it over the surface of the leather, then lay on the leaf, and apply (hot) the letters or impression you wish to transfer; lastly, dust off the loose metal with a cloth. The cloths used for this purpose become, in time, very valuable, and are often sold to the refiners for \$5 to \$7.

#### To gild on Calf and Sheep Skin.

Wet the leather with the white of eggs; when dry rub it with your hand and a little olive oil, then put the gold leaf, and apply the hot iron to it. Whatever the hot iron shall not have touched will go off by brushing.

To gild Copper, Brass, &c. (Patent.)

Fine gold 5 parts; nitric acid (sp. g. 1.45) 21 parts; hydrochloric acid (sp. g. 1.15) 17 parts; pure water 14 parts. Digest with heat in a glass vessel until all the gold is dissolved, and till red or yellow fumes cease to rise. Decant the clear liquid into some convenient vessel, and add water, 500 to 600 parts. Boil for two hours, let it stand to settle, and pour off the clear into a suitable vessel. For use, heat the liquid and suspend the articles (previously well cleaned) by means of a hair or fine wire, until sufficiently coated with gold, then well wash them in pure water.

#### To gild Glass and Porcelain.

1. Apply to the part a surface of gold size; when nearly dry lay on the leaf.

2. Gold powder 2 parts; borax 1 part; turpentine to mix. Mix and apply to the surface to be gilded with a camel-hair pencil; when quite dry, heat it in a stove until the borax vitrifies. Burnish. Platina, silver, tin, bronze, &c., may be applied in a similar manner.

#### To give Iron the color of Copper.

Take 1 oz. of copper-plates, cleansed in the fire; 3 oz. of aquafortis; dissolve the copper, and when it is cold use it by washing your iron with it by the help of a feather; it is presently cleansed and smooth, and will be of a copper color; by much using or rubbing it will wear off, but may be renewed by the same process.

A way of Gilding with Gold upon Silver.

Beat a ducat thin, and dissolve in it two ounces of aqua-regia; dip clean rags in it, and let them dry; burn the rags, and, with the tinder thereof, rub the silver with a little spittle; be sure first that the silver be cleansed from grease.

#### Gilder's Wax.

1. Yellow wax 3 pounds; verdigris 1 pound; sulphate of zinc 1 pound; red oxide of iron 2½ pounds. Powder the last three articles very fine.

2. Yellow wax 7 pounds; colcothar 7 pounds; verdigris 3

pounds; borax 1 pound; alum 1 pound.

To dye in Gold Silver Medals, or Laminas, through and through.

Take glauber salt, dissolve it in warm water, so as to form a saturated solution. In this solution put a small proportionate quantity of calx, or magister of gold. Then put and digest in it silver laminas cut small and thin, and let them lie twenty-four hours over a gentle fire. At the end of this term you will find them thoroughly dyed gold color inside and out.

#### To gild Silks, Satins, &c.

Nitromuriate of gold, in solution, 1 part; distilled water 3 parts. Mix. Lay out any design with this fluid, and expose it, while wet, to a stream of hydrogen gas; then wash it with clear water.

#### To make Transparent Silver.

Refined silver one ounce; dissolve it in two ounces of aquafortis; precipitate it with a pugil (a quantity that may be taken up between the thumb and finger) of salt, then strain it through a paper, and the remainder melt in a crucible for about half an hour, and pour it out, and it will be transparent.

#### To make Copper into a Metal like Gold.

Distilled verdigris 4 oz.; Tutiæ Alexandrinæ præparatæ two oz.; saltpetre 1 oz.; borax ½ oz. Mix all together with oil, till they be as thick as pap; then melt it in a crucible, and pour it into a fireshovel, first well warmed.

#### Mercurial Plating.

Quicksilver 4 parts; nitric acid 4 parts; finely powdered cream of tartar 2 parts; finely powdered salt of sorrel 1 part. Dissolve the silver in the acid, then add the rest, and stir until dissolved. This imparts a pleasing silvery appearance to articles formed of copper, by merely applying it with the finger.

#### Grecian Gilding.

Take sal-ammoniac and bichloride of mercury, equal parts,

dissolve in nitric acid, and make a solution of gold with this fluid, lay it on the silver, and expose it to a red heat; it will then be gilded.

To gill or silver Writing.

Let there be a little gum and lump-sugar in the ink you write with; when dry, breathe on it and apply the leaf.

To whiten Copper throughout.

Take thin plates of copper, as thin as a knife, heat them six or seven times, and quench them in water; then melt them, and to each pound add 4 ounces of saltpetre and 4 ounces of arsenic, well powdered and mixed, and first melted apart in another crucible, by gentle degrees; then take them out, and powder them; then take Venetian borax and white tartar, of each an ounce and a half; then melt these, with the former powder, in a crucible, and pour them out into some iron receiver; it will appear as clear as crystal, and is called crystallinum fixum arsenicum. Of this clear matter, broken into little pieces, throw into the melted copper (by small pieces at a time, staying five or six minutes between each injection) 4 ounces; when all is thrown in, increase the fire, till all be well melted together for a quarter of an hour; then pour it out into an ingot.

To gild Steel.

Apply an etherial solution of gold. This is equally adapted to lettering, as wholly covering the object. It may be applied with a pen, or otherwise.

## GLASS STAINS.

Red Stain for Glass.

1. Rust of iron 100 parts; glass of antimony 99 parts; yellow glass of lead 98 parts; sulphuret of silver 3 parts. Mix.

2. White hard enamel 100 parts; red chalk 50 parts; peroxide of copper 5 parts. Reduce to fine powder, and mix.

#### Blue Glass.

Plain paste 300 parts; zaffre 3 parts; manganese 1 part. If the glass should be of too deep a blue, use less zaffre and manganese; if too purple, omit the manganese altogether.

#### Black Stain for Glass.

1. Black scales of iron 29 parts; white crystal glass 4 parts; antimony 2 parts; manganese 1 part; vinegar to mix.

2. Glass of antimony 1 part; oxide of copper 2 parts; crystal

glass 3 parts. Mix.

Orange Stain for Glass.

Precipitated silver powder, yellow ochre, red ochre, equal parts. Turpentine to mix.

Brown Stain for Glass.

White glass 2 parts; manganese 1 part. Mix.

Flesh Color for staining Glass.

Red lead 1 part; red enamel 2 parts. Mix with alcohol.

Yellow Stain for Glass.

Chloride of silver 1 part; burnt pipeclay 3 parts. Reduce to fine powder, and mix. This stain must be applied to the back of the glass.

To Marble a Glass Globe.

Grind well on a stone, minimm for red, turmerie or rather cerussa citrina, for yellow, smalt for blue, verdigris for green, ceruse, or chalk, for white. Work each in oil separate, and with a hog's hair pencil, single or mixed, as you think fit, scatter the same into the glass, and roll it, or dispose the colors, as you like. Then, last of all, fling a little mead amongst them, which sovers all.

For the Magic Lantern, paint the glasses with transparent colors,

tempered with oil of spike.

# FACTITIOUS STONES.

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Factitious Amethyst.

1. Take strass 5000 parts; oxide of manganese 37 parts; oxide of cobalt 25 parts; purple of Cassius 1 part. Fuse for twenty-six hours, and cool slowly.

2. Take paste or strass 10,000 parts; oxide of manganese 25

parts; oxide of cobalt 1 part.

#### Factitious Emerald.

1. Oxide of chrome 1 part; green oxide of copper 20 parts; strass 2300 parts. Fuse with care for twenty-six hours, then cool slowly.

2. Strass 10,000 parts; acetate of copper 150 parts; protoxide of

iron 3 parts. As before.

3. Strass 6600 parts; carbonate of copper 60 parts; glass of anti-

mony 6 parts. Fuse with care.

4. Strass 500 parts; glass of antimony 20 parts; oxide of cobalt 3 parts. As before.

Artificial Coral.

Yellow resin 4 parts; vermillion 1 part. Melt. This gives a very pretty effect to glass, twigs, cinders, stones, &c., dipped into

it. It is also useful for a cement for ladies' fancy work, such as grottoes, &c.

Paste resembling the Red Cornelian.

Plain paste 1000 parts; glass of antimony 500 parts; calcined vitriol 63 parts or less; manganese 4 parts. Melt together.

Paste resembling the White Cornelian.

Plain paste 1000 parts; yellow ochre 8 parts; calcined bones 31 parts. As before.

#### Factitious Opal.

1. Strass 500 parts; horn silver 10 parts; calcined magnetic ore 2 parts; chalk marl 25 parts. Mix in fine powder, and fuse with great care.

2. Plain paste 100 parts; calcined bones 6 parts.

#### Factitious Oriental Ruby.

Strass 7000 parts; precipitate of Cassius and nitric peroxide of iron each 165 parts; golden sulphuret of antimony 160 parts; manganese calcined with nitre 150 parts; rock crystal 1000 parts. Mix in fine powder, and carefully melt.

#### Factitious Sapphire.

1. Oxide of cobalt 1 part; strass 80 parts.

2. Paste or strass 2300 parts; oxide of cobalt 34 parts. Fuse carefully for thirty hours.

3. Plain paste 100 parts; smalts 12 parts; manganese 1 part. As

before.

4. Plain paste 10 pounds; zaffre 3 drachms; precipitate of gold and tin 1 drachm. As before.

## Factitious Topaz.

1. Strass 1000 parts; glass of antimony 42 parts; purple of Cassius 1 part Fuse for twenty-four hours, and cool slowly.

2. Strass 4000 parts; saffron of Mars 40 parts. As before.

#### To solder together Rubies.

Apply them to a strong flame by means of the blow-pipe, and when sufficiently soft unite them with care; they will neither lose their color nor weight,

#### Factitious Ruby.

Strass 40 parts; oxide of manganese 1 part. Mix, and treat as for topaz.

#### White Crystal, or Factitious Diamond.

Manganese 1 part; rock crystal 2800 parts; borax 1900 parts; white lead 5700 parts. Mix in fine powder, then fuse in a clean crucible, pour it into water, dry, powder, and repeat the process two or three times.

#### Composition for Fixed Brilliants.

Meal gunpowder 16 parts; zinc, or steel, or cast-iron borings 6 parts. Mix.

#### Paste resembling Vinegar Garnet.

Plain paste 1000 parts; glass of antimony 500 parts; calcined iron 16 parts. Add the antimony last.

#### Gold or Yellow Paste.

Take plain paste (made without the saltpetre) 100 parts; oxide of iron 1 part. Fuse.

#### Factitious Lapiz Lazuli.

Plain paste 1000 parts; calcined bones 73 parts; zaffre 7 parts; magnesia 5 parts. If it is desired to vein it with gold—gold powder and borax, equal parts; vein the cakes to taste, and then heat them sufficiently hot for cementation.

#### Foils for Crystals, Pastes,

Put two or three layers of tin-foil into the socket made for the stone, heat it gently, and fill it with quicksilver, let it rest two or three minutes, then pour it out, and place in the stone.

#### Factitious Yellow Diamond.

Strass 500 parts; glass of antimony 10 parts. Fuse.

#### Another.

Strass 500 parts; chloride of silver 25 parts. Mix, and fuse.

#### Strass, or Mayence Base.

1. Pure rock crystal, or flint, 8 parts; salt of tartar 25 parts. Powder, mix well, bake, and cool, then put it into a basin of water, and add dilute nitric acid until effervescence ceases; collect, wash, and dry the powder; next add fine white-lead 12 parts. Levigate and well wash it with pure water, then of the above mixture dried 12 parts; calcined borax 1 part. Triturate them together, melt in a clean crucible, and pour the mixture into cold water; dry, powder, and melt it in the same manner, a third time, always in a fresh crucible, observing to separate any lead that may be revived. To the third frit, ground to powder, add purified nitre \$\frac{1}{2}\$ parts. Remelt, and a mass of crystal will be found in the crucible of a beautiful and diamond-like lustre.

2. Arsenic 1 part; borax 23 parts; pure pearlash 180 parts; minium 525 parts; rock crystal 338 parts. Mix, as before.

3. Arsenic 1 part; borax 30 parts; potash 105 parts; carbonate of lead 709 parts; fine white sand 315 parts. Mix with care.

4. Arsenic 1 part; borax 35 parts; potass 325 parts; minium

900 parts; rock crystal 580 parts. Treat as before.

5. Rock crystal 400 parts; pure white lead 945 parts; pure potash 140 parts; borax 41 parts.

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6. Pure potash 2 parts; fine white sand 15 parts; litharge 20 parts. See also Paste.

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# INKS.

#### Indestructible Ink.

1. Powdered copal 25 parts; oil of lavender 200 parts; lamp-

black 2 parts; indigo 1 part. Dissolve.

2. Asphaltum 1 part; lamp-black ½ part. Melt, then add oil prepared for printers' ink, by boiling and burning until sufficiently stringy, 1½ part. Mix together, and add spirits of turpentine 3 or 4 parts. We would propose this ink, made with less turpentine, so as to be sufficiently thick for stamping, as the most perfect preventive of fraud, as when applied to the surface of an engraving, or letter-press, nothing will remove it that will not also discharge the ink of the stamp. It will stand the action of the alkalies, chlorine, acids, &c., even in a heated state, when they will at once destroy the texture of the paper.

#### Lithographic Ink.

1. Take Venice turpentine 1 part; lamp-black 2 parts; tallow 6 parts; hard tallow soap 6 parts; mastic in tears 8 parts; shell-lac 12 parts; wax 16 parts. Melt, and pour it out on a slab.

2. Take dry tallow soap 5 parts; mastic in tears 5 parts; Scotch soda 5 parts; shell-lac 25 parts; lamp-black 2 parts. Fuse the

soap and lac, then add the remainder.

For use, this ink must be rubbed down with water in a saucer (warmed), until an emulsion is formed of a proper consistence to flow easily from a pen or pencil.

## Blue Writing Fluid.

1. Ferrocyanide of iron, powdered, and strong hydrochloric

acid, each 2 parts. Dissolve, and dilute with soft water.

2. Indestructible.—Shell-lae 4 parts; borax 2 parts; soft water 36 parts; boil in a close vessel till dissolved; then filter, and take of gum-arabic 2 parts; soft water 4 parts. Dissolve, and mix the two solutions together, and boil for five minutes as before, occasionally stirring to promote their union; when cold, add a sufficient quantity of finely powdered indigo and lamp-black to color; lastly, let it stand for two or three hours, until the coarser powder has subsided, and bottle for use. Use this fluid with a clean pen, and keep it in glass or earthen inkstands, as many substances will decompose it while in the liquid state. When dry, it will resist the action of water, oil, turpentine, alcohol, diluted sulphuric acid, diluted hydrochloric acid, oxalic acid, chlorine, and the caustic alkalies and alkaline earths.

#### Red Ink for Writing.

Boil over a slow fire 4 ounces of Brazil wood, in small raspings or chips, in a quart of water, till a third part of the water is evaporated. Add during the boiling 2 drachms of alum in powder. When the ink is cold steam it through a fine cloth. Vinegar or stale urine is often used instead of water. In case of using water adding a very small quantity of sal-ammoniac would improve this ink.

#### Fine Black Writing Ink.

Take 2 gallons of a strong decoction of logwood, well strained, and then add 1½ pounds blue galls in coarse powder; 6 ounces sulphate of iron; 1 ounce acetate of copper; 6 ounces of well ground sugar; and 12 ounces of gum-arabic. Set the above on the fire until it begins to boil, then set it away until it has acquired the desired black.

#### Black Ink improved.

To 1 pint of common black ink add 1 drachm of impure carbonate of potassa, and in a few minutes it will be a jet black. Be careful that the ink does not run over, during the effervescence caused by the potassa.

#### Green Ink.

1. Cream of tartar 1 part; verdigris 2 parts; water 8 parts. Boil until reduced to a proper color.

2. Crystallized acetate of copper 1 ounce; soft water 1 pint. Mix.

#### Marking Ink.

Lunar caustic 2 parts; sap green and gum-arabic each 1 part; distilled water. Dissolve.

The Preparation.—Soda 1 ounce; water 1 pint; sap green \(\frac{1}{2}\) drachm. Dissolve, and wet the linen (where you intend to write) with this mordant, then well dry it.

#### Printing Ink.

1. (Very fine.)—Balsam of capaivi 9 parts; fine lamp-black 4 parts; indigo 1 part; dry yellow soap 3 parts. Grind perfectly smooth.

2. (Extemporaneous.)—Balsam of capaivi, lamp-black to color.

Grind well together with a little soap.

3. Take linseed oil; heat it in a proper vessel until it begins to boil, then remove it from the fire, and kindle the vapor; allow it to burn till it becomes stringy when tried between the fingers, then add gradually to every quart black resin 1 pound. Dissolve, and add very cautiously dry brown soap in shavings, 4½ ounces to every quart. Set it upon the fire, and stir the mixture until the combination is complete; next, put into a suitable pot, finely ground indigo 1 ounce; fine Prussian blue 1 ounce; fine lamp-black 18

Inks. 367

ounces. For every pound of resin employed pour the liquid on the color, well mix, and lastly, subject it to the action of a mill.

#### Indelible Ink for Marking Linen.

1. The juice of sloes 1 pint; gum ½ ounce. This requires no mordant, and is very durable.

2. Nitrate of silver 1 part; water 6 parts; gum 1 part. Dissolve.

If too thick dilute with warm soft water.

#### Autographic Ink for Lithographers.

White soap 25 parts; white wax 25 parts; mutton suet 6 parts; lamp-black 6 parts; shell-lac 10 parts; mastic 10 parts. Mix with heat, and proceed as for lithographic ink.

#### To restore Writing effaced with Chlorine.

1. Expose it to the vapor of sulphuret of ammonia, or dip it into

a solution of the sulphuret.

2. Ferrocyanide of potass 5 parts; water 85 parts. Dissolve, and immerse the paper in the fluid, then slightly acidulate the solution with sulphuric acid.

#### To give an appearance of Age to Writing.

Infuse a drachm of saffron in half a pint of ink, then write with it.

#### Perpetual Ink for Tombstones, Marble, &c.

Pitch 11 parts; lamp-black 1 part; turpentine sufficient. Mix, with heat.

#### Blue Ink.

Take sulphate of indigo, dilute it with water till it produces the color required. It is with sulphate very largely diluted, that the faint blue lines of ledgers and other account books are ruled. If the ink were used strong, it would be necessary to add chalk to it to neutralize the acid. The sulphate of indigo may be had of the woollen dyers.

#### Copying Ink.

Add 1 ounce of moist sugar to every pint of common ink.

#### Red Permanent Ink.

Vermillion 4 parts; sulphate of iron 1 part; drying oil to mix. Any other color will answer besides red. This ink will resist most of the usual reagents.

#### Black Permanent Ink.

Nitrate of silver 2 parts; distilled water 28 parts; sap green 1

part. Dissolve.

For the Mordant.—Common soda 2 parts; gum-arabic 1 part; soft water 8 parts. Mix, and moisten the linen with this fluid, and well dry before using the ink.

#### Yellow Ink.

1. French berries 1 pound; alum 2 ounces; water 1 gallon. Boil and strain, then add gum-arabic 4 ounces.

2. Water 30 parts; Avignon berries 7 parts; gum and alum each

5 parts. Boil for one hour, and strain.

#### Blue Ink for Ruling.

Take 4 ounces of vitriol, best quality, to 1 ounce of indigo; pulverize the indigo very fine; put the indigo on the vitriol, let them stand exposed to the air for six days, or until dissolved; then fill the pot with chalk, add half a gill of fresh gall, boiling it before use.

#### Black Ink for Ruling.

Take good black ink, and add gall as for blue; do not cork it, as it will prevent it from turning black.

#### Red Ink for Ruling.

One pound of Brazil wood to one gallon of the best vinegar; let the vinegar simmer before you add the wood, then let them simmer together for half an hour, then add three quarters of a pound of alum to set the color; strain it through a woollen or cotton cloth, cork it tight in a stone or glass bottle. For ruling, add half a gill of fresh gall to 1 quart of red ink, then cork it up in a bottle for use.

#### Indian Ink.

1. Take finest lamp-black, and make it into a thick paste with thin isinglass; size, then mould it; attach the gold leaf, and scent with a little essence of musk.

2. Take lamp-black, make it into a thick paste with gum-water,

and mould it.

#### Carbon Ink.

Dissolve real India ink in common black ink; or add a small quantity of lamp-black, previously heated to redness, and ground perfectly smooth with a small portion of the ink.

#### Gold and Silver Ink.

Fine bronze powder, or gold or silver leaf, ground with a little sulphate of potash, and washed from the salt, is mixed with water and a sufficient quantity of gum.

#### Gluten Ink.

Dissolve wheat gluten, free from starch, in weak acetic acid of the strength of common vinegar; mix 10 gr. of lamp-black and 2 gr. of indigo with 4 oz. of the solution, and a drop or two of oil of cloves.

#### Ink for writing on Zinc Labels—Horticultural Ink.

1. Dissolve 100 gr. of chloride of platina in a pint of water. A little mucilage and lamp-black may be added.

2. Sal-ammoniac 1 dr., verdigris 1 dr., lamp-black 1 dr., water

10 dr. Mix.

#### Chrome Ink.

Extract of logwood  $\frac{1}{2}$  oz; gum  $\frac{1}{4}$  oz; water a pint. Dissolve also in 12 oz. of water  $\frac{1}{2}$  oz. of yellow chromate of potash (or  $\frac{1}{4}$  oz. each of bichromate and bicarbonate of potash). Mix the two solutions. The ink is ready for immediate use.

#### Ink for writing on Steel, Tin Plate, or Sheet Zinc.

Mix 1 ounce of powdered sulphate of copper and  $\frac{1}{2}$  ounce of powdered sal-ammoniac, with 2 ounces of diluted acetic acid; adding lamp-black or vermillion.

# WAXES.

#### Black Sealing-wax.

1. Shell-lac 2 parts; yellow resin 3 parts; ivory black 2 parts. Powder fine, and mix by melting carefully.

2. Yellow resin 15 pounds; lard 1 pound; beeswax 1 pound;

lamp-black 3 pounds. Mix with heat.

#### Soft Sealing-wax.

Yellow resin 1 part; beeswax 4 parts; lard 1 part; Venice turpentine 1 part; color to fancy. Mix with a gentle heat.

#### Gold Colored Sealing-wax.

1. Bleached shell-lac 1 pound; Venice turpentine 4 ounces.

Melt, and add gold colored tale as required.

2. Bleached shell-lac 3 pounds; turpentine 1 pound; Dutch leaf, ground fine, 1 pound or less. Mix with a gentle heat. The leaf should be ground or powdered sufficiently fine without being reduced to dust.

#### Green Sealing-wax.

Shell-lac 2 parts; yellow resin 1 part; verdigris 1 part. Powder and mix by heating slowly.

#### Scented Sealing-wax.

1. Balsam of Peru 2 parts; sealing-wax composition 130 parts. Mix, with a gentle heat.

2. Sealing-wax composition 99 parts; essence of musk 3 parts.

Add the latter when the wax is cooling, and stir well.

3. Wax composition 96 parts; oil of lavender 4 parts; oil of lemon 3 parts. As before.

#### Blue Sealing-wax.

Shell-lac 2 parts; smalts 1 part; yellow resin 2 parts. Powder. and mix carefully with heat.

#### Red Sealing-wax.

1. Shell-lac 2 parts; resin 1 part; vermillion 1 part. Powder fine, and melt over a slow fire,

2. Yellow resin 14 parts; Venetian turpentine 4 parts; beeswax 1 part; red or orange lead 5 parts. Mix, with heat.

3. Oil of turpentine 1 part; lard 1 part; vermillion 2 parts;

gum-lac 12 parts. Mix, with a gentle heat.

4. (Very fine.)-Shell-lac 4 parts; Venice turpentine 1 part; vermillion 3 parts, Mix.

#### Engravers' Border Wax.

Beeswax 1 part; pitch 2 parts; tallow 1. Mix.

#### Black Bottle Wax.

Common resin 20 pounds; tallow 5 pounds; lamp-black 4 pounds. Mix, with heat.

#### Red Bottle Wax.

Common resin 15 pounds; tallow 4 pounds; red lead 5 pounds. Mix, with heat. Any color may be employed.

#### Marbled Sealing-wax.

Take wax of different colors and melt them in separate vessels. and when they begin to cool a little stir them all together, and form the mass into sticks.

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# ENGINEER'S FIELD BOOK:

CONTAINING FORMULE

FOR THE VARIOUS METHODS OF RUNNING—AND CHANGING LINES, LOCATING SIDE TRACKS AND SWITCHES, Etc.

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### TABLES

OF RADII AND THEIR LOGARITHMS, NATURAL AND LOGARITHMIC VERSED SINES, AND EXTERNAL SECANTS, &c.

TOGETHER WITH A TABLE OF

NATURAL SINES AND TANGENTS, Etc.,

TO EVERY DEGREE AND MINUTE OF THE QUADRANT.

AND LOGARITHMS OF NUMBERS FROM 1 TO 10,000.

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# CHARLES HASLETT, Cibil Engineer.

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### RECOMMENDATIONS.

Office of the O. & M. R. R. Co., Cincinnati, May, 1854.

Having examined Mr. Haslett's Field Book for Railroad Engineers, and made use of the rules he has laid down in many instances in field work, on the division of which I have had charge, I am satisfied of its superiority to any similar work yet published, in comprehensiveness and the ready application of the rules. The introduction of versed sines and external secants into the calculations very much reduces the time and labor required by the usual method of calculations for locating lines.

I recommend it to engineers, as being a book combining accuracy

and a ready application to field practice.

J. B. CUMMINGS,

Engineer Eastern Div. Ohio and Mississippi R. R.

I most fully concur in recommending Mr. Haslett's work to the attention of Engineers, believing it better than anything of the kind yet published.

N. A. Gurney, Chief Engineer, Indiana South Western R. R.

C. A. Haslett, Esq.—Dear Sir:—I have examined with considerable care the work you propose to publish for the use of engineers in the field, and I have no hesitancy in saying that it will be the most useful of any work of its character yet offered to the public. Yours very truly,

A. S. Osgood, Division Engineer, Ohio and Mississippi R. R.

I concur with Mr. Cummings in the opinion that Mr. Haslett's mode of locating lines very much reduces the time and labor required by the usual method.

S. S. Post. Chief Engineer, Ohio and Mississippi R. R.

From statements received from engineers of the Ohio and Mississippi Railroad who have used Mr. Haslett's method, I have every reason to believe it to be an improvement in simplicity and accuracy over the old methods commonly in use.

O. M. MITCHELL, Con. Engineer, Ohio and Mississippi R. R.

From the foregoing recommendation, with a hasty examination of the tables, I concur in the opinion of Messrs. Post & Mitchell.

E. Gest. Engineer.

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#### PREFACE.

Is presenting this work to the public, the Author claims for it the adaptation of a new principle in trigonometrical analysis of the formulas generally used in field calculations. Experience has shown, that versed sines and external secants as frequently enter into calculations on curves as sines and tangents; and by their use, as illustrated in the examples given in this work, it is believed that many of the rules in general use are much simplified, and many calculations concerning curves and running lines made less intricate, and results obtained with more accuracy and far less trouble, than by any methods laid down in works of this kind.

The examples given have all been suggested by actual practice, and will explain themselves. It has not been thought necessary to enter into all the details of demonstration, as this book is intended expressly for use in the field; and engineers seldom have time to enter into tedious geometrical demonstrations, when direct application of rules is required.

As a book for practical use in field work, it is confidently believed that this is more direct in the application of rules and facility of calculation than any work now in use.

In addition to the tables generally found in books of this kind, the author has prepared, with great labor, a Table of Natural and Logarithmic Versed Sines and External Secants, calculated to degrees, for every minute; also, a Table of Radii and their Logarithms, from 1° to 60°. Rules and examples are also given for running curves without the use of an instrument; also for locating turnouts, side tracks, switches, &c.

Having been for several years engaged in surveys and locations of railroads, and practically convinced of the great saving of time

and trouble gained by using the rules and principles given in this book, the Author submits it, without further preface, to the profession, fully confident that its use will be practical proof of its merits,

The tables and examples have been prepared with great care, and their accuracy may be relied upon.

While the Author claims a fair share of originality in the following work, he would acknowledge many valuable suggestions derived from Mifflin's Piagrams, as also from Henck on Compound and Reversed Curves, authors to whom he would refer those wishing to follow the subject at greater length. On the manner of working an instrument Mifflin is very clear and concise. This work is designed especially for practical field engineers, already familiar with minor details.

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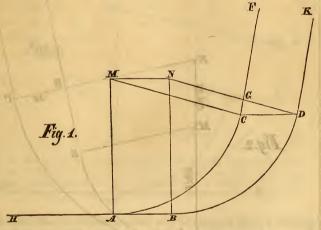
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# ENGINEER'S FIELD BOOK.

FORMULÆ FOR RUNNING LINES, LOCATING SIDE-TRACKS,

#### PROPOSITION I. Fig. 1.\*

To change the origin of a curve so that it shall terminate in a tangent parallel to a given tangent.



Suppose the curve A C to have been described containing 60° of curvature, and that the distance G D equal 50 feet.

We have by logarithms:

Sine 60° (total amour	at of c	urva	ture),	9.937531	
Is to R.	0001		11.	10.000000	
So is G D, 50 feet, .				1.698970	
To $AB = 57.73$ feet,		. 4	W.1004	1761439	
10000001	GD		50	51 01 EL	

Or by nat. sines = 
$$\frac{G D}{\sin 60^{\circ}} = \frac{50}{.86603} = 57.73$$
.

Produce the tangent from A to B = 57.73 feet; then make the

<sup>\*</sup> The diagrams in this work are not drawn to any exact scale, but are designed to represent merely the abstract geometrical relation of lines.

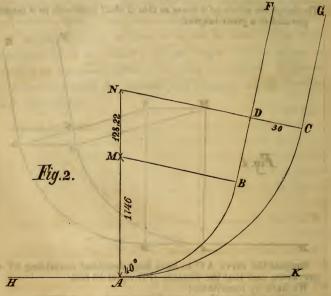
curve BD equal AC; that is AMC = BND; then the tangents will be parallel.

This rule will apply to the origin of a compound curve, using the

total amount of curvature run.

#### PROPOSITION IL Fig. 2.

Having a curve AB terminating in a tangent DF, it is required to find the radius of a curve that will give a tangent CG parallel to DF at any given distance therefrom, as at DC say 30 feet.



Let A M be the given radius = 1146 feet, the arc A B = 800 feet, containing  $40^{\circ}$ , and D C perpendicular distance 30 feet. By logarithms:

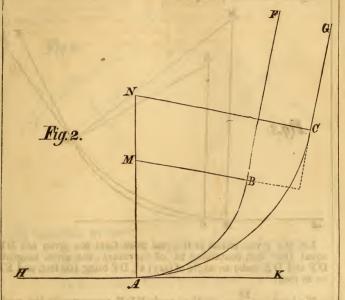
Zui i dillis .	
As versed sine 40°	9.369133
Is to R	10.000000
So is $DC = 30$ feet	1.477121
To M N=difference of radii given and	
required=128.22	2:107988

Then we have 1146 + 128 = 1272 =radius of a 4° 30′ curve. Then say: 1146 : 1272 :: 800 : 888 =arc A C.

This case is equally applicable to changing the last radius used in a compound curve terminating in a parallel tangent.

#### PROPOSITION III. Fig. 2.

In case the preceding method should consume too much of the tangent C G, it is required to change the origin of the curve, also the length of radius, so that the required tangent may commence opposite to B, running parallel to B H.



In this case the radiating point will be changed from M towards A and B, the radius shortened, and the point A moved towards K.

Let the required distance between tangents, the given radius, and curvature be as in Proposition II., then we have by logarithms:

As the external secant of 40°	45.00		9.484879
Is to radius			10.000000
So is 30 feet $=$	-14	4	1.477121
To difference of radii = 98.23	000	-1	1.992242

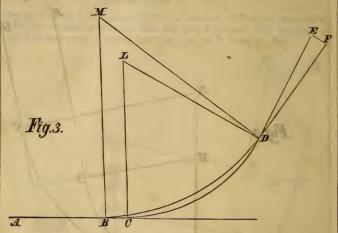
By natural external secants = 
$$\frac{30}{305407}$$
 = 98.

And 1146 — 98 = 1048 = radius of a 5° 28' curve. Then, as 1146: 1048::800: 732 = length of 5° 28' curve. 98 (natural tangent of 40° = 83910) = 82 feet.

Produce tangent 82 feet from A to K, and curve from thence 732 feet of a 5° 28' curve.

#### PROPOSITION IV. Fig. 3.

Having located a curve with a given radius, terminating in a given point, it is required to change the origin of the curve, also the radius, so as to pass through the same terminating point, with a different direction of tangent.



Let the given radius MB equal 2292 feet; the given are BD equal 1000 feet, containing 25° of curvature; the given tangents DF and DE make an angle of (say) 4°, DF being 400 feet, and EF = 28 feet.

We have  $\frac{28}{4 \times 175} = 4^{\circ}$  = angle EDF, consequently the angle

 $CLD = 25^{\circ} + 4^{\circ} = 29^{\circ}.$ 

By logarithms:

As versed sine 29° . . . . 9.098229
Is to versed sine 25° . . . 8.971703
So is radius given B M = 2292 . 3.360217
To radius required C L = 1714 feet . 3.233991

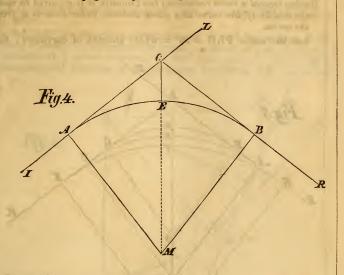
By tables 1714 feet = radius of 3° 20½' curve.

#### PROPOSITION V. Fig. 4.

Having produced the two tangents to their intersection, it is required to connect them by a curve passing a given distance from the vertical point.

Given the angle LCB = 31° 44′, and CE = 50 feet, to find the

radius MA. By geometry, the angle AME =  $\frac{1}{2}$  LCB = 15° 52'.



By logarithms we have:

,	As exter	nal se	ecant	15° 5	$2' = \frac{1}{2}$	LC	В	8.597789
]	s to 50			1	4. 2			1.698970
5	So is R.		• •					10.000000
-	Го М А=	=126	2=R.	of a	4° 32½	' cui	rve	3.101181

By natural external secants  $\frac{50}{\text{ex. sec. }15^{\circ} 52'} = \frac{50}{039603} = 1262 \text{ ft.}$ 

# CASE 2D.

To find the tangent AC, or CB; or point of curve. By logarithms:

As R				10.000000	
Is to $AM = 1262$ .	- / - 10			3.101181	
So is tangent 15° 52'				9.453668	
To A $C = 388.8$ .	- D.M.	6.0	10.0	2.554849	

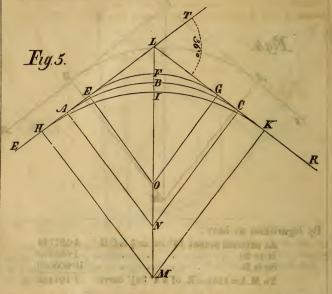
By natural tangents:

 $1262 \times (\text{natural tangent } 15^{\circ} 52' = \cdot 26546) = 388 \text{ feet}$ = C A = C B.

## PROPOSITION VI. Fig. 5.

Having located a curve connecting two tangents, it is required to move the middle of the curve any given distance, either towards or from the vertex.

Let the angle TLG = 36° = whole amount of curvature; the



arc A B C = 1200 feet; the radius A N = C N = 1910 feet, and I B = B F = 10 feet.

It is required to find the radii HM and EO.

We have by logarithms:

By natural external secants:  $\frac{10}{.054595} = 183$  ft

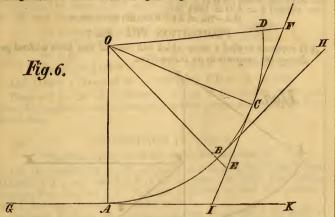
1910 + 183 = 2093 = MH = radius of a -2° 44' curve; and 1910 - 183 = 1727 = OE = radius of a 3° 19' curve.

By natural tangents:  $183 \times (\text{natural tangent } 18^{\circ} = :32429) = 59.4 = \text{HA} = \text{AE}$ 

## PROPOSITION VIL. Fig. 6.

It is required to locate a tangent from an inaccessible point on a curve.

Let ABC be the given curve with a R. of 1637 feet curving 3° 30' per 100 feet; C the inaccessible point. Assume a point B, if convenient, at a given distance, say 300 feet, from C. Throw off a tangent, and measure, at right angles therefrom, BE = external



secant of arc BC; then to find by logarithms the distance BE, we have:

As radius	10.000000
Is to $OC = 1637$	3.214122
So is external secant 10° 30′ = angle COB	8.231221
To B E = 27.88	1.445343

By natural external secants:

 $1637 \times (\text{nat. ex. sec. } 10^{\circ} 30' = .017030) = 27.88.$ 

Measure the line BE=27.88 feet at right angles to BH. Set the instrument over E, and turn off the angle  $BEC=79^{\circ}.30'=$  complement of  $10^{\circ}.30'$ . ECF will be the direction of the tangent required.

#### CASE 2D.

Suppose there be no convenient accessible point between A and C, produce the curve to D, measure the external secant DF as before, place the instrument at F, and turn off the angle DFC. This will give the direction of the tangent FC as before.

#### CASE 3D.

Should the lines AI and IC be more practicable for operating

than the curve A B C, calculate and produce the tangent from A to I, the vertex of the curve A B C, and turn off the angle K I F = A O C, and make I C = A I, as calculated.

CASE 4TH.

Again, should the last method be found impracticable, and the chord AD clear from obstructions, measure the chord AD, and turn off tangent from D.

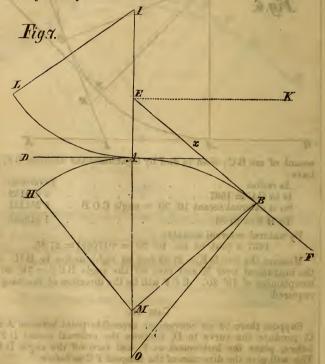
Suppose angle  $KAD = 25^{\circ}$ , then we have  $1637 \times (\text{nat. sine } 25^{\circ})$ 

= .42262) 2 = A D = 1384 feet.

Note.-The arc A B C D contains 50° curvature.

### PROPOSITION VIII. Fig. 7.

It is required to find a curve which will connect two lines without producing the tangents to an intersection.



The principle involved in this diagram affords an easy mode of solving a very interesting geographical problem. Suppose AE is a mountain near the sea or a very extensive level. Measure with an instrument for taking vertical angles the depression or "dip" of the horizon KEB=BOH; then external secant KEB radius of earth = AE height of mountain.

Let the line be either a curve L A, H A, or a tangent D A, as the case may be. Suppose it impracticable, by reason of buildings or

other obstructions, to produce the tangent to a vertex x.

At A lay off with the instrument a right angle to tangent, and produce it till it meets FB produced in E. Measure this distance, and the angle AEB; then its complement AOB will be the amount of curvature required to curve on to the tangent BF.

Suppose the angle  $A \to B = 65^{\circ}$ , then  $A \cap B = 25^{\circ}$ . Let  $A \to B$  be

= 120 feet, then we have by logarithms:

And  $1160.8 \times (tangent 25^{\circ} = .46631) = EB = 541.28$  feet.

Then will be 25° of curvature  $\div$  4°  $56\frac{1}{8}'$  = the rate of curvature, give the length of curve between the two given points A and B =  $506\cdot2$  feet.

## PROPOSITION IX. Fig. 8.

To draw a tangent to two curves already located.

Let the curve CRAGH, of 2000 feet radius, be located from tangent CK; and let ESBD be a curve of 2605 feet radius, located from tangent EF. We are required to find the points A and B having a tangent common to both.

Suppose R to be the point in the first curve, and S the point in the second. There being obstructions in the way, we will run the zigzag line RLPS, making RL tangent to R, and PS tangent

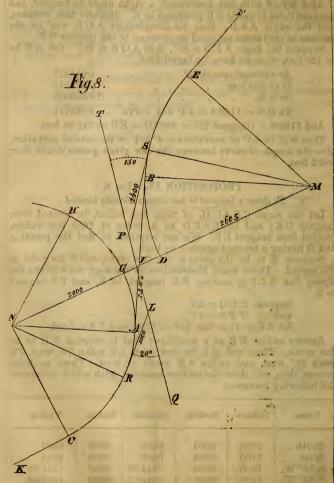
to S.

Suppose R L Q =  $20^{\circ}$  and T P S =  $15^{\circ}$ ; let R L = 1100 feet, L P = 1300, and P S = 1400.

Assume radius NR as a meridian; that is, suppose NR to be due north. Then will RL be due west, LP south 70° west, PS south 85° west, and radius SM north 5° west. These artificial courses, then, will show the *relative* bearings, with which we obtain the following traverse:

Course.	Distance. Northing.		Southing.	Easting.	Westing.	
North West	2000 1100	2000	0000 0000	0000	0000 1100	
S. 70° W. S. 85° W.	1300 1400	0000	444·63 122·02	0000	1221·60 1394·66	
N. 5° W.	2605	2595 07	0000.	0000	227.05	
		4595.07	566.65	0000	3943:31	

Difference northing and southing (4595.07 — 566.65) = 4028.42; then  $\frac{3943.31}{4028.42}$  = .97882 = natural tangent R N G = 44° 23′ = course



of N M = N. 44° 23' west, and angle S M D = 39.23, or 44°  $23' - 5^{\circ}$ .

To calculate M N make the difference of latitude 4028.42 = cosine 44° 23', and the required distance N M = radius. Then we have

by natural cosines  $\frac{4028.42}{\text{cosine }44^{\circ}23'} = \frac{4028.42}{71468} = 5636.7 = M N.$ 

Or by logarithms:

The triangles ANI and BMI being similar, we have by logarithms (Davies' Legendre, book II., prop. X)—that is, by "composition and division:"

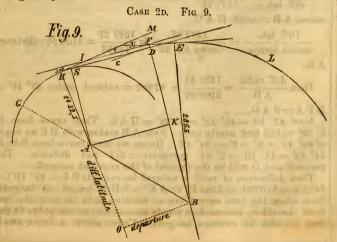
Having now determined the angle RNI =  $44^{\circ}$  23', and the angle ANI =  $35^{\circ}$  13', the angle RNA becomes = to their differ-

ence =  $9^{\circ}$  10'.

Therefore continue the curve from R towards A, 9° 10′ of curvature, and we have the tangent point A required. Again, we have S M I = 39° 23′, and the angle B M I = 35° 13′, consequently curve from S to B 4° 10′ of curvature, and we have the tangent point B required.

Now to find the length of tangent AB, multiply the sum of the radii 4605 by the natural tangent of 35° 13', and we have the

length required.



Suppose the two curves to be connected by a common tangent, instead of running in opposite directions as in Case 1st, curve the same way, as GHS and CDEL. It is required to find the

position of the tangent S D.

Assume the points H and E; from H lay off tangent H I; from E lay off tangent E F; join F and I by a straight line, if convenient, or by a traverse, if there be obstructions. Let A H be an artificial meridian, and, as in Case 1st, calculate the distance A B, also its course = angle H A G; this will give also the angle E B A.

Suppose radius A H = 1432.5, tangent H I = 500 feet, angle M I F = 6°, I F = 1000 feet, N F T = 8°, E F = 600 feet, and radius E B = 2865 feet. We will then have the following traverse, by

which to find the course and distance of AB:

Course.	Distance.	Northing.	Southing.	Easting.	Westing.
North East S. 84° E S. 76° E . S. 14° W.	1432.5. 500 1000 600 2865	1432:50	104·50 145·20 2780·07	500 984·60 582·20	692·72
non glitonagos Lauron strenge	Total	1432:50	3029:77	2066 80	692.72

Difference of latitude = 1597.27; departure = 1374.08.

 $\frac{\text{Departure}}{\text{diff. lat.}} = \frac{1374.08}{1597.27} = .86026 = \text{natural tangent 40}^{\circ} 42' =$ 

course A B = angle H A G.

$$\frac{\text{Diff. lat.}}{\text{cosine course}} = \frac{1597.27}{\text{cosine } 40^{\circ} 42'} = \frac{1597.27}{.75813} = 2106.86 = \text{distance}$$

AB.

Then 
$$\frac{\text{diff. radii}}{\text{A B}} = \frac{1432 \cdot 50}{2106 \cdot 86} = \cdot 67992 = \text{natural cosine } 47^{\circ} \cdot 10' =$$

DBA = SAG.

Now  $47^{\circ}$   $10'-40^{\circ}$   $42'=6^{\circ}$  28'=H AS. Then curve from H  $6^{\circ}$  28'=162 feet nearly to S. Now AB makes with BE an angle of  $40^{\circ}$   $42'+8^{\circ}+6^{\circ}=54^{\circ}$  42' Hence we must curve from E to D  $54^{\circ}$   $42'-47^{\circ}$   $10'=7^{\circ}$  32' curvature = 377 feet distance. The points S and D will be the termini of the required tangent.

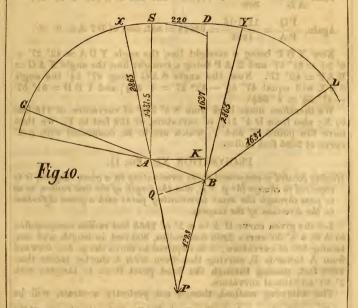
Then difference of radii  $\times$  natural tangent (DBE=47° 10')= 1432.5  $\times$  1.07864 = 1545.15 = AK = SD = length of tangent. Now when the two curves are so situated as to be seen the one from the other, assume two points as near as you can judge to the true termini of common tangent. Cause about a dozen small

straight stakes or pins to be set up endway about twenty feet apart from one of the assumed points or curves. Then set the instrument at the other, and see how tangent from instrument strikes the row of stakes. Note the difference, and move the instrument until tangent therefrom strikes as tangent to the row of stakes. Make a point where it does. Set the instrument over said point, and in like manner see how tangent from instrument strikes the other curve. Thus we dispense with all the previous calculation.

## PROPOSITION X. Fig. 10.

Having located two curves connected by a tangent, as in Case 2d, Prop. IX., it is required to throw out the tangent, and introduce instead a curve with given radius.

Let the radius AS = 1432.5 feet, BD = 1637 feet, and their common tangent SD = 220 feet. It is required to find on the two



curves two tangent points, X and Y, from which, if the required radius (say 2865 feet) be drawn, it will pass through the points A and B, intersecting in the centre P, equi-distant from X and Y.

Now in the triangle BAK we have given, difference of radii

B K = 1637 - 1432.5 = 204.5; also, A K = S D = 220, to find the angle K A B, its complement K B A = S A G,\* and the distance A B.

Then 
$$\frac{B \text{ K}}{A \text{ K}} = \frac{204.5}{220} = .92954 = \text{natural tangent of } 42^{\circ} 544' = \text{K A B}.$$

Therefore its complement KBA =  $SAG = 47^{\circ} 5\frac{1}{2}$ . Now BK × secant KBA =  $204.5 \times 1.468801 = 300.37 = AB$ ; call it 300 feet. Again, in the triangle BAP we have AB = 300, AP = 2865 - 1432.5 = 1432.5, BP = 2865 - 1637 = 1228. To find the angles ABP, BPA, and BAP, make AP = 1432.5 feet the base, and let Q be the foot of the perpendicular from B. Then by trigonometry we have:

A P: BP + BA:: BP - BA: PQ - QA, or  $1432 \cdot 5: 1228 + 300:: 1228 - 300: 989 \cdot 8 = PQ - QA$ . Then  $\frac{1432 \cdot 5 + 989 \cdot 8}{2} = PQ = 1211 \cdot 15$ , and  $\frac{1432 \cdot 5 - 989 \cdot 8}{2} = QA = 221 \cdot 35$ .

Then 
$$\frac{A Q}{A B} = \frac{221.35}{300} = .73783 = \text{nat. cos. of B A P} = 42^{\circ} 27'$$
.

Again, 
$$\frac{PQ}{PA} = \frac{1211 \cdot 15}{1228} = 98628 = \text{nat. cos. of BPA} = 9^{\circ} 30'$$
.

Now YBP being a straight line, the angle YBA =  $42^{\circ} \, 27' + 9^{\circ} \, 30' = 51^{\circ} \, 57'$  and XAP being a straight line, the angle XAG = BAP =  $42^{\circ} \, 27'$ . Now the angle SAG being  $47^{\circ} \, 5\frac{1}{2}'$  the angle SAX will equal  $47^{\circ} \, 5\frac{1}{2}' - 42^{\circ} \, 27' = 4^{\circ} \, 38\frac{1}{2}'$ , and YBD =  $51^{\circ} \, 57' - 47^{\circ} \, 5\frac{1}{2}' = 4^{\circ} \, 51\frac{1}{2}'$ .

We therefore move back from S  $4^{\circ}$   $38\frac{1}{2}'$  of curvature, or 116 feet to X; also from D  $4^{\circ}$   $51\frac{1}{2}'$  of curvature, or 139 feet to Y; we then have the points X and Y, which are to be connected with a  $2^{\circ}$ 

curve of 2865 feet radius.

## PROPOSITION XI. Fig. 11.

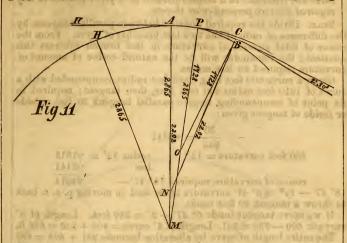
Having located a compound curve terminating in a given tangent, it is required to change the p. c. c., also the length of the last radius, so as to pass through the same terminating point with a given difference in the direction of the tangent.

Let the given curve H A be a 2° of 2865 feet radius compounded to A B, a 2° 30′ curve 2292 feet radius, 800 feet in length, and containing 20° of curvature; it is required to move the p. c. c. forward from A towards B, curving therefrom with a shorter radius than 2292 feet, passing through the fixed point B on to tangent with 2° 30′ additional curvature.

The following method, though not perfectly accurate, will be

<sup>\*</sup>Because the three angles in the triangle KAB = 180°. Also the sum of the angles on one side the line BG = 180°. Subtracting from 180° the angle A and the right angle at K, we have left the angle at B. Subtracting from 180° the angle A (as before) and the right angle SAK, we have the angle SAG; hence the angle KBA = the angle SAG.

found sufficiently so for most practical purposes. Had the 2° curve HA been continued 800 feet farther, to a point C, the variation BC would be equal 28 feet.\* Now by compounding to a 2° 30′ curve I turn off with the instrument for the chord AB 2°



more than I would for the chord AC; for  $\frac{20^{\circ}-16^{\circ}}{2}=2^{\circ}$ ; but if

the instrument set at the required point P, with a backsight on A,

and a foresight on B, I turn off  $\frac{20^{\circ} + 2^{\circ} 30'}{2} = 11^{\circ} 15'$ , that is 3° 15'

instrumental deflection over and above that required for a continuous 2° curve to C; the curve PB will therefore be shorter than AB in the ratio of 3° 15′ to 2°; hence the proportion:

$$3\frac{1}{4}:2::800:492 = length of curve P B.$$

A P then will equal 800-492=308 feet of 2° curve; but 308 feet of a 2° curve gives 6° 10′ of curvature; hence PB contains  $22^{\circ}30'-6^{\circ}10'=16^{\circ}20'$  of curvature in 492 feet distance; then

we have  $\frac{16\cdot333...}{4\cdot92} = 3\cdot3198^{\circ} = 3^{\circ}19'$ , or 1728 feet radius for the

curve PB. It will be sufficiently accurate, however, to continue the 2° curve 310 feet to P, and then run 490 feet of a 3° 20' curve.

Were HA a tangent by making AP the same length and rate of curvature as above, the curve PB would be the same also.

 $*2^{\circ} \times 1.75 \times 8 = 28.$ 

## PROPOSITION XII.

Having located a compound curve terminating in a tangent, it is required to change the point of compound curvature so that the curve will terminate in a tangent parallel to a given tangent at any required distance perpendicular thereto.

RULE. Divide the required distance between parallel tangents by the difference of radii of the two last branches of curve. From the cosine of total amount of curvature in last branch subtract this quotient; the remainder will be the natural cosine of amount of curvature required for last radius.

Given a curve 600 feet long, 2865 feet radius, compounded with a curve of 1910 feet radius 400 feet long, then tangent; required to fix point of compounding, to give parallel tangent 30 feet outside

or inside of tangent given:

$$\frac{30}{955} = .03141$$

400 feet curvature = 12° cosine 12° = .97815

less <u>'03141</u>

cosine of curvature required 18° 47' 94674 18° <math>47' 12° = 6° <math>47' curvature to be used in moving p. c. c. back to throw a tangent 30 feet inside.

If we move tangent inside  $6^{\circ}$   $47' \div 2^{\circ} = 339$  feet. Length of  $2^{\circ}$  curve = 600 - 339 = 261. Length of  $3^{\circ}$  curve = 400 + 226 = 626 ft.

The entire length of curve by alteration becomes 261 + 626 = 887 instead of 1000 feet as before, admitting of more tangent at the end.

This last rule is applicable when the movement of the p. c. c. is retrograde or from the terminating tangent, thereby increasing the amount of curvature in last curve, and diminishing that of the pre-

ceding curve.

When it is required to move the point c. c. forward, diminishing the amount of curvature in last curve, add the quotient of the required distance divided by difference of radii, to the cosine of given amount of curvature; and the sum will be the cosine of the amount of curvature required in the last curve. Find the distance as before, and move the point forward the difference of curvature, always reckoning said difference according to the rate of curvature back of p. c. c.

# PROPOSITION XIII. Fig. 12.

Having located a curve between two tangent points, it is proposed to lengthen the radii at the two termini, and shorten the radius in the middle.

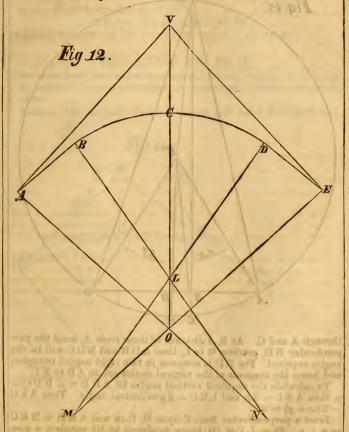
Let the proposed curve be one of 1146 feet radius = 5°, 800 feet in length, and containing 40° of curvature. It is proposed to introduce at each end 100 feet of a 2° 30' curve = 2292 feet radius. Required the other radius.

From the t. p. to the centre is 400 feet, or 20° of curvature.

Introducing 100 feet of a 2° 30′ 2292 feet R, there will be 2° 30′ of 2292 feet radius + 17° 30′ of a shorter radius.

By logarithms:

As sine 17° 30'	9.478142
Is to 2° 30′	8.639680
So is diff. radii = 1146 feet = OM.	3.059185
To difference between given radius	da Am 6 DM
and required = $167 = 0 L$ .	2.220723

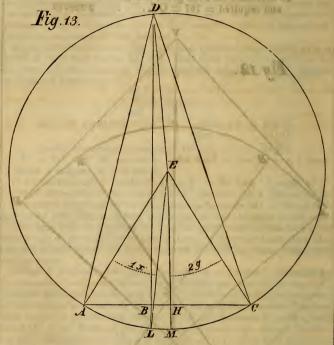


Given radius being 1146, radius required will be  $1146-167=979=\mathrm{L\,C}=a~5^\circ~51'$  curve.

# PROPOSITION XIV. LEMMA. Fig. 13.

To divide a given angle into two parts, so that the tangents of the angles will be in a given ratio.

Let the required ratio be as three to five, and the given angle  $ADC = 30^{\circ}$ ; let the straight line ABC be = 8. Make AC a chord of 60°, or twice 30°. Describe the circle ACD passing



through A and C. At B, a distance of three from A, erect the perpendicular BD, produce it to L, then ADB and BDC will be the angles required. For BD is common to two right angled triangles, and hence the tangents of the vertical angles are as AB to BC.

To calculate the required vertical angles let ADB = x, BDC = y, then AEL = 2x, and LEC = 2y = central angle. Then AEC

 $= 2(x + y) = 60^{\circ}$ .

Erect a perpendicular from E upon H, then will A E H = H E C = x + y. Then L E M (H being produced to M) equals x + y - 2x = y - x; then E L = E C = R., and L M = B H. Then

H C : (L M = B H) :: sine (x + y) : sine (y - x).

But HC is half of AC, and BH is half BC—AB, therefore  $(BC+AB):(BC-AB)::\sin(x+y):\sin(y-x)$ , that is, as the sum of the numbers expressing the ratio is to difference, so is sine of the given angle to sine of the difference required.

By logarithms:

As $3 + 5 = 8$ .	151)	2005	tad-	d la	0.903090
Is to $5 - 3 = 2$					0.301030
So is sine 30°.	25 1	D. P. D. St.	M. PS	100	9.698970
To sine $y - x =$	7° 10	38"			9:096910

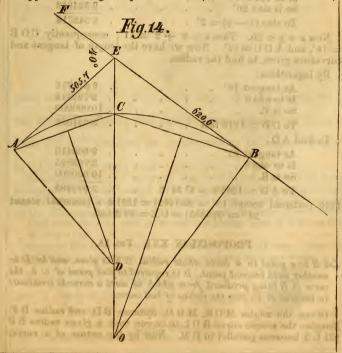
 $y + x = 30^{\circ}, y - x = 7^{\circ} 10' 38'',$ 

therefore  $2y = 37^{\circ} 10' 38''$ ,  $y = 18^{\circ} 35' 19''$ ,  $x = 11^{\circ} 24' 41''$ .

# PROPOSITION XV. Fig. 14.

From two fixed points, having produced tangents uniting in a vertex at unequal distances from them, it is required to locate a compound curve.

Suppose the tangents produced to E, and let A E = 505.7 feet,



EB = 6206 feet, the angle FEA = 40°. Required the radii of a c. c. to join A and B, and also the point of compound curvature.

We observe the external secant E C is common to both curves. Now by construction of the tables we have: external secant a =tangent  $a \times$ tangent  $\frac{1}{2}a$ , radius being unity. The angles E B C and E A C are measured by half their arcs C B and C A.

Call these angles x and y respectively. Then  $x + y = \frac{40^{\circ}}{2}$ 

20°; then  $620.6 \times \text{tangent } x = 505.7 \times \text{tangent } y$ , or 620.6 : 505.7 = tangent y : tangent x. Then by previous proposition

 $620^{\circ}6 + 505^{\circ}7 : 620^{\circ}6 - 505^{\circ}7 :: sine (x + y = 20^{\circ}) : sine (x - y)$  or,  $1126^{\circ}3 : 114^{\circ}9 :: sine 20^{\circ} : y - x$ .

Neither of the radii being given, we will assume the condition, that the p. c. C shall be in line with the vertex E and the centres O and D. We have by logarithms:

To sine  $(x-y)=2^{\circ}$ . . . . . 8.542718 Now x+y=20. Then  $x=9^{\circ}+2^{\circ}=11^{\circ}$ ; consequently COB = 18°, and ADC=22°. Now we have the length of tangent and curvature given, to find the radius.

By logarithms:

To find AD:

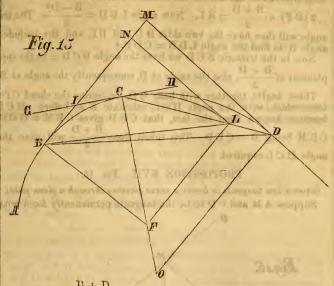
1910 (external secant  $18^{\circ} = .051462$ ) =  $1251.6 \times (external secant <math>22^{\circ} = .078535) = C E = 98.2$  feet.

# PROPOSITION XVI. Fig. 15.

Let B be a point in a curve whose radius BF is given, and let D be another fixed tangent point. It is required to find point of c. c., the curve AB being produced, from which to start a curve to terminate in tangent at D, also the radius of last curve.

Given the angles MDB, MBD, distance BD, and radius BF. Imagine the simple curve BCL to be run with a given radius BF till LN becomes parallel to DM. Now by the nature of a curve,

upon whatever point on the curve the transit be placed, the difference between backsight on B and foresight on I, is always the



same, namely,  $\frac{B+D}{2}$ . Now at the true point of c. curvature C,

the difference between backsight on B and foresight on D is also equal to  $\frac{B+D}{a}$ , therefore the transit reading the same on D as on

L, CLD must be in the same straight line.

Hence whenever the nature of the ground will admit of it, erect a flagstaff at D, curve round from B towards L until taking a back-sight the foresightnecessary to fall upon L should strike the flagstaff at D. The transit will then be at the point of c. curvature sought.

Then measure CD, and make this proportion; sine HCL\*: ½ CD

:: R: x = 0 D.

Suppose  $HCL = 8^{\circ}$ , and the distance CD = 600 feet. Then by substituting in the above proportion, we have by logarithms:

<sup>\*</sup> Because HCL =  $\frac{1}{4}$  COD.

When the ground will not admit of this method, ascertain by measurement or calculation the distance from B to D.

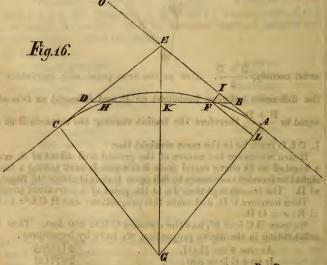
 $2 (B F) \times \frac{B+D}{2} = B L$ . Now angle  $L B D = \frac{B-D^*}{2}$ . The triangle will then have the two sides B D and B L, and the included angle B, to find the angle L D B = C D B.

Now in the triangle B C D we have the angle B C D = to the supplement of  $\frac{B+D}{2}$ , also the angle at D, consequently the angle at B.

These angles, together with base B D, determine the chord CD; from which, with the angle H CL, calculate R as before. H CL becomes known from the fact, that CBD gives CBM = GCB, CBM being B — CBD. This taken from  $\frac{B+D}{2}$  will give the angle H CL required.

# PROPOSITION XVII. Fig. 16.

Between two tangents to locate a curve possing through a given point. Suppose AB and CD to be the tangents permanently fixed with



\* Because N B L (isosceles) =  $\frac{1}{2}$  exterior angles at N and M =  $\frac{B+D}{2}$ , B being = N B D, and B  $-\frac{B+D}{2}$  =  $\frac{B-D}{2}$  = L B D.

 $\uparrow LDB = \left(CLB = \frac{B+D}{4}\right) - LBD$  which will make all the angles known.

reference to some agreement between individuals; and let F be the given point at which it is necessary to keep a given distance from some building or other object. Suppose AB and CD produced to meet in E. The angle OED, and consequently its half EBD, are known. The distance IE is also known.

Let the angle O E D =  $60^{\circ}$ , let I F = 17.5 feet. It is required to

find the point B, so that the angle FBI shall = 30°.

By natural sines:

$$-\frac{17.5}{\text{sine } 30^{\circ}} = 35 = \text{FB} = \text{H D}.$$

Now  $\sqrt{(35 + 17.5)} \times (35 - 17.5)^* = \sqrt{52.5 \times 17.5} = 30.3 = IB$ . Suppose I E measures 462 feet. Then B E will equal 462 + 30.3

=492.3.

By similar triangles FB: BE:: BI: BK, or

 $35:4923::30\cdot 3:426\cdot 2=BK=DK.$ 

Then B D = 852.4 and B H = 852.4 - 35 = 817.4.

Now we have by geometry  $\sqrt{BH \times BF} = BA$ , or  $\sqrt{817.3 \times 35} = 169.1 = BA$ .

Hence AB + BE = AE, or 169.1 + 492.3 = 661.4.

To find radius:

$$\frac{\text{A E}}{\text{tangent } 30^{\circ}} = \frac{661.4}{0.57755} = 1145.5 = \text{R}.$$

Now suppose it is inexpedient to produce the tangents to a vertex, the angle  $O \to D$  being known, find the point B as before, and turn off  $E \to D = \frac{1}{2} O \to D$ , measure B D, and calculate by trigonometry

the side ED = BE, and also BA as before.

Again, suppose the angle at E is not known, neither is it practicable to measure a direct line between the two tangents, calculate by traverse the true course and distance between any two convenient points on the tangents by Proposition VIII., from which calculate the position of E.

Without ascertaining the distance to E, the radius A G can be

calculated thus:

$$\frac{A F^2}{2 I F}$$
 = A G, or let A F = 200, then  $\frac{200^2}{17.5 \times 2}$  =  $\frac{4000}{3.5}$  = 1146 = AG.

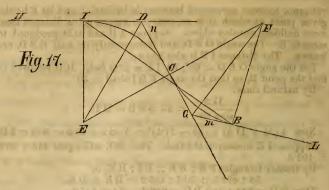
Therefore commence at A, and run 800 feet of a 5° curve to C.

# PROPOSITION XVIII. Fig. 17.

Given the length of a common tangent D G = a, and the angles of intersection n and m, to determine the common radius C E = C F = radius of a reversed curve to unite the tangents HD and BL.

Now D C = R × tangent  $\frac{1}{2}n$ , and C G = R × tangent  $\frac{1}{2}m$ ; we have therefore D G tangent = 800 ft.,  $n = 16^{\circ}$  and  $m = 12^{\circ}$ .

<sup>\*</sup>The sum of two quantities multiplied by their difference is equal to the difference of their squares.



$$R = \frac{a}{\tan \frac{1}{2}n + \tan \frac{1}{2}m} = \frac{800}{\tan 8^{\circ} + \tan 6^{\circ}} = \frac{800}{\cdot 14054 + \cdot 10510} = 3256 \cdot 7$$

$$3256 \cdot 7 \times \cdot 14054 = D \cdot C = D \cdot A = 457 \cdot 69$$

$$3256 \cdot 7 \times \cdot 10510 = C \cdot G = G \cdot B = 342 \cdot 27$$

$$799 \cdot 96$$

Suppose it to be required to introduce 200 feet of tangent between the curves, that portion of the tangent DG taken by the two curves will be 600 feet. Then we have:

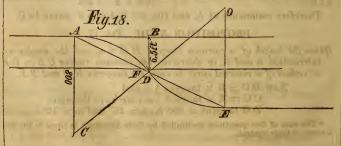
800: 600:: 3256·7 : 2442·5 radius:

 $800:600::457\cdot69:343\cdot27$  $800:600::342\cdot27:256\cdot70$  = new tangent.

599.97 = " "

# ON REVERSED CURVES, TURNOUTS, ETC. Fig. 18.

A F = 98 feet, A D = 102 feet, and D E = 102 feet. Let G = gauge of track, and R = radius of turnout, x = distance



on chord from A, the origin of curve, to F, the point of frog; then will

$$x = \sqrt{2 R \cdot G}$$

Now suppose R = 800 feet, and G = 6 feet, then will

$$x = \sqrt{2 \times 800 \times 6} = \sqrt{9600} = 98$$
 feet nearly.

Or let x = distance on main track to a point opposite of the frog. Then will

$$x = \sqrt[4]{G(2 R - G)}$$
 or  $\sqrt{6(2 \times 800) - 6} = \sqrt{6 \times 1594} = \sqrt{9564} = 97.79$  feet.

Hence the following rule is sufficiently correct for all practical purposes:

Multiply twice the radius by the gauge of track, extract the square root of the product, and we have the distance from origin of curve to point of frog.

Formula for angle of frog:  $G \div R =$ versed sine of curvature to

frog = angle of frog. Ex. 
$$\frac{6}{800} = .0075 = 7^{\circ} 2'$$
.

Make the movable end of the switch rail such a distance from the origin of the curve, that the departure of a curve of that radius for that distance will be equal to the opening of that rail at the movable end, say 51 inches.

With an 800 feet radius, the distance from origin of curve to

opening of switch rail will be = 27 feet, for 
$$\frac{27 \times 27}{1600} = \frac{11}{24} = 5\frac{1}{2}$$

inches nearly.

It will appear therefore that the opening of a 20 feet rail, with an 800 feet radius curve commencing at the other end, will be only

3 inches, for 
$$\frac{20 \times 20}{1600}$$
 = 3 inches.

If we consider the movable rail as a movable tangent, and the origin of the curve as the opening of the rail, the angle of frog and length of curve will be obtained by Proposition XII.

## EXAMPLE.

A 20 feet rail, with  $5\frac{1}{2}$  inches opening, makes an angle with the main track = 1° 18′, then on 6 feet gauge the distance from opening to other side = 5 feet  $6\frac{1}{2}$  inches = 5.54 feet. Then by Proposition XII. we have:

cosine 1° 8' = '99974  

$$\frac{554}{800} = \frac{00692}{'99282} = \text{cosine 6° 52'}$$
  
= angle of frog.

And  $6^{\circ} 52' - 1^{\circ} 18' = 5^{\circ} 34' =$  amount of curvature between open-

ing of rail and point of frog.

By the first method, when the distance between tracks = 13 feet we have  $\sqrt[4]{13 \times 800} = 102$  feet nearly for distance from origin of curve to point of reversion.

But if the point of reversion be made at the point of frog, the distance between nearest rails of tracks being 7 feet, we have 6:7::800:933.3 = radius of curve with which to leave frog, and

6:7::98:114.3 - distance from frog to end of turnout.

Or making the movable rail tangent, and its opening  $5\frac{1}{2}$  inches, angle of opening being 1° 18', the point of reversion being made at frog, to find the angle of frog, we have:

cosine 1° 18′ = '99974

$$\frac{6.54}{933.3} = 0.0780$$

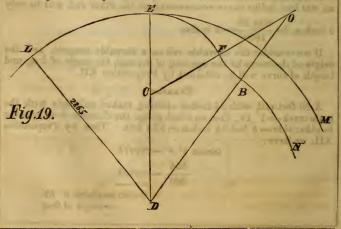
·99274 = cosine 6° 55' nearly the same as before.

## TURNOUTS ON CURVES. Fig. 19.

Suppose the turnout is on a curve running in the same direction, say a 2°, with a radius of 2865 feet. Now an 800 feet radius gives a 7° 10′ curve, and 7° 10′ - 2° = 5° 10′ = relative departure from main track. But the radius of a 5° 10′ = 1109 feet; then

 $\sqrt{2} \times 1109 \times 6 = x = 115.3$  — distance from origin of curve to point of frog.

Therefore to make a turnout from a 2° curve and running the same way would require 115 feet.



If it were required to keep the distance the same as on a straight line, it would be necessary to make the 7° 10' curve a 9° 10' curve of 625 feet radius.

If the 2° curve run in the opposite direction of the turnout, and the radius was 800 feet, then the convergence will be  $7^{\circ} 10' + 2^{\circ} = 9^{\circ} 10'$  curve, and the radius of a 9° 10' curve being 625 feet, we have:

 $x = \sqrt{2 \times 625 \times 6} = \sqrt[4]{7500} = 86.6$  — distance from origin of curve to point of frog.

When the main track is a curve, and it is required to get on to a side track running parallel thereto.

Note.—In treating of turnouts, When the main and side track are curves, the movable rail is considered a part of the curve used for turnout, according to method 1st.

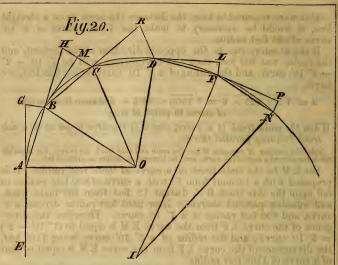
Let E M be the main track on a curve of 2865 feet radius. It is proposed with a turnout from E, with a curve of 800 feet radius, to fall upon the side track B N, distant 13 feet from the main track, and running parallel thereto. Now 2865 feet radius denotes a 2° curve, and 800 feet radius is a 7° 10′ curve. Therefore the divergence of the curve E F from the curve E M is equal to (7° 10′ — 2°) = 5° 10′ curve; and the radius of a 5° 10′ curve being 1109 feet, the divergence of the curve E F from the curve E M is equal to that of a curve of 1109 feet radius.

By similar reasoning, the convergence of the curve FB towards being parallel with EM is 9° 10′ per hundred feet, which may be expressed by a radius of 625 feet from tangent. Then we have  $1109 + 625 = 1734:1109::13:8\cdot31 = \text{distance of point of reversion from main track. Now since } x = \sqrt[4]{2 \text{ R. G}}$ , we have by substituting  $\sqrt{2 \times 1109 \times 8\cdot31} = 135\cdot7 = \text{distance from origin of curve to point of reversion, radius used being 800 feet. The radius of relative curvature being expressed in the formula, we have the proportion 1109:625::135.7:76.56 distance from reversion to 2d track.$ 

Suppose it be required to put the side track on the opposite side, then we have 1734:625:13:4.68 = distance of point of reversion from side track. Then we have the formula  $\sqrt{2 \times 625 \times 4.68} = 76.48$  distance from origin of curve to point of reversion. Then 625:1109:76.48:135.7 = distance from point of reversion to side track.

ON RUNNING CURVES BY OFFSETS, OR WITHOUT THE USE OF AN INSTRUMENT FOR MEASURING ANGLES.
Fig. 20.

From a tangent EA let it be required to run a curve ABCD, having for its radius OC. To do this we have only to find HC and its half MC = GB.



Suppose the chords AB, BC, CD are equal in length, being 100 feet each. The chords, and consequently the ares, being equal, the angle HBC is twice the angle GAB. But GAB is measured by half the arc AB = BC, consequently the angle HBC is measured by the whole arc BC. But the angle BOC is also measured by the arc BC, consequently the angles HBC and BOC are equal. Now triangle BOC is isosceles, and BH being equal to BC triangle HBC is isosceles also; consequently the two triangles are similar, and we have the proportion:

$$HC:BC:BC:BC:BC$$
, consequently  $HC=\frac{BC^2}{BO}$ , or  $HC=$ 

$$\frac{10000}{R}$$
.

Therefore M C = G B = 
$$\frac{A B^2}{2 R}$$
; hence the following rule:

The square of the uniform length of chord divided by radius will give the linear deflection from chord produced to curve, or half of this will give the deflection from tangent produced to curve.

#### EXAMPLES.

Suppose A O = 2500 feet, then 
$$\frac{10000}{2500}$$
 = H C = 4 feet, and G B

= 2 feet.

Suppose A O = 2865 feet, the radius of a 2° curve, then we have

H C = 
$$\frac{10000}{2865}$$
 = 3.49 or 3.5 feet nearly; and G B= $\frac{1}{2}$  of 3.5=1.75.

Since the angle GAB = 1° the deflection for 1° per hundred

feet is 1.75, or 0° 1' = 
$$\frac{1.75}{60}$$
 = .029, and one minute for one foot =

.00029, as by tables of natural sines.

## Case 2d.

Suppose we run the curve around to a point which we will call station 10, or 1000 feet from beginning. The point Q, which is less than 100 feet distant from station 10, say 50 feet, being at station 10 + 50.

Suppose this a 2° curve compounded at station 10 + 50 to a 3° curve of 1910 feet radius. Now the instrument setting on station 10 with a backsight on station 9, the instrumental deflection to 10 + 50, 150 feet, will be 1° 30′. Now since 1° per 100 feet is 1.75, that of 1° 30′ will be 2.62 feet. But the last chord being but 50 feet, or half of a hundred, the deflection will be half of 2.62 = 1.31; hence we have the following rule:

Multiply together half the curvature in degrees = instrumental deflection between the backsight and point required, the length of the last chord and 1.75, and the product is the distance from chord

produced to point required.

## Case 3d.

Suppose the curve from 10+50 to station 11 is a 3° curve of 1910 feet radius. Now the deflection from chord to tangent, from station 10 to station 10+50, is 0° 30′, and the deflection from tangent to chord between 10+50 and 11 is 0° 45′, therefore the entire deflection = 30'+45'=1°15'. Now 1° 15′ in a hundred =  $1°75 \times 14=2°18$ , and for 50 feet will be = 1°09 feet.

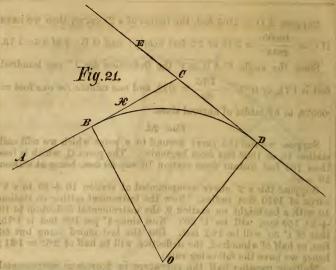
Find station 12 by Case 2d, thus  $2\frac{1}{4}^{\circ}$  (= instrumental deflection for 150 feet)  $\times$  1.75 = 3.93 = deflection from chord produced to

station 12 on curve.

Continue the curve around as at first, observing to measure from curve to tangent the same deflection as from tangent to curve, or half the usual chord deflection; the tangent point being supposed a full station. If not a full station, ascertain the tangent point by Case 2d, and the next full station on tangent by Case 3d.

Having produced two tangents to an intersection at C, it is required to connect them with a curve of given length. Fig. 21.

When the angle made by tangents is not greater than 15° the distance from vertex to the two ends of the curve will not differ materially from half the length of the curve.



Suppose the tangent D C produced 100 feet to E, measure C X = 100 feet, measure E X. Now suppose it is 21 feet.

Now the deflection of 1° for 100 feet is 1.75, and  $\frac{21}{1.75} = 12^{\circ}$  curvature.

Suppose it is required to divide the curve into 6 stations. Then  $\frac{21}{6} = 3.5$ , the deflection for 2° in 100 feet. Hence it is a 2° curve.

Or 12° divided by 6 stations gives a 2° curve also. The deflection being = 1.75 from tangent to curve.

Between two fixed points to supply the intermediate points by ordinates from the chord. Fig. 22.



By what has been previously demonstrated, the middle ordinate 4 to 4 will be expressed by  $\frac{4 \times 4}{2 \text{ R}}$ . At 3 the deflection from tan-

gent run each way from 4 to curve is  $\frac{1 \times 1}{2 R}$  at 2 it is  $\frac{2 \times 2}{2 R}$ .

Hence the ordinate 4 to  $4 = \frac{4 \times 4}{2 R}$ . Or 2 R being a common

denominator, its relative value may be expressed by  $4 \times 4$ . At points 3 and 5 on chord the distance will be  $(4 \times 4) - (1 \times 1) = 3 \times 5 = 15$ . At 6 and  $2 = (4 \times 4) - (2 \times 2) = 2 \times 6 = 12$ . At 7 and  $1 = (4 \times 4) - (3 \times 3) = 1 \times 7 = 7$ .

The ordinates are as follows:

$$1 \times 7 = 7$$
 $2 \times 6 = 12$ 
 $3 \times 5 = 15$ 
 $4 \times 4 = 16$ 

Then we observe that the sum of the two factors is equal, namely

the length of chord. Hence the following rule:

Multiply together the two segments of the chord or distance, divide by twice the radius, and the result is the distance from chord to curve.

Suppose for example the radius = 5000 feet, then at points 1 and 7

we have  $\frac{100 \times 700}{10000} = \frac{70000}{10000} = 7$  feet = offset at station 1 from end.

For 2 and 6 
$$\frac{200 \times 600}{10000} = 12 = 2d$$
 offset.

For 3 and 
$$5\frac{300 \times 500}{10000} = 15 = 3d$$
 offset,

and the entire length being 8 stations  $\frac{400 \times 400}{10000} = 16 = \text{greatest}$ 

or middle ordinate.

Had it been a 1° curve of 5730 feet radius, the ordinates would have been:

 $4 \times 4 \times \frac{7}{8} = 14.00 =$ middle ordinate; and

so in proportion to any other rate of curvature in degrees.

Hence when the rate of curvature is in degrees and no minutes, we have the following rule:

Multiply together the distances in stations each side of the point, and the rate of curvature, deduct from this product \( \frac{1}{8} \) of itself, the remainder will be the ordinate required.

<sup>\*</sup> The departure in 100 ft. of a 1° curve from tangent being = .75 = 3 of a foot.

#### CASE 2D.

Suppose that between the points 0 and 8 there occurs a point of c. c., for instance at 3 or 5, the curves compound from a 5000 feet radius to a 4000 feet radius.

By 1st method 
$$\frac{300 \times 300}{8000} = 11.25 = \text{distance from end of chord}$$

to tangent run from p. c. c., and  $\frac{500 \times 500}{10000} = 25 = \text{distance from}$ 

other end to said tangent.

Measure from ends of chords respectively 11.25 and 25 feet; on this line, at a distance 300 feet from 11.25 offset, and 500 feet from 25 feet offset, would be the point of compound curvature sought.

Or imagine either curve produced to a point opposite the end of the other; calculate by Proposition XI., and measure the distance between the two curves, then on the new chord find the p. c. c. as by simple curves. Thus:

$$\frac{300 \times 300}{8000} - \frac{300 \times 300}{10000} = 2.25.$$

Measure 2.25 from the old chord, and you have the direction of the new. Having found the p. c. c. calculate the offsets from each

chord separately.

The above rule for ordinates, although not perfectly accurate, considering the divisor always = 2 R, while it is variable, is sufficiently near for centres to grade by, when the chord subtends not more than 20° curvature.

This rule will also apply to placing centre points between

stations. Thus:

On a chord of 100 feet, radius 1000 feet, let it be required to locate a point 30 feet from one end and 70 feet from the other.

Then we have 
$$\frac{30 \times 70}{2000} = 1.05$$
.

# FOR SPRINGING RAILS.

Let L = length of rail and R = length of radius. Then:

$$\left(\frac{L}{2}\right)^2 = \frac{L^2}{8R} = \text{spring in feet.}$$

$$\frac{L^2 \times 1\frac{1}{2}}{R} = \text{spring in inches.}$$

$$\frac{L^2 \times 12}{R}$$
 = spring in eighths of an inch.

$$\left(\frac{24 L^2}{R}\right)$$
 = spring in sixteenths of an inch.

#### EXAMPLE.

Let the rail be 20 feet long, and the radius 1200 feet. Then

$$\frac{24 \times 20^2}{1200} = \frac{9600}{1200} = \frac{3}{18}.$$

Hence the rule:

24 times the square of the length of rail in feet divided by length of radius in feet, will give the spring in middle in sixteenths of an inch.

To find the length of chord for any rate of curvature (less than 8°) not specified in the Table of Chords (p 414.)

### EXAMPLE.

Let it be required to find the length of chord corresponding to 800 feet of curve for a 7° 10' curve.

 $7^{\circ}$  curve gives . 769.01  $7^{\circ}$  15' curve gives . 766.79Difference . . 2.22

Then  $15:10::2\cdot 22:1\cdot 48$ , and  $769\cdot 01-1\cdot 48=767\cdot 53$ ; or  $15:5::2\cdot 22:74$ , and  $766\cdot 79+0\cdot 74=767\cdot 53$ .

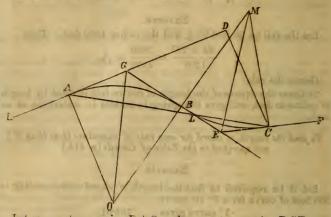
The result, as obtained by the table of sines, is 767.54, only  $\frac{1}{100}$  of a foot difference.

That is, sine 28° 40' × radius 800 × 2 = 767.54.

Suppose now it be required to find the length of chord corresponding to 950 feet of a 6° curve.

Now sine 28° 30′ × radius 955'37 × 2 = length of chord = 911'71, being only  $\frac{3}{10}$  of a foot difference, so that this table will be sufficient for ordinary purposes. For common rates of curvature for a less distance, say 650 feet, the variations from the true length would be scarcely perceptible.

PROBLEM. - Let A and C be two fixed tangent points, the positions of whose tangents are determined by the angles  $D A C = m = 18^{\circ}$ , B C E =  $n = 6^{\circ}$ , and the perpendicular distance D C = p = 463ft.\* Required the amount of curvature in the arc A B, its reversion BC, and the length of the common radius OB = MB by which the arcs A B and B C are described.



Let m = nat. vers. sine DAC, and n = nat. vers. sine BCE. Let  $x = \text{nat. vers. sine } (A \cap B - m) = (B \setminus B \cap m)$ . Or curvature A B = m + x, and curvature B C = n + x.

m + n v. s.  $18^{\circ} + v.$  s.  $6^{\circ}$ To find x we have,  $x = \frac{1}{2} = \frac{1}{2}$ 

0.048944 + 0.005478 = 0.027211 =nat. vers. sine 13° 23′ 48″.

Therefore arc A  $B = 18^{\circ} + 18^{\circ} 23' 48'' = 31^{\circ} 23' 48''$  and B C =  $6^{\circ} + 13^{\circ} 23' 48'' = 19^{\circ} 23' 48''$ . Then by principles from which Proposition XII. is derived, to find OB = R,

we have  $\frac{\text{perpd. dist. D C}}{}$ twice nat. vers. sine AB - nat. vers. sine (m-n) = R, Or

463:5 p = 463.5nat. v.s. 31° 23′ 48″  $\times$  2 — nat. v.s. 12° = 0.146420  $\times$  2 – 0.021852

 $\frac{1030}{0.270988}$  = 1710.4 = 0 B = radius of a 3° 21' curve.

 $\frac{1^{\circ} 24'}{3^{\circ} 21'}$  gives 937 ft. = arc A B, and  $\frac{19^{\circ} 24'}{3^{\circ} 21'}$  gives 579 ft = arc BC

\* If D C cannot be measured, measure A C and calculate D C. Thus if A C = 1500 ft, we have  $1500 \times \sin 15^\circ = 1500 \times 0.83902 = 463.58$ , + D G E being equal to A O B. A O B — m=A L G = C L G. Therefore x= nat. vers. sine A L G =  $13^\circ$  23° 48°.

(THE CURVATURE IS SUBTENDED BY A CHORD OF 100 FEET.)

	0 DEG	REE.	1	1 DEG	EGREE. 2 DEGREES.			
М	Radius Infinite.		М.	Radius.	, Logarithm.	M.	Radius.	Logarithms.
1	343775	5.536274	0 1	5730 5636	3·758128 3·750949	0 1	2865 2841	3·457115 3·453511
2	171887	5.235244	2	5545	3.743888	2	2818	3.449937
3	114592	5.059153	3	5457	3.736940	3	- 2795	3.446391
4	85944	4.934214	4	5372	3.730106	4	2772	3.442876
5	68755	4.837304	5	5289	3.723367	5	2750	3.439387
6	57296	4.758123	6	5209	3.716737	6	2729	3.435928
7 8	49111	4.691176	7 8	5131	3.710206	7 8	2707	3.432493
9	38197	4.633184 4.582031	9	5056 4982	3·703772 3·697432	9	2686 2665	3·429089 3·425708
10	34377	4.536274	10	4911	3.691183	10	2645	3.422356
11	31252	4 494881	11	4842	3.685023	11	2624	3.419028
12	28648	4.457093	12	4775	3.678947	12	-2605	3.415727
13	26444	4.422331	. 13	4709	3.672958	13	2585	3.412448
14	24555	4.390146	14	4646	3.667057	14	2566	3.409197
15	22918	4.360183	15	4584	3.661220	15	2547	3.405967
16	21486	4.332154	16	4523	3.655469	16	2528	3.402763
17	19099	4:305825	17 18	4465	3.649792	-17	2509	3.399581
18 19	18093	4·281002 4·257520	19	4407 4352	3·644189 3·638656	18 19	2491 2473	3·396424 3·393288
20	17189	4.235245	20	4297	3.633194	20	2456	3.390176
21	16370	4.214055	21	4244	3.627800	21	2438	3.387085
22	15626	4.193852	22	4192	3.622470	22	2421	3.384016
23	14947	4.174546	23	4142	3.617196	23	2404	3.380968
24	14324	4.156064	24	4093	3.612005	24	2387	3.377943
25	13751	4.138334	25	4045	3.006866	25	2371	3.374937
26	13222	4.121802	26	3997	3.601787	26	2355	3.371954
27	12732	4.104910	27	3952	3.596766	27	2339	3.368989
28	12278	4.089117	28	3997	3.591803	28	2323	3.366046
29 30	11854	4.073876	29 30	3863	3.586896	29	2307	3.363121
31	11459 11690	4.059154	31	3820 3778	3·582044 3·577246	30 31	2292 2277	3·360217 3·357331
32	10743	4·044912 4·031125	32	3737	3.572499	32	2261	3.354466
33	10417	4.017760	33	3697	3.567804	33	2247	3.351618
34	10111	4.004797	34	3657	3.263160	34	2232	3.348789
35	9822	3.992206	35	3619	3.558564	35	2218	3.345978
36	9549	3.979973	36	3581	3.554011	36	2204	3.343187
37	9291	3.968072	37	3544	3.549516	37	2190	3.340411
38	9047	3.956493	38	3508	3.545063	38	2176	3.337655
39	8815	3.945209	39	3473	3.540654	39	2162	3.334915
40	8594	3.934216	40	3438	3.536289	40	2149	3.332193
41 42	8385	3.923490	41	3404	3.531968	41	2135	3·329487 3·326799
42	8185 7995	3·913029 3·902806	42	3370 3338	3·527690 3·523452	42	2122 2169	3.326199
44	7813	3.892824	44	3306	3.519257	43	2098	3.321471
45	7639	3.883063	45	3274	3.212100	45	2083	3.318831
46	7473	3.873519	46	3243	3.510.985	46	2071	3.316208
47	7314	3.864179	47	3213	3.506907	47	2059	3.313600
48	7162	3·S55036	48	3183	3.502868	48	2046	3.311008
49	7016	3.846081	49	3154	3.498866	49	2034	3.308430
50	6876	3.837308	50	3125	3.494900	50	2022	3.305809
51	6741	3.828708	51	3097	3.490970	51	2010	3.309323
52	6611	3.820275	52	3069	8.487075	52	1999	3.300797
53		8.812002	53	3042	3.483205	53	1987	3.298274
54		8.803885	54 55	3016 2989	3.479389	54	1976 1965	3·295771 3·293283
56		3·795915 3·788091	56	2989	3·475596 3·471836	55	1953	3.290809
57	6021	3.780403	57	2938	3.468108	57	1942	2.288349
58		3.772851	58	2913	3.464413	58	1931	3.285902
59		3.765426	59	2889	8.460748	59	1921	3.283470
60		3.758128	60	2865	8.457115	60	1910	3.281051
1			**		,	11		

	3 DEGREES.			4 DEG	REES.	5 DEGREES.		
M.	Radius.	Logarithm.	м.	Radius.	Logarithm.	М.	Radius.	Logarithm
()	1910	3.281051	0	1493	3.156151	0	1146	3.059290
1	1900	3.278646	1	1427	3.154544	1	1142	3.057845
2	1889	3.276253	2	1421	3.152548	2	1189	3.056407
3	1879	3.273875	3	1415	3.150758	3	1135	3.055010
4	1869	3.271508	4	1409	3.148975	4	1131	3.053542
5	1858	3.269155	5	1403	3.147100	5	1127	3.052115
6	1848	3.262814	6	1398	3.145431	6	1124	3.050696
7	1839	3.264486	7	1392	3.143670	7	1120	8.049279
8	1829	3.262170	8	1386	3.141916	8	1116	3.047808
9	1819	3.259867	9	1381	3.140170	9	1113	3.046461
10	1810	3.257576		1375	3.138430	10	11(9	3.045059
11 12	1800 1791	3·255297 3·253029	11 12	1370 1364	3.136697	11 12	1106	3.043662
			13	1859	3.134977		1(99	3.042268
13	1781	3·250771 3·248530	14	1854	3.133251	13	1(95	3.040879
14	1772	3.248530	15	1348	3.131539	14	1092	3.039495
15 16	1763 1754	3.246291	16	1343	3·129833 3·128134	15 16	1092	3.038114 3.036740
17	1745	3.241867	17	1338	3.128134	17	1085	3.035368
18	1736	3.239669	18	1333	3.124756	18	1081	3.034002
19	1728	3.237481	19	1328	3.123075	19	1078	3.032636
20	1719	3.235305	20	1322	3.121404	20	1075	3.031281
21	1710	3.233140	21	1317	3.119737	21	1071	3.029927
22	1702	3.230985	22	1312	3.118078	22	1068	3.028577
23	1694	3.228841	23	1307	3.116423	23	1065	3.027230
24	1686	3.226707	24	1302	3.114773	24	1061	3.025890
25	1677	3.224584	25	1298	3.113134	25	1058	3.024552
26	1669	3.222479	26	1293	3.111401	26	1055	3.023219
27	1661	3.220369	27	, 1288	3.1(9871	27	1052	3.021889
28	1653	3.218277	28	1283	3.108249	28	1048	3.02056
29	1645	3.216128	29	1278	3.106632	29	1045	3.019248
30	1637	3.214122	30	1273	3.105022	30	1042	3.017927
31	1630	3.212060	31	1269	3.103418	31	1029	3.016614
32	1622	3.210007	32	1264	3.101818	82	1086	3.01530
33	1614	3.207963	33	1260	3.100225	83	1083	3.013999
34	1607	3.205930	34	1255	3.098638	34	1030	3.012698
35	1599	3.203906	35	1250	3.(97(56	35	1027	3.011400
36	1592	3.201892	36	1246	3 (95481	36	1024	3.010107
37	1584	3.199891	37	1241	3.(93910	37	1021	3.008813
38	1577	3.197890	38	1237	3.(92374	38	1017	3.007539
39	1570	3.195903	39	1232	83.(90788	39	1014	3.006249
40	1563	3.193925	40	1228	2.089236	40	1011	3.004979
41	1556	3.191957	41	1224	3.787689	41	1008	3.003098
42	1549	3.189996	42	1219	3.086147	42	1006	3.00242
43	1542	3.188045	43	1215	3.084610	43	1003	3.001159
44	1535	3.186103	44	1211	3.083079	44	1000	2.99989
45	1528	3.184168	45	1207	3.081553	45	996.9	2.99863
46	1521	3.182244	46	1202	3.080033	46	994.0	2.99738
47	1515	3.180327	47	1193	3.078518	47	991.1	2.99612
48	1508	3.178419	48	1194	3.077002	48	988.3	2.99488
49	1501	3.176519	49	1190	3.075503	49	985·4 982·6	2.99363
50	1495	3.174627	50	1186	3.074005	50	952.6	2.99289 2.99115
51	1489	3.172742	51	1182	3.072511	51	977.1	2.98992
52	1482	3·170868 3·169001	52	1178	3.071022	52 53	974.3	2.98869
53	1476 1469	3.167142	53	1174 1170	3·069537 3·068059	54	971.5	2 98746
54	1469	3.165290		1166		55	968.7	2.98619
55			55		3.066584	56	966.1	2 98019
56 57	1457 1451	3·163447 3·161612	56	1162 1158	3.065116 3.063648	57	963.4	2.98386
58	1445	3.159784	58	1154	3.062194	58	960.7	2.98258
59	1439	3.157963	59	1150	3.060738	59	958.0	2.98137
60	1433	3·156151	60	1146	3.059290	60	955.4	2.98017
00	1400	9 190191	00	1140	0 000200	00	300 1	20001

			H.	* DEG	o DEGI	· · · · · · · · · · · · · · · · · · ·		
	6 DEG	REES.	l	7 DEG	KEES.		8 DEGI	EES.
М.	Radius.	Logarithm.	M.	Radiu.	Logarithm.	м.	Radius.	Logarithm.
0	955.4	2.980170	0	819.0	2.913295	0	716.8	2.855385
1	952.7	2.978967	1	817.1	2.912266	$\frac{1}{2}$	715·3 713·8	2.854483
3	950·1 947·5	2·977766 2·976569	3	815·1 813·2	2·911234 2·910208	3	712.3	2·8535S3 2·8526S4
4	944.9	2.975875	4	811.3	2.9 9183	4	710.9	2.851787
5	942.3	2.974186	5	8:9.4	2.938161	5	709.4	2.850891
6	939.7	2.972997	6	807.5	2.907142	6 7 8	707.9	2.349999
7	937.2	2.971814	7	835.6	2.906124	7	706.5	2.849107
8	934.6	2.970633	8	833.7	2.905111	9	705.0	2.848219
19	932·1 929·6	2·939456 2·968282	9	801.9 800.0	2·904097 2·903090	10	702.2	2·847829 2·846445
11	927.1	2.937111	11	793.1	2/902082	11	700.7	2.845562
12	924.6	2.935943	12	796.3	2.9.1076	12	699.3	2.344679
13	922.1	2.934778	13	794.5	2.900073	13	697.9	2.843799
14	919.6	2.363616	14	792.6	2.899073	14	693.5	2.342921
15	917.2	2.962458	15	790.8	2.\$93075	15	695·1 693·7	2.842044
16 17	914·3 912·3	2·931303 2·930150	16	789·0 787·2	2·397078 2·393085	16 17	692.3	2·841169 2·840296
18	919.9	2.959301	13	785.4	2.395094	18	690.9	2.839424
19	9.7.5	2.957854	19	783.6	2.894103	19	689.5	2.338554
2)	905.1	2.955711	2)	781·8	2.893118	20	688.2	2.837687
21	9)2.8	2.955572	21	780.1	2.892134	21	686.8	2.836821
22	930.4	2.954434	22	778.3	2.891151	22	685.4	2.335956
23	893·0 895·7	2.958800	23	776·6 774·8	2.890171	23 24	684·1 682·7	2.835093
24 25	893.4	2·952168 2·951049	24 25	773.1	2·889193 2·888218	25	681.4	2·S34232 2·333373
26	891.1	2.949915	26	771.3	2.887244	26	680.0	2.832515
27	888.8	2.948792	27	769.6	2.886272	27	678.7	2.831659
28	886.5	2.947673	28	767-9	2.885303	23	677.4	2.330805
29	884.5	2.946555	29	766.2	2.384336	29	676.0	2.829953
30	882.0	2.945452	30	764.4	2.883371	30	674.7	2.829102
31 32	879·7 877·5	2·944330 2·943223	31 32	762·8 761·1	2·882409 2·881445	31 32	673·4 672·1	2·828253 2·827405
33	875.2	2.942116	33	759.4	2.380490	33	670.7	2.826560
34	873.0	2.941015	34	757.8	2.879534	34	669.4	2.825715
85	870.8	2.939914	35	756.1	2.878580	35	668.1	2.824873
36	868.3	2.938819	36	754.4	2.877627	36	666.9	2.324332
37	866.4	2.937722	37	752.8	2.876678	37	665.6	2.323192
38	864·2 862·1	2·936633 2·935543	38	751·2 749·5	2·875730 2·874783	33	664.3	2·322355 2·321519
40	859.9	2.934459	40	747.9	2.373840	40	661.7	2.821619
41	857.7	2.933337	41	746.3	2.872900	41	660.5	2.319352
42	855.6	2.932295	42	744.7	2.871959	42	659.2	2.819,121
43	\$53.2	2.931218	43	743.1	2.871022	43	657.9	2.818191
44	851.4	2.930142	44	741.5	2.370086	44	656.7	2.317363
45	849°3 847°2	2·929J70 2·928000	45	739·9 738·3	2·869153 2·868221	45	655·4 654·2	2.316587
47	845.1	2.926933	47	736.7	2.867291	47	653.0	2·815712 2·814888
48	843.1	2.925867	48	735.1	2.866363	48	651.7	2.814963
49	841.0	2.924306	49	733.6	2.865438	49	650.5	2.313246
50	839.0	2.923747	59	732.0	2.864514	50	649.3	2.812428
51	836.9	2.922691	51	730.5	2.863593	51	648.1	2.811611
52	834.9	2.921637	52	728.9	2.862673	52	646.8	2.810793
53 54	832·9 830·9	2·92.)585 , 2·919586	53 54	727·4 725·8	2·861756 2·860840	58 54	645.6 644.4	2·309082 2·809169
55	\$28·9	2.918489	55	724.3	2.859926	55	643.2	2.808358
56	826.9	2.917446	56	722.8	2.859014	56	642.0	2.807594
57	824.9	2.916403	57	721.3	2.858104	57	640.8	2.806741
58	822.9	2.915365	58	719.8	2.857196	58	639.6	2.835935
59	821.0	2.914827	59	715.3	2.856289	59	638.5	2.805130
60	819.0	2.913295	60	716.8	2.855385	60	637.3	2.804327
L			The Real Property lies					

	9 DEG	REES.	Marie and Marie	10 DEG	REES.		REES.	
M,	Radius.	Logarithm,	M.	Rad'u.	Logarithm.	M.	Radius.	Logarithm.
0	637.3	2.804327	0	573.7	2.758674	0	521.7	2.717397
1	636.1	2.803526	1	572.7	2.757953	1	520.9	2.716742
2	634.9	2.802724	2 3	571.8	2.757232	2	520.1	2.716087
3 4	633·8 632·6	2·801926 2·801128	4	570·8 569·9	2·756514 2·755796	3 4	519·3 518·5	2·715434 2·714781
5	631.4	2.800832	5	569.0	2.755079		517.8	2.714130
6	630.3	2.799538	6	568.0	2.754364	5 6	517.0	2.713479
7	629.1	2.793745	7	567.1	2.753650	7	516.2	- 2.712830
8 9	628.0	2.797953	8	566.2	2.752937	8	515.4	2.712181
	626.8	2.797163	9	565.2	2.752225	9	514.7	2.711533
1)	625·7 624·6	2·796374 2·795587	10	564·3 563·4	2·751514 2·750804	10 11	513·9 513·1	2·710887 2·710241
12	623.5	2.794801	12	562.5	2.750096	12	512.4	2.709596
13	622.3	2.794017	13	561.6	2.749389	13	511.6	2.708953
14	621.2	2.793234	14	560.6	2.748683	14	510.9	2.708310
15	62).1	2.792452	15	559.7	2.747978	15	510.1	2.707668
16	619.0	2.791673	16	558.8	2.747274	16	509.3	2.707027
17 18	617·9 616·8	2·793S94 2·793117	17 18	557·9 557·0	2·746572 2·745870	17 18	508·6 507·9	2·706387 2·705748
19	615.7	2.789340	19	556.1	2.745170	19	507.1	2.705110
20	614.6	2.788566	20	555.2	2.744471	20	506.4	2.704473
21	613.5	2.787794	21	554.3	2.743773	21	505.6	2.703837
22	612.4	2.787021	22	553.4	2.743076	22	504.9	2.703202
23	611.3	2.786252	23	552.6	2.742380	23	504.1	2.702568
24 25	610.2	2.785482	24	551.7	2.741686	24 25	503·4 502·7	2.701934
26	609·1 608·1	2·784715 2·783948	25 26	550·8 549·9	2·740990 2·740300	26	501.9	2·701302 2·700671
27	607.0	2·7S3183	27	549.0	2.739669	27	501.2	2.700040
28	605.9	2.782420	28	548.2	2.738918	28	500.5	2.699410
29	604.9	2.781657	29	547.3	2.738229	29	499.8	2.698782
30	603.8	2.780897	30	546.4	2.737541	30	499.0	2.698154
31	602.8	2.780138	31	545.6	2.736854	31	493.3	2.697527
32 33	601.7	2·779379 2·778622	32	544·7 543·8	2·736169 2·735484	32   33	497·6 496·9	2·696901 2·696276
34	599.6	2.777863	34	543.0	2.734830	34	493.2	2.695652
35	598.6	2.777113	35	542.1	2.734118	35	495.5	2.695029
36	597.5	2.776360	36	541.3	2.733436	36	494.8	2.694497
37	596.5	2.775608	37	543.4	2.732756	37	494.1	2.693785
38 39	595.5	2.774858	38	539.6	2.732077	38	493·4 492·7	2.693165
49	594·4 593·4	2·7741 08 2·773361	39 40	53S·8 537·9	2·731398 2·730721	39	492.0	2·692545 2·691926
41	592.4	2.772616	41	537.1	2.730045	41	491.3	2.691308
42	591.4	2.771870	42	536.3	2.729370	42	490.6	2.690692
43	593.4	2.771124	43	535.4	2.728696	43	489.9	2.690076
44	589.4	2.770383	44	534.6	2.728023	44	489.2	2.689460
45 46	538·4 587·4	2.769642 2.768902	45 46	533·S 532·9	2·727351 2·726684	45	488.5 487.8	2.688846 2.688233
47	586.4	2.768163	47	532.1	2.726010	47	487.1	2.687620
48	585.4	2.767426	48	531.3	2.725342	48	486.4	2.687008
49	584.4	2.766689	49	530.5	2.724674	49	485.7	2.686398
50	583.4	2.765955	50	529.7	2.724008	50	485.0	2 685788
51	582.4	2.765223	51	528.9	2.723342	51	484.4	2.685179
52 53	581·4 580·4	2·764489 2·763758	52	528·0 527·2	2.722677	52 58	483·7 483·0	2.684570 2.683963
54	579.5	2.763028	54	526.4	2·722014 2·721351	54	482.3	2.683357
55	578.5	2.762299	55	525.6	2.720690	55	481.7	2.682751
56	577.5	2.761572	56	524.8	2.720019	56	481.0	2.682146
57	576.6	2.760845	57	524.0	2.719370	57	480.3	2.681542
58	575.6	2.760120	58	523.2	2.718711	58	479.7	2.680939
59 60	574·6 573·7	2·759398 2·758674	59 60	522·5 521·7	2·718054 2·717397	59 60	479·0 478·3	2·680337 2·679735
00	0101	2 100014	00	021	2111001	00	1100	3 010100

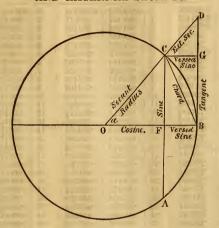
		IABLE OF	LUA	DII AND	IIIEII LIOG	ARITHMS. 410			
	12 DEC	FREES.		13 DE	FREES.	14 DEGREES.			
M.	Radius.	Logarithm.	M.	Radius.	Logarithm.	M.	Radius.	Logarithm.	
0	478.3	2.679735	0	441.7	2.645111	0	410.3	2.613075	
1	477.7	2.679135	1	441.1	2.644557	1	409.8	2.612561	
2	477.0	2.678535	2	440.5	2.644004	2	40.9.3	2.612048	
3	476.3	2.677936	3	440.0	2.643451	3	408.8	2.611535	
4	475.6	2.677238	5	459.4	2.642900	4	408.3	2.611023	
5	475.0	2.676741	6	438.9	2.642348	5	407.9	2.610511	
7	474·4 473·8	2.676145	7	438·3 437·8	2.641798	7	406.9	2·610000 2·6(9490	
	473.1	2·675549 2·674954	8	437.2	2·641248 2·640699	8	406.4	2.608980	
8 9	472.5	2.674860	9	436.7	2.640150	9	406.0	2.608471	
10	471.8	2.673767	10	436.1	2.639603	10	405.5	2.607962	
11	471.2	2.673175	îĭ	435.6	2.689056	11	405.0	2.607454	
12	470.5	2.672584	12	435.0	2.638510	12	404.5	2.606946	
13	469.9	2.671993	. 13	434.5	2.637964	13	404.0	2.606489	
14	469.2	2.671403	14	433.9	2.637419	14	403.6	2.605933	
15	468.6	2.670814	15	433.4	2.636875	15	403.1	2.605428	
16	468.0	2.670226	16	432.8	2.636332	16	462.6	2.604923	
17	467.3	2.669638	17	432.3	2.635789	17	402.2	2.604418	
18	466.7	2.669052	13	481.8	2.635247	18	401.7	2.608914	
19 20	466.1	2.668466	19 20	431.2	2.634705	19	401.2	2.603411	
21	465·5 464·8	2.667881	20	430.7	2.634164	20	400.8	2.602908	
22	464.2	2.667297 2.666713	22	430·2 429·6	2.633624	21 22	400·3 399·9	2.602406 2.601905	
23	463.6	2.666131	23	429 0	2.633085 2.632546	23	399.4	2.601404	
24	463.0	2.665549	24	428.6	2.682308	24	398.9	2.600904	
25	462.3	2.664968	25	428.0	2.631471	25	398.5	2.600404	
26	461.7	2.664387	26	427.5	2.68(934	26	398.0	2.599905	
27	461.1	2.663808	27	427.0	2.630388	27	397.6	2.599406	
28	460.5	2.663229	28	426.4	2.629863	28	397.1	2.598908	
29	459.9	2.662651	29	425.9	2.629328	29	396.7	2.598411	
30	459.2	2.662074	30	425.4	2.628794	30	£96·2	2.597914	
31 32	458.6	2.661498	31	424.9	2.628261	31	895.7	2.597418	
33	458.0	2.660922	32	424.4	2.627728	32	895.3	2.596922	
34	457·4 456·8	2.660347	33 34	423.8	2.627196	33	394.8	2.596427	
35	456.2	2.659773 2.659200	35	423·3 422·8	2.626665	34	894·4 893·9	2·595933 2·595439	
36	455.6	2.658628	36	422.3	2·626134 2·625604	35 36	393.5	2.594946	
37	455.0	2.658056	37	421.8	2.625074	37	393.0	2.594453	
38	454.4	2.657485	38	421.3	2.624546	38	892.6	2.595961	
39	453.8	2.656915	39	420.7	2.624018	39	392.2	2.593469	
40	453.2	2.656345	40	420.2	2.623490	40	391.7	2.592978	
41	452.7	2.655776	41	419.7	2.622963	41	391.2	2.592487	
42	452.1	2.655208	42	419.2	2.622437	42	390.8	2.591997	
43	451.5	2.654641	43	418.7	2.621912	48	390.4	2.591508	
44	450.9	2.654075	44	418.2	2.621387	44	390.0	2.591019	
46	450.3	2.653509	45	417.7	2.620863	45	389.5	2.590531	
47	449·7 449·1	2.652944	46	417.2	2.620339	46	389.1	2:590043	
48	449.1	2.652380 2.651816	47 48	416.7	2.619816	47	388·6 388·2	2.589556	
49	448.0	2.651254	49	416·2 415·7	2.619294	48 49	385°2 387°8	2.589069 2.588583	
50	447.4	2.650691	50	415.2	2·618772 2·618251	50	387.3	2.588(97	
51	446.8	2.650130	51	414.7	2.617731	51	386.9	2.587612	
52	446.2	2.649570	52	414.2	2.617211	52	386.5	2.587128	
53	445.7	2.649010	53	413.7	2.616692	53	386.0	2:586644	
54	445.1	2.648451	54	413.2	2.616173	54	385.6	2.586161	
55	444.5	2.647892	55	412.7	2.615655	55	385.2	2.585678	
56	444.0	2.647335	56	412.2	2.615138	56	384.8	2.585196	
57	443.4	2.646778	57	411.7	2.614622	57	384.3	2.584714	
58 59	442.8	2.646222	58	411.2	2.614106	58	383.9	2.584233	
60	442·2 441·7	2.645666	59	410.8	2.613590	59	383.5	2.583752	
00	4111	2.645111	60	410.3	2.613075	60	383.1	2.583272	
-									

## TABLE

Of Chords corresponding to every 100 feet on curve from 200 to 1000 feet, calculated to every 15 minutes' rate of curvature, from 15 minutes to 8 degrees, radius of 1° being 5730 feet.

Rate of curvature.	200 feet.	800 feet.	400 feet.	500 feet.	600 feet.	700 feet.	800 feet.	900 feet.	1000 ft.
15'	200:00	300.00	400.00	499-99	599-98	699-97	799.96	899-94	999.92
30'	200.00	299.99	399.98	499.96	599.93	699.89	799-84	899.77	999.69
45'	200	299.98	399.95	499-91	599.84	699.76	799.64	899.49	999-30
1°	199.99	299.97	399.92	499.85	599.78	699.57	799.36	899.69	998.75
1° 15'	199.99	299.95	399.88	499.76	599.58	699.33	799-00	898.57	998.05
1° 30'	199.98	299.93	399.83	499.66	599.40	699.04	798.56	897.95	997.18
1° 45'	199.98	299-91	399.77	499.53	599.18	698.69	798.04	897-20	996.15
2°	199.97	299.88	399.70	499.39	598.94	698.30	797.44	\$96.35	994.98
2° 15'	199.96	299.85	399.61	499-23	598.65	697.84	796.76	895.38	993.65
2° 30'	199.95	299.81	399.52	499.05	598.34	697.34	796.01	894.30	992.17
2° 45′	199.94	299.77	399.42	498.85	597.99	696.78	795.17	893.10	990.52
3°	199.93	299.73	399.32	498.63	597.61	696.17	794.25	891.80	988.73
3° 15'	199.92	299.68	399.19	498.39	597.19	695.50	793.26	890.38	986.78
3° 30′	199.91	299.63	399.07	498.14	596.74	694.79	792.18	888.85	984.68
3° 45	199.89	299.57	398.93	497.86	596.26	694.02	791.03	887.21	982.42
4°	199.88	299.51	398.78	497.57	595.74	693-20	789.80	885.45	979-99
4° 15′	199.86	299.45	398.63	497.25	595.20	692-32	788-49	883.58	977.46
4° 30′	199.85	299-38	398.46	496-92	594.62	691.40	787.11	881.61	974.75
4° 45′	199.83	299.31	398-28	496.57	594.00	690.42	785.64	879.52	971.89
5°	199.81	299.24	398.10	496.20	593.36	689.39	784·10 782·48	877-32	968.87
5° 15′	199·79 199·77	299·16 299·08	397·90 397·70	495.81	592.68	688·30 687·17	780.79	875·02 872·61	965.72
5° 30'	199.75	299.08	397.49	495.40	591.97	685.93	779.01	870.03	958-96
5° 45′	199.73	298.90	397.26	494.53	59045	684.75	777.16	867.45	955.37
6° 15'	199.70	298.81	397.03	494.07	589.64	683.46	775-24	864.72	951.63
6, 30,	199.68	298.72	396.80	493.60	588.81	682.13	773.26	861.90	947.75
6° 45	199.65	298.61	396.54	493.09	587.93	680.73	771.16	858.93	943.71
7°	199.63	298.51	396.28	492.57	587.02	679.29	769.01	855.87	939.54
7. 15	199.60	298.40	396.01	492.03	586.08	677.79	766-79	852.72	935.23
7° 30'	199.57	298-29	395.73	491.47	585.11	676.25	764.49	849.45	930-78
7° 45'	199.54	298-17	495.44	490.90	584.12	674.66	762-12	846.09	926-20
8.	199.51	298.05	395.14	490.31	583.08	673.01	759.67	842.62	921.47

## TABLES OF NATURAL AND LOGARITHMIC VERSED SINES, AND EXTERNAL SECANTS.



On the Construction of the Tables of Versed Sines and External Secants.

In the above figure it is required to find the value of versed sine FB = CG, of arc BC = AB angle a, and of external secant CD in terms of sine CF and tangent BD.

The chord BC = 2 sine ½ BC, and angle FCB is measured by

 $\frac{1}{2}$  are AB  $=\frac{1}{2}$  are BC.

Therefore making chord B C radius, B F will be the sine of angle F C B, and we have:

Versed sine B F =  $2 \times \overline{\text{sine F C B}^2} = 2 \times (\text{sine } \frac{1}{2} \text{ a})^2$ .

That is, twice the square of sine of half given are = versed sine. Making CF radius. BF becomes tangent, and we have, versed sine BF = CF  $\times$  tangent FCB, or sine  $a \times$  tangent  $\frac{1}{2}a$ .

Now by similar triangles v. s. a: ex. sec. a:: cos. a: radius; and v. s. a: ex. sec. a:: sine a: tangent a;

or, ex. sec.  $a = v. s. a \times radius$  = tan.  $a \times tangent \frac{1}{2} a.$ 

Then  $\log_a v$ , s.  $a = \log_a \sin a + \log_a \tan \frac{1}{2} a - (10 = \log_a \text{ of R.})$ , and  $\log_a ex$ , see,  $a = \log_a v$ , s.  $a + 10 - \log_a \cos_a a$ ; or,  $\log_a ex$ , sec,  $a = \log_a \tan_a a + \log_a \tan_a \frac{1}{2} a - 10$ .

## EXAMPLE.

Log. sine  $40^{\circ} = 9.808067$ Log. tan.  $20^{\circ} = 9.561066$ Log. v. s.  $40^{\circ} = 9.369133$ Log. tan.  $40^{\circ} = 9.23813$ Log. tan.  $20^{\circ} = 9.561066$ Ex. sec.  $40^{\circ} = 9.484879$ 

	0 DEGRI	EE.		1 DEGR	EE.		2 DEGRI	EES.
Min.	Nat. No	Logarithm.	Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Logari:hm.
0	0.000000	0.000000	0	0.000152	6.182714	0	0.000609	6.784740
1	.0000000	2.621422	1	*000157	197071	1	.000619	·791948
2 3	.0000000	3-228482	2	.000162	211194	2	.000630	•799:97
4	.000000	*580664 *830542	3	·000168 ·000173	*225091 *238770	3 4	*000640 *000650	*806 <b>1</b> 87 *8132 <b>19</b>
5	-000001	4.024362	5	000179	252227	5	*000661	820194
6	•300002	182724	6	000184	265496	6.	.000672	·827114
7	.300002	*316618	7 8	.000190	278557	7	·0006S2	*833980
8	*300003	·432602		.000196	291426	8	.000693	*840792
10	*300003 *300004	·534906 = ·626422	9	·000201 ·000207	*304106 *316604	9	·000704 ·000715	*847551 *854257
11	·300005	709206	11	000201	328925	11	000726	860912
12	·300006	·784784	12	.000219	*841072	12	000737	·867516
13	*300007	·854306	13	.000225	*853051	13	.000748	·874070
14	·300008	918678	14	.000232	364868	14	.000759	-880577
15 16	*300010 *300011	978602 5.034662	15 16	·000238 ·000244	*376528 *388032	15 16	·000771 ·000782	*887033 *893444
17	*300011	087316	17	000244	388032	17	*000794	·S99S06
18	.300014	136966	18	000257	410592	18	·000S05	906123
19	·J00015	183924	19	.000264	421657	19	-000817	-912393
20	*300017	228480	20	*000271	*432582	20	*000829	918618
21 22	*300018 *300020	·270856 ·311266	$\frac{21}{22}$	·000278 ·000284	*443372	21 22	*000841 *000853	*924800 *930937
23	·J00022	349877	23	000294	*454030 *464538	23	000865	937032
24	*300024	386842	24	000298	474960	24	000877	943084
25	*000026	·422302	25	.000306	485238	25	-000889	*949093
26	*300029	*456366	26	.000313	·495396	26	.000962	955062
27 28	*000031	489140	27 28	*000320	505438	27 28	*000914	960991
29	*000033 *000035	·520736 ·551216	28	*000328 *000335	·515364 ·525179	28	*000926 *000939	966879
30	-300038	*580662	30	0000343	534882	30	-006952	978536
31	.000040	·609143	31	.000350	•544480	31	.000964	934305
32	*000043	*636720	32	.000358	*553972	32	.000977	990038
33 34	*000046 *000049	·663449 ·689376	33 34	·000366 ·000374	*563362 *572651	33 34	·000990 ·001013	*995733 7.001391
35	000052	.714558	35	*000382	581841	35	.001016	007013
36	.000055	·739024	36	.000390	•590937	36	.001029	.012597
37	*000058	·762S21	37	.000398	•599936	37	001043	018147
38	*000061 *000064	785984	38	*000406	*608845	38	·001056 ·001069	*023660 *029139
40	·000068	*808549 *830538	40	·000415 ·000423	·617662 ·626393	40	•001083	029159
41	.300071	851985	41	-000431	635034	41	-001097	039995
42	.300075	*872916	42	.000440	•643591	42	.001110	045372
43	*300078	*893353	43	.000449	*652064	43	001124	050717
44 45	*300082 *300086	•913322 •932845	44 45	·000458 ·000466	-660456 -668768	44 45	·001138 ·001152	*056027 *061307
46	.000090	951932	46	000400	676999	46	.001166	066554
47	.000093	970611	47	000484	*685156	47	.001180	-071771
48	·300097	•938893	48	.000493	*693234	48	*001194	-076955
49	*000102	6.006770	49	•000503	*701240	49	*001208	082119
50 51	300106	·024354 ·041559	50	*000512 *000521	·709171 ·717032	50	001222	087232
52	.000114	058420	52	000521	724820	52	001251	097388
53	.300119	074965	53	*000540	•732540	53	.001266	102423
54	*000123	•091200	54	*000550	•740192	54	001281	107428
55 56	000128	·107146 ·122788	55 56	000559	747778	55	·001295 ·001310	112405 117853
57	200137	138167	57	000509	762752	57	·001310	122272
58	*000142	153268	58	000589	.770144	58	*001340	122272 127165
59	*000147	·168116	59	-000599	.777472	59	*001355	132031
60	000152	182714	60	•000609	784740	60	*001370	136868

	0 DEGR	EE.		1 DEGR	EE.		2-DEGRI	EES.
Min.	Nat. No.	Logarithm,	Min.	Nat No.	Logarithm.	Min.	Nat. No.	Logarithm.
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1	•000000	2.626422	1	.000157	·197139	1	*000620	·792217
2	.000000	3.228482	2	*000163	•211265	2	•000630	•799371
3	•0000000	580604	3	*000168	225164	3	*000640	*806465
5	•000000 •000000	*830542 4*024362	4 5	·000173 ·000179	*238845 *252305	4	*000651 *000661	*813502 *820481
6	*000001	182725	6	000184	265576	5 6	000672	827406
6	000002	*316619	7	.000190	278639	7	.000683	·S34276
8	-000003	•432603	8	.000196	291511	8	.000€94	841093
9	.000003	•534907	9	.000201	*304193	9	*000704	*847857
10	·000004	•626424	10	.000207	316694	10	.000715	854568
11	•000005	709209	11	*000213	*329018	11	000726	861227
12 13	-000006 -000007	·784787 ·854309	12 13	·000219 ·000225	*341167 *353149	12 13	*000738 *000749	·\$67836
14	-000008	918682	14	000223	364969	14	000760	*874395 *880907
15	-000010	978606	15	.000238	376631	15	000772	887368
16	•000011	5.034667	16	000244	388138	16	000783	893784
17	-000012	.087321	17	.000251	*899486	17	.000795	900157
18	·000014	·136974	18	000257	·410704	18	*000806	906473
19	•000015	·183933	19	*000264	*421772	19	.000818	912748
20	•000017	•228487	20	*000271	*432700	20	*000830	918978
21 22	-000018 -000020	·270864 ·311275	21 22	·000278 ·000285	*448493 *454154	21 22	*000842 *000854	925165 931368
23	-000020	311213	23	•000292	*464685	23	*000866	937408
24	-000024	386853	24	-000299	-475090	24	*000878	943465
25	-000026	*422314	25	-000306	485371	25	.000890	949479
26	-000029	456378	26	•000313	·495532	26	*000908	.955454
27	-000031	·489153	27	•000320	*505577	27	*000915	·961388
28	•000033	•520750	28	•000328	•515506	28	·000927	967282
29	•000036 •000038	*551280	29 30	*000335 *000343	525325	29	*000940	973134
31	-000038	*580679 *619151	31	000345	*535031 *544632	31	*000953 *000965	·978950 ·984724
32	•000043	636739	32	•000358	554128	32	000978	990463
33	-000046	663469	33	-000366	563521	33	.000991	996163
34	-000049	.689397	34	.000374	.572813	84	.001014	7.001827
35	-000052	·714581	35	•000382	582007	35	.001017	007455
36	•000055	·739048	36	•000390	•591106	36	.001031	*013044
37	·000058	762846	37	*000398	*600169	37	001044	*018600
38	·000061 ·00064	*786013 *808577	38 39	*000406 *000415	*609022 *617842	38 39	*001057 *001071	*024119 *029604
40	-000068	830567	40	000413	626577	40	001084	029004
41	-000071	852016	41	•000432	635222	41	.001098	030000
42	-000075	*872948	42	.000440	*643782	42	*001111	045854
43	-060078	*893387	43	000449	*652259	43	.001125	.051205
44	-000082	•913358	44	.000458	*660655	44	.001139	.056521
45	•000086	932882	45	*000466	668771	45	001153	*061807
46	•000090 •000094	951971	46	*000476 *000485	*677206	46	*001167	067061
47	-000097	•970652 •988940	48	000494	*685366 *693448	47	'001181 '001195	072284
49	-000102	6.006814	49	000503	•701458	49	.001210	082644
50	-000106	.024400	50	*000512	•709893	50	001224	087768
51	-000110	.041607	51	•000522	.717258	51	.001238	.(92862
52	•000114	*058470	52	•000531	725051	52	*001253	*(97932
53	•000119	•075017	53	*000540	732775	53	*001268	102978
54	•000123	*091254	54	*000550	*740431	54	001282	107985
55	·000128 ·000138	107202	55	000560	*748021	55	001297	112968
56	000133	·122846 ·128227	56	000570	·755544 ·763004	56	·001312 ·001327	·117922 ·122848
58	000131	153330	58	000589	103004	58	001321	127747
59	000147	168180	59	•000599	•777732	59	001357	132620
60	000152	182780	60	.000610	·785005	60	001372	137464
	1		11	1		II.	1	

	3 DEGR	EES.		4 DEGR	EES.	5 DEGREES.		
Min.	Nat. No.	Logarithm.	Min.	Nat. No	Logarithm.	Min.	Nat. No.	Logarithm.
0	0.001370	7:136868	. 0	0.002436	7.386669	0	0.003805	7.580389
1 2 3	*001386	141679	1 2	062456	-890273	1	*003831	583272
2	*001401	·146464	3	*002477	*393524	2	*003856	*586156
8	*001417	151225	3	*002497 *002518	*397455 *401019	3 4	*008582 *0089.7	589026 591886
4 5	*061432 *001448	•155955 •160661	4 5	*062538	·464572	5	.)08933	591735
6	*001463	165342	6	*002559	408108	6	.003959	597578
6 7 8	-301479	169999	6 7	*062580	411629	6 7 8	.003985	600410
8	001495	174629	8	*002601	*415187	8	*004010	*608284
9	001511	179236	9	*062622	*418632	9	*004037	*606043
19 11	*001527 *001543	188819 188877	10 11	*002643 *002664	·422111 ·425577	10 11	*J04063 *J04089	·608852 ·611647
12	·001545	192912	12	*002004	429329	12	004116	614434
13	.001000	197422	13	*002707	432463	13	004142	617210
14	*001592	201910	14	*062728	435892	14	*004109	-619930
15	001008	206876	15	*002750	·439303	15	'004195	622740
16	.001625	·210S17	16	002771	*442702	16	004222	*625490
17	.061641	215237	17	*002793	*4460S7	17	64248	·62S234
13 19	001058	219002	18 19	*062815 *062837	•449458 •452817	18	004275 004302	*630.966
20	*001075 *001692	*224018 *228360	20	002859	456162	20	004329	*633692 *636409
21	0017.9	232692	21	062331	459494	21	004356	689117
22	-001726	237000	22	*002903	462815	22	004382	641816
23	*001748	•241259	23	*062925	*466121	23	*004410	·644506
24	-001760	245555	24	*002947	469417	24	'004438	647170
25	-301777	*249802	25	*002970	472099	25	'004466	*649864
26 27	-001795 -001813	254026 258282	26 27	*002992 *003015	475969 479227	26 27	'004493 '004521	*652532 *655190
28	001313	262416	28	.003013	482472	28	004543	657840
29	*001847	266582	29	003060	485705	29	004576	660482
30	*061865	270725	30	*003083	488926	20	*004604	.663116
81	*001883	274852	31	*003106	492137	81	*004682	665743
82 88	*001901	278957	32 33	*003129	*495834	32	004669	·66S360
34	*001919 *001987	*283043 *287169	33 34	*003152 *003175	*498523 *501094	33 34	'004688 '004716	·67(972 ·673574
35	*001955	291156	35	003193	*504857	35	064744	676168
36	0(1973	·2951S7	36	*063221	508008	36	004773	678759
37	.001992	•299196	37	*003244.	511147	37	'004801	681334
38	*062010	203190	38	*003268	*514275	38	*004830	·6SS936
39	•062628	307162	39	003291	*517891	89	*004858	686470
40 41	-062047 -062066	*311119 *815056	40 41	*003315 *003339	*520498 *523593	40	*004887	*689026
42	·002000 ·002085	318977	41	003362	526677	41 42	*004916 *004944	·691574 ·694116
43	•302103	-322879	43	003386	529750	43	'004973	-696649
41	•362122	-326764	44	'003410	532812	44	'005062	-699176
45	.002141	*330634	45	003434	535863	45	005031	•701696
46	002160	*334483	46	003459	*538904	46	*005061	1704208
47 48	*002179 *002198	*388316 *342133	47	'003483 '003507	541933 544953	47	005090	706713
49	-002198	342133	48	003501	547961	48 49	*005119 *005149	·709210 ·711700
50	002237	349716	50	002556	550961	50	005178	·714184
51	-002257	*353482	51	'003581	555948	51	'005208	.716658
52	.002276	357233	52	*003605	*556927	52	*005238	•719128
53	002296	360967	53	'003630	559895	53	*005267	-721589
54	*002316 *002336	364687	54	1003655	*562852	54	*005297	*724044
55 56	002355	·368393 ·372076	55 56	*003680 *003705	*565800 *568737	55 56	005827	*726492 *728934
57	002375	375746	57	003730	571665	57	1.05337	731367
58	002396	-379403	58	003755	*574582	58	005417	·733796
59	*002416	*883043	59	'003780	577492	59	.005448	-736217
60	*002436	386669	60	'003805	•580389	60	.005478	738630

	DATERAL DECENTS: TIV											
	_ 4	3 DEGR	EES.	-	4 DEGR	EES.		5 DEGRE	ES.			
-	Min.	Nat. No.	lo, r thm.	Min.	Na , No	Log. rt .	Min.	Nat. No.	Log rithm.			
	0	0.301372	7.137464	0	0.002442	7.387728	0	0.003820	7.592045			
	$\frac{1}{2}$	.001388	142281	1	. 002462	391346	1	*003845	•584946			
	2	•301403	147073	2 3	*002483	*894951 *893541	2 3	·003871 ·003897	•587934 •590715			
	3 4	*301419 *301434	151841 156577	4	*002508 *002524	4,2114	4	003923	593586			
	5	001459	-161290	5	002545	405676	5	.003949	•596446			
	6	*001465	165978	6	.002566	409221	6	.003975	•599301			
-	7	001481	170642	7	002587	412751	8	*004001	*602144			
1	8 9	*001497 *001513	175279 179893	8 9	·002608 ·002629	*416268 *419772	9	·004027 ·004053	*604979 *607805			
	10	. 001519	- 184483	10	002650	423261	10	004080	610620			
	11	.001545	·189048	11	.002671	*426736	11	.004107	*613427			
	12	001562	193590	12	.002693	•430197	12	004138	*616225			
1	18 14	*001578	·198107 ·202602	13	·002714 ·002736	*433645 *437079	13 14	*004159 *004186	·619013 ·621704			
	15	· 001594 · 001611	202002	15	002757	440499	15	*004213	624566			
	16	001628	211523	16	.002779	•443907	16	.004240	627327			
	-17	. 001644	215951	17	*002301	.447302	17	.004267	*630183			
	18	.001661	220853	18	*002823	450682	18	*304294	632827			
	19	001678	·224736 ·229095	19 20	*002845 *002867	·454051 ·457405	19	*004021 *004348	*635564 *638293			
	21	001093	233435	21	*002889	460747	21	•004375	*641013			
1	22	.001729	-237750	22	*002911	464077	22	.004403	*643724			
	23.	*001746	242047	23	*002934	•467393	23	·004430	646426			
	24	.001763	246320	24	*002956	470699	24 25	*004458	649102			
	25 26	*001781 *001798	·250575 ·254806	·25 26	*002978 *003001	·473991 ·477210	26	·004485 ·004513	·651808 ·654488			
	27	301816	259020	27	003024	480538	27	004541	657158			
	.28	*001833	.263211	28	*003046	483793	28	*004569	·659S20			
	29	*001851	267385	29	.003069	·487036	29	•004597	*662474			
	30 31	*001869 **001887	·271536 ·275671	30 31	·008092 ·003115	·490267 ·493488	30 31	*004625 *004653	·665120 ·667759			
	32	001001	279783	82	003138	496694	32	·0046S1	·670388			
	33	*001928	293377	33	.003161	499894	33	.004710	.673013			
	34	*001941	- 287951	34	.003185	503075	34	.004738	.675627			
	85 36	*001959	292006	-35 36	*003208	506248	35	·004767	*678233			
	37	*001977 - 001996	*296045 *300062	37	*003232 *003255	*509409 *512558	36	·004795 ·004824	*680837 *683424			
	38	002014	*304064	38	003279	515697	38	*004S53	·686009			
	39	*002032	*308044	39	*003302	*518823	39	·004882	*688585			
	40	*002051	312009	40	. *003326	521940	40	*304911	*691154			
	41 42	*002070 *002089	*315954 *319383	$\frac{41}{42}$	*003374	*525045 *528140	41 42	*004940 *004969	*693714 *696269			
	43	002108	323793	43	. 003398	531223	43	·004909	698814			
	44	*002127	327688	44	*003422	*534296	44	·005028	·701354			
	45	'002146	*331565	45	.003446	537357	45	.005057	·708887			
	46	*002165 *002184	*835422	46	·003471 ·003495	540409 543448	46	*005086 *005116	*706411			
	48	00218	*843089	47 48	*003519	546479	47 48	*305146	·708929 ·711439			
	49	.002223	-346896	49	*003544	549497	49	.005175	.718942			
	50	*002242	·3506S9	50	*003569	552508	50	*005205	.716439			
	51	002262	*354463	51	*003593	*555506	51	005235	•718926			
	52 53	*002281 *002801	*358223 *361965	52 53	*003618 *003643	553496 561474	52 53	*005265 *005295	·721409 ·723883			
	54	002301	365694	54	·003668	551442	54	·005325	·726351			
	55	002341	*369406	55	.003693	*567401	55	-005856	·72SS12			
	56	002361	373100	56	003718	•570349	56	·0053S6	*731267			
	57 58	*002381 *002401	*876779 *880445	57	*003744 *003769	*573288	57	*005416	•738718 •786155			
	59	002401	£81093	59	003794	*576216 *579137	58 59	·005417 ·005478	7885£9			
-	60	002442	387728	60	003820	582045	60	.005508	·711616			
-							!					

1		6 DEGR	EES.		7 DEGR	EES.	1	8 DEGR	EES.
M	lin.	Nat. No.	Logarithm,	Min	Nat. No.	Logarithm.	Min.	Nat No.	Logarithm.
T	0	0.005478	7.738630	0	0.007454	7.872380	0	0.009732	7-988199
10	1	.005509	.741038	1	·0074S9	·874444	1	.009772	.990003
	2 3	.005539	•743438	2	007525	876502	2	*009803	•991804
	4	*005570 *005600	·745831 ·748220	3 4	·007561 ·007596	*878555 *880603	3 4	·009854 ·009894	993601
	5	005631	750601	5	007632	*882647	5	009935	997185
	6	.005662	.752974	6	007663	·8S46S6	6	0009976	993972
	67	.005693	•755342	7	-007704	*886719	7	.010017	8.000754
	8 9	.005724	.757704	6 7 8 9	.007740	·SSS749	8	.010058	*002532
١.		005755	•760057	9	.007776	890773	9	.010099	*004307
	0	.005786 .005818	·762496 ·764749	10 11	*007813 *007849	*892793 *894808	10 11	*010141 *010181	*006079 *007847
	2	005849	•767084	12	007885	895818	12	010131	001341
Î	3	.005880	•769413	13	.007922	*898824	13	.010265	011371
	4	.005912	·771738	14	.007958	900825	14	.010307	013128
	5	*005944	·774055	15	007995	902821	15	.010348	014883
	6	005975	. 776364	16	008032	934813	16	.010390	*016632
1 1		*006007 *006039	·778671 ·780968	17 18	·008069 ·008106	-906800 -908783	17	·010432 ·010474	*018379 *020121
1		.006059	783261	19	·008143	910761	19	010516	020121
2		006103	·785547	20	008180	912734	20	010558	023597
2	1	.006135	·787829	21	.008217	914704	21	.010600	025329
2		.006167	. 790102	22	.008254	916670	22	.010643	.027058
2		.006200	-792369	23	*008291	918623	23	010685	028783
2		*006232	·794633	24 25	·008329	920584	24 25	010728	030505
2		*006265 *006297	·796891 ·799140	26	·008366 ·008404	·922536 ·924483	26	·010770 ·010813	*032223 *033939
2	7	006330	·8013S5	27	008412	926425	27	010856	035651
2	3	.006362	803624	28	008479	·92S363	28	010898	*037359
2	9	.006395	*805859	29	·00S517	930297	29	010941	.039064
3		006428	808086	30	·00S555	932227	30	010984	*040766
3		*006461	810307	31	008593	934152	31	011027	042465
35		006494	·812524 ·814734	32 33	-008631 -008669	•936074 •937990	32 33	·011070 ·011113	*044159 *045850
3		006560	816939	34	008708	939903	34	011157	047539
3		.006594	819139	35	-008746	941811	35	011200	*049225
3		.006627	·821332	36	:0CS784	943715	36	.011243	*050906
3		.006661	·S23521	37	008823	945615	37	011287	052584
33		006694	·925704	38	008862	947511	38	011331	*054260
33		006728	*\$27881 *830052	39 40	·008930 ·008939	·949403 ·951290	39	·011374 ·011418	*(55931 *057601
4		006795	·S32218	41	008978	953173	41	011462	059266
4:	2	.006829	·834379	42	000017	955( 52	42	.011506	·06092S
45	3	.006863	·S36535	43	009056	956927	43	.011550	062588
4		006897	*S386S5	44	009095	958799	44	011594	*064243
4		006932	*840830	45	009134	960666	45	011638	065896
40		·006966 ·007000	·842969 ·845115	46	*009173 *009213	964388	46	·011682 ·011727	·067546 ·069192
49		.007034	847232	48	009213	966243	48	011772	·070836
49		-007069	·S49356	49	009292	-968094	49	.011816	.072476
50		.007104	·851475	50	.009331	969842	50	011860	.074113
51		007138	853589	51	*009371	971784	51	011905	075747
59		007173	·S55697	52	000411	·973624 ·975459	52	011950	·077378 ·079007
59 54		·007208 ·007243	·S57800 ·S59893	53 54	*009450 *009491	977291	54	·011995 ·012049	080631
56		007278	·861991	55	000431	979118	55	012085	·0S2253
56		007313	·864079	56	000001	980942	56	012130	083872
57		.007348	·866162	57	.009611	982762	57	012175	085488
58		.007383	·868240	58	*009351	934578	58	012220	087100
59		067418	·S70312	59	*0000001	936390	59	012266	088710
6	1	007454	872380	60	0009782	938199	60	012311	*090316
			- 11			- 11			

	6 DEGR	EES.		7 DEGR	EES.		8 DEGR	EES.
Min.	Nat. No.	Logarithm.	Min	Nat. No.	Logarithm,	Mm.	Nat No.	Logarithm.
0	0.005508	7.741016	0	0.007510	7.875628	0	0.009828	7.992447
1 2	*005589	•743437	$\frac{1}{2}$	·007546 ·007581	877768 879782	1 2	·009873 ·009910	994268
3	*005570 *005601	·745850 ·748257	3	007618	881851	3	009910	·996087 ·997902
4	005632	•750659	4	007654	883915	4	003302	999715
5	.005663	753054	5	.007691	885974	5	.010035	8.001521
6	.005694	.755440	6	.007727	888929	6	.010077	.003326
6 7 8 9	-005726	757822	7	007764	890078	7	010119	.005126
8	*005757 *005788	·760197 ·762564	8 9	·007801 ·007837	*892124 *894163	8 9	010160	006921
10	005133	764926	10	007874	896199	10	616245	·008716 ·010505
11	005852	·767283	11	007911	*898230	11	016287	-012292
12	*005888	•769632	12	·007948	900256	12	010329	.014074
13	.005915	·771974	13	•007985	902278	13	010372	015852
14	•005947	•774313	14 15	-008022 -008059	•904295 •906307	14	*010414	017627
15 16	·005979 ·006011	·776644 ·778967	16	008097	908315	15	·010457 ·010499	·019401 ·021148
17	006043	781288	17	008134	910518	17	010542	021140
18	-006076	·783599	18	-008172	912318	18	-01(585	.024694
19	.006108	·785906	19	068269	914312	19	.010628	.026452
20	*006141	788206	20	008247	916301	20	010671	·(28207
21 22	·006178 ·006206	·790502	$\frac{21}{22}$	·008285 ·008328	·918287 ·920270	21	010714	029957
23	000200	·792789 ·795070	23	008361	920210	23	·016757 ·016860	·031705 ·033449
24	000230	797348	24	·068399	924216	24	010844	035189
25	.006304	·799620	25	-008437	926185	25	-01(887	·C3C926
26	.006337	·801SS3	26	008475	928148	. 26	*01(931	·C\$8661
27	.006370	*804143	27	•008513	930107	27	01(975	.040391
28 29	*006403 *006436	*806396	28 29	-0€8552 -0€8590	·932061 ·934012	28 29	011018	*042118 *042842
30	000450	:808645 :810887	30	008629	935958	30	-0111062	045563
31	.006508	813122	31	-0(8668	937900	31	011150	·C47281
32	.006537	*815354	32	-008706	939839	32	.011194	·C48994
33	.006570	817578	33	-008745	941771	33	011238	.050704
34	*006604	*819798	34	008784	943761	34	011282	*052412
35 36	·006638 ·006671	*822012 *824220	35 36	·008823 ·008862	·945626 ·947547	35	·011326 ·011371	·055817
37	006705	826423	37	-008901	949464	37	011416	057514
38	.006739	828621	38	-068941	951377	38	.011461	059209
39 .	.006773	*830813	39	-008980	953286	39	.011506	.060899
40	.006898	*832993	40	009020	955190	40	.011550	062588
41 42	·006842 ·006876	*835179	41 42	-009059 -009099	·957090 ·958986	41 42	·011595 ·011640	·064278 ·065954
48	000510	*837355 *839526	43	009139	966878	43	011685	667633
44	006945	841691	44	-009178	962767	44	011730	-009308
45	.006980	·843851	45	-009218	964651	45	.011776	.07( 980
46	-007015	·846005	46	009258	966531	46	011821	.072650
47	*907049	*848155	47	·009298 ·009339	968408	47	011866	074815
48	*007084 *007119	·859298 ·852437	48 49	009379	·970280 ·972148	48 49	·011912 ·011957	·075979 ·077688
50	007154	854571	50	009419	974013	50	0112003	079295
51	007189	856700	51	.009460	975873	51	012049	-08(949
52	007225	*858823	52	.009500	977730	52	012095	·C82599
53	.007260	*860942	58	009541	979583	53	012140	·084248
54 55	*007295 *007331	863055	54 55	·009581 ·009622	981432	54	·012187 ·012232	085892 087534
56	007367	·865163 ·867267	56	009663	·983277 ·985119	55 56	012232	(89172
57	.307402	869365	57	009704	986956	57	012325	(9(808
58	007438	·ST1458	58	009745	.988790	58	012372	(92440
59	.007474	873546	59	-009786	990619	59	012418	•(94060
60	.007510	875628	60	009828	992446	60	012465	·( 956 <b>96</b>
		1				1		

	9 DEGRI	EES.		10 DEGRI	EES.	11 DEGREES.			
Min.	Nat No	Logarithm	Min	Nat. No.	Logarithm.	Min.	Nat. No	Logarithm.	
0	0.012311	8.090316	0	0.015192	8.181622	0	0.018373	8.264176	
1	.012357	.091920	1	*015242	183065	1	018428	265486	
2	*012403	093521	2	015293	184595	2	:018484	- 266796	
3	*012448	095119	3	015349	185943	3	018541	268133	
5	·012494 ·012540	·093714 ·098306	4 5	015395	187378 188811	5	*018596 *018651	-209407 -270711	
	012586	099894	6	·015446 ·015497	190242	6	018707	272012	
6	012632	10148)	7	015548	191671	7	018762	273298	
8	*312678	103064	8	*015599	193097	8	-018819	2746:8	
9	-012724	104644	9	015650	194520	9	·018876	2759 4	
10	012770	106221	10	*015701	195942	10	.018932	277197	
11	012817	107796	11	015752	197361	11 -	-018988	278487	
12	012864	109367	12	*015804	198778	12	019045	.279777	
13	.012910	110936	13	.015856	200192	13	.019101	·2S1065	
14 15	·012957 ·013003	112501 114065	14	0159.8	201604	14	·019158 ·019215	·282350 ·283634	
16	·013003	115625	15 16	*015959 *016011	·203014 ·204421	15 16	019215	·253034 ·284915	
17	013097	117182	17	016063	204421	17	019328	286194	
18	013144	118737	18	016115	207229	18	019385	287474	
19	-013191	120238	19	*016167	-208639	19	019442	288749	
20	013238	121338	20	*016219	210028	20	•019499	-290623	
21	.013286	123334	21	016271	-211424	21	.019557	291296	
22	.013333	124927	22	*016323	212827	22	-019614	292566	
23	•013380	126468	23	-016876	214209	23	•019671	293835	
$\frac{24}{25}$	·013428 ·013475	128306	24	*016428	215598	24 25	019729	295101	
26	013523	129542 131074	25 26	016481	·216986 ·218371	26	·019786 ·019844	296366 297629	
27	013570	132303	27	016586	219753	27	019902	-298889	
28	-013618	154131	28	*016639	221134	28	019959	300149	
29	-013366	135635	29	016692	222502	29	- 020017	-300466	
30	013714	137176	30	'016745	223887	30	.020075	302661	
31	.013762	138695	31	.016798	225261	31	•020133	303916	
32	013810	140212	32	016851	226633	32	020191	305167	
33 34	·013859 ·013907	·141726 ·143236	33 34	016958	·22S002 ·229370	33 34	*020250 *020308	306417	
35	013955	145250	35	017011	230734	35	-020366	307666	
36	014003	146251	36	017065	232097	36	020425	310156	
37	014052	147754	37	017118	233458	37	-020483	311399	
38	•014101	·149255	33	017171	234817	38	·020541	312630	
39	014149	153752	39	017225	236173	89	.020600	31388	
40	014193	152248	4.0	017279	237528	49	•020659	315117	
41 42	·014247 ·014296	153741	41	*017333	238880	41	-020718	316352	
42	*014295	·155231 ·156719	42	*017887 *017441	*240230 *241578	42	·020777 ·020836	*317587 *318818	
44	014343	158233	41	017495	241018	44	020895	\$20049	
45	014443	159686	45	017550	244267	45	020954	\$21278	
46	.014493	161165	46	017604	245609	46	-021014	-322508	
47	.014542	162643	47	017658	246949	47	.021073	323730	
48	014592	164118	48	*017712	248286	48	021133	324958	
49	014641	165589	49	017767	249621	49	021192	22617-	
5:	014691	16706)	50	017822	250955	50	·021252 ·021311	32789	
51 52	014741	168527 169992	51 52	*017877 *017931	·252286 ·258615	51 52	021311	-328613 -329829	
53	014791	171454	53	017986	254942	53	021371	33104	
54	014891	172914	54	018041	256267	54	021491	33225	
55	014941	174372	55	318096	257591	55	•021551	38346	
56	014991	175827	56	013151	258911	56	-021611	83467	
57	•015041	177279	57	*318206	260230	57	.021671	-33588	
58	-015091	178789	58	018262	261548	58	*621732	837(.9:	
59	015141	187177	59	313317	262862	59	021792	-83829	
60	015192	181623	60	018373	264176	60	021852	35949	

1	DATEMAL SECRETS.										
	9 DEGRI	EES.		10 DEGR	EES.		11 DEGRI	EES.			
Min.	Nat. No.	Loga: ithm.	Min.	Nat No.	Logarithm.	Min.	Nat. No.	Logarithm			
0.0	0.012465	8.095696	0	0.615426	8.188271	0	0.018717	8-272229			
1	•012512	097320	1	•015478	189732	1	•018774	273564			
2 3	·012559 ·012605	·093941 ·100559	2 3	··015580 ··015583	·191198 ·192658	2 3	·018832 ·018891	·274899 ·276260			
4	012652	100000	4	·015636	194116	4	·018948	277559			
5	-012699	103787	5	015688	195571	5	-019006	278888			
6	-012746	105395	6	015749	197025	- 6	·019064	280213			
7	•012794	107001	7	.015793	193476	7	•019122	281527			
8 9	-012841 -012889	·108605 ·110206	8	·015846 ·015899	·199925 ·201371	8 9	·019180 ·019289	·282859 ·284180			
10	-012936	111804	10	015353	202815	10	-019297	285494			
11	012984	113399	11	.016005	204257	11	.019356	286813			
12	·013031	·114990	12	·016058	205697	12	019415	·288128			
13	•013079	- 116579	13	.016111	207133	13	·019473	289441			
14	·013127 ·013175	118165 119749	14 15	·016164 ·016218	-208568 -210001	14 15	·019582 ·019591	·290751 ·292060			
16	013113	119149	16	010210	210001	16	019650	293366			
17	.013271	122938	17	.016325	212859	17	-019709	294670			
18	.013319	·1244S3	18	·016379	214285	18	-019769	295976			
19	.013367	126055	19	.016433	215718	19	-019828	297276			
20	.013416	127626	20	.016486	217139	20	•019837	298575			
21 22	·013464 ·018513	129193 130756	21 22	·016540 ·016594	·218549 ·219965	21 22	·019947 ·020006	·299874 ·301169			
23	013561	132318	23	-016649	219905	23	·020066	302463			
24	•913610	133877	24	.016703	-222792	24	020126	- 303755			
25	013659	135434	25	·016757	-224203	25	-020186	*305045			
26	-013708	136987	26	•016811	225612	26	.020246	*306334			
27	013757	138537	27	•016866	-227017	27	020306	307619			
28 29	·013836 ·013856	140086 141631	28 29	·016920 ·016975	·228421 ·229922	28 29	·020366 ·020426	*308905 *310188			
30	-013905	143174	30	017030	231221	30	020486	·811469			
31	.013954	144714	31	-017085	-232618	31	-020547	312749			
32	-014004	146252	32	017140	284014	32	-020608	314026			
33	•914054	147787	33	.017195	•235406	33	-020668	*315302			
34	014103	149318	34	-017259 -017805	-236798	34	·020729 ·020790	316576			
35 36	·014158 ·014208	150849 152876	35 36	-017369	·238185 ·239572	35 36	02:193	317848			
37	-014253	153900	37	017416	-24: 957	37	02.912	320387			
38	-014302	155423	38	*017472	242339	33	020973	321644			
39	•014353	156941	39	•017527	243719	39	021034	322920			
40	-014403	158458	40	017582	245093	40	021095	324183			
41 42	·014453 ·014503	159973	41 42	·017638 ·017695	246474 247848	41 42	021156	*825 <del>111</del> *826705			
43	014554	162094	43	017751	241848	43	021218	320103			
44	-014605	-164500	44	0178 7	25,1589	44	-021341	329220			
45	.014655	166004	45	017803	251956	45	+021403	330475			
46	•014706	167505	46	017919	253822	46	021465	931728			
47	-014757	169005	47	017975	254686	47	021527	332979			
48	·0148)8 ·014859	170502 171995	49	·018;32	256047 257407	48	021589	·334229 ·335477			
50	014939	173488	50	018145	258765	50	021031	386724			
51	•614961	174977	51	.018202	260120	51	-021776	-837969			
52	-015013	173464	52	018258	261473	52	-021838	339211			
53	015064	177948	53	018315	262825	53	021930	340453			
54 55	·015115 ·015167	179430	54 55	·018372 ·018430	·264174 ·265522	54 55	-021963 -022026	·341691 ·342931			
56	015218	182387	56	018487	266867	56	-022020	344167			
57	015270	- 183361	57	018544	268210	57	022151	345400			
58	•015322	185343	58	018601	269552	58	022214	346634			
59	•015374	- 18383	59	018659	270891	59	022277	847865			
60	-015426	188271	60	018717	272229	60	023341	*349095			
-			11	1				-			

:	12 DEGR	EES.	1	S'DEGRI	EES.	1	4 DEGRI	EES.
Min.	Nat. No.	Logari hr.	Nin.	Nat No	Logarithm.	Min.	Nat. No.	Logarithm
0	0.021852	8.559499	0	0.025630	8.408747	0	0.629704	8.472819
1	021913	·340700	1	025695	•4(9856	1	029775	·473S4S
2 -	.021974	341900	2	(25761	41(962	2 3	*029845	474874
3	*022034	*343(97	3 4	·025827 ·025892	·412067 ·413171	3 4	*029916 *029986	475899
4 5	·022095 ·022156	*344293 *345488	5	025958	414273	5	030057	·476925 ·477948
6	022217	346681	6	.026024	415274	6	.030127	478970
7	-022278	-347877	7	.026(90	416474	7	*030199	•479991
8	.022338	*349062	8	.026156	417573	8	.03(270	·4S1011
9	*022400	*350249	9	.026222	418669	9	*030341	·482029
10 11	*022461 *022528	*351435 *352620	10 11	·026288 ·026355	·419764 ·420858	10 11	*030412 *030483	·483046 ·484062
12	·022584	*355S02	12	·C26421	421951	12	*030555	484002
13	.022646	354984	13	26498	•423042	13	*030626	486091
14	-022707	*356163	14	*026564	424131	14	·C30.697	·487103
15	-022769	*357342	15	*026621	425219	15	*030709	488115
16	·022S31	*258518	16	(23687	*4263(9	16	(3.841	489125
17 18	*022892 -*022954	*859693 *360867	17 18	·026754 ·026821	*427893 *429477	17- 18	*(3: 912 *(3: 984	·490183 ·491141
19	-023016	362989	19	·026888	429560	19	·C31(56	•492148
20	-023079	*363208	20	*026955	480641	20	631128	493153
21	-023141	364376	21	*027022	*481722	21	*031200	494157
22	.023203	*865543	22	·U270S9	*432800	22	·C31272	495160
23	023266	366719	23	*027157	433877	23	*081845	496162
24 25	·023328 ·023390	·367872 ·369035	24 25	127224 1027292	*434954 *436029	24 25	*031417 *031489	·497162 ·498162
26	023453	370195	26	027359	430023	26	(31562	499160
27	023515	*371354	27	027427	438174	27	031634	500158
28	·023578	372511	28	*027494	439244	23	.031707	-501153
29	023641	373667	29	.027562	440314	29	.031780	502148
30	023704	374822	30	*027630	*441382	30	*031852	•503142
32	·028767 ·023830	*375974 *327125	31 32	*027693 *027766	·442449 ·443514	31 32	*081925 *081998	·504134 ·505125
33	·023S93	378275	33	027834	444578	33	*032071	506115
34	-023956	.379423	34	·027992	•445641	34	.032144	-507105
35	•024320	*380569	35	*027971	446762	35	*032218	·50SC93
36	024083	*381715	36	*028039	447762	36	*032291	•509079
37 38	·024147 ·024210	*382858 *384001	37 38	·028107 ·028176	*448821 *449878	37 38	*032364 *032438	*510065 *511049
39	-024279	*385141	39	028110	45 935	39	032511	012032
40	-024338	386279	40	028313	451990	40	032585	·513014
41	.024402	*387417	41	·02S3S2	*453043	41	.032659	.513996
42	024465	*388553	42	028451	454996	42	032732	•514976
43	·024529 ·024594	388687	43	028520	455147	43 44	*032806 *032880	515955
44 45	024558	*393S21 *391952	44 45	*02S5S9 *02S65S	*456196 *457244	44 45	032580	•516933 •517909
46	024722	-393082	46	028727	458291	46	033028	518884
47	024786	.394210	47	028796	•459338	47	*033102	·51985S
48	•024851	*395333	48	·028866	*460382	48	033177	-520832
-49	•024915	*396463	49	028935	*461425	49	033251	•521804
50 51	·024930 ·025044	*397587 *398710	50	°029005 °029074	*462468 *463508	50 51	*033325 *033400	*522775 *523745
52	025944	395710	52	029144	464547	52	033475	524714
53	025174	400951	53	.029214	465586	53	033549	•525681
54	•025489	402069	54	-029233	466623	54	*033624	-526648
55	025304	403185	55	*029353	467659	55	033699	527614
56	025369	404300	56	029423	468693	56	·033774 ·033849	*52\$578 *529541
57 58	·025434 ·025499	·405414 ·406527	57	029493	-469726 -470759	58	033924	530504
59	025564	407637	59	029634	471789	59	033999	531465
60		408747	60	029704	472819	60	034074	532425

	12 DEGR	EES.		13 DEGR	EES.	14 DEGREES.			
Min	Nat. No.	Loga, ichm.	Mir.	Nat. No	Logari hm.	Min.	Nat. No.	Logarithm.	
0	0.022341	8.349,195	0	0.026304	8.420023	0	0.030614	8.485915	
11	.0224)4	•350322	1	026373	•421161	0	·030688	486975	
2	.022467	•351549	2	026442	•422295	2	.030763	488033	
3	022531	•352773	3	026511	423431	3	*030838	·489090	
4	.022594	*353996	.4	·0265S1	•424564	4	.030913	•490147	
5	022658	•355218	5	026650	*425695	5	-030983	•491202	
6	022722	·356433	6	026720	426826	6 7	*031064	492256	
7 8	022786 022349	*357662 *358374	7 8	026789	427955	8	:031139 :031215	•493308 •494360	
9	022913	360088	9	026928	•429084 •430209	9	031213	495410	
10	022977	*361301	10	026998	431334	10	·081366	•496459	
11	023042	*362513	11	027068	432457	11	.031442	497507	
12	023106	*363723	12	027138	433580	12	•031518	498555	
13	023170	-364932	13	.027208	434700	13	*031594	·499600	
14	023235	·366138	14	.027278	435819	14	.031670	*500644	
15	.023299	367345	15	*027849	•436937	15	*031746	501683	
16	023364	*368548	16	.027419	·43S055	16	.031822	•502730	
17	023429	•369751	17	*027490	439170	17	.031899	503770	
18	023994	•370952	18	.027560	·4402S4	13	•031975	•504810	
19	*023559	•372152	19	*027631	•441397	19	•032052	•505849	
2)	023624	•373343	2)	027702	*442508	20 21	·032128 ·032205	500887	
22	023059	374544	21 22	*027773	*443619	21 22	032282	507928	
23	023820	·375739 ·376942	23	*027844 *027915	·444727 ·445834	23	032359	*508958 *509990	
21	023885	378123	24	027986	•446941	24	032436	511025	
25	023950	379314	25	028057	•448046	25	•032513	•512058	
26	024016	380502	26	028129	•449149	26	.032590	•513089	
27	024082	*331639	27	.028200	450252	27	·032668	•514119	
23	'024148	·3S2S74	23	028272	·451352	23	.032745	•515140	
29	024214	*384058	29	:028343	452452	29	.032823	.516174	
30	024280	·3S5240	30	*028415	*453551	30	.032900	517200	
31	024346	386421	31	028487	·454648	31	032978	*51822	
82	024412	387600	32	*028559	455743	32	033056	519249	
33	024478	388778	33	*028631	456838	33	033134	520272	
31 35	024544	389954	34 35	*028703	457931	34 35	·033212 ·033290	•521294 •522315	
36	024678	·891128 ·892302	36	*028775   *028248 *	459023 460118 -	35	-033368	523334	
37	024744	393474	37	*028920	461203	37	•033447	•524350	
38	024811	394645	33	028993	462290	38	-033525	525370	
39	024878	395813	39	029365	463378	39	033604	•526386	
40	024945	396979	40	*029138	464464	40	.033682	•527401	
41	025012	*898146	41	029211	•465547	41	033761	•528410	
42	025079	*399310	42	029284	•466631	42	.033340	•529429	
43	025146	*490473	43	*029357	467713	43	-033919	•530441	
41	025214	·401635	44	.029430	•468793	44	.033998	531453	
45	025281	•402795	45	.029593	469872	45	.034077	•532463	
46	025348	403954	45	.029577	470950	46	034156	•533470	
47	025416	405110	47	*029650	472023	47	*034236	534478	
49	*025484	*406257	48	029724	479103	48	034315	535485	
50	*025552 *025620	407421 408573	49 57	·029797 ·029871	·474177 ·475251	49 50	·034395 ·034474	536490 537495	
51	025688	408373	51	029945	476322	51	034554	538493	
52	025755	·410S75	52	020019	477392	52	034634	*539501	
53	025824	412024	53	030098	478462	53	·034714	•540501	
54	025892	•413171	54	:030167	479031	54	034794	•541502	
55	025961	414316	55	.030241	480593	55	.034874	*542501	
56	026029	·415460	56	.030315	481663	56	.034954	543499	
57	*026093	416603	57	.030390	482728	57	035035	.544496	
58	*026166	417745	53	.030464	483792	58	085115	*545493	
59 60	026235	418884	59	*030539 *030614	484853	59 60	*035195 *035276	•546487 •547481	
	*026304	420023	60		485915				

15 DEGREES.				16 DEGR	EES.	17 DEGREES.			
Min.	Nat. No.	Logarithm.	Min.	Nat, No.	Logarithm.	Min.	Nat No.	Logarithm	
0	0.034074	9.582425	0	0.038738	8.588140	0	0.043695	8.640434	
1	034150	•533334	1	.038818	•59938	1	*04378)	641279	
2 3	034225	•534342	2	*038899	- 599936	3	*043865	642123	
3	034300	•535299	3 4	*038979	593833	4	*043951 *044036	642966	
<b>4</b> 5	*034376 *034452	·536255 ·537210	5	*039060 *039140	-591728 -592623	5	044121	·643809 ·644650	
6	034527	538163	6	039221	593517	6	044207	645491	
6 7 8	034603	•589116	7	.039301	594409	7	.044292	646330	
8	-034679	•540068	8	039382	.595301	8	*044378	647169	
9	034755	•541018	9	*039463	*596193	9	.044464	648008	
10	.034831	•541968	10	*039544	597083	10	*044550	648845	
11	034907	•542916	11	*039625	597971	11	044636	649682	
12 13	034983	•543863	12 13	039706	598859	12 13	·044722 ·044808	650517	
14	*035060 *035136	•544809 •545755	14	*039787 *039869	·599747 ·600633	14	044894	651352 652187	
15	035213	546699	15	039950	601518	15	044980	653020	
16	035289	547642	16	040032	602403	16	.045066	653852	
17	*035366	•548584	17	040113	*603286	17	.045158	654683	
18	*035443	549525	18	.040195	·604169	18	.045239	655514	
19	.035520	550466	19	*040276	605051	19	045326	656345	
20	.035596	.551405	2)	*040358	605931	23	045412	:657174	
$\frac{21}{22}$	*035673	552342	22	040440	606811	21	045499	658002	
23	*035750 *035827	553279 554215	23	·040522 ·040604	-607690 -608568	22 23	045586 045673	·659830 ·659657	
24	035935	555150	24	040686	-609445	24	045760	660485	
25	035982	556034	25	040768	610322	25	045847	661308	
26	.036059	-557017	26	040850	-611196	26	.045934	662132	
27	.036137	.557948	27	.040933	612071	27	.046021	662956	
28	036214	-553880	28	·041015	612945	23	.046109	663779	
29	*036292	559309	29	.041093	613817	29	046196	664601	
30. 31	036370	560738	30	041180	614689	30 31	046283	665422	
32	·036447 ·036525	561665	32	·041268 ·041846	·615569 ·616430	32	046370	·666242 ·667061	
33	036603	•563518	83	041428	617299	33	046546	667881	
34	036681	.564443	34	-041511	618167	34	.046633	668698	
35	036759	565366	35	*041594	619085	85	.046721	669516	
36	.036337	.566289	36	041678	619901	36	.046809	670333	
37	036916	567211	37	.041761	620766	37	.046897	671148	
38	036994	568132	38	041844	621631	38	046985	671963	
39 40	037072	569052	39 40	041927	622495	39 40	047073	672776	
41	037151	569971 570888	41	*042010 *042094	·623357 ·624220	41	·047162 ·047250	·673590 ·674403	
42	037308	571805	42	042178	625081	42	047339	675215	
43	037387	572721	43	042261	625941	43	047427	676025	
44	037466	573635	41	.042345	626800	44	*047516	676836	
45	*037545	574550	45	.042429	- 627659	45	.047604	-677646	
46	037624	575462	46	042513	628517	46	047693	678454	
47	.037703	*576374	47	042597	629373	47	047782	679262	
48	·037782 ·037861	*577285 *578194	48	·042681 ·042765	·630230 ·631085	48	047871	680069 680875	
50	037940	579103	50	042103	631939	50	043049	681681	
51	038020	580012	51	042933	- 632792	51	048138	682485	
52	-038100	580919	52	.043017	633645	52	.048227	683290	
53	038179	. 581825	53	.043102	634496	53	.048316	*684093	
54	038259	582730	54	.043186	·635347	54	.048406	684896	
55	038338	583634	55	.043271	636197	55	048495	685698	
56	038418	584537	56	043355	637046	56	048584	·686498	
57 58	038498	585439	57 58	043441	637895	57	·048674 ·048764	·687298 ·688098	
59	·038578 ·038658	*586341 *587241	59	·043525 ·043619	·638742 ·639588	59	048764	-688896	
60	038738	558140	60	043695	640434	60	048944	689694	

	EXTERNAL SECONIS. 421											
F	15 DEGR	EES.		16 DEGR	EES.		17 DEGR	EES.				
Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Logarithm.	Mm.	Nat No.	Logarithm.				
0	0.035276	8.547481	0	0.040299	3.605299	0	0.045692	8.659838				
1 2	.035357	548473	1	.040386	.606233	1	.045785	660721				
2	.035438	•549466	2	.040473	.607167	2	·C45878	.661604				
3	.035519	. 550457	3	.040560	608100	3	·045971	662486				
4	035600	551447	4	.040647	669032	4	046065	.663367				
5	035681	552436	5	*040735	*609963	5	046158	664247				
6	035762	553423	6 7	040822	610893	6 7	046252	665127				
9	·035843 ·035925	·554400 ·555396	8	·040909 ·040997	·611822 ·612750	8	·046345 ·046439	.666965 .666583				
4 5 6 7 8 9	036006	556381	9	041085	613679	9	·C46533	667761				
10	.036088	•557364	10	041172	614605	10	.046627	668637				
11	036170	558347	11	.041260	615530	11	.046721	669513				
12	036252	559328	12	.041348	616455	12	046815	.670387				
13	036334	560309	13	.041437	617380	13	.040910	671261				
14	.036416	561289	14	.041524	618362	14	·C47004	672135				
15	.036498	562267	15	.041613	619224	15	.047099	.673008				
16 17	036580	563245	16 17	041701	620146	-16 17	047193	673879				
18	·036662 ·036745	*564221 *565197	18	·041789 ·041878	·621066 ·621982	18	·047288 ·047383	·674749 ·675619				
19	036828	566172	19	041967	622905	19	047478	676490				
20	036910	567146	20	042055	623822	20	047573	.677358				
21	036993	568118	21	042144	624739	21	047668	678226				
22	.037076	569089	22	.042238	625655	22	047763	679093				
23	.037159	570060	23	.042322	626570	23	047859	679960				
24	037242	571030	24	.042412	627484	24	047954	680827				
25	037325	571999	25	*042501	628398	25	.048050	681690				
26 27	037408	572967	26	042590	629310	26	.048145	*682553				
28	037492	573937	27 28	*042680	630222	27	048241	683417				
29	·037575 ·037658	·574899 ·575863	29	·042770 ·042859	·631133 ·632043	29	·048337 ·048433	684280 685142				
30	037742	576827	30	042949	632952	30	.048529	686002				
31	037826	577790	31	.043039	633861	31	048625	686862				
32	.037910	.578752	32	043129	634768	32	.048722	687721				
33	.037994	579713	33	043219	635674	33	048818	688581				
34	038078	580673	34	043309	636580	34	048915	.689438				
35	.038162	581631	35	.043400	637486	35	.049011	€90296				
36 37	038246	582589	36 37	043490	638389	36	049108	691153				
38	·038331 ·038415	583547 584503	38	·043580 ·043671	639292 640195	38	*C49205 *049302	*692008 *692863				
39	038500	585458	39	043762	641696	39	049302	693717				
40	038585	586412	40	043853	641997	40	.049296	694571				
41	-038669	587365	41	043943	642899	41	·C49593	.695424				
42	038754	588318	42	.044035	643796	42	.049691	696276				
43	038839	589269	43	044126	644694	43	.049788	€97127				
44	038924	590219	44	044217	645591	44	·C49886	697978				
45 46	039009	591169	45	044309	646488	45	049983	·69S829				
47	-039095 -039181	592117	46 47	*044400	·647384 ·648272	46	·050081 ·050179	·699677				
48	039181	593075 594012	48	·044491 ·044583	649173	48	050179	·700526 ·701378				
49	039351	594958	49	044676	650076	49	.050376	702220				
50	.039437	595902	50	.044767	650958	50	.040474	703066				
51	.039523	*596846	51	.044859	651850	51	*050572	•708911				
52	.039603	.597789	52	.044951	652741	52	.050671	.704757				
53	039695	598731	53	•045043	653630	53	.050769	•705600				
54	039781	599672	54	045136	654520	54	050868	.706444				
55	039867	600612	55	045228	655408	55	050967	·707287				
56	·039953 ·049040	·601551 ·602489	56 57	·045321 ·045413	·656296 ·657183	56	·051066 ·051165	·708128 ·708969				
58	040126	603427	58	045418	658969	58	051264	709810				
59	040120	604263	59	045599	658953	59	051363	·710649				
60	040299	605299	60	045692	.659883	60	051462	.711489				

	18 DEGRI	EES.	1	DEGR.	EES.	20 DEGREES.		
Min.	Nat No	Loga ithm.	Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Logarithn
0	0.048944	8.689694	0	0.054481	8.736248	0	0.060308	8.78087
1	•040)33	690492	1	*054 • 76	•737003	1	•060407	·7810S
2	.049123	.691288	2	054671	·737758	2	060507	·7818
3	*049213	692084	3	054766	738510	3	.060606	78251
4 5	*049304 *049394	*692880 *692674	5	054861	739263 749014	5	*060706 *060806	·78323 ·78394
6	049484	*694467	6	·054956 ·055051	740766	6	060906	78465
7	049575	•695260	7	055146	741517	7	.061006	.78537
8	049365	-696052	8	₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹ ₹	742266	8	-061106	·78608
9	.049756	·696S43	8 9	055837	•743015	9	-061206	.78679
10	*049346	697633	10	055432	•743764	10	·061306	.78750
11	049937	*698423	11	055527	•744512	11	·061407	·78S21
12	050028	699213	12	*055623	•745259	12	.061507	78892
13	050119	700001	13	.055719	•746005	13	•061608	78963
1.1	*050210 *050301	·700788 ·701576	14	055815	•746752	14	·061708 ·061809	79034 79104
15 16	050392	701376	15 16	*055911 *056007	·747497 ·748241	15 16	·061909	:79104
17	·050382	703147	17	056103	•748945	17	•062010	79246
18	050574	•703931	18	056199	749728	18	062111	·79316
19	.050666	•704716	19	*056295	.750472	19	.062212	-79387
20	.050757	•705498	2)	056891	.751213	20	.062313	-79457
21	050849	•706232	21	*056483	751955	21	•062414	•79528
22	050941	·707063	22	656581	752096	22	•062515	79598
23	051032	707845	23	056681	•753436	23	·062617	-79669
24	051124	708624	24	*056777	754175	24	·062718 ·062820	79739
25 26	·051216 ·051308	·709404 ·710183	25 26	*056874 *056971	·754918 ·755652	25 26	-062921	79809 79879
27	051400	·710961	27	*057068	756390	27	002521	79949
28	051492	711739	23	057164	.757126	23	063124	80019
29	-051584	-712516	29	.057261	.757862	29	-063226	80089
30	051676	·713291	80	*057858	·758597	30	.063328	*80159
31	.051769	714067	31	*057456	•759333	31	•063430	80229
32	.051861	·714842	32	*057558	•760067	32	-063532	*80299
33	051953	715615	33	*057650	•760800	33	•063634	*80368
34 35	*052046	·716389 ·717162	34	057748	761534	34 35	-068736	·S0438
36	·052139 ·052232	717933	35 36	057845	·762266 ·762992	36	·063838 ·063940	*80508 *80577
37	052324	-718704	37	058040	763728	37	005345	80647
35	052417	•719474	38	058138	764459	38	•064145	-80716
39	052510	•720244	39	058236	-765189	39	.064248	·8078a
40	.052603	•721013	40	*058334	.765918	40	.064350	·S0855
41	-052697	·721782	41	*058432	.766647	41	•064458	·S0924
42	•052790	•722549	42	*058530	•767375	42	.064556	:80993
43	052883	•723316	43	058628	·768101	43	064659	-81062
44 45	052976	724082	44 45	*058726 *058824	768829	41	-064762 -064865	·S1131
46	·053970 ·053163	·724848 ·725613	46	058922	·769555 ·770279	45 46	·06496S	81200
47	055105	726377	47	059021	•771005	47	-065971	81333
48	053351	-727140	48	059119	771729	48	-065174	-81407
49	*053444	-727903	49	*059218	772453	49	.065278	S1470
50	.053538	·72S666	50	059316	773175	50	·0653S1	·S1545
51	053632	-729427	51	059415	•773897	51	•065485	81618
52	053726	•730183	52	059514	•774619	52	·065558	8168
53	*053820	·730947	53	059613	.775349	58	·065692	·81751 ·81819 ·81889
54 55	·053915 ·054009	·731706 ·732465	54 55	059712	776060	54 55	·065796 ·065890	.2100
56	054103	132400	56	059811	776780 777500	56	066003	81950
57	054103	•783981	57	039910	-778218	57	-366167	82324
58	054292	-784787	58	-360109	•778936	58	-066211	82098
59	054387	•735493	59	.060208	-779653	59	-066315	82161
60		-736243	60	.060308	.780871	60	.066420	*82229

	18 DEGRI	EES.	i	19 DEGR	EES.	20 DEGREES.			
Min.	Nat. No.	Logarithm.	Min.	Nat No.	Logarithm	Min.	Nat. No.	Logarithm	
0	0.051462	8.711489	0	0.057621	8.760578	0	0.064178	8.807885	
1	.051562	•712327	1	.057727	·761376	1	•664290	·808147	
2	.051661	·713164	2	057833	.762174	2	·064403	·808908	
3	•051761	•714001	3	057989	762971	3	•064511	*809669	
4	-051861	·714838 ·715673	4 5	*058045 *058152	·763767 ·764562	4 5	+064619 +064743	·810430 ·811190	
5 6	-051960 -052060	716508	6	058258	765358	6	-064856	8111950	
7	052161	•717842	7	058365	•766152	7	-064969	·S12708	
8.	-052261	•718175	8	058472	.766945	8	-665083	813465	
9	-052361	•719008	9	·05\$579	.767738	9	-06,197	·S14224	
10	-052461	•719839	10	.058686	•768531	10	-065310	·814981	
11	•052562	•720671	11	058793	769323	11	065424	*815737	
12 13	-052663 -052763	•721502 •722332	12	·058900 ·059007	·770114 ·770904	12 13	•065538 •065652	*816493 *817249	
14	-052864	723160	11 14	059301	-771695	14	065766	·S18903	
15	-052965	•72399.)	15	059222	·7724S4	15	·0658S1	·S1S75S	
16	-053066	-724817	16	•059330	.773272	16	-065995	·S19511	
17	-053167	•725644	17	.059438	·774960	17	•066110	*820265	
18	-053268	·726470	18	•059545	•774848	18	.066224	821018	
19	•053370	•727297	19	059654	•775636	19	-066329	*821769	
20	*053471	728122	20	•059762	776421	23	·066454	*822521	
$\begin{array}{c} 21 \\ 22 \end{array}$	-053573 -053675	·728947 ·729770	21 22	·059870 ·059978	·777207 ·777993	$\frac{21}{22}$	·066569 ·066684	*823272 *824023	
23	-053777	•730594	23	-060087	•778777	23	·066830	824778	
24	-053879	·731415	24	-060195	•779561	24	•066915	·S25523	
25	-053981	•732237	25	-060304	·780343	25	-067030	·S26271	
26	-054083	•733058	26	-060412	-781127	26	.067146	827019	
27	-054185	.733878	27	•060521	•781909	27	-067262	·S27767	
28	-054287	•734698	28	060630	782690	28	•067377	*828514	
29 30	·054390 ·054492	·735517 ·736335	29	·060740 ·060849	·783471 ·784252	29 30	·067493 ·067609	*829260	
31	054595	*737153	31	·060958	785031	31	-067726	*830007 *830753	
32	-054698	•737970	32	-061068	·785810	32	-067842	*831497	
33	-054801	-738785	33	-061177	·786588	33	-067958	*832242	
34	.054904	•734602	34	-061287	·787367	34	-06SU75	*832986	
35	-055007	•740417	35	•061397	·783144	35	-068191	.833720	
36	•055110	•741231	36	•061506	·7SS915	36	·068308	834472	
37 38	·055213 ·055317	·742044 ·742857	37	061616	·789396	37	068425	*885214	
39	055420	·743670	39	·061726 ·061837	·790472 ·791247	38	·068542 ·068669	- 835957 -836697	
40	(55524	•744482	40	•061947	•792021	40	-068775	*837439	
41	055628	•745293	41	-062058	792795	41	008893	·SSS17S	
42	-055732	•746103	42	•062168	-793568	42	-009311	·S38919	
43	-055836	·746912	43	.062279	•794340	43	-069129	*889658	
41	•055940	•747721	44	•062390	•795118	44	-069247	840397	
45	-056044	•748530	45	062501	•795884	45	•009364	*841135	
46 47	·056148 ·056253	·749338 ·750145	46	·062612 ·062723	·796654 ·797424	46	·069482 ·069600	841871	
48	+056357	750951	48	062834	798197	47	-069718	*842608 *843845	
49	056462	•751757	49	062945	-798964	49	069836	844082	
50	-056567	.752563	50	•063057	.799731	50	-069955	*844817	
51	.056672	753367	51	·063168	*800499	51	.070073	*845553	
52	-056777	.754171	52	·063280	.801267	52	070192	846287	
53	056882	•754973	53	068392	802033	53	070311	847021	
54 55	-056987	·755776	54	063504	*832799	54	070430	*847754	
56	·057092 ·057198	·756578 ·757380	55 56	063728	*803565 *804381	55	·070549 ·070668	*848487	
57	057804	758181	57	063840	804351	56	070787	·849220 ·849952	
58	057409	-758980	58	063953	805858	58	.070936	850682	
	-057515	.759779	59	-064965	806621	59	071025	851414	
59 60	057621	760578	100	OOTOO	000021	00	0 10 20	001414	

- 2	21 DEGREES.			22 DEGRI	EES.	23 DEGREES.			
Min.	Nat. No.	Logarithm.	Min.	Nat. No	Logarithm.	Min.	Nat. No.	Logarithm	
0	0.066420	8.822296	0	0.072816	8.862227	0	0.079498	8 900340	
1	*066524	·S22977	1	072925	*862877	1	-079609	900 902	
2	-066628	*823658	2	*073034	*863526	2	079723	901582	
3	.066733	824338	3	*073143	*864175	3	079837	902201	
4 5	*066837	·825018 ·825697	5	*073253 *073362	*864823 *865471	4 5	079951 080064	902821	
6	·066942 ·067047	\$26376	6	073471	866118	6	080178	·903439 ·904057	
7	067151	·S27054	7	073581	*866765	7	*080293	904673	
8	067256	·S27731	8	.073690	*867411	8	*080407	.905298	
9	-067361	-3284(9	9	.073800	-868056	9	-080521	905910	
10	.067466	*829085	10	.073910	-S68701	10	*080636	90652	
11	.067571	829760	11	.074020	·869346	11	080750	90714	
12	.067676	*S30436	12	.074130	·S69991	12	*080865	90775	
13	.067781	.831110	13	074239	*870634	13	*08(979	90837	
14	.067887	:831785	14	074349	-871277	14	*081(94	9.898	
15 16	·067992	.832459	15 16	074460	871920	15	081209	90960	
17	*068097 *068203	·833131 ·833304	17	·074570 ·074680	·872562 ·873203	16 17	*081324 *681489	91021	
18	-0683/9	834476	18	074790	873845	18	(81554	.91144	
19	068415	835148	. 19	074901	874486	19	€816€9	91205	
20	-068520	835819	20	.075011	-875126	20	081784	91266	
21	-068626	·S36489	21	.075122	875766	21	*081899	91327	
22	.068732	:837159	22	.075232	*876405	22	*082014	91389	
23	·06S838	*837829	23	.075343	877044	23	*082130	91450	
24	·068944	:838497	24	075454	·S776S2	24	*082245	91511	
25	•369 59	:839165	25	075565	·S7S320	25	082361	91572	
26	·009157	:809833	26	075676	878957	26	082476	91633	
27 28	*069263	:840501	27 23	*075787 *075898	*879594 *880230	27 23	082592	91695	
29	-069369 -069476	:841167 :841834	29	-076009	*880866	29	082824	91754	
30	069582	842499	30	·676121	881502	30	*082940	91876	
51	•369389	840165	31	076232	882137	31	*083056	91937	
52	-069796	*848829	32	-076343	*882770	32	083172	91997	
83	-909003	·S14493	. 33	*076455	*883405	33	*083288	92058	
37	070010	845157	34	.076566	*884038	34	*0.83404	92118	
35	•070117	. \$47.830	35	<b>176678</b>	*884670	35	083521	92179	
36	•070224	·S46483	36	£76790	-885303	36	083637	92240	
87	•070931	·S47145	37	.077002	*SS5935	37	083754	92300	
38 39	+ ·070433 - ·070545	*S478°5 *S4S467	38	•077014 •077125	*886567 *887197	38	*C83871 *C83987	92360 92421	
40	•070653	849127	40	-077237	887828	40	084104	92481	
41	.070760	\$49787	41	-077850	888458	41	*084221	92541	
42	-070867	*850446	42	-577562	1839088	42	*084337	92602	
43	.070975	851136	43	.077574	-889717	43	084454	92662	
41	· 071083	851764	41	·077687	·S90346	44	*084572	92722	
45	·371193	·S52422	45	077799	890974	45	*084689	92782	
46	•071293	*853079	46	077912	*891602	46	*084806	92842	
47	•371406	853735	47	·078024 ·078137	-892229 -892853	47	084923	92902	
48	·071514 ·071622	*854301 *855048	49	078250	893482	49	085158	93022	
50	071730	855703	50	078363	894108	50	085275	93082	
51	-071839	*S56358	51	078476	894734	51	085393	93142	
52	-071947	857012	52	078589	895358	52	085510	93201	
53	.072055	857665	53	078702	*895983	53	085628	93261	
54	.072164	:858319	54	·078S15	896607	54	085746	93321	
55	:072272	:358972	55	073928	897230	55	.085864	93381	
56	•072381	*859624	56	*079041	·S97853	56	085982	93440	
57	:07249.)	:860275	57	*079154	898475	57	086100	93500	
58 59	*072593 *072707	*86°027 *S61578	58 59	·079268 ·079382	*899097 *899719	58 59	*086218 *086336	93559	
93	072816	S62227	63	079495	900340	60	086454	93678	

	21 DEGR	EES.		22 DEGR	EES.	2	3 DEGRE	ES.
Min	Nat. No.	L.iga, ithm.	Min.	Nat. No.	Logari.bm.	Min.	Nat. No.	Logarithm.
0	0.071145	8.852144	. 0	0.078535	8.895061	0	0.086360	8.936314
1	071265	852374	1	078662	*895762	1	.086495	•936990
3	071384	*853603	2	078789	*895462	2 3	086629	•937663
4	·071504 ·071624	*854362 *855061	3 4	·078916 ·079343	·897102 ·897862	4	·086763 ·086898	•93S336 •939010
5	071744	855788	5	079170	898561	5	·087033	939682
6	.071865	*856516	6	079297	899259	6	·C87167	•940353
7	071935	.857243	7	.079425	-899957	7	*087302	941025
8	072105	857969	8	079553	•930655	8	087437	941697
9 10	*072226 *072347	858695	9	079680	991851	10	·087573	·942368 ·943040
11	072468	·859423 ·860144	10	*079838 *079938	·952343 ·952744	11	•087708 •087843	943709
12	072539	-850869	12	080065	903441	12	087979	944379
13	072710	861592	13	.080193	904135	13	·083115	945049
14	072831	*862316	14	*080321	•904830	14	·08S251	.945717
15	072952	-863039	15	080450	905525	15	·088387	946386
16	073074	853761	16	*083578	906218	16 .	*088522	947053
17 18	*073195 *073317	*864483 *865204	17 18	*080707 *081836	·906911 ·907605	-17. 18	*088659 *088795	·947722 ·948389
19	073439	865925	19	*080965	908298	19	•088932	949057
2)	.073531	*866646	2)	081094	•908990	20	-089368	-949723
21	.073683	*867365	21	.081223	959681	21	-089205	950389
22	*073805	868088	22	*081853	910372	22	•089342	•951054
23	*073927	838334	23	*081482	•911063	23	.089479	•951720
24 25	*074049 *074172	·869521 ·870239	24 25	*081612 *081742	·911754 ·912444	24 25	-089616 -089753	952384 953049
23	074294	870956	26	081872	913133	26	•089S91	953714
27	074117	871674	27	082302	913822	27	-090023	954377
28	074540	872390	28	*082132	914510	28	-090165	•955040
29	*074663	·873106	29	*082262	·915193	29	•090308	•955768
30	074787	873829	30	*082392	915887	30	•090441	•956366
31 32	*074910	874537	31	*082523	916574	31	•090579	957028
33	*075J33 *075156	·875251 ·875965	32 33	*082653 *082784	·917260 ·917947	32 33	•090717 •090855	*957689 *958350
34	07528)	876678	34	082915	918632	34	-093994	•959011
85	075404	*877391	35	*083946	919317	35	*091132	959672
36	075527	*878103	36	.083177	-920002	36	*691271	960333
37	*075651	878316	37	-083308	920687	37	•091410	96. 992
38 39	075775	*879527	38	*083440	921372	38	*091553	961652
40	.075930 .076324	*889239 *883949	39 40	*083570 *083702	·922054 ·922738	40	*091683 *091827	*962310 *962969
41	076143	*831659	41	083834	923421	41	·C91966	963627
42	076273	832368	42	.083966	.924104	42	•092105	964285
43	*076393	*883079	43	.084098	924786	43	•092245	964942
44	076522	*893787	44	*084230	•925467	44	-092385	965600
45 46	076647	*884495	45	·084362 ·084495	926148	45 46	*092524 *692664	966255
47	·076772 ·076397	*885203 *885909	46	084493	•926829 •927510	46	*092804	·966912 ·967567
48	077022	886616	48	084760	928190	48	-092944	968223
49	077148	*837323	49	*084893	928869	49	·0930S5	·96S878
50	.077273	*888.)29	50	.085025	•929548	50	•093225	969532
51	.077399	*883734	51	*085158	930227	51	-093366	.970187
52 53	077525	989439	52	*085291	930904	52 53	·093506	970840
54	*077659 *077776	*890143 *890848	53 54	*085425 *085558	·931583 ·932260	54	·093647 ·093788	971494 972147
55	.077903	*891551	55	085691	932636	55	093029	972890
56	.078029	892254	55	*085825	933613	56	.094070	973452
57	.078155	·S92956	57	*085958	•934288	57	*094212	.974104
58	.078232	*893659	58	.086992	934964	58	•094353	974755
59	.078108	894361	59	:086225	935631	59	*01495	975407
63	*078535	- *895061	60	*086360	936314	60	•094636	976057

!	24 DEGR	EES.		25 DEGI	EES.		26 DEGR	EES.
Min.	Nat. No.	Logarithm.	Min	Nat. No.	Logarithm.	Min,	Nat. No.	Logarithm.
0	0.086454	8.936787	0	0.093692	8.971768	0	0.101206	9.005206
1 2	*086573 *086695	937382 937975	1 2	*695815 *695959	·972273 ·972843	1 2	·101333 ·101461	*005753 *006300
3	*0S0810	983539	3	094061	973411	3	101588	*006843
4.	*086929	:939162	4	004184	978979	4	101716	007392
5	.087047	939754	5	.094308	974547	11 5	101845	- 007938
6	*087166	940346	6	094431	975115	6	101973	*008485
7	087286	•940938	7	*004555	975683	7	102100	009027
8 9	*087404 *087523	•941529 •942129	8 9	·094678 ·094802	976250 976816	8	1 2229 1 2357	009572 010116
10	·087642	942711	10	*(94925	97788)	10	1.2485	.010660
11	087761	•943300	11	(95)49	977948	11	1.2313	.011204
12	·0S7880	943889	12	.095173	978514	12	102743	.011746
13	.087999	•941478	13	.095297	979078	18	102870	012289
14	088119	945667	14	095421	979643	14	102999	012832
15 16	*088238 *088358	•945656 •946248	15 16	*095545 *095669	98.207 98)771	15 16	·103128 ·103256	·013373 ·013915
17		<b>→94683</b> 0	17	095703	981384	17	103230	013313
18	-088597	947418	18	·095918	981898	18	103514	014998
19	-088716	·94S004	19	.096042	932460	19	·103643	*015538
20	*088836	•948590	2)	*093163	933023	20	103772	.016078
21 22	088956	949175	21	*093291	933585	21	108901	016618
23	*089376   *089196	•949761 •950346	22 23	*096415 *096540	984146 984707	22   23	·104030 ·104159	·017157 ·017696
24	389316	950931	24	096665	985268	24	104288	018235
25	089437	951515	25	.09679.)	935829	25	104417	018773
26	*089557	·952098	26	.096914	986388	26	104547	.019311
27	*089677	·9526S1	27	*697049	986948	27	104676	·019S47
28	*089798	953265	28	097164	937507	23	104806	*020387
29	*089918	953848	29 30	097290	988336	29	104936	·020924 ·021460
31	*090039 *090159	·954429 ·955011	31	·097415 ·09754)	988624	30	·105066 ·105196	021400
32	093133	955592	32	097666	989741	32	105326	022533
33	.090401	956173	33	.097791	990298	33	105456	.023069
34	090522	956758	34	.097916	990854	34	105586	023603
35	*090643	957333	35	*098042	991411	35	105716	*024189
36	*090764	·957918 ·958492	36 37	*098168 *098293	991968	36	·105846 ·165977	·024673 ·025210
38	*090885 *091006	959971	38	093293	993079	37 38	106107	025742
39	-091127	959649	39	*098545	993634	39	106237	026275
40	.091249	960228	40	·098671	994189	40	100367	026808
41	*091370	960805	41	093797	994743	41	106498	.027342
42	*691492	961882	42	*098923	995297	42	106629	027874
43	*091618 *091735	961959 962535	43	·099:49 ·099175	995851	43	·106760 ·106890	·028406 ·028938
45	10911357	963111	45	099302	996404	45	107021	020330
46	091979	963657	46	099428	9975(9	46	107152	-030000
47	*092101	964262	47	099555	998061	47	107283	.030531
48	*092223	:964836	48	099681	998613	48	107414	031061
49	1092345	965412	49	-099308	999164	49	107545	031592
50	*092467 *092589	*965985 *966559	50 51	·099934 ·100061	999715	50 51	·107677 ·107808	*032121 *032651
52	692711	967131	52	100001	*000200	52	107940	033180
53	092834	-967705	53	100315	-001366	53	108071	.033709
54	*092356	·96S277	54	100442	-001916	54	108202	034237
55	*093078	968349	55	100570	2002465	55	108334	034765
56	093201	969421	56	100697	2003014	56	108466	·035293 ·035820
58	093324	·969991 ·970563	58	100824 100951	*003563 *004111	57 58	·108598 ·108730	036348
59	093569	971138	59	101079	004111	59	108862	036874
69	·\$93692	971703	60	111206	-005206	60	108994	037401
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	24 DEGE	REES.		25 DEGR	EES.		26 DEGR	EES.
Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Logarithm.	Mm.	Nat No.	Logarithm.
0	0.094636	8.976057	C	0.103378	9.014427	0	0.112602	9.051546
1	-094778	976708	1	103528	015056	1	112760	.052154
2	•094920	977357	2	103678	015685	2	112918	.052763
3	•095062	978008	3 4	103828	·016312 ·016939	3 4	113076	.053370
4 5	·095204 ·095347	978657	5	·103977 ·104128	010959	5	·113235 ·113393	*053979 *C54586
6	-095489	979954	6	104123	018194	6	113552	055195
7	-095632	980603	6 7	104429	018821	6 7	113710	.055799
8	-095775	981250	8	104580	019447	8	113869	.056406
9	-095918	. 981898	9	104730	.020072	9	·114628	.057012
10	-096061	932546	10	104881	.020696	10	·114187	057618
11 12	096204	933191	11	105032	021323	11	114347	058224
13	·096347 ·096490	933837	12 13	·105184 ·105835	·021948 ·022572	12	·114506 ·114666	·058828 ·059434
14	·096634	·984483 ·985129	14	105486	022312	14	114826	060039
15	-096777	985774	15	105638	023130	15	114985	060642
16	-096921	986417	16	105790	.024444	_16	115145	.061246
17	-097065	987062	17	105942	.025066	17	·115306	.061850
18	-097209	937707	18	106094	.025690	18	115466	.062454
19	-097353	988350	19	106246	.026312	19	115626	*063057
20 21	·097493	*988994	20	106398	026934	20	115787	.063660
22	·097642 ·097737	989636	21 22	106551 106703	·027556 ·028177	21 22	115948	·064262 ·064863
23	-097931	990279 990921	23	106856	028798	23	116269	065465
24	-098076	991563	24	107009	029419	24	116431	-066067
25	-098221	992235	25	107162	030040	25	116592	066667
26	·098366	992845	26	107315	*030659	26	116753	.067268
27	•098511	993486	27	107468	.031279	27	116915	·C67869
28	:098657	.994127	28	107621	.031898	28	·117077	·C68470
29	:098802 :098948	994766	29	107775	*032518	29	117289	069070
31	99094	·995406 ·996046	31	·107929 ·108082	·033136 ·033754	30 31	·117400 ·117562	·670269
32	(99240	996684	32	108236	034373	32	117725	070868
33	-099386	997323	33	108390	084991	33	117888	071467
34	.099532	997961	34	108544	.035607	34	118049	.072064
35	-099678	998599	35	108699	036225	35	·118212	.072663
36	·099824	.999236	36	108854	.036842	36	118375	.073261
37	099971	999873	37	109008	037459	¥ 87	118539	073861
39	·100118 ·100264	9.000510	38	109163	038074	38	118762	074456
40	100204	·001146 ·001783	39 40	·109318 ·109473	·028690	39 40	·118865 ·119028	·075053 ·075649
41	100558	001133	41	109473	039920	41	119028	076246
42	100706	.003053	42	109783	030520	42	119355	076842
43	100853	*003688	43	109939	.041150	43	119519	.077438
44	101000	.004322	44	110694	.041764	44	119683	.078033
45	101148	0.04957	45	110250	.042378	45	·119848	.078629
46	101296	.005591	46	110406	.042991	46	120012	079222
48	101444	*006224	47	110561	.043604	47	120176	079817
49	101331	·006857 ·007491	48	·110717 ·110874	·044217 ·044829	48	·120340 ·120505	·080412 ·081006
50	101885	008122	50	111030	045441	50	120505	-081599
51	102037	008755	51	111187	046053	51	120835	082193
52	102185	009385	52	111341	046665	52	121000	082786
53	102334	.010018	53	·111500	.047276	53	121166	·083379
54	102482	.010649	54	111657	.047887	54	121331	.083971
55	102631	011279	55	111814	048497	55	121496	•084568
56 57	102780 102930	011910	56	111972	.049108	56	121662	085155
58	102930	·012539 ·013170	57 58	·112129 ·112287	*049718 *050828	57	·121828 ·121994	·085746 ·086388
59	103223	013798	59	112287	050938	59	121994	080929
60	103378	014427	60	112602	.051546	60	122327	087520
			00	112002	OLUADAO	00	10001	

1	27 DEGREES 28 DEGREES, 29 DEGREES,										
-											
,	die —	Nat Na	Logarithm	Min,	Nat No	Logariti.m.	Min.	Nat. No	Logarithm.		
1	0	0·105994 109126	9·037401 037927	0	0.117052	9.068380	0	0·125380 ·125522	9.(98229		
	2	109120	031921	1 2	·117189 ·117326	*068887 *069393	2	1255622	·(98717 ·(99206		
	3	109890	-038978	3	117462	•069899	3	125804	-099693		
	4	·109522	.039502	4	117599	070404	4	125945	100191		
	5	109655	.040027	5	117736	070910	5	126086	100669		
	6	·109787 ·109920	*049551 *041076	6 7	117873 118010	.071415 .071919	6 7	126228 126370	101155 101642		
	8	110053	.041600	8	118147	072424	8	126512	102129		
	9	. 110185	042123	9	118285	072928	9	126653	102614		
	10	110318	042645	10	118422	.073432	10	126794	103100		
	11 12	·110451 ·110584	*043168 *043690	11 12	·118559 ·118696	·073935 ·074437	11 12	126936	1035S5 104070		
	13	110354	043093	13	118834	074941	13	127078 127220	104555		
	14	·110859	.044735	14	118972	.075453	14	127362	105040		
	15	110983	*045256	15	·119110	.075946	15	127564	105523		
	16	1111116	045777	16	119247	076448	16	127646	106008		
	17 18	·111249 ·111383	*046297 *046818	17 18	·119385 ·119528	·076948 ·077450	17 18	127789 127931	-106491 -106974		
	19	111516	047338	19	119661	077951	19	128073	107457		
	20	·111659	.047857	20	·119799	078452	20	128216	107940		
	21	·111783	*048377	21	119937	078952	21	128358	108423		
1	$\frac{22}{23}$	·111917 ·112051	*048896 *049415	22 23	*120075 *120213	·079452 ·079951	22 23	128511 128643	108906 109387		
	$\frac{25}{24}$	·112185	049933	24	120213	080451	24	128786	109869		
1	25	112319	050451	25	120490	-080951	25	128929	110350		
1	26	112453	050968	26	120628	*081449	26	129072	110831		
1	27 28	112587	.051487	27 28	120767	.081947	27 28	129215	111312		
	29	·112721 ·112855	·052004 ·052520	28	·120905 ·121044	·082445 ·082943	28	·129858 ·129501	111793 112278		
	30	112989	.053037	30	121183	083441	30	129644	112754		
	31	113124	*053553	31	121322	.083938	31	129788	·113233		
	32	113258	.054069	82	121461	(84435	32	129931	113712		
	33 34	·113393 ·113527	*054584 *055099	33 34	*121600 *121739	·084932 ·085428	33 34	·130074 ·130218	114192 114671		
	35	113662	055614	35	121878	085924	35	130362	115149		
	36	113797	.056129	36	·122017	.086420	36	·130505	·115627		
	37	113931	.056642	37	122157	*086916	37	130649	116105		
	38 39	*114066 *114201	·057157 ·057670	38	·122296 ·122435	*087411 *087905	38	•130793 •130936	·116583 ·117060		
	40	114336	058188	40	122455	088401	40	131080	117537		
	41	-114471	058696	41	122714	·088895	41	·131224	118015		
	42	114606	059208	42	122854	*089388	42	·131368	118491		
	43	·114742 ·114877	*059721 *060232	43	122994 123134	·089882 ·090376	43	·131513 ·131657	·118968 ·119443		
	45	114511	060745	45	123134	090869	45	131801	119445		
	46	115148	061256	46	123413	-091361	46	131945	120394		
	47	•115283	061766	47	123553	.091854	47	132090	120570		
	48	115419	-062277	48	123693	*692346	43	132235	121345		
	49 50	·115555 ·115691	*062788 *063298	49 50	123834 123974	·092838 ·093329	49 50	·132379 ·132524	121819 122294		
	51	115827	-063807	51	124114	093821	51	132669	122768		
1	52	115962	064316	52 53	124255	(94312	52	132814	123242		
	53	116093	*064826	53	124395	094802	53	132958	123715		
1	54 55	116235 116371	*065335 *065843	54 55	124535 124676	*095293 *095783	54 55	·133103 ·133243	·124188 ·124661		
	56	116507	1066351	5.6	124817	096272	56	133394	125135		
	57	116643	•066859	57	124958	096763	57	·133539	125667		
	58	116779	067366	58	125098	097251	58	133684	126079		
	59 60	116916 117052	*067874 *068380	59	125239 125380	097740	59	133830 133975	126551 127022		
	30	111004	000000	00	1,20000	000220	1 00	700010	12.022		

	27 DEGRI	EES.		28 DEGR	EES.	9	29 DEGR	EES.
Min	Nat. No	Logarithm.	Min.	Nat No.	Logarithm.	Min.	Nat No	Logarithm.
0	0.122327	9:087520	0	0.132570	9.122445	0	0.143354	9.156410
1	-122493	.088111	1	132745	123019	1	·143538	·156968
2	122660	·088700	2	132920	123593	2	·143723	157527
3	122826	(89290	3	133696	124166	3	•143908	158084
4	·122993	.089879	4	133272	124738	4	•144(93	158642
5	123160	•090469	5	133448	125312	5	·144278	159199
6	123327	·681657	6	133624	125884	6	144463	159757
7	·123495 ·123662	·(91647 ·(92236	7 8	·133800 ·133976	·126453 ·127028	7 8	·144649 ·144834	·160314 ·160869
8 9	123829	·(92823	9	134153	127600	9	145020	161427
10	-128997	.693410	10	•134330	128171	10	145206	161983
11	-124165	-093998	11	134506	128742	îĭ	145391	162589
12	124333	(94585	12	-134683	129312	12	·145578	•168(95
13	·124501	-095173	13	134860	·129883	13	·145764	.163650
14	124669	· C95760	: 14	135037	130453	14	145950	·1642(·6
15	-124888	·096346	15	•135215	·131024	15	•146137	164760
16	·125006	.096932	16	185892	131594	16	•146324	165315
17	125175	097579	17	135570	132162	17	146511	165869
18 19	·125344 ·125513	*098103 *098088	18	·135748 ·135926	·132732 ·133301	18 19	·146098 ·146885	166423 166977
20	125513	(99273	20	136104	133870	20	147072	167531
21	125062	(99858	21	136282	134418	21	·147260	168085
22	126021	100442	22	136460	135006	22	·147448	168689
23	126191	101027	23	136689	135574	23	147636	·1C9191
24	126360	101610	24	-136818	136142	24	·147825	·109749
25	126530	·102194	25	136997	136710	25	·148: 12	170296
26	126700	·102776	26	137176	137277	26	·148200	170849
27	·126871	103361	27	137355	137843	27	·148289	171401
28	127041	108944	28	137534	1384(9	28	•148577	171953
29	127211	104525	29 30	137713	138976 139542	29 30	148766	172505
31	127382	·105108 ·105690	21	138073	139342	31	·148956 ·149145	173657 173668
32	127724	106272	32	138253	140108	32	149334	174158
33	127895	106853	33	138433	141289	33	•149524	174710
34	128066	107434	34	138613	141804	34	•149714	175261
35	128237	108014	35	138793	142369	35	·149903	·175810
36	128409	108596	36	138974	·142934	36	·150(93	176360
37	128581	109175	37	•139155	143499	37	·150283	176910
38	128753	1(9756	38	139336	144063	38	150474	177460
39	128925	110335	39	139517	144626	39	150664	178008
40	129097	110914	40	139698	145191	40	150854	178557
41	·129269 ·129441	·111493 ·112072	41 42	·139880 ·140061	145754 146316	41 42	·151045 ·151236	179107 179655
43	129441	112072	43	140001	146879	43	151256	180205
44	129787	113228	44	140424	147442	44	151619	180752
45	129960	113808	45	140 606	148005	45	151810	181300
46	130132	114385	46	140788	148566	46	·152001	181847
47	130305	114962	47	14(.970	149128	47	152193	182395
48	130479	115539	48	·141153	149690	48	·152385	182943
49	·130652	116117	49	141336	·15(251	49	152577	183489
50	130826	116694	50	141518	150812	50	152709	184036
51	130999	117269	51	•141701	151878	51	152962	184583
52	131173	117845	52	141884	151934	52	153154	185129
53	131347	118422	53 54	·142067 ·142250	152494	53	158847	185675
54 55	131522 131696	·118998 ·119573	55	·142230 ·142434	158614	54 55	·153540 ·153733	186221
56	131871	119313	56	142454	154173	56	153926	187313
57	132046	120723	57	142502	154734	57	154120	187858
58	132220	120123	58	142986	155292	58	154313	188408
59	132395	1.121872	59	143170	155851	59	154507	188947
60	132570	122445	60	143354	156410	60	154700	189491
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	30 DEGRI	EES.		31 DEGR	EES.	3:	2 DEGRE	ES.
Min	Nat. No.	Logarithm.	Min.	Nat No.	Logarithm	Min.	Nat No	Logarithm
0	0.133975	9.127(22	0	0.142833	9.154827	0	0.151952	9.181706
1	·134120	127494	1	·142983	155283	1	·152106	182147
2	134266	127964	2	·143133	155738	0 2	152261	182587
3	184412	128436	3	143282	156192	3	152415	183627
5	134558	128906	5	·143482 ·143583	156647 1571(2	5	·152569 ·152724	183466
6	·134703 ·134849	·129376 ·129846	6	143733	157556	6	152878	·183906 ·184345
7	184995	130316	7	143883	-158010	7	158033	184784
8	185141	130786	8	•144034	158464	8	153188	185223
9	135287	131254	9	·144184	158917	-9	153342	·185661
10	135433	131724	10	144335	159370	10	153497	186100
11	135579	132192	. 11	144485	1-159823	11	•153652	·186538
12 13	135725	132660	12	144636	-160275 -160728	12 13	·153807 ·158962	186975
14	135872 136018	·133128 ·133596	14	·144787 ·144937	161180	14	154117	·187413 ·187850
15	136165	134064	15	145088	161632	15	154272	188287
16	136311	134531	16	145229	·162083	16	154427	188724
17	136458	134998	17	145390	·162535	17	154583	189161
18	136605	·135465	18	145541	·162986	18	154798	189598
19	136751	185931	19	145092	·163436	19	·154894	190033
20 21	136898	136897	20 21	·145844 ·145995	·163887 ·164337	20 21	·155049 ·155205	·190469 ·190905
22	137045 137192	136863	22	146146	164788	22	155360	190905
23	137239	·137829 ·137794	23	146298	165238	23	.155516	191775
24	137486	138259	24	140450	165687	24	155672	192210
25	137633	138724	25	.146601	·166137	25	155828	192645
26	137781	139189	26	146752	166585	26	155984	193080
27	137928	139653	27	1409(4	167034	27 28	·156140	193514
28 29	*138076 *138223	·140117 ·140581	28 29	147056 1472(8	167483 167931	28	·156296 ·156452	*198948 *194382
30	138371	141045	30	147360	168379	30	1566(9	194815
31	138518	141507	31	147512	168827	31	156765	195249
32	138666	141971	32	147664	109274	32	-15€921	195682
33	138814	142434	33	147817	169722	33	·157078	196115
34	138962	142896	34	147969	170169	34 35	157234	196547
85 36	139110 139258	143358 143820	35	·148121 ·148273	170615	36	·157891 ·157548	196979 197412
37	139406	144282	37	158426	171509	37	1577(5	197844
38	139554	144743	38	148578	171954	38	.157861	198275
39	139703	145204	89	148730	172400	39	158018	198707
40	139851	•145665	40	148888	.172846	40	·158175	199138
41	139999	146125	41	149086	173292	41	158332	199569
42	140147 140296	·146585 ·147046	42 43	·149189 ·149342	173736 174181	42	·158490 ·158647	·200000 ·200430
44	140290	147506	45	149342	174626	44	158804	200860
45	140594	147965	45	149648	175070	45	·15S962	201290
46	140742	·148424	46	149801	175514	46	159119	201720
47	140891	·148883	47	149954	175958	47	159276	202149
48	141040	149342	48	150107	176401	48	159433	202579
49 50	141189 141388	·149801 ·150259	49 50	·150261 ·150414	·176845 ·177288	49 50	159591 159749	·203068 ·203487
51	141555	150209	51	150568	177731	51	159907	203866
52	141636	151175	52	150721	178174	52	160065	204295
53	141786	151632	53	150875	178616	53	160228	-204723
54	141935	·152089	54	151028	179058	54	160380	205151
55	142085	152546	55	151182	179500	55	160598	205579
56 57	·142234 ·142384	153003 153460	56 57	·151336 ·151490	·179942 ·180384	56	·160697 ·160855	·206006 ·206433
58	142533	153916	58	151644	180824	58	161013	206860
59	142683	154372	59	151798	181265	59	161171	207287
60	142833	154827	60	151952	181706	60	161330	207714
-	1 11000	10101	1	10100	1 102,00	00	!	20,122

	30 DEGR	EES.		31 DEGR	EES.		32 DEGREES.		
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0	0.154700	9.189491	0	0.166633	9.221761	0	0.179179	9.253286	
1	154894	•190036	1	166837	•222293	1	179393	253805	
2	155089	190579	2	167041	*222824	2	179608	254324	
3	·155283 ·155478	·191124 ·191668	3 4	167245 167450	·223354 ·223885	3 4	·179S22 ·180037	·254844 ·255362	
5	155578	191008	5	167655	223583	5	180252	255881	
6	155867	192754	6	167860	224917	6	180467	256399	
7	156062	•193297	7	168065	225477	7	.180683	256917	
8	·156257	193840	8	·168270	*226007	8	180899	257436	
9	153452	195382	9	168476	•226537	9	181115	257953	
10	·156648 ·156844	·194925 ·195467	10 11	·168681 ·168887	227066	10 11	·181331 ·181547	·258471 ·258989	
12	157040	196308	12	169093	*227595 *228124	12	181763	259505	
13	157236	196550	13	169299	228653	13	182080	260023	
14	157432	·197091	14	·169505	•229182	14	182197	260540	
15	157623	197633	15	169711	229711	15	182113	261056	
16	157824	198174	16	169918	230238	<b>16</b>	182630	261573	
17 13	·158021 ·158218	193714	17	170125	230767	17	·182848 ·183066	•262090	
19	158218	·199255 ·199795	18	·170332 ·170539	·231295 ·231822	18 19	183283	·262607 ·263122	
20	153312	200335	20	170746	232350	20	183501	263638	
21	153839	230875	21	170953	232877	21	·183719	264154	
22	159 107	201415	22	.171161	233405	22	183937	264669	
23	·159204	201944	23	·171369	233932	23	184156	265184	
24	150102	202493	24	171577	234458	24	184374	265699	
25 26	·159600 ·159798	·203032 ·203571	25 26	·171785 ·171993	234985	25 26	·184593 ·184812	·266214 ·266729	
27	159997	205511	27	172201	·235510 ·236036	27	185031	267244	
28	160195	204648	28	172410	236562	23	185250	267758	
29	160393	205186	29	·172619	237088	29	185469	.268272	
80	·160592	205725	30	·172828	237613	30	185689	·268786	
81	160791	206261	31	173037	238139	81	185909	269300	
32 33	·160991 ·161190	·206800 ·207337	32	·173246 ·173456	·238663 ·239189	32	·186129 ·186349	·269814 ·270327	
34	161390	201331	34	173665	239189	33 34	186570	270840	
85	161589	208410	35	173875	240237	35	186790	271353	
36	·161789	208947	36	•174085	-240763	36	•187011	271867	
37	·161939	2.9484	37	174295	·241286	37	187232	272379	
38	162189	210020	38	174505	241809	38	187453	272891	
39	·162389 ·162589	210555	39	174716	242333	39	187674	273494	
41	162789	·211091 ·211626	40	·174927 ·175088	·242857 ·243381	40	187896 188117	·273916 ·274428	
42	162990	211020	42	175349	243903	42	188339	274940	
43	163191	212697	43	175560	244426	43	188561	275451	
44	163392	*213232	44	.175772	244949	44	·188783	275933	
45	163594	213766	45	175983	245471	45	·189006	·276475	
46	153795	*214301	46	176195	245993	46	189228	276985	
47	·163997 ·164198	*214835 *215368	47	·176497	·246516 ·247037	47	189450 189673	·277495 ·278006	
49	164400	215903	49	176832	247559	49	189896	278517	
50	164603	216437	50	177044	248081	50	190120	279028	
51	164805	216970	51	-177257	248602	51	·190344	·279538	
52	165008	217594	52	177570	219124	52	190568	289049	
53	165210	218036	53	177283	249644	53	190792	280559	
54 55	·165413 ·165616	·218569 ·219101	54 55	·177896	·250165 ·250685	54	·191015 ·191240	281068 281578	
56	165819	219101	56	178322	251206	55 56	191240	281018	
57	166023	220167	57	178536	251727	57	·1916S9	282596	
58	166226	*220690	58	178750	252246	58	191914	283105	
59	166430	221231	59	178964	252766	59	192189	288614	
60	·166633	221761	60	179179	253286	60	192364	284123	
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	33 DEGR	EES.		34 DEGR	EES.		85 DEGR	EES.								
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0	0.161330	9.207714	0	0.170963	9.232901	0	0.180848	9.257313								
1	161488	•208140	1	171126	233314	1	181015	257714								
2 3	161647	208566	2 3	·171289 ·171452	233727	2	181182	258114								
4	·161805 ·161964	·208992 ·209418	4	171614	·234189 ·234552	3 4	·181349 ·181516	·258514 ·258914								
5	162123	209843	5	171777	234964	5	181683	259314								
6	162282	210269	6	171940	235376	6	181850	259714								
7	162440	210693	7	172103	235788	7	-182018	260114								
8	162599	211118	8	172266	236199	8	182185	260513								
9	162758	•211543	9	172430	236611	9	182353	260912								
10	·162917 ·163076	·211967 ·212391	10 11	172593 172756	·237022 ·237433	10 11	·182520 ·182688	261310 261709								
12	163235	212814	12	172920	237844	12	182855	262107								
13	163395	-213238	13	173083	238255	13	183023	262505								
14	163555	213662	14	173247	238665	14	·183191	262903								
15	163714	214085	15	173410	239075	15	183359	263301								
16	163874	214509	16	173574	239485	16	183527	263699								
17 18	·164033	·214931 ·215353	17 18	·173738 ·173932	239895	17 18	183695 183863	·264096 ·264493								
19	164353	215555	19	174066	·240304 ·240713	19	184031	264890								
20	164512	216198	20	174230	241122	20	184199	265286								
21	164672	216620	21	174394	241531	21	184367	265683								
22	164832	217042	22	174558	241940	22	184535	266080								
23	164992	217462	23	174723	-242349	23	184704	266476								
24 25	165152	217884	24 25	174887	242757	24	184872	266871								
23	·165312 ·165473	·218305 :218726	26	175051 175216	·243165 ·243572	25 26	·185041 ·185210	·267267 ·267663								
27	165633	219146	27	175380	243980	27	185378	268058								
28	165793	219567	28	175544	244387	28	185547	268453								
29	165954	219987	29	175709	244794	29	185716	268848								
30	166114	220496	30	175874	245201	30	185885	.269243								
31	166275	221826	31	176039	245608	31	186054	269637								
32 33	·166436 ·166597	·221246 ·221665	32	176204 176369	246014	32	186223	·270032 ·270426								
34	166757	222084	34	176534	·246421 ·246827	34	186561	270820								
35	166918	222502	35	176699	247233	35	186730	271214								
36	167079	.222922	86	176864	247639	36	186900	271608								
37	167240	223340	37	177029	•248044	37	-187069	272001								
38	167401	223758	38	177194	248449	38	187238	272394								
39	·167562 ·167723	·224175 ·224593	39 40	177369 177525	248855	39	·187408 ·187577	·272787 ·273180								
41	167885	224095	41	177699	·249259 ·249664	41	187747	273573								
42	168046	225427	42	177856	250069	42	187917	-273965								
43	168208	225845	43	178022	250473	43	188087	274357								
44	168369	223262	44	178187	250876	44	188256	274749								
45	168530	226678	45	178353	-251280	45	188426	275140								
46 47	168692 168354	·227094 ·227511	46	178519 178685	251684 252087	46 47	·188596 ·188766	·275532 ·275924								
48	169016	227927	48	178851	252491	48	188936	276315								
49	169178	·22S342	49	179017	252894	49	189106	276706								
50	169340	228758	50	179183	253297	50	189277	277097								
51	169502	•229173	51	179349	253699	51	189447	277487								
52	169663	229587	52	179515	254101	52	189617	277878								
53 54	·169826 ·169983	·230003 ·230418	53 54	179682 179848	*254504 *354906	53 54	·189788 ·189958	·278268 ·278658								
55	170150	230818	55	180015	255308	55	190129	279048								
56	170312	231246	56	1801182	255710	56	190300	279438								
57	170475	231660	57	180348	256111	57	190471	279828								
58	·170638	232074	58	180515	256512	58	190641	280217								
59	170800	232487	59	180681	256913	59	190812	280606								
60	170963	232901	60	180848	257313	60	190983	280995								
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	88 DEGR	EES.		34 DEGR	EES.		25 DEGREES.		
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0	0.192364	9.284123	0	0.206218	9.314326	0	0.220775	9.343949	
1 2	·192589 ·192814	·284631 ·285139	1 2	·206455 ·206692	314S25 315323	1 2	·221024 ·221272	*344438 *344927	
3	193040	285647	3	200032	315821	3	221212	345415	
4	·193266	286155	4	-207167	316319	4	221771	*845904	
5	193492	286662	5	207404	316817	5	222020	346392	
6 7	·193718 ·193945	·287171 ·287677	6 7	207642	*317315 *317812	6	·222270 ·222520	346881 347370	
8	194172	-288185 -	8	208118	318309	8	-222771	347858	
9	·194399	288692	9	208356	*318806	9	223021	*348346	
10	194625	289199	10	208594	319302	10	223272	*348833	
12	·194852 ·195080	·289705 ·290211	12	·208833 ·209072	*319799 *320296	11 12	·223523 ·223774	*349321 *349808	
13	·195307	290718	13	209311	*320793	13	-224025	*350295	
14	·195535	290224	14	209550	*321288	14	-224276	350782	
15 16	·195763 ·195992	·291730 ·292237	15 16	·209790 ·210030	*321785 *322280	15 -16	·224528 ·225780	*351270 *351757	
17	196220	292251	17	210270	322777	17	225031	352243	
18	·196448	293247	18	210510	*323272	18	.225284	352730	
19	196677	293753	19	210750	323767	19	-225536	353216	
20 21	·196906 ·197135	·294258 ·294763	$\frac{20}{21}$	·210991 ·211231	*324263 *324758	$\frac{20}{21}$	·225789 ·226042	*853702 *354189	
22	197364	295268	22	211472	325253	22	226295	354675	
23	197593	295771	23	211714	*825749	23	-226548	·355161	
24 25	197823	296277	24	211955	326243	24	226801	*355646	
26	198053 198283	·296781 ·297285	25 26	·212197 ·212438	*326738 *327232	25 26	·227055 ·227310	*856131 *856617	
27	198513	297789	27	212480	327726	27	227564	357102	
28	198744	298293	28	212922	*328220	28	-227818	*357587	
29 30	198974	298797	29	213164	328713	29	-228072	358072	
31	·199205 ·199436	·299299 ·299803	31	·213457 ·213650	*329207 *329701	30	·228326 ·228581	*358557 *359041	
32	199667	*300307	32	213892	*330194	32	228837	359526	
33	199899	*300809	33	214135	*330688	33	229092	360011	
34	·200130 ·200362	301312	34 35	·214379 ·214622	331181	34 35	·229348 ·229604	*360495 *360979	
36	200502	301815 302317	36	214866	*881674 *832167	36	229860	361463	
37	200826	.302820	37	215110	*332659	87	230116	361947	
38	201058	*303322	88	215354	*333152	88	230373	362431	
39 40	·201290 ·201523	*303823 *304325	39	215598 215842	*833644 *834136	39 40	·230630 ·230886	·862914 ·863398	
41	201325	304827	41	216087	334629	41	231148	363881	
42	201990	*305328	42	216332	*885121	42	231400	364364	
43	202228	*305830	43	216577	*885618	43	231658	364847	
44 45	·202456 ·202690	*806331 *306S32	44 45	·216822 ·217068	*836104 *336595	44 45	·281916 ·232178	*365330 *365812	
46	202090	307333	46	217313	337086	46	232431	366295	
47	203158	307834	47	217559	837577	47	232690	.366778	
48	203392	*308334	48	217806	338069	48	232949	367260	
50	·203626 ·203861	*308834 *309334	49 50	·218052 ·218299	*338560 *339050	49 50	·233207 ·233466	·367742 ·368224	
51	204096	309834	51	218545	839541	51	233726	368706	
52	204331	310334	52	218792	*340031	52	233985	*369188	
53 54	·204568 ·204801	*310834	53 54	219040	*840522	58	·234245 ·234505	·869670 ·870151	
55	204801	*311333 *311832	55	·219287 ·219535	·841012 ·841502	54 55	234505	370632	
56	-205273	312331	56	219782	841992	56	235025	·871114	
57	205509	*312830	57	220030	842481	57	235285	·871595	
58 59	·205745 ·205981	*313329 *313828	58 59	·220278 ·220526	·342970 ·343460	58 59	235546	·372076 ·372557	
60	206218	314326	60	220775	343949	60	236068	373037	
	1	11020	00		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	-	1	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	

110			1	or DEGE				
	36 DEGR	EES.		97 DEGRI	EES.		BS DEGRI	EES.
Min.	Nat No	Logarithm	Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Logarithm.
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1	191154	281384	1	201540	*304361	1	•212169	·3266S1
2 3	·191325 ·191496	*281772 *282160	2 3	201715	304737	2 3	*212348	327047
4	191496	282169	4	*201890 *202065	*305115 *305492	4	·212527 ·212706	*327414 *327780
5	·191S39	- 282936	5	-202240	305868	5	212886	328146
6	192010	283324	6	202416	306245	6	213065	-323512
7	192181	283711	7	202591	.306621	7	·213244	-328877
8	192353	284099	8	202767	*306998	8	213424	*329243
9	-192525	-284456	9	2)2943	307374	9	213603	*329608
10	192796	*284873	10	2)3113	307749	10	213783	*829974
11 12	·192868 ·193040	*285260 *285947	11 12	*2)3294 *2)3470	*308125 *308501	11 12	·213963 ·214143	*330289 *330704
13	193212	·283033	13	2)3646	308876	13	214323	331069
14	193334	-283419	14	2)3822	3(9251	14	214503	351433
15	193555	286895	15	203993	309625	15	214683	-331798
16	193727	-287191	16	2)4174	·310000	16	214963	332162
17	193900	287576	17	204350	*310375	17	*215043	332526
13	194)72	287962	13	204527	310749	13	-215224	332890
19 20	·194244 ·194416	·258347 ·288732	19	*204703 *204830	*311124 *311498	19	-215404 -215585	·333254 ·333618
21	194588	289117	21	204550	311493	21	215765	333933
22	194761	280502	22	205237	312246	22	-215945	*334344
23	:194934	-259887	23	205409	312619	23	-216126	334706
24	·195106	·29 j271	24	205586	*312993	24	216307	*335070
25	195279	290655	25	2)5762	*313366	25	216487	335432
26	195452	291039	23	205939	313738	26	216668	335795
27 28	·195625 ·195797	291423 291846	27 23	*206115 *206293	*314111 *314484	27 23	*216849 *217030	336520
29	195970	291500	29	206470	314356	29	217030	336882
30	196143	292573	30	206647	315228	30	217392	337244
31	·196316	-292956	31	206824	315601	31	217573	337605
32	196490	293339	32	207001	*315992	32	217754	337966
33	•196663	293721	33	207178	316344	33	217935	*338328
34	196836	294104	34	207356	*316716	34 35	*218117	338689
35	197009 197182	·294868 ·294868	35 36	*207533 *207710	317087 317458	33	*218299 *218480	*339050 *339411
37	197356	295250	37	207880	317529	37	218661	-339771
38	197530	295632	33	-208066	318200	38	218843	*340132
39	197703	293013	39	·20S243	*318571	39	-219024	340492
40	197877	•293395	40	208421	318942	40	219206	340852
41	·198051 ·198225	293776	41	208599	*319311	41 42	*219388	341212
42	198225	·297157 ·297537	42	·208777 ·208954	319682 320051	43	-219570 -219752	*341573 *341932
44	198572	297918	41	203934	320421	41	219934	342292
45	198746	•293293	45	209309	320791	45	-220116	*342651
46	193920	293679	46	209489	321161	46	-220293	*343010
47	199 94	-299.)59	47	209667	321530	47	-220480	343369
48	199269	299439	48	209345	321899	48	220662	*343728
49 50	192443	299319	49 50	*210023	*322267 *322636	49 50	*220844 *221027	311086
51	199792	*300193 *300577	51	*210202 *210380	323005	51	221021	311803
52	199956	300956	52	210559	323373	52	-221311	345161
53	200141	301335	53	210738	323742	53	*221574	.345519
54	200315	301714	54	210916	*324110	54	221757	*345877
55	200590	302093	55	211095	324477	55	221940	*346235
56	200665	302471	56	211273	324844	56	*222122 *222305	·346592 ·346950
57	200840 201015	*802850 *803228	57 58	·211452 ·211631	*325212 *325579	57 58	*222305 *2224SS	340900
59	201013	303605	59	211810	325947	59	222671	*347664
60	201365	*303983	60	211990	326314	60	-222954	-348021
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2	236591	•373998	2	*252685	402579	2	269595	*430712
3	•236853	•374478	3	252960	403052	3	269884	*431178
4	237115	374958	4	253235	*403525 *403997	5	·270174 ·270463	•431643 •432108
5 6	·237377 ·237640	*375438 *375918	5	·253511 ·253787	404469	6	270753	432573
7	237932	376397	7	254763	404941	7	271042	433037
8	238165	376877	8	254339	405413	8	271332	•433502
9	-238428	*377357	9	254615	405884	9	271623	- 433967
10	238691	.377836	10	254892	406355	10	271914	·434432
11	•238954	*378315	11	255169	406827	11	272205	434896
12	-239218	378794	12 13	255446	·407299 ·407770	12 13	·272496 ·272788	·435361 ·435825
13	-·239482 ·239747	379752	14	·255723 ·256000	4 8241	14	273080	436289
15	249011	380231	15	256278	408711	15	273372	436753
16	-240276	380709	16	256556	409182	16	273664	437217
17	•240540	381187	17	256834	409653	17	278956	•437680
18	240805	381666	18	257113	410124	18	·274249	*438144
19	241070	*382143	19	257392	410595	19	274542	438608
20	241335	382621	20	257671	411065	20	274835	*439072
21 22	·241601 ·241867	·383099 ·383577	21 22	*257950 *258230	*411534 *412006	21 22	·275128 ·275421	·439534 ·439998
23	242133	384055	23	258509	412475	23	275715	440460
24	242400	*384532	24	258789	*412946	24	276010	.440924
25	-242567	*385010	25	-259769	413415	25	-276304	441386
26	•242933	*385487	26	259349	*413884	26	276598	·441849
27	•243200	385964	27	259630	414354	27	•276893	•442311
28	•243467	*386440	28	259910	*414824	28	277188	*442774
29	·243735 ·244002	*386918 *387394	30	*260191 *260472	*415292 *415761	29	·277584 ·277780	·443237 ·443700
31	244270	387871	31	260754	416231	31	278075	444161
32	244539	388347	32	261035	416699	32	278370	•444623
33	-244807	*388823	33	261317	417168	33	278867	•445085
34	245075	*389299	34	*261600	417638	34	278963	•445547
35	•245344	*389775	35	261882	*418106	35	279260	*446069
36	•245613	*390251	36	262165	*418574	36	279557	*446471
37	·245882 ·246152	*390727 *391203	37 38	·262448 ·262731	·419043 ·419511	37	·279855 ·280152	*446932 *447893
39	246132	391678	39	263015	419980	39	280102	447854
40	246691	392154	40	263298	420447	40	280748	448316
41	•246961	392629	41	263581	420914	41	281046	•448777
42	•247273	*393104	42	263865	421382	42	281345	•449239
43	•247502	393579	43	264150	421849	43	281643	449699
44	247773	*394054	44	264435	422318	44	281942	450160
45	·248044 ·248315	*394528 *395003	45	·264729 ·265005	·422785 ·423253	45	·282242 ·282541	*450621 *451081
46	248587	395478	47	265290	423203	40	282341	451542
48	248859	395952	48	265575	424187	48	283140	452002
49	•249131	*396427	49	265860	*424653	49	·2S3440	452462
50	•249403	*396901	50	*266146	425120	59	283741	452922
51	249675	*897374	51	266432	425587	51	284042	458382
52	249948	397848	52	266719	426053	52	284343	453842
53 54	*250220 *250493	398321	53 54	·267006 ·267293	'426520 '426987	58 54	·284644 ·284946	*454302 *454762
55	250766	399269	55	267580	420981	55	285248	455222
56	251040	399742	56	267867	427918	56	285550	455681
57	251314	400216	57	268154	428384	57	285852	456141
58	251588	400689	58	268-42	*428850	58	286154	456600
59	251862	*401161	59	268730	429316	59	286457	*457059
60	•252136	401684	60	269019	429782	60	285760	457518
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	00 7077 (170		ll .		0.				
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1	223037	348377	1	234143	*369480	1	•245481	290018	
2	223220	*348734	2	234330	369827	2	•245672	290356	
3	223404	*349090	3	234517	370174	3	245864	*390694	
4	223587	349446	4	*234704	370520	4	·246055 ·246246	£91031	
- 5	·223770 ·223954	*349802 *350158	5	·234891 ·2350 <b>79</b>	370867 371213	5 6	246437	*891368 *£91705	
6	223934	350514	6 7	235266	371559	7	246629	÷892042	
8	224320	350869	8	235454	371905	8	-246820	392379	
9	224504	351224	9	235641	372251	9	247010	- 892719	
10	·2246SS	*351579	10	235829	372597	10	-2472(2	293052	
11	224871	*851984	11	236016	372942	11	247894	.593388	
12	225055	352289	12	236204	373287	12	247586	÷93725	
13	225239	352644	13	236392	*373632	13	247777	'294060	
14	225423	852999	14	236580	373978	14	247968 248160	·894896	
15 16	·225607 ·225791	*353353 *353707	15 16	*236768 *236956	·374322 ·374667	15 16	248100	*£94732 *395067	
17	225976	354062	17	237144	375011	17	248544	395403	
18	226160	*854415	18	237332	375355	18	248786	295738	
19	226344	-854769	19	237520	375700	19	248928	·\$96074	
20	.226528	355122	20	237708	376044	20	249120	*396408	
21	226723	*855476	21	237897	·376388	21	*249312	*396743	
22	226893	*355830	22	238185	376731	22	•249504	-897078	
23	227682	356183	23	238273	*377075	23	249696	297412	
24	·227266 ·227451	356535	24	238462	377418	24	*249889 *250082	*297747 *398082	
25 26	227431	*3568SS *357241	25 26	*238650 *238839	377762 378105	25 26	250275	398416	
27	227821	357593	27	289028	378448	27	250466	398749	
28	.228005	357945	28	289216	378790	28	250659	-299(83	
29	228190	358297	29	289405	379133	2S 29	250852	-299417	
30	228375	*358650	30	239594	379476	30	251045	•399751	
31	228560	*359001	31	289783	379818	31	251237	·4000S3	
32	·228746 ·228931	*359353	32	239972	380160	32	251430	400417	
33 34	225951	*359704 *360056	33 34	*240162 *240351	*380503 *380845	33 34	*251623 *251816	·400750 ·401083	
85	229301	360407	35	240540	381186	35	2520(9	401415	
36	•229486	-360757	36	240729	381528	36	2522(2	•401748	
37	229672	·361108	37	240919	*381870	37	252395	•402081	
38	229857	*361459	38	•941108	*382211	38	252588	402413	
39	230043	*361809	39	241297	382552	39	-252782	402745	
40	230229	*362160	40	241486	*382892	40	*252975	403077	
41 42	·230415 ·230600	*362510 *362860	41 42	·241676 ·241866	*383233 *383574	41 42	*25316S *253362	403409 403741	
43	230786	363210	42	241800	383915	43	253566	404073	
41	230972	*363559	44	242245	*884255	44	253749	404404	
45	•231158	*363909	45	242435	*384595	45	253942	*404785	
46	231344	*364259	46	242625	*384935	46	254136	405067	
47	281530	364608	47	•242815	385275	47	254330	405398	
48	·231716 ·231903	*364957	48	243005	*385615	48	254524	*405729	
49 50	281908	*365306 *365654	49 50	*243195 *243385	*385955 *386294	50	·254718 ·254912	*406060 *406390	
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52	232461	*866351	52	243766	386973	52	255300	407051	
53	232649	*366699	53	•243956	-387312	53	255494	•407281	
54	232835	*367048	54	•244146	- 387650	54	255689	407711	
55	233021	*367396	55	•244937	387989	55	255883	408041	
56	233209	*367744	56	244528	*388328	56	256077	408371	
57 58	233395 233582	*369991 *368439	57 58	·244719 ·244909	*388667 *389004	57 58	·256272 ·256466	*408701 *409030	
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59									

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4	2			2			2		512796
6         285883         460720         7         307644         488049         7         327020         3           8         288193         461187         8         307965         488501         8         327702         3           9         289498         461645         9         305283         488954         9         325340         3           11         299100         462102         10         308607         489406         10         3258716         3           11         29,100         463018         12         309250         499310         12         329353         41         328716         3           12         291415         463418         12         309250         499101         12         329353         4           14         291023         468394         14         39392         491214         14         329781         4         329781         4         329781         4         329781         4         381118         493019         18         38110         4         381118         493019         18         38110         4         38111         38110         4         381433         4         38143         3	1						1		*513244 *513691
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11 12	·259000 ·259196	413628	11 12	·270833 ·271032	·432701 ·438020	11 12	·282887 ·283090	451613 451924
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17	260173	415262	17	272028	434013	17	284104	453477
18 19	·260369 ·260565	·415889 ·415916	18 19	·272227 ·272427	·434931 ·435250	18 19	·284307 ·284510	*453788 *454098
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28	262330	418847	23	274225	438107	28	286342	456885
29	262526	419172	29	274425	438424	29	286546	457194
30	262722	419497	30	274625	438741	30	286750	457503
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33 34	·263313 ·263510	*420472 *420796	33 34	275226	439690	33 34	287361	·458428
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	200020							

Min.   Nat. No.   Logarithm.   Min.   Nat. No.   Logarithm.   Min.   Nat. No.   Logarithm.		42 DEGR	EES.		43 DEGR	EES.		44 DEGR	EES.
1	Min.	Nat. No.	Logarithm.	Min.	Nat, No.	Logarithm.	Min.	Nat. No.	Logarithm.
2 946338 959942 3 368441 566363 2 391386 50595 4 9347044 540885 4 368818 566807 4 391728 50295 5 347399 540898 5 369196 567245 5 692111 584290 6 9347173 541712 7 369982 567684 6 392131 593854 7 348107 541712 7 369982 567684 6 392513 593854 7 348107 541712 7 369982 567684 6 392513 593854 7 348107 541712 7 369982 567684 6 392513 593854 7 348107 541712 7 369982 567684 6 392513 593854 10 349172 54369 10 371052 569485 10 394055 505501 10 349172 543039 10 371052 569485 10 394055 505501 11 349528 543482 11 371427 569674 11 394479 596024 12 349884 543924 12 371801 570311 12 39474 596024 13 350240 544366 13 372176 570749 13 395029 596536 14 350597 544808 14 372551 571156 14 39564 570756 15 350954 545249 15 372926 571623 15 396059 597760 16 331310 545699 16 373802 572061 16 396555 598194 17 351667 546132 17 373679 572498 17 396615 598514 18 352025 546574 18 374655 572985 18 397247 599661 19 352884 547016 19 374432 573810 20 389841 599928 20 352742 547457 20 374809 573810 20 389841 599928 21 383100 547898 21 375165 574248 21 389499 60028 22 353459 548389 22 375565 574685 22 39887 600795 22 353459 548589 22 375565 574685 22 39887 600795 22 353459 54868 25 376700 575895 24 400831 60252 24 354173 549922 24 37631 576422 23 399925 60122 24 354173 549922 24 37631 576485 22 39887 600795 25 354589 550104 26 376070 575955 24 400831 60252 27 355258 550144 27 377478 57688 27 400831 60252 28 355619 550950 55748 29 375818 577924 401631 602528 29 353980 551495 29 375218 577448 34 403657 605991 25 354598 550104 26 376070 575955 24 400831 602528 26 35498 550104 26 376070 575955 24 400831 602528 27 355258 550644 27 377418 57688 27 400831 602528 28 355619 550958 38 37596 576458 34 40367 60591 38 357497 553199 38 37790 576445 399925 601252 38 35619 550958 38 37898 57790 440441 602528 38 35944 555389 38 38663 551049 440462 60025 38 357497 553199 38 387697 576488 440406088 60858 34 35799 55966 38 38988 55097 54 400837 60591 36 364479 55645 49 38888 55640 49 40771 612477 50 36687 566467 45 388818 55807 56 412160 61666 50 365447 56289 56 388604	0	0.345633	9.538615	0	0.367328	9.565054	0	0.390164	9.591247
4         **347044         **540828         5         **36818         **566807         4         **291728         **59213         **598240           6         **347738         **541270         6         **36955         **567634         6         **92513         **59824           7         **345107         **541712         7         **36905         **568122         7         **82905         **54725           9         **34517         **542156         8         **370805         **56850         8         **392293         *505157           10         **349172         **543089         10         **31075         **56674         11         **34955         **505057           11         **34952         **543482         11         **371427         **56664         11         **39455         **505051           12         **349884         **543924         12         **371497         13         **805299         **506644         11         **39447         **506624           13         **350597         **544808         14         **372176         **507196         11         **389641         **508564         **57326         **576749         11         **38664         **57326 <th< td=""><td>1</td><td>*345985</td><td></td><td></td><td></td><td></td><td>1</td><td></td><td></td></th<>	1	*345985					1		
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6         347739         540828         5         369136         567245         5         392121         593420           7         345107         541712         7         369932         565122         7         892905         59428           8         343462         542156         8         370305         568567         8         393293         594722           9         343817         542597         9         370678         568997         9         893622         395157           10         349172         543039         10         371052         569485         10         394055         505390           11         349524         544368         11         37181         570741         11         394479         506024           12         349884         543824         12         371801         570311         12         394574         5064969           14         350597         544808         14         372551         571163         14         395604         597760           16         351310         545690         16         373679         571283         15         396055         598194           17         35167 <td>3</td> <td></td> <td></td> <td>3</td> <td></td> <td></td> <td>3</td> <td></td> <td></td>	3			3			3		
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25						575559			
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\$39									
40									
41         360337         556709         41         382804         582977         41         406462         60920           42         360702         557149         42         383158         583412         42         406867         609452           48         361068         557559         43         383573         553348         43         407272         60984           44         361493         558067         45         38434         584719         44         407673         610316           45         361799         558467         45         384343         584719         45         468490         611181           47         362522         559346         47         385115         58591         47         408996         611613           48         362899         559786         48         385501         586026         48         499403         611245           49         363266         560625         49         385883         586462         49         409710         612477           50         3643634         560665         50         386275         586896         50         410117         612908           51 <td< td=""><td>40</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>	40								
48         361068         557589         43         388573         583848         43         407272         669884           44         361433         558028         44         383998         584844         44         407678         610316           45         361799         58467         45         384343         584719         45         408844         610748           46         362166         558907         46         384729         585155         46         468490         611181           47         362829         559786         48         385501         586026         48         408906         611613           48         363266         560225         49         385881         586462         49         409710         612477           50         363634         560665         50         388275         58696         50         41017         612908           51         364302         561104         51         386662         58732         51         41055         613340           52         364370         561952         53         387438         58803         54         411751         614635           54         36					382804	•582977	41	·406462	669620
44         861483         558028         44         383958         584284         44         407678         610316           45         361799         558467         45         884343         584719         45         408684         610748           46         362166         558907         46         384729         585155         46         468490         611181           47         362592         559346         47         385115         585591         47         408996         611018           48         363266         560225         49         385885         586462         49         409710         612477           50         363634         560665         50         386275         586696         50         410117         612908           51         364002         561104         51         38662         57332         51         410525         613340           52         364739         561982         38         38748         588203         38         41132         614208           54         365108         562421         48         387826         588037         54         411751         614035           55									
45         361799         558467         45         384343         584719         45         408084         610748           46         362166         558997         46         384729         585155         46         408096         611181           47         362522         559346         47         385115         585591         47         408996         611613           48         362866         560225         49         385881         586026         48         409403         612045           49         363266         560225         49         385883         586462         49         409710         612477           50         363634         560665         50         386275         58696         9         410117         612905           51         364002         5611543         52         387000         587767         52         41034         61372           53         364730         561952         53         387438         588203         3411312         614203           54         365108         562421         54         38738         58867         54         411751         614635           55         365477									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$									
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48         -362899         -559786         48         -385501         -586026         48         -4C9403         -612045           49         -363266         -560225         49         -85588         -586462         49         -409710         -712477           50         -363634         -560665         50         -386275         -586896         9         -409710         -712477           51         -364002         -561144         51         -386662         -587332         51         -410525         -613340           52         -364370         -561543         52         -387438         -588203         53         411312         -614203           54         -365108         -562421         54         -387348         -588203         53         411312         -614203           55         -365477         -562860         55         -388215         -589702         55         -41250         -615066           56         -365847         -563738         57         -386804         -589507         56         412570         -615466           57         -366217         -563738         57         -388933         -589877         58         413391         -61361									
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$									
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51         364002         561104         51         386662         587332         51         410525         613340           52         364370         561543         52         387050         587767         52         41034         61372           53         364739         561952         53         387438         58803         33         411342         614203           54         365108         562421         54         387826         588637         54         411751         614655           55         365477         562860         55         388215         589702         55         412160         615066           56         365847         563738         57         388933         589942         57         412951         615930           57         366217         563738         57         388933         599877         58         413391         61361           59         366587         564176         58         389383         590877         58         413391         61361           59         386657         564176         58         389373         590812         59         413802         616798									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	52								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	53								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			\ .562421				54		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		365477	.562860		-388215	.589702	55	•412160	.615066
58         366587         ·564176         58         389383         ·590877         58         ·413391         ·616361           59         ·86957         ·564615         59         ·889773         ·590812         59         ·413802         ·616798			•563299						
59 866957 564615 59 889778 590812 59 413802 616798									
1 00   001025   000034   00   '890104   '091241   00   '414218   '611224									
00 11110	00	301328	300004	00	390104	091246	60	414218	011224

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Min.	Nat. No.	Loga ithm	Min,	Nat No.	Logarit. m	Min.	Nat No	Logarithm.
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1	293099	•467014	0	*305551	485083	1	318214	.502720
2	293305	467319	2	*305760	485381	2 3	318427	503010
3 4	·293511 ·293717	·467624 ·467928	3 4	*305970 *306180	*485678 *485976	3 4	*318640 *318853	*503300 *503590
5	293923	-468233	5	306339	486273	5	319066	503380
6	29 1129	•463537		306598	486570	6	319279	504170
6 7	294335	-468842	6 7	*306808	486866	7 8	*319492	•504460
8	294541	*469146	8	307017	487163	8	319705	•504750
9	·294747 ·294953	·469 149 ·469 753	9	*307227 *307437	487460 487757	9	·319918 ·320132	*505089 *505329
11	295159	470056	11	307647	488053	11	320345	505618
12	295365	•470360	12	307857	488349	12	320558	505907
13	295572	•470663	13	308067	·488645	13	320772	506196
14	295778	470936	14	308277	488941	14	*320986	•506486
15 16	·295985 ·293192	·471270 ·471578	15 16	308487 308697	·489237 ·489532	15 16	*321200 *321414	*506775 *507064
17	293393	471876	17	308907	489828		321627	•507352
18	296605	472179	13	309118	-490124	17 18	*321841	•597641
19	293812	472481	19	309328	•490419	19	*322054	•507929
20 21	*297019 *297226	·472784 ·473087	23 21	*309538	490714	20 21	*322268 *322482	*508217 *508505
22	297433	473389	22	*309748 *309959	·491009 ·491305	22	*322696	•508793
23	297640	·473691	23	*310170	.491600	23	*322910 .	509081
24	297847	·473993	24	*310381	•491895	24	323124	509369
25	298054	•474295	25	310591	*492189	25	•323338	509657
26 27	·293261 ·298468	•474597 •474898	26 27	310801 311012	*492483 *492778	26 27	•323552 •323766	5509944 510231
28	293676	475200	28	311223	493072	28	323931	-510519
29	298833	•475502	29	*311434	493366	29	*324196	-510807
30	299091	•475833	30	311645	493660	30	324410	•511094
31 32	299298 299506	•476104 •476405	31 32	*311856 *312068	493955	31 32	·324624 ·324839	•511381 •511668
33	299713	476706	33	312279	·494249 ·494543	33	325053	511955
34	299921	·477007 ·477308	34	312490	494836	34	•325268	•512242
35	*300129		35	*312702	•495130	35	*325483	.512529
36	*390337 *390545	477609	36	*312913	495423	36	*325693	·512815 ·513101
38	300752	•477939 •478239	37 33	*313124 *313335	·495716 ·496009	38	*325912 *326127	·518387
39	300960	478509	39	313547	496302	39	326342	513673
40	301168	478809	40	*313759	496596	40	*326557	•513959
41	301376	479109	41	*313970	496838	41	326772	514245
42	*301584 *301793	·479409 ·479709	42	*314182 *314893	·497181 ·497474	42	*326987 *327203	*514531 *514817
44	302001	480008	44	314605	497766	44	327418	.515102
45	*302210	480308	45	314817	493058	45	*327633	515388
46	*302418	483607	46	315029	•498350	46	*327848	515673
47	*302626 *302835	430907 481206	47 48	*315241	498642	47	*328064 *328280	•51595S •516244
49	- 303043	481505	49	*\$15453 *315665	*493934 *409226	49	328495	516529
50	303252	481804	50	315877	499518	50	328711	516814
51	*303461	*482102	51	*316089	499809	51	*328926	•517098
52 53	303670	482401	52	316301	500101	52	*329142	517393
54	*303878 *304087	482699 482998	53 54	*316513 *316726	500392 500684	53 54	*829358 *829578	517668 517952
55	334296	483296	55	316939	500005	55	-329789	•518236
56	*304505	-483595	56	*317152	501267	56	339005	518521
57	304714	*483893	57	317364	*501557	57	*330221	. 518905
58 59	*304923 *305132	*484191 *484488	58 59	317576	501848 502139	58 59	*330437 *330653	•519089 •519373
60	305342	484786	60	318001	502429	60	*330869	519656
	1		11		1	II	7	

-		45 DEGRI	EES.		46 DEGR	EES.	4	17 DEGRI	EES.
1	Min.	Nat. No.	Logarithm.	Min.	Nat No	Logarithm	Min.	Nat. No.	Logarithm
	0	0·414213 ·414625	9.617224	0	0·439557 ·439991	9.643015	0	0·466279 ·466737	9.668646 .669072
	2	•415037	-618087	2	•440425	-643872	2	•467195	-669493
	3	•415450	618518	3	•440859	*644300	3	·467653	.669924
	4	•415863	·61S950	4	•441294	644728	4	468112	•670350
	5	416276	619381	5	·441729 ·442164	·645156 ·645584	5	468571	670776
	6 7	·4166S9 ·417102	·619811 ·620242	6 7	442104	646012	6 7	·469030 ·469490	·671201 ·671627
i	8	417516	620673	8	•443037	646440	8	•469951	-672(53
	9	417920	621094	9	•443475	•646869	9	•470412	672478
	10	•419345	·621585	10	•448912	•647297	10	·470873	*672904
	11	·418760	·621965	11	•444350	•647725	11	•471335	.673330
	12	•419176	622396	12	•444788	•648158	12	•471797	•673755
	13	·419592 ·420008	·622827 ·623257	13 14	•445226 •445665	·648581 ·649369	13	·472260 ·472723	·674181 ·674607
	15	·420008	623688	15	•446105	•649437	14 15	473187	675033
	16	·420842	624119	16	•446544	649364	16	•473650	675458
	17	•421259	·624543	17	·416984	·650292	17	•474114	·6758S3
	18	·421677	.624980	18	•447425	650720	18	·474579	.676369
	19	•422095	.62541€	19	•447865	6.1147	19	475044	.676734
	20 21	*422513	625840	20	•448306	651574	20	475509	677159
	22	·422932 ·423351	·626271 ·626701	21 22	·448748 ·449190	*652002 *552430	21 22	·475975 ·476442	·677584 ·678010
	23	•423771	627131	23	449632	652857	23	476908	678435
	24	•424191	627561	24	•450075	653285	24	477375	.678860
	25	•424611	627991	25	·450518	.653712	25	•477843	679285
	26	•425031	623421	26	·450961	·654189	26	•478311	.679710
	27	•425452	628851	27	•451405	654567	27	·478779	•680135
	28 29	425874	*629281	28	·451850 ·452294	654994	28	·479248	·680560
1	30	·426296 ·426718	·629711 ·630141	29 30	452789	·655421 ·655848	29 30	·479718 ·480188	·68^986 ·681411
	31	427141	-630571	31	453185	656276	31	·480658	681836
	32	427563	-631000	32	•453631	656703	32	•481129	·682261
	33	•427936	.631430	33	•454)77	657130	33	481600	682686
-	34	•428410	•631860	34	•454524	657357	34	482071 482543	·683111
1	35	•423835	-632290	35	•454971	.6573 ₹	85		6883586
	36	·429260 ·429684	·63272) ·633149	36	·455419 ·455867	*658411 *658838	36 37	·483015 ·483487	·683937 ·684385
	- 38	43.1.9	683578	38	•456315	659265	83	•483960	6848 0
	39	•430534	634008	39	•456764	659692	39	•481433	685234
	40	43 970	.631137	40	·457213	.660119	40	•484907	.685658
-	41	•431386	634866	41	•457662	660545	41	•485381	·686.83
	42	431812	*635295	42	•458112	*660972	42	·435856	-686508
	43	·432239 ·432367	*635724 *686154	43	•458562 •459013	·661398 ·661825	43	•486332 •486848	·6S6933 ·6S735S
	45	433.95	-636583	45	459464	662251	45	487284	•687782
1	46	433323	637012	46	•459915	662678	46	·487760	·68S206
	47	•433951	637441	47	•460367	663104	47	·433237	·6SS631
1	48	•434383	637370	4.9	•460820	*663531	48	•483714	•689355
	49	•434810	638299	49	•461273	*663958	49	·4S9192	*689479
	50	*435239	638728	50	461726	664384	50	·4S9670	689904
	51 52	·435669 ·436100	·639157 ·639586	51 52	·462179 ·462632	*664810 *665236	51 52	·493149 ·493628	690328 690752
	53	·436539	640014	53	463087	665663	53	•491108	691177
	54	436961	640443	54	•463542	.666989	54	•491588	691601
	55	437093	64 872	55	•468993	*666516	55	•492369	*692026
1	56	*437825	641301	56	•464453	666942	56	•492550	.692450
	57	438258	641730	57	•464906	667368	57	493031	692874
	58 59	·438097 ·430123	642158	58 59	·465365 ·465822	*667794	58 59	•493512 •405904	·693293 ·693722
	60	+439557	643015	69	466279	668546	6)	494177	694146
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	48 DEGREES.			49 DEGR	EES.	50 DEGREES.			
Min.	Nat No.	Logarithm.	Min.	Nat. No.	Logarithm.	Min.	Nat. No	Logarithm	
0	0.330869	9.519656	0	0.343941	9.536484	0	0.357213	9.55292	
1	•331085	.519940	1	344160	•536761	1	•357435	.55319	
2	331302	520224	2	*344380	537038	2	-357658	*55346	
3 4	*331518 *331735	*520507 *520791	3	*344600 *344820	537315 537592	3	-357881 -358104	55373	
5	*331951	521074	4 5	345039	537868	5	258327	*55400 *55428	
6	-332167	521357	6	345259	538145	6	-358550	55455	
7	*332384	•521640	7	*345479	.538422	7	-858774	-55482	
8	*302600	•521923	8	•345699	-588698	8	-858997	.555(.9	
9	·332S17	.522206	9	•345919	-538975	9	-259220	55536	
10	*833034	•522489	10	*346139	-559251	10	*859443	55563	
11 12	·333251 ·333468	·522771 ·523054	11 12	·346359 ·346580	·539527 ·589803	11 12	+859666   +859890	·55590 ·55617	
13	333684	523336	13	*346800	540079	13	366114	55644	
14	333901	-523618	14	*347020	540354	14	-360337	55670	
15	*334118	.523900	15	*347240	.540630	15	-36(561	55097	
16	334335	.524182	16	.347461	.54(906	16	-360784	.55724	
17	334552	•524464	17	-347681	541181	17	·361008	.55751	
18	•334770	524746	18	*347901	-541456	18	•361232	55778	
19	*334987	525028	19	*345122	541731	19	361456	55805	
20 21	·335204 ·335421	525369 525591	20	*34S342 *34S563	·542006 ·542281	20 21	*361680 *361904	-55832 -55859	
22	335638	525872	22	*348784	542556	21 22	-362128	55886	
23	*835856	526153	23	-349005	•542831	23	-362352	-55913	
24	336073	526434	24	349226	•543106	24	-362576	** 5989	
25	-336291	526715	25	*349447	543381	25	·362\$00	55966	
26	336509	•526997	26	*349668	•543656	26	-363024	.55 993	
27	336727	527278	27	349889	•543930	27	-263249	*56(20	
28 29	·336944 ·337162	·527558 ·527838	28 29	*850110 *850381	·544204 ·544479	2S 29	-863473 -368697	56047	
30	337380	528119	30	350552	544753	30	-368922	-56100	
31	337598	528400	31	350773	545026	31	-364146	56127	
32	.337816	.528680	32	*350994	545300	32	-364371	.56154	
33	*338034	.528960	33	*351215	*545574	33	-864595	.56181	
34	338252	.529240	34	*351437	545848	34	-364820	56207	
85	·338470	•529520	35	*351659	546122	35	*365045	56284	
36 37	*338688 *338906	*529800 *530080	36 37	*351880 *352102	•546895 •546668	36	*365269 *365495	56261 56288	
38	339124	*530359	38	*852323	546941	38	*365719	56314	
39	339342	•530638	39	352544	547214	39	365944	56341	
40	339560	•530918	49	*352766	547487	40	-366169	-56368	
41	-839779	.531197	41	·352988	547760	41	-366894	.56394	
42	-339998	531476	42	353210	•548033	42	-366619	56421	
43	*340216	531755	43	353432	548306	43	•266844	56448	
44 45	*840435 *840654	·532034 ·532313	44	·353654 ·353876	*548579 *548851	44 45	·367069 ·367294	*56474	
46	340054	532513	45 46	354098	549124	46	·367520	56501 5652S	
47	341092	532871	47	354320	549396	47	-367745	56554	
48	341311	•533150	48	354542	•549668	48	-367970	•56581	
49	*341529	*533428	49	354764	•549940	49	-368196	*56607	
50	•341748	•533706	50	*354987	550212	50	-368421	56634	
51	341967	*533985	51	355209	550484	51	-368647	56661	
52	·342157 ·342406	534263	52	355431	550756	52	*368873	56687	
53 54	*342406 *342625	*534541 *534819	53 54	*355653 *355876	551027 551299	53 54	•369098 •369324	56714	
55	342844	535097	55	356(98	551570	55	*369550	56767	
56	•343063	535074	56	*356321	551842	56	-369776	56793	
57	•343283	.535652	57	*356544	.552114	57	370002	56820	
58	•343502	•535929	58	356767	.552385	58	·370228	*56846	
59	*343721	536206	59	356990	•552656	59	370454	56873	
60	*343941	536484	60	357213	.552927	60	·3706S0	•56899	

	48 DEGR	EES.		49 DEGR	EES.		59 DEGR	EES.
Min.	Nat. No.	Logari:hm	Min	Nat No	Logari-hm	Min.	Nat No	Logarithm
0	0.494477	9.691146	0	0.524253	9.719541	0	0.555724	9.744859
1 2	•494960	.694570	1	•524763	•719963	1	•556263	.745280
2	*495443	-694994	2	•525274	•720386	2 3	•556804	745702
3 4	495927	695418	3 4	525785	·720868 ·721231	4	·557344 ·557885	·746123 ·746545
5	·495412 ·495896	695842	5	·526297 ·526809	721653	5	.558427	746966
6	497381	696689		-527322	722376	6	558969	•747383
7	497867	697113	6 7	•527835	-722498	7	.559511	747819
8	•493353	-697537	8 9	•528348	.722920	8	•560054	748230
9	•498340	697961		-528863	723343	9	560598	.748652
10	•499327	698335	10	•529378	723766	10	561142	•749073
11	•499314	•693808	11	•529893	.724188	11	561687	749491
12	•599392	699232	12	530408	724610	12 13	562232	749916
13	500790	·699656 ·700079	13 14	·530924 ·531440	725032	13	·562778 ·563324	750337
15	501279 501768	700503	15	531957	725454 725877	15	563871	750758 751180
16	502258	.700927	16	532475	726299	16	564418	751601
17	5.12749	701351	17	532992	726721	17	564966	•752022
13	-503239	.701774	18	533510	727143	18	.565514	•752443
19	•503730	.702193	19	534029	727565	19	.566063	752865
20	.5.)4221	.702621	20	534548	727937	20	566612	•753286
21	•5)4713	703045	21	•535068	728409	21	567102	.753707
22	505205	.703463	22	585589	•728832	22	567712	·754128
23	5)5693	703891	23	536110	729254	23	568263	*754549
25	506191	*704315	24	536631	729676	24	*568815	754971
26	•536585 •537189	704738	25 26	537153 537675	*730093 *730520	25 26	•569367 •569919	·755892 ·755813
27	507674	·705162 ·705585	27	538193	730942	27	570472	756214
23	508169	706308	23	538721	731364	23	571025	756655
29	508664	706431	29	539245	731786	29	571579	757076
80	-509160	*706854	30	-539769	.732208	30	572134	.757498
81	•509357	.707278	31	540294	.732630	31	572689	.757919
82	•510154	707701	32	•540819	733052	32	573244	758340
83	•51.0651	708124	33	541345	733474	33	573800	758761
34	511148	708547	34	541871	733896	34	574357	•759182
35 36	·511646 ·512145	708970	35 36	542398	*734318	35 36	574914	759303
37	512645	·709394 ·709317	37	542925	734740	37	•575472 •576030	·760024 ·760445
33	513145	710240	38	543930	·7355S3	38	576589	760866
39	513345	710663	39	544508	736004	39	577148	·761287
40	514146	.711087	40	•545037	- 736426	40	577708	761708
41	.514647	711509	41	.545567	.736848	41	578268	.762129
42	.515148	711932	42	•546097	*737270	42	578829	•762550
43	•515659	•712355	43	•546623	737692	43	579390	•762971
44 45	516152	.712778	44	•547159	738114	44	579952	763392
46	516655	713200	45	547690	738535	45	580514	763813
47	·517158 ·517662	·713623 ·714046	46	*548222 *548755	·738957 ·739379	46	*581077 *581641	·764234 ·764655
48	518166	714469	48	•549288	739300	48	582205	765076
49	518670	.714892	49	•549321	740221	49	·5S2770	765497
50	519175	715314	50	•550355	.740643	50	583335	765918
51	-519681	.715737	51	•550890	.741065	51	*583900	·766339
52	520188	716160	52	•551426	.741487	52	584466	.766760
53	520695	•716583	53	•551961	741908	53	•585088	767181
54	521202	717006	54	552497	.742330	54	585600	767602
55 56	521709	717428	55	•558083	742751	55	586168	·768022
57	*522216 *522725	717850	56	553571	748173	56	586787	·768443 ·768864
58	523234	·718273 ·718696	57 58	*554109 *554647	·743595 ·744017	57 58	·587396 ·587875	·769285
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Min	Nat. No.	Logarithm	Min	Nat No	Logarithm.	Min.	Nat No.	Logarithn	
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2	371132	.569528	2	*384797	585232	2	*898650	600591	
3 4	•371358	569793	3	385027	585491	3	*398882	*600843	
5	371584	*570057	5	385256	*585749	4	*\$99115	601098	
0	·371810 ·372037	·570322 ·570586	5	*385485	*586008	5 6	*399347	*601351	
6	372263	570850	6 7 8 9	385944	*586266 *586525	7	·399580 ·399812	601608 601856	
å	272100	571114	8	386174	586783	7 8	400045	602109	
8	·372490 ·372716	571378	9	386404	587041	9	400278	602362	
10	372943	.571642	10	386633	•587299	10	400510	602614	
11	-373170	.571906	11	386863	.587557	11	400743	602867	
12	-373396	-572170	12	387093	587815	12	40(976	-603119	
13	-373623	.572434	13	387323	558073	13	*401209	603371	
14	•373850	.572697	14	*387553	·58S331	14	*401442	*603628	
15	*374076	572960	15	387783	588588	15	401675	603875	
16	*374303	573224	16	388013	588846	16	*401908	604127	
17	*374530	573487	17	*388243	.589103	17	*402142	*604379	
18 19	374757	573750	18	388473	589361	18 19	402375	604631	
20	374984	·574013 ·574276	19	388703 388933	589618	20	*402608 *402841	604582	
21	·375211 ·375439	574539	21	389164	-589875 -590132	21	403074	605355	
22	375666	574802	22	389394	590389	22	403308	605637	
23	375893	575064	23	389624	590646	23	403541	605588	
24	376120	575327	24	389855	590903	24	403775	•606139	
25	376348	575589	25	390085	591160	25	4040(9	*606391	
26	376575	.575852	26	390316	591416	26	404242	*606642	
27	*376803	576114	27	*390547	:591673	27	404476	-606893	
28	377030	576376	28	390777	591929	28	404710	607144	
29	377258	.576638	29	391008	.592186	29	·404943	.607394	
30	377485	•576900	30	391239	592442	30	405177	607645	
31 32	377713	577162	31 32	391469	592698	31 32	405410	607896	
33	377941 378168	·577424 ·577685	33	391700 391931	*592954	33	405645	·608146 ·608397	
34	378396	577947	34	392162	·593210 ·593466	34	·405879 ·406113	608647	
35	378624	578208	35	392393	593721	35	406347	-608897	
36	-378852	578470	36	392624	593977	36	406581	609147	
37	379080	578731	37	392855	594233	37	·406S15	-609397	
38	:379308	578992	38	393086	·5944S8	38	407049	-609647	
39	379536	:579253	39	393317	.594743	39	.407284	609897	
40	379764	-579514	40	*393549	*594999	40	*407518	610147	
41	*379992	579775	41	393780	*595254	41	407753	610397	
42	*380221	*580636	42	394012	.595509	42	407987	610646	
43	380449	:580297	43	394243	595764	43	408221	610896	
44	380677	580557	44 45	394474	596019	44	408456	611145	
45 46	*380906 *381134	·580818 ·581078	46	394706 394938	·596274 ·596528	45	·408690 ·408925	·611394 ·611644	
47	331363	581339	47	395169	596783	47	409160	611893	
48	381592	581599	48	395401	597038	48	409100	612142	
49	381820	581859	49	395632	597292	49	409629	612391	
50	382049	582119	50	395864	-597546	50	409864	612640	
51	-382278	582379	51	396096	.597801	51	410099	612888	
52	382506	-582639	52	:396328	-598055	52	410334	613137	
53	*382735	582899	53	396560	-598309	53	410569	613386	
54	382964	.583158	54	396792	.598563	54	410804	613634	
55	383193	*583418	55	397024	-598817	55	411039	-613883	
56	383422	553677	56	397256	•599071	56	411274	614131	
57	383657	583937	57	397488	599324	57 58	·411509 ·411744	·614379 ·614627	
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Min.	Nat. No.	Logarithm	Min	Nat No	Logarithm	Mm	Nat No	Logarithm
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2 3	-590159 -590731	·770969 ·771389	2 3	·625480 ·626086	·796214 ·796634	2 3	·662924 ·663567	·\$21464 ·821885
4	591303	771810	4	:626693	·797055	. 4	-664211	822306
5	•591876	-772231	- 5	627300	.797476	5	-664855	-822727
6	*592450	.772652	6	627908	.797896	6 7	665500	·S23148
7	593025	.773073	7	628517	*798317	7	666145	-823509
8 9	•593600 •594175	·773494 ·773914	8	·629126 ·629736	·798738 ·799158	8 9	·666791 ·667439	*823990 *824411
10	•594751	774335	10	630346	-799579	10	668086	824833
11	*595327	774756	11	·63(.957	-800000	11	-668734	825254
12	.595904	775177	12	.631569	800421	12	-669383	*825675
13	*596482	775598	13 14	·632181 ·632794	*800841 *801262	13	670032	826(96
15	·597060 ·597639	·776018 ·776439	15	633407	801683	14 15	·670682 ·671333	*826517 *826938
16	598219	776860	16	634021	802104	16	-671985	·827860
17-	.598799	777281	17	-634635	*802524	17	672637	827781
18	•599380	777702	18	635251	*802945	18	678290	8282(2
19	599960	778122	19 20	635867	·803366 ·803787	19	678943	·828623
21	·600542 ·601124	·778543 ·778964	20 21	·636483 ·637100	804207	20 21	·674597 ·675252	*829044 *829406
22	601706	779385	22	637717	804628	22	-675907	829887
23	602289	779805	23	638335	*805049	23	-676563	.63(3(8
24	602873	780226	24	638954	:805470	24	-677220	830729
25 26	603458	780647	25 26	639574	*805891	25	677877	831751
27	·604043 ·604628	·781068 ·781488	26	·640194 ·640814	·806311 ·806732	26 27	·678534 ·679193	·831572 ·831993
28	605214	781909	28	641435	·807153	28	679852	832415
29	605800	*782330	29	642057	*807574	29	·680512	*832836
30	606387	782750	30	642680	807995	30	681173	833257
31 32	606975	783171	31 32	643303	·808415 ·808836	31	·(81834	833679
33	·607564 ·608153	783592	33	·643926 ·644550	809257	82 33	·682496 ·683159	·834100 ·834522
34	608742	-784433	34	645175	809678	34	683822	*834943
35	609332	784854	35	645801	*810(99	35	684486	835364
36	609923	785275	36	.646427	*810520	36	·685150	.835786
37	610514	785696	37	647681	·810940 ·811361	37	-685815 -686481	·836207 ·836629
39	611106	786116	39	648309	811782	38	687148	837(50
40	612291	786958	40	648938	812203	40	·C87815	837472
	612884	·787378	41	.649567	*812624	41	688483	837893
42	613478	787799	42	650197	*813045	42	·689152	838315
43	·614073 ·614668	·788220 ·788640	43	·650827 ·651458	·813466 ·813887	43	·689821 ·690491	·838736 ·839158
45	615264	789061	45	652090	814307	45	-691161	839579
46	615860	789482	46	652722	814728	46	-691832	840001
47	615457	.789903	47	653355	*815149	47	·C92504	840423
48	617054	790323	48	653989	815570	48	·693177	.840844
49 50	·617652 ·618251	·790744 ·791165	49 50	·654623 ·655258	·815991 ·816412	49 50	·693850 ·694524	*841266 *841688
51	618251	791586	51	655893	816833	51	·695199	8421088
52	·619450	792006	52	-656529	817254	52	·695874	842531
53	*620050	792427	53	-657166	817675	53	-696550	842953
54	620651	792848	54	657803	818096	54	·697227	*848874
55 56	·621253 ·621855	-793268 -793689	55 56	·658441 ·659080	·818517 ·818938	55 56	·697904 ·698582	·843796 ·844218
57	622458	794110	57	659719	819359	57	699261	844689
58	623061	.794531	58	660359	819780	58	699941	*845061
59	623665	•794951	59	-660999	*820201	59	700621	845488
60	624269	.795372	60	-661640	820622	60	701302	845905

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Min-	Nat No	Logarithm.	Min	Nat. No.	Logarithm.	Min.	Nat No	Logarithm
0	0.412215	9.615124	0	0.426423	9.629841	0	0.440807	9.644249
1	412450	615371	1 2 3	•426662	630084	1	•441048	644480
2	412685	615619	2	426900	*630326	2	•441289	*644724
3	412921	615867		427139	*630569	3	*441531	644961
5	·413156 ·413392	·616114 ·616362	4 5 6 7	·427377 ·427616	·630811 ·631054	5	•441772 •442013	·645198 ·645435
6	413628	616610	- 6	•427854	631296	6	442255	645678
7	413863	-616857	7	•428093	631538	7	•442496	645910
8	414099	617104	8	•428331	631780	8	•442738	-646147
9	•414335	.617351	9	•428570	*632022	9	•442980	646384
10	•414571	617599	10	428809	632264	10	•443221	*646620
11	414807	·617846	11	•429047	*632505	11	•443463	*646857
12	415042	618092	12	•429286	632747	12	•443704	647094
13	-415278	618339	13	429525	632989	13	•443946	·647330
14 15	·415514 ·415750	·618586 ·618833	14 15	·429764 ·430003	·633230 ·633472	14 15	·444188 ·444430	·647567 ·647803
16	415150	619079	16	•430042	633713	16	444672	648040
17	416223	619326	17	430481	633954	17	•444914	648276
18	416459	·619572	18	430720	634195	18	•445156	648512
19	·416695	·619818	- 19	·430960	*634437	19	•445398	648748
20	·416931	620065	2)	•431199	634678	20	•445640	648984
21	·417168	620311	21	•431438	634919	21	•445852	649220
22	417404	620557	22	·431677	.635159	22	•446224	649456
23	417641	620803	23	431917	635400	23	•446366	649691
24 25	·417877 ·418114	·621049 ·621294	24 25	·432156 ·432396	·635641 ·635881	24 25	•446668 •446851	·649927 ·650162
26	418350	621549	26	432635	636122	26	447093	650398
27	418587	621786	27	432875	636362	27	447835	650633
28	418823	622331	28	•433114	636603	28	447578	.650869
29	419060	622276	29	•433354	.636843	29	447820	651104
30	419297	622522	30	•433594	637083	30	448063	651339
31	•419534	622767	31	•433833	637323	31	·448306	651574
32	419771	623012	32	•434073	637563	- 32	•448548	*651809
33	420008	*623257	33	434313	637803	33	•448791	652044
34 35	·420245 ·420482	·623502 ·623747	34 35	·434553 ·434793	·638043 ·638283	34 35	·449034 ·449276	-652279 -652514
36	420402	623992	36	435033	638522	36	449519	652748
37	420956	624237	37	435273	-638762	37	•449762	-652983
38	421193	624481	38	•435513	-639001	. 38	450005	653217
39	421430	624726	39	·435753	639241	39	450248	653452
40	·421668	624970	40	•435993	.639480	40	450491	653686
41	421905	625215	41	•436234	639719	41	450734	653920
42	422143	625459	42	436474	·639958	42	450977	654155
43 44	·422380 ·422617	·625703 ·625947	43	436714	·640197 ·640436	43	·451220 ·451463	·654389 ·654623
45	422855	626191	45	·436955 ·437195	640675	44 45	451707	654857
46	423092	626435	46	437435	640914	46	451950	655090
47	•423330	626679	47	437676	641153	47	452193	655324
48	423568	*626923	48	437916	641391	48	452437	655558
49	423805	627166	49	·438157	.641630	49	·452680	655791
50	424043	627410	50	•438398	·641868	50	•452924	656025
51	424281	627654	51	438639	642107	51	453167	656258
52 53	·424519 ·424757	·627897 ·628140	52 53	·438879	·642345 ·642583	52 53	·453411 ·453654	·656492 ·656725
54	424757	628384	54	·439120 ·439361	·642821	54	453898	656958
55	424990	628627	55	439361	643060	55	455090	657191
56	425471	628870	56	439843	643298	56	·4543S5	657424
57	425709	629113	57	440084	•643535	57	•454629	657657
58	425947	.629356	58	•440325	·643773	58	454873	.657890
59	426185	•629598	59	•440566	•644011	59	455117	.658123
60	•426423	·629841	60	·440807	644249	60	•455361	·658356

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Min.	Nat No.	Logarithm.	Min.	Nat. No.	Logarithm.	Min.	Nat. No.	Lugarithm
0	0.701302	9.845905	0	0.743447	9.871250	0	0.788291	9.896687
1	•701983	*846327	1	•744172	871673	1	789063	·S97112
2	702665	*846749	2	744897	872096	2	*789836	897537
3	·703348 ·704032	·847170 ·847592	3	·745623 ·746350	·872519 ·872942	3	·790609 ·791383	*897962 *898887
4 5	•704716	*848014	5	-747078	873366	5	792158	898812
6	•705401	*848436	6	•747806	873789	6	•792934	-899237
6	-706087	*848858	6 7	-748535	*874212	7	.793710	*899662
8	•706773	*849280	8	-749265	*874635	8 9	•794488	900087
9	707460	849702	9	•749996	*875059		·795266	900512
10	.708148	*850124	10	-750727	*875482	10	796045	900938
11 12	708836	850546	11 12	•751459	*875905	11	·796825	•901368 •901788
13	·709525 ·710215	·850968 ·851390	13	·752192 ·752926	*876329 *876752	12 13	·797606 ·798387	902218
14	-710906	851812	14	-753661	877176	14	•799169	902639
15	711597	*852234	15	•754396	877599	15	·799952	-903064
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17	•712982	*853078	17	·755869	878447	17	*801521	903913
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20	715064	854345	20	·758084	*879717	20	*803881	905192
21 22	·715760	854767	$\begin{array}{c} 21 \\ 22 \end{array}$	·758824	*880141	21	*804669	905617
23	·716456 ·717158	*855189 *855612	23	·759564 ·760305	*880 <b>564</b> *880 <b>9</b> 88	22 23	*805458 *806248	90604
24	717850	856034	24	·761048	881412	23 24	807089	906894
25	·718548	*856456	25	.761791	881836	25	807830	90732
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28	720648	*857723	28	·764024	*883107	28	*810210	908598
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30	•722051	*858568	30	.765517	883955	30	811801	9.9450
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37	.726984	.861525	37	·770767	*886923	37	817396	·912432
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41 42	·729820 ·730530	*863216	41 42	.773784	*888620	41	820611	·914138 ·914564
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45	·732666	864906	45	·776S15	890317	45	823842	915846
46	733389	*865329	46	·777574	890742	46	824651	916270
47	·734094	*865752	47	•778334	891166	47	825462	916697
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54	739115	·S68712	54	.783679	894138	53 54	830343	919233
55	·739835	869135	55	·7S4446	894563	55	831977	920112
56	740556	*869558	56	785213	894988	56	·S32796	•920589
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59	-742723	870827	59 60	·787520 ·788291	*896262	59	·S35256	•921820
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Min. 0 1 2 3 4 4 5 6 7 8 9 10 11 12 13 14 15	Nat No 0:455861 -455605 -455609 -456093 -456387 -456581 -456581 -457314 -457314 -457318 -457808 -457808 -458947 -458292 -458586	9-658856 -658889 -658891 -659054 -659286 -659518 -65952 -660446 -6604678 -660910	Min. 0 1 2 3 4 5 6 7 8 9	Nat. No.    0.470081   .470827   .470574   .470821   .47168   .471815   .471869   .472.56	9-672178 -672400 -672628 -672856 -673(83 -673811 -673589	Min. 0 1 2 3 4 5 6	Nat No 0.484962 .485211 .485460 .485710 .485960 .4862(9	9-£85768 - £85768 - £85931 - £86154 - £86877 - £86660 - £86823
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	'455605 '455849 '456093 '456337 '456381 '456825 '457070 '457314 '457558 '457803 '458047 '458292	658588 658821 659054 659286 659286 659518 6659750 659982 666215 666446 660678	1 2 3 4 5 6 7 8 9	*470327 *470574 *470821 *471668 *471315 *471562 *471809	672400 672628 672856 673(83 673311 673539	1 2 3 4 5	485211 485460 485710 485960	*C85931 *C86154 *C86877 *C86600
2 3 4 5 6 7 8 9 10 11 12 13 14 15	455849 456093 456387 456581 456825 457070 457314 457558 457803 458047 458292	658821 659054 659286 659518 659750 659982 660215 660446 660678 660910	2 3 4 5 6 7 8 9	*470574 *47(821 *471068 *471315 *471562 *471809	·672629 ·672856 ·673(83 ·673311 ·673589	2 3 4 5	485460 485710 485960	**C86154 **C86877 **C86660
3 4 5 6 7 8 9 10 11 12 13 14 15	456093 456387 456581 456825 457070 457314 457558 457803 458047 458292	659054 659286 659518 659750 659982 660215 660446 660678 660910	4 5 6 7 8 9	·47(821 ·471068 ·471315 ·471562 ·471809	672856 673(83 673311 673539	3 4 5	·485710 ·485960	**C86877 **C86600
4 5 6 7 8 9 10 11 12 13 14 15	'456387 '456581 '456825 '457070 '457314 '457558 '457803 '458047 '458292	659286 659518 659750 659982 660215 660446 660678	4 5 6 7 8 9	·471668 ·471315 ·471562 ·471809	·673(83 ·673311 ·673539	5	485960	·686600
5 6 7 8 9 10 11 12 13 14 15	456581 456825 457070 457314 457558 457803 458047 458292	659518 659750 659982 660215 660446 660678	5 6 7 8 9	·471315 ·471562 ·471809	·673311 ·673539	5		
6 7 8 9 10 11 12 13 14 15	'456825 '457070 '457314 '457558 '457803 '458047 '458292	659750 659982 660215 660446 660678 660910	6 7 8 9	·471562 ·471809	.673539			
7 8 9 10 11 12 13 14 15	457070 457314 457558 457803 458047 458292	659982 660215 660446 660678 660910	9			11 0	*486459	T*687646
9 10 11 12 13 14 15	*457558 *457803 *458047 *458292	660446 660678 660910	9	*470 EP	673766	7	486768	··· 687269
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16	459270	·662068 ·662300	16 17	·474033 ·474281	·6758(9 ·676(36	16 17	488957	689270
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36	464173	-666680	36	478991	680927	36	.498966	.093697
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	57 DEGR	EES.		58 DEGR	EES.		59 DEGR	EES.
Mra.	Nat No	Legarithm.	Min.	Nat. No.	Logarithm.	Min.	Nat No	Logarithm.
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2	*837725	-923101	3	-888339	948823 949253	2	•943486	974735
3 4	·833550 ·839375	·923529 ·933956	4	+889720 +890601	949233	3 4	·944429 ·945373	975169 975603
5	*84)2)2	924384	5	891484	950114	5	946317	976037
6	841029	924811	6	892368	·950544		947263	976471
7	*841357	.924238	7	·893253	950975	6 7	·948210	976905
8	842686	925666	8 9	·894139 ·895)26	951405 951836	8	949158	977889
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11	*84518)	923949	ii	-896802	952697	10 11	952009	978641
12	*843)12	927377	12	897692	953127	12	952931	979075
13	·846816	.927814	13	.893583	.953558	13	·953915	.979510
14 15	817631	928232	14	899475	953939	14	954870	979944
16	·848516 ·849352	·928360 ·929)88	15 16	·900368 ·901262	·954420 ·954851	15	·955S26 ·9567S2	·980379 ·980813
17	·85)19)	929516	17	902156	955282	16 17	957740	981248
18	-351023	929944	18	903 52	.955713	18	958699	981682
19	·851837	930372	19	·9 33949	.956144	19	959659	982117
20	852707	.93)800	20	904847	956575	20	-960621	982552
21 22	·853848 ·854390	931223 931656	21 22	·905746 ·906645	*957006 *957487	21	·961583 ·962546	992987
23	855233	932)85	23	937546	957869	22 23	963511	·983422 ·983857
24	·856.)77	932513	24	9 8448	.958300	24	964477	934292
25	·853921	932341	25	•909351	.958732	25	.965444	984727
26	·857767	933369	26	91 255	959163	26	·966411	.985162
27 28	*853514	933798	27	911160	•959595	27	967380	985597
29	·859451 ·83031)	·934226 ·934655	23 29	·912966 ·912973	*960026 *960458	28 29	•968350 •969322	986033 986468
30	831159	935383	30	913881	960890	30	970294	986903
31	*832 109	935512	31	·914790	961321	31	971268	987339
32	-83233)	935941	32	915700	*961753	32	.972242	987775
33 34	·863712 ·864535	·936369 ·936793	33 34	·916611 ·917523	962185 962617	33	·973218 ·974195	988210
35	·85512)	937227	35	918436	963049	34 35	975173	988646 989082
36	-866275	937656	36	919350	963481	36	976152	989518
37	·867131	.938)85	37	•920265	963913	37	977133	.939954
38 39	867937	938514	38	921182	*934345	38	971815	990390
40	*863345 *869704	·938942 ·939371	39 40	·922099 ·923017	*964777 *935210	39	·979097 ·980081	990826
41	870564	939371	41	923937	965642	40	981066	991202
42	·871425	91023)	42	924857	966075	41	982052	992134
43	*872233	94)659	43	·925778	•966507	43	-983039	992571
44	·873148	911083	44	923701	960949	44	.984027	993007
45 45	·874312 ·874377	·941517 ·941947	45 46	927624	957372	45	•985017 •986008	993444
47	875742	942376	45	·928549 ·929475	*967805 *968238	46	986008	99358)
48	·8765)8	942316	48	930401	968670	48	987993	994754
49	·877475	943235	49	·931329	969103	49	988987	995191
50	878314	913665	50	932258	969536	50	989982	-995627
51 52	·879213 ·831083	·911091 ·911521	51	933188	969969	51	990979	996064
53	83)954	914953	52 53	·934119 ·935050	·970402 ·970835	52 53	991977	·996501 ·996938
54	·831827	945383	54	935983	971268	54	993975	997376
55	-88270)	945813	55	936917	971701	55	994976	997813
56	*893574	946243	56	937853	972135	56	995978	998250
57 58	·881419 ·885325	946673	57	938789	972568	57	996982	998687
59	·886202	947103 947533	58 59	·939726 ·940664	·973001 ·973435	58 59	997987	999125
60	887080	947963	60	941604	973868	60	10.00000	1.0000000
			1	1	1	11	1	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

## NATURAL SINES AND TANGENTS,

TO EVERY DEGREE AND MINUTE OF THE QUADRANT.

EXTENDED TO SEVEN PLACES OF DECIMALS.

-	1	(	,•		ı°	9	2°		3°		1.°		5°.	(	° -	7	2	,
1	0	000	0000	017	4524	084	8995	052	2360	069	7565	087	1557	104	5255	191	8693	60
1	1		20.9		7482				6264		0467		4455		\$178		1581	59
	2		5818	018	0341		4809		9169		3368		7353	105	1070		4468	58
	3	004	8727		3249	000	7716	053	2074		6270	088	6251		3963	100	7355	57
	5	201	1636 4544		6158 9066	036	0623 3530		4979 7883	071	$9171 \\ 2073$		3148 6046		6856 9748	123	C241 3128	56 55
	6		7453	010	1974			054	6788		4974		S943	108			6315	54
-	6 7	002	0362	010	4883		9344	004	3693		7876	089	1840	100	5533		S9 1	53
	8 1		3271		7791	037	2251		6597	072	0777		4738		8425	124	1788	52
	9		6180	020	0699		5158		9502		3678		7635	107	1318		4674	51
	10	000	989		3608		8065	055	2406			690	0532		4210	405	7560	50
	11 12	003	1998 4907		$6516 \\ 9424$	038	0971 3878		5311 8215	079	$9481 \\ 2382$		$\frac{3429}{6326}$		7102 9994	125	0446 3332	49 48
	13		7815	021	2332		6785	056	1119		5283		9223	108	2855		6218	47
		004	0724	021	5241		9692	000	4024		8184		2119	100	5777		9104	46
	15		3633		8149	039	2598		6928		1085		5016		8669	126	1990	45
	16		6542	022	1057		5505		9832		3986			109	1530		4875	44
	17	005	9451		3965	0.40	8411	057	2736		6887	692	0859		4452	105	7761	43
	18 19	000	2360 5268		6873 9781	040	0318 4224		5640 8544		9787 2688		$\frac{3706}{6602}$	110	7343 $0234$	121	0646 3531	42 41
	20		8177	093	2690		7131	058	1448		5589		9499	110	3126		6416	40
		006	1086	020	5598	041	0037	000	4352				2395	II	6017	33	9302	39
	22		3995		8506		2944		7256	076	1390		5291		89.38	128	2186	38
1	23			024	1414		5850	059	0160		4290			111	1799		5071	37
	24	0.07	9813		4322	0.40	8757		3064				1083		4689	100	7956	36
	25 26	007	2721 5630	กอร	$7230 \\ 0138$	042	1663 4569		5967 8871	011	$0091 \\ 2991$		3979 6875	110	7580 0471	129	0841 3725	35 34
	27		8539	020	3046		7475	060	1775	LL I	5891		9771	112	3361		66(9)	33
1		008	1448		5954	043	0382	000	4678		8791	095	2666	100	6252		9494	32
П	29		4357		S862		3288		7582		1691		5562		9142	130	2378	31
	30		7265	026	1769		6194	061	0485		4591			113	2082		5262	30
		009	0174 3083		4677	044	9100		33S9 6292		7491	096	1353		4922	101	8146	29
	32 33		5992	097	0493		2006 4912		9196		0391 3290		4248	114	0702	131	1(3) 3913	2S 27
	34	=0	8900	021	3401		7818	062	2099		6190		0039	114	3592		6797	26
П	35	010	1809			045	0724		5002		9090		2934	1	6482		9681	25
	36		4718		9216		3630		7905		1989		5829		9372		2564	24
П	37		7627	028	2124		6536	063	0808		4889		8724	115	2261		5447	23
	38 39	011	$0535 \\ 3444$		$5032 \\ 7940$	040	9442	٠.	3711		7789		1619 4514		5151 8040	100	8330 1213	22 21
	49		6333	090	0847	940	2347 5253		9517		$0687 \\ 3587$		7408		(929		4(96	20
П	41		9261	020	3755		8159	064	2420		6486		0303		3818		6979	19
	42	012	2170		6662	047	1065		5323		9385		3197		6707		9862	18
į)	43		5079		9570		3970		8226		2284		6092		9596		27-14	17
1	44		7987		2478		6876	065	1129		5188		8986				5627	16
10	45 46	013	0896 3805		5385 8293	042	9781 2687		4031		8082 0981		1881 4775		5374 8263		8509 1892	15
П	47			021	1200	045	5592		9836		3880				1151		4274	13
П	48	1	9622		4168		8498		2739				0563		4040		7156	12
Ш	49	014	2530		7015	049	1403		5641		9677		3457		6928		0058	11
	50		5439		9922		4308				2576		6351		9816		2919	10
	51		8348				7214	067			5474		9245		2704		5801	9
b	52 53	015	1256		5737	059	0119		4349				2138		5593		8683 1564	8 7
	54		$\frac{4165}{7073}$		864 <del>4</del> 1552		3024 $5929$				$\frac{1271}{4169}$		5082 7925		8481 1368		4445	6-
	55		9982		4459		8835		3055				6819		4256		7327	6 5
	56	016	2890			051	1740		5957		9966		3712		7144		0208	4
-	57				0274		4645		8859				6605		0031		3089	3 2
-	58	045	8707		3181				1761		5762		9499		2919		5970	2
	59 60	017	$1616 \\ 4524$		6088 8995		0455		4663				2592 $5285$		5806 8693		SS50 1731	1 0
	1	0	4524  9°		8993 38°		3360 7°	0	7900 36°	081	1557 5°	0	9289 4°		8093 33°		.5. .1 (21	1 ,
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0	000 0000	J17 4551	034 9208	052 4078	009 9268	087 4887	105 1042	122 7846	60
1	2909	7460	035 2120	6995	070 2191	7818	3983	123 0798	59
2 3	5818				5115 8088	088 0749 3681	6925 9866	3752 6705	58 57
4	8727 001 1636	3280 6190	036 0858			6612		9658	56
5	4544	9100		8663	8835	9544	5750		55
6 7	7453			054 1581	6809		8692	5566	54
8	002 0362 3271	4920 7830		4498 7416	9733 072 2657	54(8 8341	107 1634 4576	8520 125 1474	53 52
9	6180				5581		7519	4429	51
10	9389	3650		3251	85.5	4206		7384	50
11	003 1998	6560		6169		7138	3405		49
12 13	4907 7816	9470 021 2383		9087 056 2005	4354 7279	091 0071 3004	6348 9291	3294 6249	48 47
14	004 0725	5291			074 0203	5938		9205	46
15	3634	82.1		7841	3128	8871	5178		45
16	6542		5814		6053		8122	5117	44
17	9451 005 2360	4021 6932	8728	3678 6596	8979	4728 7672	110 1066 4010	8073 128 1030	43 42
18 19	5269	9842		9515	075 1904 4829		6955	3986	41
20	8178			058 2434	7755	3540	9899	6943	40
21	006 1087	5668	041 0383		076 0680		111 2844	9900	29
22	3996 6905	8574		8271	8606	9409	5789	129 2858 5815	38 37
23 24	9814	024 1484 4895		059 1190 41(9	6532 9458	094 2344 5278	8734 112 1680	8778	36
25	007 2723	7895		7029		8213	4625		35
26	5632	025 0216	4952	9948	5311	095 1148	7571	4690	34
27 28	8541	3127			8237	4084		7648	33 32
29	008 1450 4360	6038 8948	043 0781 3695	8766	078 1164 4090	7019 9955	3463 6410	131 0607 3566	31
30	7269				7017	096 2890	9356	6525	30
31	000 0178	4770	9524	4546	9944	5826	114 2303	9484	29
32	3087		044 2438	7466		8763	5250		28
33 34	5996 8905	027 0592 8508			5798 8726	097 1099 4685	8197 115 1144	5404 8864	27 26
35	010 1814		045 1183	6226		7572	4092	133 1324	25
36	4724	9825	4097	9147	4581	098 0509	7039	4285	24
37	7633				7509	3446	9937	7246	23
3S 39	011 0542 8451	5148 8059	9927 046 2812	4988 79.8	0437 3365	6383 9320	116 2936 5884	134 0207 3168	22 21
40	6361			064 CS29	6293		8S32	6129	20
41	9270	3882	8673	3750	9221	5194	117 1781	9:91	19
42	012 2179	6793		6671		8133	4730		18
43 44	50SS 7998	$9705 \\ 030 \ 2616$		9592 065 2518	5078 8007	100 1071 4009	7679 118 6628	5015 7978	17 16
45	013 0997		048 0334	5435		6947	3578	136 0940	15
46	3317	8439	3250	8356	3865	9886	6528	8908	14
47	6726		6166		6794		9478	6866	13
48 49	9635 $014$ $2545$	4263 7174		4199 7121	9723 084 2653	5763 8762	119 2428 5378	9830 137 2793	12 11
50	5454				55S3		8329	5757	10
51	8364	2998	7829	2965	8512	4580	120 1279	8721	9
52	015 1273	5910	050 0746	5887		7520	4230	138 1685	8
53 54	4183 7093	8822 033 1734		88.9 068 1732	4372 7302	103 0460 3399	7182 $121 0183$	4650 7615	7 6
55	016 0002	4646		4654	083 0233	6340	3085		5
56	2912	7558	051 2411	7577	3163	9280	6036	8545	4
57	5821		5328		6094		8988	6510	3
58 59	8731 017 1641	\$383 6295		8422 6345	9025 087 1956	5161 8161	122 1941 4893	9476 140 2442	2
60	4551	9208		9268	4887	105 1042	7S46		0
1	89°	88°	87°	860	85°	8.4°	833	850	1
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NATURAL COTANGENTS.

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0	139 179	1 156	4345	173	6482	190	8090	207	9117	224	9511	241	9219		8190	60
$\frac{1}{2}$	461		7218		9346	191	(945	208	1962	225	2345	242		259	1600	59
3	140 037		0091 2963		5075		3801 6656	=	4807 7652	PAF	5179 8013		4863 7685		3810 6619	58 57
4	325	2	5836		7939		9510	209	0497		0846		0507		9428	56
5	618				0803		2365		3341		3680			260	2237	55
6	141 189		1581 4453		3667 6531		5220 8074		6186 9030		6513 9346		6150 5971	1	5045 7853	54 53
8	477		7325			193			1874		0170	0.11			0662	52
9	765	1 159	0197	176	2258		3782	-	4718		5012		4613		3469	51
10	142 053		3069		5121		6636	011	7561	000	1014		7433		6277	50
11 12	341 628		5940	177	7984 0847	191	9344	211	$0405 \\ 3248$		35(9		2074		9085 1892	49 48
13			1683	***	3710	104	5197		6091		6341		5894		4699	47
14	143 204	7	4555		6573		8050	3	8934	. 0	9172		8713	-	7506	
15 16	492		7426 0297	170	9435	195	0903 3756	212	1777	229	2004 4835	246	1533 4352	263	0312	45
	144 068		3167		5160		6609		$\frac{4619}{7462}$		7666		7171		5925	43
18	350	2	6038		8022		9461	213	0304	230	C497	1	9990	}	8730	42
19	644		8909	179	0884	196	2314		3146		3328	247	28(9	264	1536	41
20 21	931 $145 219$		1779		3746		5166 8018		5988		6159 8989		5627 8445		4342	40 39
22	507		4650 7520		8607 9469	197			8829 1671		1819	248	1263		7147 9952	58
23	795	3 163	0390	180	2330		3722		4512		4649	-	4081	205	2757	37
24 25	146 088		3260	-	5191		6573	~	7353		7479		€899		5561	36
26	370 658		6129	101	8052 (913)	100	9425 2276		0194 3035		0309		9716 2533		\$366 1170	35 84
27			1868	101	3774	193	5127		5876		5967		5250		3973	
27 28	147 234	0	4738		6635		7978		8716	-	8796		8167	-	6777	32
29 30	521		7607	100	9495	199	0829		1556		1625		(984		9581	31
	148 697		0476 3345	182	$2355 \\ 5215$		3679 6530		4£96 7236		4454 7282		3800 6616		23S4 5187	30
32	384		6214		2075		9380	217	0076	234	0110		9432		7989	28
33	672	4	9082	183	0935	200	2230		2915		2938	251	2248	268	0792	27
34 35			1951		3795		5080		5754		5766		5063		3594	26 25
36	149 247 535		4819 7687		6654 9514	201	7930	218	8593 1432	225	\$594 1421		7879 0694		6896 9198	
37			0556	184	2373	201	3629		4271		4248		35(8		2000	23
38	150 110		3423		5232		6478		7110		7075		6323		4801	22
39	398		6291		8091		9327	010	9948		9902		9137		7602 0403	21 20
41	685 979		2026		0949 3808		$2176 \\ 5024$		2786 5624		5555		4766		3204	19
42	151 260		4894		6666		7873	-	8462		8381		7579		6004	18
43	548		7761		9524		0721		1300	237	1207	254	0893	-	8805	17
44 45	152 128	9 169	0628 3495	186	$\frac{2382}{5240}$		3569 6418	11	4137 0974		4033 6859		3206 6019		1605 4404	16 15
46	410		6862	1	8098		9265		9811	-	9684		8832		7204	14
47	698	4	9228		0956	204	2113	221	2648	238	2510	255	1645	272	0003	13
48			2095		3813		4961		5485		5335		4458		2862	12
49 50	153 278 560		4961 7828		6670		7808 0655	222	8321 1158		\$159 COS4	056	7220 0082	1	5601 8400	11 10
51			0694	188	2385	200	3502		3994		3808	200	2894	273	1198	9
52	154 133	66	3560		5241		6349		6830		6633		5705	1	3997	8
53	42		6425		8098		9195		9666		9457		8517		6794	7
54 55	710	$\frac{ 4 }{ 8 172}$			0954 3811		2042 4888		2501 5337	240	2280 5104	257	1328 4139		9592 2390	5
56	155 28		5022		6667		7734		8172	1	7927		6950		5187	4
57	579	25	7887		9523	207	0580	224	1007	241	0751		9760		6984	3
58		8 178			2379		0420		3842		3574		2570		0781	8 7 6 5 4 3 2 1
59	156 14 43		3617 6482		5234 8090		6272 9117	1	6676 9511		6396 9219	=	5381 8190		3577 6374	0
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0	140 5408	158		176				212								60 -
1 2	$\begin{bmatrix} 8375 \\ 141 & 1342 \end{bmatrix}$		6826 98: 9		$\frac{6269}{9269}$		6822 9841	012	8606	231	1746 4811	100	6370 9460		2610 5728	59 58
3	4308		2791	177	2269		2861	210	4688		7876	250	2551		8847	57
4	7276	36.7	5774		5270		5881	-	7730		6941		5642	269	1967	56
5	142 0243		8757		8270				0772		4007	074	8734		5087	55
6	6179	160	$\frac{1140}{4724}$	110	4273	190	1922 4943		3814 6857		7073 0140		1826 4919		$8267 \\ 1328$	54 53
8	9147		77.8		7274	1	7964		9900		3207		8012		4449	52
9	143 2115	161	0692	179	0276		6936		2944		6274		1106		7571	51
10	5084		3677		3279 6281		4008		5988 9082		9342 2410		$\frac{4200}{7294}$		0694	50
12	8953 144 1022		$\frac{6662}{9647}$		9284		7031 0053	216	2077		5479				3817 6940	49 48
13				18)	2287	100	3076	210	5122	0	8548		3484	272	0064	47
14	6931		5618		5291		6100		8167		1617	1977	6580		3183	46
15 16	9931		3603	101	\$295	100	9124	217	1213		4687	054	9676		6313 9438	45
17	145 29J1 5872		1590 4576	181	1299 4308	199	2148 5172		4259 7806	236	7758 0829	204	2773 5870		2564	443
18	8842		7563		7308		8197	218	0353		3900		8968		5690	42
19	146 1813			182	0313	200	1222	17	3400		6971		2066		8817	41
20 21	4784		3537		3319		4248		6448 9496		0044		5165	274	1945 5072	40 39
22	7756 $147 0727$		6525 9513		6324 9330		7274	219	2544	1	3116 6189		8264 $1363$		8201	38
23	3699			183		-01	3327	-10	5593		9262		4463		1330	37
24	6672		5489		5343		6354		8643	238	2336	Y	7564		4459	36_
25 26	9544 $148 2617$		8478	104	8350	909	9381	223	1692				0664		7589	35 34
27	148 2617 5590		$\frac{1457}{4456}$	19-1	1358 4365	202	$\frac{2409}{5437}$		$\frac{4742}{7793}$	239	8485 1560	1	3766 6868	216	0719 3850	33
28	8563		7446		7373		8465	221	0844		4635		9970		6981	32
29	149 1536			185	0382		1494		3895		7711		3073		0113	31
30 31	$\frac{4510}{7484}$		3426		339)		4523		6947	240	0788 3864		6176		3245 6378	30 29
32	150 0458		6417 9407		6399 9409		$7552 \\ 0582$	222	9999 3051	-	6942	259	928) 2384	-	9512	28
33		168		186	2418	204	3612	222	6104	241	0019	200	5488		2646	27
34	6408		539)		5428		6643		9157		3697		8593	1	5780	26
35 36	9383 $151$ $2358$		8381 1373	107	8439 1449	005	9674 $2705$	223	$\frac{2211}{5265}$		6176 9255	260	1699 4805	970	8915 2050	$\frac{25}{24}$
37	5333		4366	101	4469		5737		8319	242	2334	10	7911	219	5186	23
38	8309		7358		7471			224	1374			261	1018		8322	22
39	152 1285			188	0483	206	1801		4429		8494	-1.46	4126		1459	21
40	4262 7238		3344 6338		3495 6507		4834 7867	OOK	$7485 \\ 0541$	243	$1575 \\ 4656$	000	7234 $0342$		4597	20 19
42	153 0215		9331		9520	207	0900	220	3597		7737	202	3451	281	7735 (873)	18
43	3192	171	2325	189	2533		3934		6654	244	0819		6560		4012	17
44	6170		532)		5546	200	6968	202	9711		3902	0.00	9670	200	7152	16
45 46	9147 154 2125		8314	103	8559 1573	208	0003 3038	226	2769 5827	045	6984 0068	263	2780 5891	282	$0292 \\ 3432$	15 14
47	5103		4304	100	4587		6073		8885	240	3151		9002	1	6578	13
48	8082	.571	7300		76.12		9109	227	1944			264	2114		9715	12
49 50	155 1061					209	2145		5003	010	9320	100	5226	283	2857	11
51	4040 7019		$\frac{3292}{6288}$		3632 6648		5181 8218	999	8063 1123	246	2405	985	8339 1452	-	5999 9143	10
52	9998		9285		9664	210	1255	220	4184		8577	200	4566	284	2286	8
53	156 2978	174	2282	192	268)	A.A.	4293		7244		1663		7680		5430	7
54 55	5958		5279		5696		7331	229	0306			266	0794	208	8575	6
56	8939 157 1919		8277 $1275$	199	8713 1731	211	0369		8367	210	7837 $6925$		$\frac{3909}{7025}$	285	1720 4866	5 4
57	4900		4273	100	4748	1	6446		6492	240	4013	267	0141		8012	3
58	7881		7272	10	7766		9486	230	2555		7102	1	3257	286	1159	2
59 60	158 0863 3844			194	0784	212	2525		5618	249	0191		6374		4306	1
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NATURAL COTANGENTS.

,	16°	17°	18°	19°	20°	21°	22°	23°	,
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1	9170								59
2 3	276 1965 4761			326 1182 3932		359 1825	375 1459 4156		58 57
4	7556		310 1234		343 1133			8019	56
5	277 0352		3999	9430	3865			392 0695	55
6		294 0403		327 2179			376 2243		54
7	5941					360 2682		6047	53
8	\$736 278 1530		311 2294	328 0424	344 2060 4791		7632 877 0327		52
9	4324					361 0821	3021	4071	51 50
11	7118		312 0586		345 0252				
12	9911	7081	3349	8666	2982	6246	8408	9419	48
13	279 2704			329 1413				394 2093	
14	5497			4160		362 1669			46
15	8290 280 1083		313 1638 4490			4380 7091		7439 395 0111	45
16 17		297 0971		380 2398					43
18	6667	3749							42
19	9459		314 2686	7889	347 2085	5222			41
20	281 2251			331 0634		7932		396 0798	40
21		298 2079		3379			380 2634		39
22	7833 $282 0624$		315 0069		34S 0267 2994	3351			38
23 24		7632 299 0408		332 1611	5720	6059	8014 381 0704		37 36
25	6205					365 1476			35
26	8995		316 2010			4184		6818	34
27	283 1785	8794			3898	6891		9486	33
28		300 1509		333 2584			382 1459		32
29	7364		317 0288			266 2306		4823	81
30	284 0153 2942			334 0S10	350 2074 4798	5012 7719	6834	7491 399 0158	30 29
31 32		301 2606					383 2209	2825	28
33	8520		318 1321		351 0246				27
34	285 1308					5836		8158	26
35		302 0926		335 1775			384 6268		25
36	6884					368 1246			24
37	9671 $286$ $2458$		319 2350 5106			3950 6654		6156 8S21	23 22
38 39		303 2016			6584	9358		401 1486	21
40	8032		320 0619			869 2061		4150	20
41	287 0819	7559	3374	8214		4765		6814	19
42		304 0331				7468			18
43	6391					370 0170			17
44	9177 288 1963		321 1640 4395		354 0190 2910	2872 5574		4804 7467	16 15
45 46		305 1413		338 195		8276			14
47	7533						387 2474		13
48	289 0318	6953	322 2657	7379	355 1070	3678	5156	5453	12
49	3103	9723	5411	339 0116	3789	63/79	7837	8114	11
50		306 2492	8164			9079	388 0518		10
51	8671 $290$ $1455$		323 0917 3670			872 1780 4479		3436 6096	9 8
52 53	290 1455 4239			8525 340 1060		7179		8756	7
54	7022					9878		405 1416	6
55	9805		324 1926		357 0097	373 2577	8919	4075	5
56	291 2588	9102	4678	9265	2814	5275	6598	6734	4
57	5371			341 2000		7973	9277	9393	3
58	8153		325 0180	4734			390 1955		2
59 60	292 0935	7408 309 0170		342 6201	358 0964 3679	3369 6066		4709 7366	1 0
	0111		0002	334 CAC1		0000			0
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-14		0.17						1 1	7
6		649 4076	674 5085	700 2075	726 5425	753 5541	781 2856 7542	809 7840 810 2658	60 59
1 2	625 2739 6783	8212 $650$ $2350$				754 0102 4666			58
3	626 0834	6490	779)	5089	8767				57
4	4331		$676 2028 \\ 6268$			755 3799 8369			56
5 6	8935 627 2938	4774 8918				756 2941			55 54
7	7042	652 3964	4752	703 2464	6582			813 1611	53
8.	628 1093	7211 653 1360	8997 678 3312	6813 704 1163				6444 814 1280	52 51
9 10	5155 9214				9963	758 1248	9808		
11	629 3274	9363	679 1741						49
12		654 3817 7972							48
13 14	630 1399 5464	655 2129	4501						46
15	9530	6287						817 0343	45
16		656 0447	681 3016 7276		6777 734 1253				44
17 18	632 1738				5730	7959	7524		42
19	5810	657 2937	58,1	4763	735 0210				
21	9333 633 3959					7157 $  763 $ $  1759$		5 819 4625 9488	
22	8035							820 4354	
23	634 2113	9612	634 2871	710 2253	8147	764 0969			37
$\frac{24}{25}$	6193 635 0274							821 4093 8965	
26		660 2136						822 3840	
27	8141	6313	9969		6115		794 0121		33
28 29	636 2527 6614							823 3597 8479	32 31
30	637 0703			713 2931	9611			824 3364	
31	4793	662 304)	7093						
32 33	8385 638 2978					768 2517 $7144$		825 3149 8031	28 27
34	7073							826 2925	
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36 37	9366	664 3934 8178				5770 1037		827 2719	
38		665 2373						828 2523	
39	7569								21
40	641 1673 5779					9388		3 S29 2337 7247	20
42	9336	9171	4328	5729	745 3770	8878	8 801 1511	S30 2160	18
43	642 3934					3773 3526			17
41 45	8105 643 2216					1774 2827		$   \begin{array}{ccccccccccccccccccccccccccccccccccc$	16 15
46	6329	5995	694 1557	720 3387	747 1886	3 7481	803 0632	832 1834	14
47		669 0205				775 2137			13
48	4560 8378				748 0950	1776 1455	5 804 0206 5 4997		
50	645 2797	670 2345	8818	722 1075		6118	979	834 1547	10.
51 52	6918 646 1041						2 805 458		9
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54	9290	9721	6097	8798	8212		8988	3836 1298	6.
55 56	647 3417 7546	672 3944			751 2762		807 3787		5.4
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58	5808	6624	699 8499	6540	642:	3780 3492	821:	2838 1087	2
59 69	9941 649 4976	674 0854			758 0981		809 8027		1 0
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0	642	7876	656		669			9934						3398	731	3537	6
1		0104		2785			682	2111		8676		3124		5418		5521	5
2		2332		498)		5628				0767		5180		7438		7503	5
3		4559		7174		7789		6363		2858		7236		9457	1.7	9486	5
4		6785	0==	9367		9948		8489		4949	=00	9291	720			1467	
5			169	1560	010	2108	683	$0613 \\ 2738$		9128	108	1345		3494		3449	5
6		1236		3752 5944		$4266 \\ 6424$		4861		9128		3398		5511		5429	5
7		$\frac{3461}{5685}$		8135		8582		6984	1	3305	-	5451 7504		7528 9544		7409 9388	5
8			659	0326	671			9107		5392				1559			5
9 10	645	0132		2516	0.1	2895	694	1229		7470	700	1607	121	3574	199	3345	5
11		2355		4706		5051	002	$\frac{1229}{3350}$		9565		3657		5589		5322	4
12		4577		6895	-3,	7206		5471	697	1651		5707		7602		7299	4
13		6793		9083		9361		7591		3736		7757		9615		9275	4
14			659	1271	672	1515		9711		5821	200	9806	722	1629	734	1250	4
15		1240		3458		3668	685	1830		7905	710	1854		3640		$\frac{1250}{3225}$	4
16		3460		5645		5821		3948	410	9938		3901		5651		5199	4
17		5679		7831	-	7973		6066	698	2071		5948		7661		7173	
18		7898	660	0017	673	0125		8184		4153		7995	63	9671		9146	4
19	647	0116		2202		2276	686	0300				0041	723	1681		1118	4
20		2334		4386	100	4427	-	2416		8315	2 0	2086		3690		3090	
21	-	4551		6570		6577				0396		4130		5693		5061	3
22		6767		8754	L.	8727		6647		2476		6174		7705		7032	3
23	10.		661	0936	674			8761		4555		8218	111	9712	1.0	9002	3
24	648	1199	71	3119	T 10			0375		6633	712					0971	3
25		3414		5300		5172		2988		8711		2303		3724	109	2940	3
26		5623		7482	1	7319				0789		4344		5729		4908	3
27	0.00	7842		9662		9466		7213	1	2866		6385		7734		6875	3
28	649			1842				9325		4942		8426		9738	707	8842	3
29		2268		4022				1435	5					1741	131		3
30	-	4480	1113	6200		5902		3546		9093		2504		3744		2773	3
31		6692	000	8379 0557	070	8046		7765		1167 3241		4543 6581	1	5746		4738	2
32	eko	1114		2734	010	2333		9873		5314		8618	- 33	7747 9748	200	6703 8666	2 2
33 34	000	3324		4910	6			1981		7997	714	0010	796	1740	790	0629	2
35	1	5533		7087		6618		4089		9459	ITT	2691		3748		2592	2
36		7742		9262		8760				1531		4727		5747	-	4553	
37				1437				8302		3601		6762	20.	7745	20	6515	2
38	651	2158		3612				0407		5672		8796		9743		8475	$\tilde{2}$
39	1001	4366		5785		5181		2512				0830			739	0435	2
40		6572		7959		7320		4617		9811		2863		3736		2394	2
41	-			0131		9459				1879	-	4895		5732		4353	
42	652	0984				1597	-	8824		3947		6927	1	7728		6311	i
43		3189		4475		3734	691	0927		6014		8959		9722		8268	1
44		5394		6646		5871		3029		8081	716	0989	728		740	0225	1
45		7598		8817		8007		5131	704	0147		3019	113	3710		2131	1
46	1 1			0987	679			7232		2213		5049		5703		4137	1
47	653	2004		3156		2278		9332		4278		7078		7695		6092	1
48		4206		5325				1432		6342		9106		9686		8046	
49	1	6498		7493		6547		3531								0000	1
50	0-	8609		9661		8681				0469		3161		3668	- 0	1953	1
51	004			1828	680			7728	17	2532		5187		5657	10	3905	
52		3010		3994		2946		9825		4594		7213		7646		5857	
53		5209		6160				1922		6655		9238		9635	1	7808	
54		7408		8326		7209		4018				$\frac{1263}{3287}$			740	9758	
55 56	655	1804		0490	601	9339 1469		8209		0776 2835		5310		5597	142	1708 3658	
57	000	4002		4818				0304		4894		7333		7583		5606	
58		6198		6981		5728		2398		6953		9355		9568	2	7554	
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5   5812   2845   913   0411   935   2380   968   5085   29131   55499   55006   55     6   512   0788   878   3556   5693   7384   969   674   34968   91388   61282     7   5775   8689   904   0979   936   3292   970   1962   46651   1-04   36645   73845   5085     9   57718   8935   905   1557   937   4216   7610   52497   09704   80132   51     10   844   0685   874   4067   6651   9883   5153   8917   64201   21838   92718   80132   51     11   5670   9201   906   2147   938   5153   8917   64201   21838   92718   80132   14   816   6038   876   4629   8153   945   15767   7058   83977   1-08   6321   4   16   6038   876   4629   8153   945   15767   7058   83977   1-08   6321   4   16   6038   876   4629   816   816   816   817   817   816   817							5131	1			9399							
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12   815   0655 875   4388   7446 930   0625   972   4575   70058   27904   99018   418   148   1845   6643   9478   970   2748   6101   973   0236   75918   33977   108   058281   47   1845   1845   0633   876   4620   8363   940   1579   974   1569   87649   46188   17939   4845   47   17   5617   873   0062   919   934   8038   875   2914   99394   58310   30573   4845   4848   4						026				971								
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17    5617 878   0069 9.99   3934   8038   975 2914   99894   58810   36781   43   43   6419   917   918   45   64   919   917   976   4272   11153   70498   43223   41   21   5631   831   0689 911   5265 944   0013   977 5643   22925   82702   55889   39   22 853 0640   5852 912   0592   5516   978 1333   28817   88869   62228   88   24   851   0667   6186 913   1255   6530   979 2724   40610   105 01034   74918   36   36   35   36   370   914   20   92   7556   989   424   46512   07153   81269   35   35   35   35   35   35   35   3				077		908		041		914				4	.6136			
18 819   0617   5215   9300 912   8523   8591   1010   5772   64402   36896   42   20   819   0624   5523   9940 943   4515   9956   17038   76598   49534   4512   21   5631   830   0689 911   5265 944   0013   977   5643   22925   82702   55889   39   22   850   0640   5852 912   0592   5516   978   1383   28817   88560   6228   88   22   853   0688   832   1357   6591 946   2042   8424   46512   07153   81269   55   555   555   944   1129   7027   34712   94920   68571   37   24   551   0667   6531   914   1299   7556   980   4127   52418   13275   87624   8424   46512   07153   81269   35   228   530   704   6531   914   1299   7556   980   4127   52418   13275   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   80512   7778   87624   8424   8612   8778   87624   8424   80513   8777   8725   916   8312   9646   6973   76074   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   87601   87604   8760						9.)9		J±L		975				5	8310			
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23   50   649   5552   912   0592   5516   978   1383   28817   88869   6228   88   5653   831   1017   5922   945   1021   7027   34712   94920   68571   37   24   851   1067   6186   913   1255   6530   979   2724   40610   1-05   1034   74918   36   36   37   37   37   37   37   37						911			4013	977								
24 851         0667         6186 913         1255         6580         979         2724         40610 1 0 5 01084         74918         36         25         5684         832         1857         6591 946         2042         8424         46512         07153         81269         35           26 852 0704         6531 914         1929         7556         980         4127         52418         18275         87624         34           27 5726 833         1707         7270 947         3074         9838         58386         19401         99884         38           29 5777         884         2068         7962 948         4119         982 1256         70155         31664         06714         31           30 551 0837         7630 917         4020 950         0709         83 2592         81997         43942         1940         98           33 5910 886         2322         9379         6245         985 2603         102 05723         66288         38610         26           36 557 1037         84155         5471 952         2871         986 1389         11664         74704         45002         25           37 6031 838         8619 920         0841         8420				037		912		JII										
25   5684   S32   1357,   6591   946   2042   8424   46512   07153   81269   85   2516   5732   5735   S33   1707   7270   947   8074   9838   58326   19401   93984   33   28   533   0750   6836   915   2615   8595   981   5543   64239   25531   1.09   00847   32   29   5777   854   2068   7092   948   4119   982   1256   70155   8164   06714   31   30   854   0837   7253   916   3812   9646   6973   76074   37801   13085   30   31   5839   855   2440   8665   949   5176   883   2692   81997   43942   19460   29   28   2553   7737   7630   917   4020   950   7079   8415   87923   50087   25640   28   33   5910   856   2322   9379   6245   984   4141   93858   56235   32223   27   28   28   28   28   28   28   28				831				945										
26 852 0704         6581 914 1929         7556         980 4127         52418         13275         87624         34           271 5726 883 1707         7270 947 3074         9833 58326         19401         93984 33         38           28 533 0750 6836 915 2515         8595 981 5543         64239         25531 109 00347         32           29 5777 894 2068         7962 948 4119         982 1256         70153         31664         06714         31           30 S51 9837         7253 916         3812 9646         6973 76074         37801         19460         29           31 5838 985 2440         8665 949 5176         983 2692         81997         43942         19460         29           32 557 6873         7630 917 4020 950 0709         8415         87923         50087         25540         28           35 5992 887 3215 919         9104         7326         984 4141         93553         50235         32232         27           48 53 0955         8017 918 4740 951         1784         9871         99786         62388         38610         26           35 5992 887 2215 919         1014         7326         85651         5471 952         8871         98786         8389         11664         74704				000		913		040		979				1.050	7150			
27          5728  583         1707          7270 947         8074         9888         58826          19401          99884         38           29          5777          884         2068         7082 948         4119         982         1256         70155         31664         06714         31           30         537         6387         7253         916         3812         9646         6673         76674         37801         13085         30           31          5898         852         449          8665         949         5176         983         2692         81997         43942         19460         29           32         855         0973         7630         917         4020         950         0709         8415         87923         50087         2540         28           33         5910         856         2322         9379         66245         984         4141         9851         9851         56235         32223         27           34         853         9351         8161         5471         952         985         5603         102         65723         66244         4500         252         36644 <t< td=""><td></td><td></td><td></td><td>334</td><td></td><td>914</td><td></td><td>9+0</td><td></td><td>980</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>				334		914		9+0		980								
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3	25635		38679	71030	22465		89108	57
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4 5 6 7 8 9	45182	44316	59866		45566	18750	14458	54
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19	30329	32916	52190	89484	38488 46270	24177	25019	41
20	36909	39763	59327	96933	54057	32331	33571	40
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22	50081	53472	73615	11848	69649	48658	50698	38
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26	76478	74071	1.21 02252	34260	93081 1·30 06904	73198 81390	76440 85034	34
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29		1.17 01691	23783	64219		1.05 06006	10860	31
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36	42773	49960	74199	16860	79457	63670	71367	24
37	49427	56888	81422	24402	87345	71934	80039	23
38	56085	63820	88650	31950	95239	80204	88718	22
39	62747	70756	95883		1.31 03140	88481	97405	21 20
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42	82761	91595	17613	62196	26876	13359	23506	18
43	89441	98551	24866	69772	34801	21653	32221	17
44		1.18 05512	32125	77353	42731	29963	40943	16
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46	09508	19447	46658	92532	58610	46602	58409	14
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4		8189		6877		3037		6641		7660		6066		1832	56
5		9854	1	8500		4618		8179	1	9155		7517	1	3239	5
6	820	1519	S30	0123	-	6199	1	9717	858			8967		4645	54
7		3183		1745	1	7778	849			2143				6051	55
8		4846	1	3366	1	9357		2790		3635		1866	1	7455	52
9		6509		4987	840		1	4325		5127		3314		8859	51
10		8170	1	6607	1	2513		5860		6619		4762	87		50
1	204	9832		8226	1	4090		7394	1	81(9		6209	1	1665	49
	521	1492	004	9845	1	5666	1000	8927	-	9599		7655	-	3067	45
3		3152	831		-	7241	850	0459	859			9100	1	4468	47
5		4811		3080	0.44	8816		1991		2576			1	5868	46
0		6469		4696	811	0390	-	3522		4064		1988		7268	45
6		8127		6312		1963		5053		5551	1	3431	1071	8666	44
7 8	322	9784		7927	i	3536		6582	1	7037		4874	87		43
9	5ZZ	1440	000	9541	i	5108		8111	1000	8523	1	6315		1462	42
0		3096	832	1155		6679	054	9639	860			7756		2858	41
1		4751		2768		8249	851			1491	1000	9196		4254	40 89
2		6405		4387	1040	9819	1	2693		2975	SCS		1	5649	1 38
3		8059 9712		5991	S42			4219	1	4457		2074		7043	37
	000	1364		7602		2956		5745		5989 7420	1	3512	1	8437	36
5	20	3015	000	9212 0822	1	4524 6091		7269 8793		8901	-	4949 6886	0=0	9830 3 1222	35
6		4666	000	2430		7657	852		861	0380			010	2613	34
7		6316					1892		901	1859		7821		4004	33
8		7965		4038 5646	1040	9222 0787	1	1839 3360	1	3337	070	9256 0691		5894	32
9		9614	1	7252	0.50	2351	1	4881		4815	1000	2124		6783	31
	24	1262		8858		3914		6402		6292		3557		8171	30
1			821	0463		5477		7921	ì	7768		4989		9559	29
2		4556	003	2068		7039		9440		9243	1	6420	879	C946	28
3		6202		3672		8600	853	0958	862	0717	1	7851	10.0	2332	27
4		7847		5275	811	0161	1000	2475		2191		9281		3717	26
5		9491	1	6877	011	1720		3992		3664	871	0710		5102	25
6 8		1135	1	8479	1	3279		5508		5137		2138		(48)	24
7		2778	835	0080	!	4838		7023		6608		3566		7869	23
8		4420		1680		6395		8538		8079		4993		9251	22
9		6062		3279		7952	S54	0051		9549		6419	880	0633	21
0		7703		4878		9508		1564	863	1019	-	7844		2014	20
1		9343		6476	845	1064		3077		2488		9269		3394	19
$2 \mid 8$	26	0983		8074		2618		4588		3956	872	0693		4774	18
3		2622		9670		4172		6099		5423		2116		6152	17
4		4260	836	1266		5726		7609		6889		3538		7530	16
5		5897		2862		7278		9119		8355		4960		8907	15
6		7534		4456		8830	855	0627	a al	9820		6381	881	0284	14
7	-	9170		6050	846	0381		2135	864	1284		7801		1660	13
8 8		0806		7643		1932		3643		2748	070	9221		3085	12
9		2440		9236		3481		5149		4211	873			4409	11
0		4074	837			5030		6655		5673		2058		5782	10
1		5708		2418		6579		8160		7134		3475		7155	9
2		7340		4009		8126	050	9664	COK	8595		4891		8527	8
3	00	8972		5593	047	9678	856	1168		0055		6307	000	9898	7
4 8	28	0 303	-	7187	847	1219		2671		1514		7722	882	1269 2688	6 5
5		2234	000	8775 0363		2765		4178 5674		2973	074	9137			4
6		3864	838	0868		4309		7175		4430	014	0550		4(07	3
7		5493	- 5	1950		5853		7175		5887		1963		5376 6743	
8 9		7121		3536 5121		7397 8939	857	8675		7344 8799		3375 4786		8110	2
	200	8749 0376		6706	949	0481	001	1673	988	0254		6197		9476	0
0 0		4		3°		0401 32°		1015 31°		0°		9°	-	28°	,

1	55°	56°	57°	58°	59°	60°	61°	1
0	1.42 81480	1.48 25610	1.53 98650	1.60 03345	1.66 42795	1.73 20508	1.80 40478	60
1	90326		1.54 08460		53766	32149	52860	59
1 2 3 4	99178	44231	18280	24082	64748	43803	65256	58
3	1.43 08039	53554	28108		75741	55468	77664	57
4	16906	62884	37946	44858	86744	67144	90086	56
5	25781	72223	47792	55260	97758	78833	1.81 02521	55
6	34664	81570	57647	65672	1.67 08782	90533	14969	54
7	43554	90925	67510	76094		1.74 02245	27430	53
8 9	52451	1.49 00288	77383		30864	13969	39904	52
	61356	09659	87264		41921	25705	52391	51
10	70268	19039		1.61 07417	52988	37453	64892	50
11	79187		1.55 07054		64067	49213	77405	49
12	88114	37822	16963	28349	75156	60984	89932	48
13	97049	47225	26880		86256		1.82 02473	47
14	1.44 05991	56637	36806	49320	97367	84564	15026	46
15	14940	66058	46741		1.68 08489	96871	27593	45
16	23897	75486	56685	70330		1.75 08191	40173	44
17	32862	84923	66639	80850	30765	20023	52767	43
18	41834	94367	76601		41919 53085	31866 - 43722	65374 77994	42 41
19		1.50 03821		1.62 01920				40
20 21	59861 68796	13282 22751	96552 $1.5606542$	12469 23029	64261 75449	55590	90628 1.83 03275	39
22	77798	32229	16540		86647	79362	15936	38
23	86808	41716	26548	44178	97856	91267	28610	37
24	95825	51210	36564			1.76 03183	41297	36
25	1.45 04850	60713	46590	65368	20308	15112	53999	35
26	13883	76224	56625	75977	31550	27053	66713	34
27	22923	79743	66669	86597	42804	39007	79442	33
28	31971	89271	76722	97227	54069	50972	92184	32
29	41027	98807		1.63 07867	65344		1.84 04940	31
30		1.51 08352	96856	18517	76631	74940	17769	30
31	59161		1.57 06936	29177	87929	86943	30492	29
32	68240	27466	17026	39847	99238	98958	43289	28
33	77326	37036	27126	5:528	1.70 10559		56099	27
34	86420	46614	37234	61218	21890	23024	68923	26
35	95522	56201	47352	71919	33233	35076	81761	25
36	1.46 04632	65796	57479	82630	44587	47141	94613	24
37	13749	75400	67615	93351	55953	59218	1.85 07479	23
38	22874	85012	77760		67329	71307	20358	22
89	32007	94632	87915	14824	78717	834(9	33252	21
40		1.5204261	98079	25576	90116	95524	46159	20 .
41	50296		1.58 08253		1.71 01527	1.78 07651	59080	19
42	59452	23545	18436	47111	12949	19790	72015	18
43	68616	332.00	28628	57893	24382	31943	84965	17
44	77788	42863	38830	68687	35827	44107	97928	16
45	86967	52535	49041	79490	47283	56285	1.86 10905	15
46	96155	62215	59261	90304	58751	68475	23896	14
47 48	1.47 05350	71904			70230	80678	36902	13 12
48	$\begin{array}{r} 14553 \\ 23764 \end{array}$	81602 91308	79731 89979	11963 22808	81720 93222	92893 $1.7905121$	49921 62955	11
50		1.53 01023			1.72 04736	17362	76003	10
51	42210	10746	10505	44529	16261	29616	89065	9
52	51445	20479	20783	55405	27797		1.87 02141	8
53	60688	3.219	31070	66292	39346	54162	15231	7
54	69938	39969	41366	77189	56905	66454	28336	6
55	79197	49727	51672	88097	62477	78759	41455	5
56	88463	59494	61987	99016	74060	91077	54588	4
57	97738	69270		1.66 09945	85654	1.80 03408	67736	3
58	1.48 07021	79054	82647	20884	97260	15751	80898	2
59	16311	88848	92991	31834	1.73 08378	28108	94074	ĩ a
60	25610		1.60 03345	42795	2.508		1.88 07265	Ô
1	34°	33°	32°	S1°	300	29°	28°	1
	1 01	0			0.,		20	
			NATITI	DAT COTAL	CENTO			

,	62°	68	3°	6	4°	(	35°	1	36°	1	37°	(	88°	1
0	882 9476	891 0	0065	898	7940	906	3078	913	5455	920	5049	927	1839	60
1	883 0841	1	385		9215	1	4307	1	6637	1	6185	1	2928	59
2	2206		705	899	0489		5535	1	7819	1	7320		4016	58
3	3569		1024		1763		6762	1 3	9001		8455	1 3	5104	57
4	4933		342		3035		7989	914	0181		9589		6191	56
5	6295		659		4307	-	9215		1361	921	0722	1 6	7277	55
6	7656		975		5578	907	0440		2540		1854		8363	54
4 5 6 7 8	9017 884 0377	892 0	291		6848 8117		1665 2888		3718 4895		2986 4116	000	9447	53 52
9	1736		920		9386		4111		6072		5246	928	0531 1614	51
10	3095		234	900	0654	-	5333	100	7247		6375		2696	50
11	4453		546	200	1921		6554		8422		7504		3778	49
12	5810		858		3188		7775		9597	100	8632	1	4858	48
13	7166		169		4453		8995	915			9758		5938	47
14	8522	8	3480		5718	908	0214	1	1943	922			7017	46
15	9876		789		6982	1	1432		3115		2010		8096	45
16	885 1230	893 1			8246		2649		4286		3134	1 2	9173	44
17	2584		406	004	9508		3866		5456		4258	929	0250	43
18	3936		3714	901	0770		5082	1	6626		5381		1326	42
19	5288		021		2031		6297		7795		6503		2401	41
20 21	6639 7989		632		3292		7511 8725	010	8963 0130	1	7624		3475	40 39
22	9339		936		4551 5810		9938	910	1297		8745 9865		4549 5622	28
23	886 0688	894 0			7068	909	1150		2462	923			6694	37
24	2036		542		8325	1000	2361		3627	020	2102		7765	36
25	3383		844		9582		3572		4791		3220		8885	35
26	4730		146	902	0838		4781		5955		4336		99(5	34
27	6075		5446		2092		5990		7118		5452	930	0974	33
27 28	7420	6	3746		3347		7199		8279		6567		2042	32
29	8765		045		4600		8406		9440		7682		31(9	31
30	887 0108		344		5853	1	9613	917	0601		8795	-	4176	30
31	1451	895 0			7105	910	0819		1760	1	9938		5241	29
32	2793		938		8356		2024		2919	924	1020		6306	28
33	4134		3234 1529	903	9606		3228		4077		2131		7370 8434	27
34 85	5475 6815		824	900	0856 2105		4432 5635		5234 6391		3242 4351	1 3	9496	26 25
36	8154		118		3553		6837		7546		5460	931		24
37	9492		411		4600		8038		8701		6568	301	1619	23
38	888 0830		703		5847		9238		9855		7676		2679	22
39	2166	896 C			7093	911	0438	918	1009		8782		3739	21
40	3503		285		8338	1	1637	1	2161		9888		4797	20
41	4838		575		9582	1	2835		3313	925	0993	1	5855	19
42	6172		864	904	0825		4033		4464		2097		6912	18
43	7506		153		2068		5229		5614		3201		7969	17
44	8839		440		3310		6425		6763		4303	000	9024	16
45	889 0171		727		4551		7620		7912		5405	932	0079	15
46 47	1503 2834	897 0	299		5792 7032	010	8815 0068	010	9060 0207		6506 7606		1133 2186	14
48	4164		584		8271	912	1201	319	1353		8706		3238	12
49	5493		868		9509		2393		2499		9805		4290	11
50	6822			905	0746	1	3584		3644	926	0902	-	5340	10
51	8149		433	-00	1983		4775		4788	1	2000		6390	9
52	9476	7	715		3219		5965		5931		3096		7489	8
53	890 0803	8	996		4454		7154		7073		4192		8488	7
54	2128	893 0			5688		8342		8215		5286	1 2	9535	6
55	3453		555		6922		9529		9356		6380	933	0582	5
56	4777		834		8154	913	0716	920	0496		7474		1628	4
57	6100		112	000	9386		1902		1635		8566		2673	3
58	7423			906	0613	-	3087		2774	007	9658		3718	2
59	8744 891 0065		940		1848 3078		4271 5455		3912 5049	927	0748 1839		4761 5804	1 0
60														

'	62°	63°	64°	65°	66°	67°	68°	′
0	1.88 07265	1.96 26105						60
1	20470					77590		59
2	33690	54364	33349	77683	95580	96683	92386	58
3	46924	68518	48531	94021	2.25 13221	2.36 15801	2.48 13190	57
4	60172	82688		2.15 10378	30885			56
5	73436	96874	78950	26757	48572	54118	54887	55
6		1.97 11077	94187	43156	66283	73316		54
7	1.89 00006		2.06 69442	59575	84016	92540	96706	53
8.	13313	39531	24716				2.49 17660	52
9	26635	53782	40008	92476	19554		38645	51
10	39971	68050		2.16 08958	37857	50372	59661	50
11	53322	82334	70646	25460	55184	69703	80707	49
12	66688	93635	85994	41983	73035		2.50 01784	48
13		1.98 10952		58527	90909	2.38 08444		47
14	93464	25286	16743		2.27 08807		44029	45
15	1.90 06874	39636	32146	91677	26729 44674	47293 66758	65198 86398	40
16	20299	54003 68387		2·17 08283 24011	62643	00100	2.51 07629	43
17	33738 47193	82787	63007	41559		2.39 05769	28890	42
18 19	60663	97204	78465	58229	98653		50183	41
20		1.99 11637	93942	74090	2.28 16693	44889	71507	40
21	87647	26087		91631	34758	64490		39
	1.91 01162	40554	24953	2.18 08364	59946	24110	2.52 14249	38
23	14691	55038	56039	25119	70050	84118 2·40 03774	35667	37
24	23236	69539		41894	89096	23457	57117	36
25	41795	84056	71610 87200	59801	2.29 07257	43168	78593	35
26	55370		2.09 02809	75510	25442		2.53 00111	34
27		2.00 13142			43651	82672	21655	33
28	32565	27710	10401	92349 2·19 09210	61885	2.41 02465	43231	32
29	96186	42295	49751	26093	80143	22286	64839	31
	1.92 09821	56897	65436	42997	98425	42136	86479	30
31	23472	71516	81140		0 90 16790	69019	2.54 08151	29
32	37138	86153	06964	76871	35064	$\begin{array}{r} 81918 \\ 2.42\ 01851 \\ 21812 \end{array}$	29855	28
33	50819	2.01 00806	2.10 10007	93840	53420	2.42 01851	51591	27
34	64516	15477	28369	2.20 10831	71801	21812	73359	26
35	78228	30164	44150	27843	90206	41801		$\tilde{25}$
36	91956	44869	59951		2.31 08637	61819	2.55 16992	24
37	1.93 05699	59592	75771	61934	27692	81864 2·43 01938 22041	38858	23
38	19457	74331	91611	79012	455.71	2.43 01938	60756	22
39	33231		2 11 07470	96112	64076	22041	82686	21
40	47020	2.02 03862	23348	2.21 13234	82606	42172	2.56 04649	20
41	60825	18654	39246	30379	2.32 01160	62331	26645	19
42	74645	33462	55164	47545	19740	82519	48674	18
43	88481	48289	71101	64733	38345	2.44 02736	70735	17
44	1.94 02333	63133	87057	81944	56975	22982	92830	16
45	16200	77994	2.12 03034	99177	75630		2.57 14957	15
46	30083	92873	19030	2.22 16432	94311	63559		14
47		2.03 07769	35046	33709	2.33 13017	83891	59312	13
48	57896	22683	51082	51009		2.4504252	81539	12
49	71826	37615	67137	68331	50505		2.58 03800	11
50	85772	52565	83213	85676	69287	45061		10
51	99733	67532	99308	2.23 03043	88095	65510	48421	9
	1.9513711	S2517 9	2.13 15423		2.34 06928	85987		8 7
53	27704	97519	31559	37845	25787	2.46 06494	93177	6
54		2.04 12540	47714	55280	44672		2.59 15606	6
55	55739	27578	63890	72738	63582	47596	38068	5
56	69780	42634	82085	90218	82519	68191	60564	4
57	83837	57708	93301	2.24 07721	2.35 01481	88816	83095	3
58	97910	72800	2.14 12537	25247		2.47 09470		$\frac{2}{1}$
59	1.96 12000	87910	28793	42796	39483	30155		
60	26105	2.0503038	45069	60368	58524	50869	50891	0
,	27°	26°	25°	24°	23°	$22^{\circ}$	21°	

1	1	69°	1	70°	1	71°	1	72°	T	73°	T	74°		75°	,
Texas	0	933 5804	939	6926	945	5186	951	0565	956	3048	961	2617	96	5 9958	60
2         7888 S         8914 (17078 238)         2385 (1507)         5593 (1007 1891)         9917 (1891)         9918 (1508)         5593 (1007 1891)         9911 (1795 1638)         5593 (1007 1891)         9911 (1795 1638)         5693 (1796)         2268 (1798)         5693 (1798)         3661 (1798)         3661 (1798)         3661 (1798)         3683 (1798)         3761 (1			000		1		00.		1000		001				59
8         8928         999, 994         809         8968         4154         643         5595         5019         1512         5         5 934         1007         1891         9511         5050         7290         6616         3012         5           7         3082         3871         1795         6888         8981         8210         4508         3           8         4119         4860         2736         7781         9925         9005         5255         55           10         6189         6835         4616         9514         1512         992         6090         5255         55         5255         592         0404         2354         1887         7480         212         8257         8808         6493         1294         2384         4835         2972         8914         6746         541           11         7223         7523         7822         5555         592 0404         2384         1887         7490         6615         2972         8917         466         5012         7490         941         747         441         2354         4852         967         0449         441         747         441 <t< td=""><td></td><td>7888</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>1</td><td></td><td>58</td></t<>		7888											1		58
5         994 1007         1891         9911         5050         7290         6616         3012         5           6         2045         581         46 (6854)         5944         8136         7418         4508         5           8         4119         4860         2736         7781         9925         9905         5255         52         525         52         51         5255         52         51         6888         8981         18210         6646         560         6616         9890         6601         5255         52         6698         1820         6646         6646         564         1887         7490         4646         564         1887         7490         8414         935         2821         941         0777         8806         3071         4875         3762         9718         449         7430         2188         4085         2972         8977         441         935         2821         941         0777         8806         3071         4875         3762         9718         44         971         9718         44         972         9714         4952         967         0459         9718         44         972 <td< td=""><td>3</td><td>8928</td><td>1</td><td>9917</td><td></td><td>8023</td><td></td><td>3258</td><td></td><td>5595</td><td></td><td>5019</td><td></td><td></td><td>57</td></td<>	3	8928	1	9917		8023		3258		5595		5019			57
6         2045         2881         946         6854         5944         8136         7413         3761         58           8         4119         4568         2736         7731         9825         9905         5255         55           9         5154         5548         3677         8623         957         0609         9890         6001         51           10         6189         6835         4616         9514         1512         902         6594         6746         51           11         7223         7822         5555         392         0404         2354         1387         7490         44           12         8257         8808         6931         1944         3175         2185         2183         2184         4185         2187         474           14         935         6321         941         0717         8366         3971         4875         3762         971         44           16         2382         2143         947         223         4814         4875         3762         971         44           16         2382         214836         3872         4914         2	4		940				1								56
8         4119         4860         2736         7731         9525         9905         6901         5255         10           10         6189         6835         4616         9514         1512         962         0594         6746         51           11         7223         7822         5555         952         0404         2354         1387         7490         44           12         8257         8808         6493         1294         3195         2185         8234         48           13         9280         9793         7430         2183         4035         2972         8977         47           15         1552         1769         9301         3958         5714         4552         9670         49718           16         2332         2243         947         036         4844         6552         5842         120         6495         6665         3965         57499         9060         7704         3411         120         6655         3965         7499         9060         7704         3415         44         450         92         85517         8993         5840         44152         44         450 <td>5</td> <td></td> <td></td> <td></td> <td>1</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>55</td>	5				1										55
8         4119         4860         2736         7731         9525         9905         6901         5255         10           10         6189         6835         4616         9514         1512         962         0594         6746         51           11         7223         7822         5555         952         0404         2354         1387         7490         44           12         8257         8808         6493         1294         3195         2185         8234         48           13         9280         9793         7430         2183         4035         2972         8977         47           15         1552         1769         9301         3958         5714         4552         9670         49718           16         2332         2243         947         036         4844         6552         5842         120         6495         6665         3965         57499         9060         7704         3411         120         6655         3965         7499         9060         7704         3415         44         450         92         85517         8993         5840         44152         44         450 <td>6</td> <td></td> <td></td> <td></td> <td>946</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>54</td>	6				946										54
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14         935         0321         941         0777         8366         3971         4875         3762         9718         44           15         1352         1760         9301         3958         5714         4552         967         0459         44           16         2382         2743         947         0236         4844         6552         5842         1290         44           17         3412         3724         1170         5730         7889         6130         1999         44           18         4440         4705         2103         6615         8225         6917         2673         45           20         6495         6665         3906         8882         9895         8490         4152         40           21         7521         7644         4597         9264         958         6720         9275         4888         39           22         8547         8621         5527         953         0146         1562         963         0060         5624         38           23         9571         9598         6676         1027         2994         084         6858 <td< td=""><td></td><td></td><td>1</td><td></td><td></td><td></td><td>1</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>			1				1								
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24         936         0595         942         6575         7684         1997         3226         1626         7692         38           26         2641         2525         9598         3864         4856         3189         8557         34           27         3662         3498         948         0464         4542         5715         3969         9288         38           28         4663         4471         1889         5418         6543         4478         968         0618         32           29         5703         5444         2313         6294         7371         5527         0748         31           30         6722         6415         8237         7170         8197         6305         1476         30           31         7749         7386         4159         8044         9023         7081         2204         29           22         8758         8355         5081         8917         948         7858         2931         28           33         9774         9324         6002         9790         959 0672         8683         3658         27           35 <td< td=""><td>23</td><td></td><td>-</td><td></td><td></td><td>6756</td><td>1</td><td></td><td>-</td><td></td><td></td><td></td><td></td><td></td><td>87</td></td<>	23		-			6756	1		-						87
26           2641           2525           9583           3664           4886           3189           5557           328             27           3662           3493           948           464           4542           5715           3909           9288           328             28           4683           4471           1889           5418           6543           4748           968           6618           329             29           5703           5444           2313           6294           7371           5527           0748           31             30           6722           6415           3237           7170           8197           6805           1476           30             31           7740           7386           4159           8044           9023           7081           2204           29             32           8774           9824           6002           9790           950           6672           8688           3688           268           2520           2227           8760           2403           3140           6954           5832           244             37           3833           3192           9678           3273           3961           1		936 0595	942					1907	1	3226	1			7092	36
27         3662         3498         948         0464         4542         5715         8969         9288         83           29         5703         5444         1880         5418         6543         4748         968         0618         32           29         5703         5444         2313         6294         7371         5527         0748         31           30         6722         6415         3237         7170         8197         6305         1476         30           31         7749         7386         4159         8044         9023         7081         2204         29           32         8758         8355         5081         8917         9848         7858         2931         28           34         937 0790         948         0293         6922         954         6662         1496         9407         4383         26           35         1806         1260         7342         1533         2318         964         0181         5108         25227         8760         2403         3140         0.954         5832         24           37         3833         3192         99078	25	1618	13	1559				2786	1	4056		2408			35
29         4683         4471         1889         5418         6543         4748         968 0618         32           29         5703         5444         2313         6294         7371         5527         0748         32           30         6722         6415         3237         7170         8197         6305         1476         30           31         7740         7386         4159         8044         9023         7081         2204         29           32         8758         8355         5081         8917         9848         7858         2931         28           34         937 0790         943 0293         6922         954 0662         1496         9407         4383         265           35         1806         1260         7342         1533         2318         964 0181         5108         25           36         2820         2227         8760         2403         3140         0954         5882         24           37         3833         3192         9678         3273         3961         1726         6555         23           38         4816         4157         940 6595							-	3664		4886		3189		8557	34
29         5763         5444         2313         6294         7871         5527         0748         31           30         6722         6415         8237         7170         8197         6305         1476         32           31         1774         7386         4159         8844         9023         7081         2204         29           32         8758         8355         5081         8917         9848         7858         2931         28           33         9774         9324         6002         9799         950         6072         8638         3658         27           34         937 0790         948 0293         6922         954 0662         1496         9407         4383         26           35         1866         1260         7342         1533         2318         964 0181         5108         254         6655         22         27         8760         2403         3140         9674         5832         24         37         3833         3192         9673         2973         3961         1726         6555         23         23         88         4846         4157         940 0595         4141	27				948						= 1	3969			33
89         6722         6415         8237         7170         8197         6805         1476         29           81         7740         7366         4159         8044         9023         7081         2024         29           82         8758         8355         5081         8917         9848         7858         2981         28           83         9774         9824         6002         9790         959         0672         8638         3658         2981         28           84         987         790         943         7851         1496         9407         4888         26           55         1806         1260         7842         1583         2318         964         0181         5108         25           36         2820         2227         8760         2403         3140         0.954         5832         24           37         3838         3192         94078         8273         3961         1726         6555         23           38         4846         4157         940 6595         4141         4781         2497         7277         22           40         6869         <	28												968		
81         7740         7386         4159         8044         9023         7081         2204         2204         283         9774         9824         6002         9790         9848         7858         2931         28         38         9774         9824         6002         9790         959         6672         8638         3658         27         34         937         0790         943         0293         6922         954         6662         1496         9407         4383         26         35         1806         1260         7842         1593         2318         964         0181         5108         25         36         2820         2227         8760         2403         3140         0954         6582         24         37         3833         3192         9078         3273         3961         1726         6555         23         38         4846         4157         940         6595         44141         4781         2497         7277         22         24         4411         7850         7048         3341         6743         7236         4806         9438         19         42         8859         8910         4255         7608         8953	29				-				-				1 0		
82         8758         8355         5081         8917         9848         7858         2931         28           34         937 0790         948         0922         954 0662         1496         9407         4383         26           35         1806         1260         7342         1533         2318         964         0181         5108         252           36         2520         2227         7860         2403         310         9673         8273         3961         1726         6555         23           37         3833         3192         9673         8273         3961         1726         6555         23           38         4846         4157         940         6595         4141         4781         2497         7277         22           40         6869         6635         2426         5876         6418         4037         8719         20           41         7889         7048         3341         6743         7236         4806         9438         19           42         8889         8971         5168         8473         88653         5574         969         0157         13	30					3237		7170			-				
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85         1806         1260         7842         1583         2918         964         9181         5108         25         2483         3140         0.954         5882         24         37         3833         3192         9978         8278         3901         1726         6555         23         28         8446         4157         940         6595         4141         4781         2497         7277         22         7277         22         1511         5069         5600         3268         7998         21         40         6869         6685         2426         5876         6418         4037         8719         20         41         7850         7048         3341         6748         7296         4806         9438         19         42         8889         8971         5168         8473         8699         6341         6875         11         43         9898         8971         5168         8473         8699         6341         6875         18         44         9898         8971         5689         9960         6499         7873         2369         15         44         9389         991         6889         9936         6844         7108         <							~~ .		959				-		
88         2820         2227         8760         2403         8140         6954         5832         24           37         3833         3192         9678         8273         3961         1726         6555         24           38         4846         4157         940         6595         4141         4781         2497         7277         22           39         5558         5122         1511         5069         5600         3268         7998         21           40         6869         6685         2426         5876         6418         4037         8719         20           41         7580         7048         3341         6743         7236         4806         9488         19           42         8859         8810         4255         7608         8053         5574         969         0157         18           43         9808         8971         5168         8473         8869         6341         6875         17           44         938         6931         6680         9931         6680         9550         9960         4999         7873         2309         15 <td< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td>904</td><td></td><td>1</td><td></td><td>001</td><td></td><td></td><td></td><td></td></td<>							904		1		001				
87         8933         3192         9673         8273         8961         1726         6555         23           89         4846         4157         940         6595         4141         4781         2497         7277         72           89         5558         5122         1511         5069         5600         3268         7993         21           40         6869         6685         2426         5876         6418         4037         8719         20           41         7880         7048         3341         6743         7236         4806         9438         19           42         8889         8971         5168         8473         8869         6341         6875         13           43         9888         8971         5168         8473         8869         6341         6875         17           44         938         (996         9931         6689         9386         9684         7108         1593         164           49         131         944         6890         6991         955         6199         960         0499         7873         2309         15           4											964				
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89         5553         5122         1511         5069         5600         3268         7998         21           40         6869         6085         2426         5876         6418         4037         8719         20           41         7880         7048         3341         6743         7236         4806         9438         19           42         8889         8910         4255         7608         8053         5574         99 0157         18           43         9898         8971         5168         8473         8869         6341         (875)         17           44         938         (936)         9931         6080         9336         960         499         7183         2369         16           45         1913         944         (890         6091         955         6199         960         499         7873         2369         16           46         2920         1819         7912         1062         1912         868         8025         14           47         3925         2807         8812         1023         2125         9402         3740         13 <td< td=""><td>90</td><td></td><td></td><td></td><td>0.40</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>	90				0.40										
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0	2.60 50891	2.74 74774	2.9042169	3.07 76835	3-27 08526	3.48 74144	8.78 20508	60
ı				3.08 07325		3.49 12470		59
2		2.75 24588	97089	37869	76715		3.74 07546	58
3			2.91 24649		3.28 1(907			57
4			52256	99122		3.50 27916		56
5	64571			3.09 29831			3.75 38815	55
6	87411	2.76 24695 2	2.92 07610:	60596		8.51 05273		54
7	2.62 10286		35358	91416	48330		3.76 26807	53
8	33196	74990		3.10 22291	82851	82946	70947	52
9		2.77 00199	90995.	53223	3.30 17438	3.52 21902	3.77 15185	51
10	79121		93 18885	84210	52091	6(938)		50
11	2.63 02136	50738.	46822	3.11 15254		3.53 00054	3.78 03951	49
12	25186	76069	74807	46353	3.31 21598	89251	48481	48
13	48271	2.78 01440 2	94 02840	775(9	56452	78528	93109	47
14	71392	26853	30921	3.12 08722	91373	3.54 17886	3.79 37835	46
15	94549	52307	59050	39991	3.32 26362	57325	82661	45
16	2.64 17741	77802	87227	71317	61419		3.89 27585	44
17		2.79 03339 2				3.55 36449	72669	43
18	64232	28917	43727		3.33 31736		3.81 17733	42
19	87531	54537	72050	65639		3.56 15900		41
20	2.65 10867		.96 00422		3.34 02326		3.8208281	40
21		2.80 05901		3.14 28807	37724	95681	53707	59
22	57645	31646	57312	60478		3.57 35696	99233	38
23	81089	57433	85831		3.35 08728		3.83 44861	37
24	2.66 04569			3.15 23994		3.58 15975	90591	36
25		2.81 09134	43016	55840	80008		3.84 36424	35
26	51638	35048	71683		3.36 15753	96590	82358	34
27	75227		93 00400 8			3.59 37024		33
28	98853	87003	29167	51728	87453	77543	74537	32
29	2.67 22516		57983			3.60 18146		31
30	46215	39129		3.17 15948	59434	58835	67131	30
31	69951		99 15766	48147	95531		3.87 13584	29
32	93725	91426	44734		3.38 31699 8		60142	28
33	2.68 17535		00 02820	18 12724	67938 3·39 04249 8		3·88 06805 58574	27 26
34 35	41383 65267	70196	31939	77540	40631		3.89 00448	25
36	89190	96539		19 10039		3.63 04771	47429	24
37	2.69 13149 9		90830		3.40 13612	46064	94516	23
38	87147		01 19603	75217	50210		3.90 41710	22
39	61181	75831		20 07897	86889 9	3.64 28911	89011	21
40		2.85 02349	78301		3.41 23626			20
41	2.70 09364		02 07728	73440		3.65 12111		19
42	33513	55517		21 06304	97333			18
43	57699	82168	66737		42 34297	95665		17
44		2.86 08863	96320	72215		3.6637575		16
45	2.71 06186			22 05263 3		79575		15
46	30487	62386	55641	38373,	45631 8	667 21665 3		14
47	54826	89215	85381	71546	82991	63845		13
48		2.87 16088 3		23 04780 3			95 19615	12
	2.72 03520	43007	45018	38078	57635	48475		11
50	28076	69970	74915	71438	95120	90927,3	96 16518	10
51	52569			24 04860 3			65137.	9
52	77102 2	2.88 24033	34870	38346	70315		97 13868	8
	2.73 01674	51132	64928		·46 08026 3	70 18830	62712	7
54	26284	78277		25 05508	45813		98 11669	6
55		989 05467 3		39184		71 04558.	60739	5
56	75623	32704	55421		47 21616		99 09924	4
	2.74 00352	59983		26 06728	59632	90658	59223	3
58	25120	873143		40596		72 33847 4		2
59		90 14688	46400		48 35896	77131	58165	1
60	74774	42109		27 08526		73 20508 4		0
1	20°	19°	18°	17°	16°	15°	140	

1   3661   4355   2080   6826   582 9877 338 9	82° ' 902 681 60 903 085 59
1 3661 4355 2080 6826 582 9877 338 9	903 085 59
2 4363 5008 2684 7380 9849 686 792	489 58
8 5065 5660 3287 7933 589 9878 245	891 57
4 5766 6311 3889 8485 9850 091 697 9	904 293   56
5 6466 6932 4499 9037 593 9879 148	694   55
6 7165 7612 5599 9587 9851 693 599 9 7 7863 8261 5689 982 0137 593 9880 048 9	905 095 54 494 53
8 8561 89.9 6288 0686 9852 692 497	$ \begin{array}{c cccc} 494 & 53 \\ 893 & 52 \end{array} $
9 9258 9556 6886 1234 590 945 0	906 290 51
10 9953 975 0203 7483 1781 9853 087 9881 392	687 50
	907 083 49
12     1343     1494     8674     2873     9854     079     9882     284       13     2086     2183     9268     3417     574     728	478 48
	908 266 46
15 3421 3423 379 0455 4504 561 615	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
16 4112 4065 1047 5046 9856 053 9884 057 98	909 051 44
17 4832 4706 1638 5587 544 498	442 43
18 5491 5345 2228 6128 9857 635 939	832 42
	910 221 41
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	997   39
23   8926   8533   5167   8818   9859 475   9887 128	770 37
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25 972 0294 9802 6337 9888 9860 445 998	540 35
26 0976 976 0435 6921 983 0422 929 9888 432	923 34
	013 306 33
28 2339 1699 8086 1487 894 9889 297 99 3020 2330 8668 2019 9862 375 728 98	688   32
29   3029   2330   8668   2019   9852 375   728   98 30   3699   2930   9247   2549   856   9890 159	014 069   31 449   30
31 4378 3589 9827 3079 9863 836 588	828 29
	015 206 28
33   5733   4845   0983   4136   9864 293   445	584 27
34 6409 5472 1560 4663 770 872	951   26
	016 337 25
$egin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$egin{array}{c c c c c c c c c c c c c c c c c c c $	459 23
39 9777 8593 4433 7286 9867 143 994	832 21
40 973 0449 9215 5005 7808 615 9894 416 99	18 204   20
41 1119 9836 5576 8830 9868 087 838	574 19
42 1789 977 0456 6147 8850 557 9895 258	944 18
	19 314 17 682 16
44     3125     1693     7285     9880     496     9896     096       45     3793     2311     7853     984     0407     964     514     99	
46 4459 2928 8420 0924 9870 481 931	416 14
47 5124 3544 8986 1441 897 9897 847	782 13
48   5789   4159   9552   1956   9871 363   762   99	21 147   12
49 6453 4773 981 0116 2471 827 9898 177	511 11
50 7116 5387 0680 2985 9872 291 590 590 590 590 590 590 590 590 590 590	874 10
51     7778     5999     1243     3498     754     9899     903     99       52     8439     6611     1805     4010     9873     216     415	22 237   9 599   8
$egin{array}{c c c c c c c c c c c c c c c c c c c $	959 8
54 9760 7832 2927 5032 9874 188 9900 237 99	
55 974 0419 8442 3486 5542 598 646	679   5
56   1077   9050   4045   6050   9875 057   9901 055   99	24 037 4
57 1734 9658 4608 6558 514 462	394 3
58   2390 978 0265   5160   7666   972   869   59   8046   0871   5716   7572 9876 428 9902 275 99	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
59         8046         0871         5716         7572         9876         428         9902         275         99           60         3701         1476         6272         8078         883         681         681	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
' 13' 12° 11° 10° 9° 8°	7° '
Namer Day Course	

			-		-			
,	76°	770	78°	79°	80°	81°	82°	1
0	4.01 07809	4.33 14759	4.70 46301	5.14 45540	5.6712818	6.3 137515	7.1 153697	60
1	57570		4.71 13686	5.15 25557	809446		304190	59
2		4.34 30018		5.16 05813	906394	376126	455308	58
3	57440		4.72 49012		5.7 003663	496092	607056	57
4		4.35 45861			101256	616502	759487	56
5		4.36 04003	80083	5.18 48035	199173	737359	912456 $7.2066116$	55 54
67	4.04 08125	4.37 20731	4.14 99401	5.19 29264	297416 895988	980422	220422	53
8	4.05 09174		90603			6.4 102633	375378	52
9	50877	4.38 38054			594122	225301	530987	51
10	4.06 10700	96940	4.77 28568	5.22 56647	693688	348428	687255	50
11		4.39 55977	97837	5·22 56647 5·23 39116	793588	472017	844184	49
12	4.07 12707	4.40 15164	4'78 67300	5.24 21836	893825		7.3 001780	48
13	63892		4.79 36957		994400	720591	160047	47
14	4.08 15199	4.41 33996	4.80 06808		5.8 095315	845581	318989	46
15	66627	93641		5.26 71517	196572	971043	478610	45
16		4.42 53439				6.5 096981	638916	44
17		4.43 13392			400117	223396	799909	43
18	4.10 21649	73500	88174	5.29 23505	502410	350293	961595	42
19- 20		4.44 33762	4·83 59010 4·84 30045	92793	605051 708042	605538	7·4 128978 287064	41
21	4.11 25614	4.45 54756			811386	733892	450S55	39
22		4.46 15489		5.32 63131	915084	862739	615357	38
23	82499			5.33 48696		992080	780576	37
24		4.47 37428	1.87 16201	5.34 34527		6 6 121919	946514	36
25	87719	98636		5.35 20626	228322		7.5 113178	35
26		4.48 60004 4			333455	383100	280571	34
27	93446	4.49 21532		93630	488952	514449	448699	33
28	4.15 46501		1.90 05620		544815	646307	617567	32
29	99685	4.50 45072		5.88 67718	651045	778677	787179	31
30		4.51 07085 4			757644	911562	957541	30
31	4.17 06440		1.92 24859			3.7 044966 7		29
32 33		4.52 31601	95555	5·41 30906 5·42 19188	971957	178891	300533	28
34	4.18 13713	4.53 56773 4	1:04 45000	5-42 19100 (	187772	313341 448318	473174 6465S4	27 26
35		4.54 19608 4		96592	296247	583826	820769	25
36	75606	82608		5.44 85715	405103	719867	995735	24
37	4.20 29835	4.55 45776 4	96 69037	5.45 75121	514343		7.7 171486	23
38	84196	4.56 09111 4	97 43817	5.46 64812	623967	993565	348028	22
39	4.21 38690	72615 4	98 18813	5.47 54788		3.8 131227	525366	21
40	93318	1.57 36287		5.48 45052	844381	269437	703506	20
41	4.22 48080	4.58 00129 4	99 69459	5.49 35604	955174	408196	882453	19
	4.23 02977	64141 5	00 45111	5.50 26446 (				18
43		4.59 28325 5			177943	687878		17
44 45	4.24 13177	92680	97018	5.52 09005	280923	827897	424191	16 15
46	4.25 22029	4·60 57207 5 4·61 21908 5	02 10000	09740	402303	968799 3.9 110859	606423	14
47	79501	867885	04 26700	554 85052	628272	252489		13
48	4.26 35218	1.62 51832 5	05 03690	5.55 77663	741865			12
49		1.63 17056	80907	5.56 70574	855867	538478	343758	11
50	4.27 47066	82457 5	06 58352 5	5.57 63786	970279	682335	530224	10
51	4.28 03199	1.64 48034 5	07 36025	5:58 57302 6	3.2 (85106	826781	717555	9
52	59472	1.65 13788 5	08 13923	5 59 51121	200347	971806	905756	8
53	4.29 15885	79721		5.60 45247		0 117411 8		7
54	72440 4	1.66 45832 5	09 70426	5.61 39680	432086	263662	284796	6
55		1.67 12124 5			548588	410482	475647	5
56 57	85974		11 27855 5		665515	557905	667394	4
58	4·31 42955 4 4·32 00079 4	1.63 45248 5		5.65 20516	782868	705934	860042	3
59	57847	79100	12 65769	5.66 16509 6	900651	9 61 05500 Lt	248071	1
60		1.70 46301 5	14 45540	5.67 12818	137515	153697	443464	0
1	13°	12°	11°	10°	90	8°	120404	1
	10	14	- 11	10	1 1	0 1		
			NATUR	AT COTAN	OPNING			

′		83°	8	34°	8	5°	8	6° .	8	37°	8	88°-	8	9°	
0	992	5 462	9945			647			9980			908	9298	3 477	16
1	1	816		523	9962	200		843		447	9994	009		527	1 5
2	9926	169		825		452		045		598		110		577	1
3		521	9946	127		704			1	748	-	209		625	5
4	1	873	1	428		954		445	1.0	898		308		673	5
5	9927	224		729	9963	204		645	9987	7 046		405	1	720	5
6	-	573	9947		1	453		843		194		502	13.	766	5
7	777	922		327		701	9977	.040		340		598		812	5
8	9928			625	1	948		237	-	486		693		856	5
9		618		921	9964	195		433		631	111	788	100	900	5
10	113	965	9948	217	1	440	1	627	1	775		881	1	942	5
11	9929	310		513		685	9978	821	1	919	1	974		984	4
12		655		807		929	9978	015	9988	061	9995		9999	025	4
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14	9930	342		398		414		399	1	344 484		247	-	105	4
15	1	685		685	2	655	1	589		484		336	111	143	4
16	9931		1	976		895	1	779	-	623	1.01	477		181	4
17		367	9950		9966		-	968		761	-	512 599 684		218	4
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	6932			844		612		343 530	9989			C84		289	4
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21		721		419	9967		100	716		306	1	854		357	3
	9933			705		321		900		440		937		389	3
23		393		990	1	555	9980	084		573	9996	020		421	3
24		728	9952		1500	789	-	267		706		101 182 262 841		452	3
	9934		1	557	9968			450 631		897		182		₹82	3
26	- 100	395	-	840	1-	254	1	631	1	968		262		511	3
27		727	9953			485		811	9990		1	341		539	3
	9935			403	-8	715		991		227		419	-	567	3
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	9936		9954		1-	401				6.9		6.9	1	644	2
32		375		518		628	1	701	1	734		157		668	- 28
33		703		795		854		877	1	859	1.0	793		602	2
	9937		9955		9970		9982	052		983	1	871		714	20
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36		679		620	1 1	528					9997		1	756	24
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38		326	9956		0074	972	1333	742		470	1	156		795	29
39		648		437	9971	193		912		590		224		813	21
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	9939		00==	978	1	633		200		827	10	360			18
12		610	9957			851		418	0000	944		426		863	18
13	00.40	928		515	9972	286	1	485 751	9992	060		556	- 1-	878	17
	9940			783						176				892	16
15		568	9958		-	502 717	9984	917		290		620		905	15
16	00.44	880		500		001				404		683		917	14
	9941			580 844	9973	931		245 408		517 629		745		928	18
18		510 823	9959									807		909	12
19	9942		9900	970		357 569		570 731		740				949	11
	9942			631						851		927 986		908	10
1 2		448 760		892		780 990	9985	891	9993	960	9998			079	9
	9943		9960	150	9974	100		209			3333	101	<u>'</u>	070	8
	9943				9914	408		209		177		157		919	7
14		379		411 669	1	615		100		284	4	101		980	6
5		688						024		390		213	1 1 1	909	5
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8		609	19.	408	101	407	0000	989		704		100	1.3000	993	2
9	0045	914	5901	093		431	9986	143		806		426	1.0000	000	1
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1	83°	84°	85°	86°	87°	88°	89°	,
		-						-
0		9.5 143645						
1	639780							
2	837941			421230				58
3	8.2 035239		546093	482278				
5		9.6 220486 493475	585294 624761	543833 605916				
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6 7	635547	9.7 044075	704500	731679				54 53
1 0	8.3 040586		744779	795372			66.105473	
8 9	244577	600927	785333	859616		959928		
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11		9.8 164140	867282	989784		528392		
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13	8.4 070515	733823	950370	122242				47
14		9.9 021125	992349	189349	693220			46
15	489573	310088	12.034622	257052	818828	730264		45
16	700651	600724	077192	325358	945966			44
17	912772	893050	120062	394276		366194		43
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22	989290	133054	339028	748337	742569	35.069546	80.463336	38
23	8.6 207833	168332	383768	821105	881251	431282	82.968487	37
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25	648223	229428	474221	968667	163980	36:177596	88.217943	35
26	870088	26)249		16 043482	308097	562659	101.10690	34
27	8.7 093077	291255	565997	118998	454096	956001	104.17094	33
28	317193	322447	612390	195225	692015	37.357892	107.42648	32
29	542461	353827	659125	272174	751392	768613	110.89205	31
30 31	768874	385397	706205	349855	903766	38.188459	114.58865	30 29
32	996446 8·8 225186	417158 449112	753634	428279 507456	23.057677; 213666	617738 89:056771	118.54018 122.77896	28
33	455103	481261	801417 849557	587396	371777	505895	127.32134	27
34	686206	513697	893058	668112	532052	965460	132.21851	26
35	918505	546151	946924	749614	694537	40.435837	137.59745	25
36	8.9 152009	578895	993160	831915	859277	917412	148-23712	24
37	386726		13.045769	915025	24:026320	41.410588	149.46502	23
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39	859843	678348	146127	17:083724	367509	42.433464	163.70019	21
40	9.0 093261	711913	196883	169337	541758	964077	171.88549	20
41	337933	745687	248031	255809	718512	43.508122	189.93220	19
42	578867	779373	299574	343155	897826	44.066113	190.98419	18
43	821074	813872	351518	431385	25.079757	638596	202.21875	17
44	9.1 064564	848283	403867	520516	264361	45.226141	214.85762	16
45	309348	882921	456625	610559	451700	829351	229.18166	15
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47	8)2838	952850	563391	793442	834823	47.085343	264.44080	13
48	9.2 051564	988150	617409	886310	23.030736	739501	286.47773	12
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51 52	805802 9·3 059936	095416	782060	170897	636690	815726	381.97099	9
53	315450	131635 168089	837827 894045	267654	844984	50·548506 51·303157	429.71757 491.10600	8 7 6
54	572355	204780	950719	365537 464471	27.056557 271486	52.080673	572.95721	G
55	830663		14.007856	564473	489853	882109	687.54887	5
56	9.4 090384	278885	065459	665562	711740	53.708587	859:43630	4
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58	614116	353970	182092	871068	28.166422	55.441517	1718.8732	2
59	878149	391885	241134	975523	399397	56.350590	3437.7467	1
60	9.5 143645	430052		19.081137	636253	57.289962	Infinite.	ō
,	6°	5°	4°	3°	2°	1°	0°	1
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			NATUR.	AL COTAN	GENTS.			

## LOGARITHMS OF NUMBERS

FROM 1 TO 10,000.

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1	0.000000	26	1.414973	51	1.707570	76	1.880814
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3	0.477121	28	1.447158	53	1.724276	78	1.892095
4	0.602060	29	1.462398	54	1.732394	79	1.897627
5	0.698970	30	1.477121	55	1.740363	80	1.903090
6	0.778151	31	1.491362	56	1.748188	81	1.908485
7	0.845098	32	1.505150	57	1.755875	82	1.913814
8	0.803080	33	1.518514	58	1.763428	83	1.919078
9	0.954243	34	1.531479	59	1.770852	84	1.924279
10	1.000000	35	1.544068	60	1:778151	85	1.929419
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11	1.041393	36	1.556303	61	1.785330	86	1.934498
12	1.079181	37	1.568202	62	1.792392	87	1.939519
13	1.113943	38	1.579784	63	1.799341	88	1.944483
14	1.146128	39	1.591065	64	1.806180	89	1.949390
15	1.176091	40	1.602060	65	1.812913	90	1.954243
16	1.204120	41	1:612784	66	1.819544	91	1:959041
17	1 · 230449	42	1.623249	67	1 · 826075	92	1.963788
18	1 · 255273	43	1.633468	68	1 . 832500	93	1.968483
19	1.278754	44	1.643453	69	1.838849	94	1.973128
20	1.301030	45	1.653213	70	1.845098	95	1.977724
						-	
21	1.322219	46	1.662758	71	1.851258	96	1.982271
22	1.342423	47	1.672098	72	1.857332	97	1.986772
23	1:361728	48	1.681241	73	1.863323	98	1.991226
24	1:380211	49	1.690196	74	1.869232	99	1.995635
25	1:397940	50	1.698970	75	1.875061	100	2.000000

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1	1	2	3	4	5	6	7	8	9	Diff.
2 860 3 (1283) 4 703: 5 (2118: 6 530: 7 938: 8 (8342- 110 (4139: 1 532: 2 921: 3 (5507: 4 69: 5 (60:69: 6 445: 7 816: 8 (71882) 9 (79181: 1 (8278: 2 (636: 8 (71882) 9 (79181: 1 (8278: 2 (636: 8 (71882) 1 (1059:		4 000868								
3 (1283) 4 703: 5 (02118: 6 530: 7 93: 8 (03342- 9 742: 110 (44139: 2 921: 3 (05307: 4 69:: 5 (60:69: 6 4455 7 818: 2 (63:69: 6 (30:69:							7321			428
4 703. 5 02118: 6 5300 7 938. 8 03342. 9 7426 110 04139: 1 532: 2 9218: 8 05304. 1 532: 2 9218: 8 05307. 1 082785 2 06306. 8 071882 9 5547 120 079181 1 082785 2 06306. 8 071882 9 100371 7 38344 1 1 7211 2 100574 8 7210 9 110590 130 113943 1 7211 2 120574 8 38502 4 7105 5 180334 6 3539 9 143015 140 146128 9 152288 9 367 7 6721 8 9379 9 143015 140 146128 1 7219 2 152288 7 7317 8 170262 9 1386 1 76691 1 1 76291 1 1 7721 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		6 9451 9 013680			4940		011570 5779			
5 02118: 6 5300 7 938 8 63342-9 7 424 110 C41393 1 5322 9211 1 5322 921 1 1 0 53275 5 66 64 4458 7 8156 6 6 4458 7 120 079181 1 052785 5 6910 6 100371 7 8 814 1 7211 2 120574 8 957 9 143015 140 146128 1 1 15228 3 15228 4 150 15228 5 161865 6 4553 7 7317 8 170262 9 3186 150 176091 1 8977 2 181844 4 4991 1 8977 2 181844 4 4991 1 8977 2 181844 4 4991 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				8700	9116	9532		020361	020775	
7 938 8 68342-9 9 7427 110 64139: 1 532: 2 9218 8 65367-4 6 6938-4 6 60698-6 6 4455-5 7 8156-8 8 071852-2 6366-7 10 0279181 1 082785-2 2 6366-8 8 071852-9 9 9055-4 093422-5 6 1008717-7 8 8344-7 1 10259-3 1 13948-1 7 271-1 1 10259-3 1 13948-1 1 7210-1 1 10259-3 1 13948-1 1 7210-1 1 10259-3 1 13948-1 1 1 12285-4 8 3852-2 9 1 143015-1 1 152288-3 9 1 152288-3 1 152288-3 1 7 317-8 1 7 7 317-8 1 7 7 17 181844-4 8 1 7 17 181844-4 8 1 7 181844-4 8 1 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		3 022016				023664	024075	4486	4896	412
8 (3342-9 7424 9 7424 110 (4189) 1 5322 9 9218 2 9218 5 (653073 4 6938 5 (653073 4 6938 7 8186 8 671885 9 5544 120 079181 1 082765 2 6366 3 9905 4 9934922 5 6910 6 100871 7 8844 7210 9 110590 1130 43 7210 9 110590 1 13094 1 7271 2 120574 8 8552 4 7105 5 180334 6 6 3539 7 7621 8 9379 9 143015 140 146128 1 9219 2 152288 3 8362 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521				6942	7350		8164		8978	4(8
9 7426 110 C4139: 1 582: 2 9218: 3 (5307: 4 693: 5 (64069: 6 4458: 8 (71882: 9 5547 120 079181 1 082785 2 6366 6 108371 7 3834 4 093422 5 (911059) 130 113943 1 7211 2 120574 3 8852 4 71059 143015 140 146128 9 152288 3 58536 4 8362 5 161368 4 8362 5 161368 7 7317 8 170262 9 1386 150 176691 1 8977 2 181844 3 4991 2 152288		9030195 $4227$	4628	5029	5430		032216 6230			
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1 582: 2 9218 2 9218 3 (55307; 4 69): 5 (66): 69; 5 (66): 69; 6 4455 8 (771832) 9 5547 120 079181 1 082785 2 6366 3 9905 4 093422 5 6910 1 110590 1 113948 1 7211 2 120574 8 9852 4 7105 5 180334 6 3539 6 7791 8 146128 1 9219 2 152288 1 52288 4 8362 5 161365 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 1 818144 3 44991 4 7521	3 041787	1	042576	042909	048862			17 50	2 / 1	
8 (659)74 4 (69)84 5 (60)69 6 (44)56 7 (81)68 8 (71)832 9 (50)74 1 (82)78 2 (63)60 3 (99)42 2 (63)60 4 (99)42 2 (63)60 1 (10)590 1 (10)5		6105	6495	6885	7275	7664	8053	8442	8830	1 890
4 69.26 5 060.069 6 4455 7 8156 8 071882 9 5544 120 079181 1 082785 2 6360 3 9905 4 093422 5 6910 6 100877 7 8844 7210 9 110590 130 113943 1 7271 2 120574 4 7105 5 180334 6 3539 7 6721 8 9579 9 143015 140 146128 1 9219 2 152288 4 8362 5 161865 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521	8' 9606	9993	05088)							
5   061698   4458   5647   8186   8   71882   9   5547   120   079181   1   082785   2   6360   6   100371   7   3834   8   7210   9   110590   130   113943   1   7271   120574   8   38502   4   7105   5   180334   6   3539   14018   152288   3   5366   4   3539   150288   3   5366   4   5367   7317   170262   9   3186   150   176691   1   8977   181844   3   44991   1   8977   181844   3   44991   4   7521   4   7521   4   7521   4   7521   1   1   1   1   1   1   1   1   1	S 053463		4230 8046	4613 8426	4996	5378 9185	5760 9563			283
6 4455 7 8186 7 8186 9 5547 120 079181 1 082785 2 6360 3 9905 4 093422 4 6910 100371 7 8814 8 7210 9 110590 113948 1 7271 2 120574 8 9859 9 143015 140 146128 1 9219 2 152288 3 5386 4 4553 7 7317 8 176962 9 3186 150 176691 1 8977 2 181844 3 44991 4 7521		6061452							060320 4083	
8 071882 9 5547 120 079181 1 082785 2 6360 3 9905 4 093422 5 6910 8 7210 9 110590 130 113948 1 7271 2 120574 8 8852 4 7105 5 180334 6 3539 7 76721 8 9579 148015 152288 3 5836 4 8362 5 161868 6 4353 7 7317 8 170262 9 18184 8 977 2 181844 8 4891 1 1 70262 9 18186			5580	5953	6326	6699	7671	7443		373
120 079181 1 082785 2 6366 3 9995 4 093422 5 6910 6 100877 7 88344 8 7210 9 110590 130 113948 1 7271 2 129574 8 9879 9 143015 140 146128 1 9219 2 152288 3 5336 4 8362 5 161365 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521			9298		C70038			071145	(71514	370
120 079181 1 082785 2 6366 3 9995 4 093422 5 6916 6 100371 7 3894 8 7210 9 110590 130 113943 1 7271 1 120574 8 3852 4 7105 5 180334 6 3539 7 6721 8 9579 1 443015 140 146128 9 143015 140 146128 1 52288 3 5386 4 8362 5 161365 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 181844 3 4991 4 7521			072985 ( 6640)	$073352 \\ 7004$	3718 7368	4085 7731	4451 8094	4816	5182	366
1 082785 2 6366 2 9995 4 093422 5 6916 6 100371 7 3834 8 7210 9 110590 130 113943 1 7271 2 120574 3 8852 4 7105 5 180334 6 3539 9 143015 140 146128 1 9219 2 152288 3 5366 4 8367 7 317 8 170262 9 1386 150 176691 1 8977 181844 3 4991 4 7521		1	-			-	-	8457	8819	363
2 6366 3 9905 4 093422 5 6910 6 100871 7 38344 8 7210 9 110590 130 113948 1 7271 2 120574 4 7105 5 136334 6 3539 7 6721 8 9879 9 143015 140 146128 1 9219 2 152288 3 5336 4 8362 5 161368 6 4553 7 7317 8 176262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521			080266 ( 3861	$089626 \\ 4219$	CSC987 4576	(81347 4934				360
8 9905 4 093422 5 6910 6 100871 7 8844 8 7210 9 110590 130 113943 1 7271 2 120574 3 8852 4 7105 5 180834 6 6 3539 7 6721 8 9579 9 143015 140 146128 1 9219 2 152288 4 8362 5 161368 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521			7426	7781	8136	8490	8845	5647 9198	6004 9552	357 355
5   6910   100871   7   88:144   8   72:10   9   110590   110590   110590   110590   120574		090611								852
6 100871 7 8804 8 7210 9 110590 130 113943 1 7271 2 129574 3 8852 4 7105 5 180384 6 3539 7 6721 8 9579 9 143015 140 146128 1 9219 2 152288 3 5830 4 8362 5 161365 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 1 818144 3 4991 4 7521			4471	4820	5109	5518	5866	6215		349
7			7951	8298	8644	8990			100 26 3462	346 343
8 72.10 9 1130439 1 7271 2 120574 8 8552 4 7105 5 180384 6 3539 6 6721 8 9879 9 143015 140 146128 1 9219 2 152288 3 5386 4 8362 5 161365 6 4253 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521			4828	5169.	5510	5851	6191	6531	6871	341
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1 7271 2 120574 3 8852 4 7105 5 180334 6 8539 7 6721 8 9579 9 143015 140 146128 1 9219 2 152288 3 5386 4 8362 5 161368 6 44558 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521	110926	111263	111599	111934	112270	112605	112940	115275	3609	335
2 129574 3 8552 4 7105 5 180383 6 6 3539 7 6721 8 9579 9 143015 140 146128 1 9219 2 152288 3 52288 4 8362 5 161368 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521	3 114277	114611	114944 1	15278	115611	115943	116276	116668	116940	333
8 8852 4 7105 5 180834 6 6 6 6 6 7 6721 8 9819 9 143015 140 146128 3 5336 4 8362 5 161868 6 4553 7 7317 8 170262 9 3186 150 176691 1 8917 2 181844 3 4691 4 7521			8265	8595	8926	9256	9586		120245	330
4 7105 5 180334 6 3539 7 6721 8 9879 9 143015 140 146128 1 9219 2 152288 3 5336 4 8362 5 161368 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521			$1215691 \\ 4830$	5156	5481	122544 5806	6131	123198 6456	3525 6781	328 325
5 180384 6 3539 7 6721 8 9579 9 143015 140 146128 3 5836 4 8362 5 161368 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521			8076	8399	8722	9045	9368		130012	523
7 6721 8 9879 9 143015 140 146128 1 9219 2 152288 3 5386 4 8362 5 161365 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4991 4 7521	1 130655	130977		31619	131939				3219	321
8 9579 9 143015 140 146128 1 9219 2 152288 3 5336 4 8362 5 161368 6 4353 7 7817 8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521			4496	4814	5133	5451	5769	6(86	6403	318
9 143015 140 146128 1 9219 2 152288 3 5336 4 8362 5 161368 6 4553 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521		7354 140508	7671 140822 1	-7987	8303	8618	8934 142076	9249	9564 $142702$	316 314
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1 9219 2 152288 3 5336 4 8362 5 161368 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521			200	70.0	0.000	77.5	1 1 1 1 1		148911	3(9
3   5386 4   8362 5   161368 6   4253 7   170262 9   3186 150   176691 1   8977 2   181844 3   4691 4   7521			1501421							307
4   \$362 5   161368 6   4353 7   70262 9   3186 150   176091 1   8977 2   181844 3   4691 4   7521	152594		3205	3510	3815	4120	4424	4728	5032	305
5 161368 6 4353 7 7317 8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521			6246 9266	6549 9567	6852	7154	7457 160469	7759	8061	303 301
6   4353 7   7317 8   170262 9   3186 150   176691 1   8977 2   181844 3   4691 4   7521		161967				3161	3460	3758	4055	299
8 170262 9 3186 150 176691 1 8977 2 181844 3 4691 4 7521	3 4650	4947	5244	5541	5838	6134	6430	6726	7022	297
9   3186 150   176691 1   8977 2   181844 3   4691 4   7521			8203	8497	8792	9686	9380	9674	9968	295
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1 8977 2 181844 3 4691 4 7521						1000	50	100.00	34-1	289
2 181844 3 4691 4 7521		9552					178113 1 180 <b>98</b> 6 1		178689	289
3   4691 4   7521		182415	182700	2985	3270	3555	3889	4123	4407	285
	4975	5259	5542	5825	6108	6391	6674	6956	9239	283
K 1100000			8366	8647	8928	9209	9490		2846	281 279
5 190832 6 3125		190892 : 3681	191171 1   3959	914511 $4237$	4514	4792	5069	5346	5623	278
7 5900		6453	6729	7005	7281	7556	7832	8107	8382	276
8 8657	6176	9206	9481	9755 2			00577 2			274
9 201397	8932	1171110	2022169	202488.	2761	3033	3305	3577	3848	272
No. 0		201945	3							Diff.

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1	No.	0	1	2	3	4	5	6	7	8	9	Diff.
9 9515   788 214051   210319 21658 210583 211121   211388 211654 211921   267 8 212188 918454   2790   2986   2925   2818   3783   4049   4814   475   2266 4 4844   51199   5873   5698   5992   6166   6430   6694   6957   7221   224 6 220108 223370   220681   220892   221163   221414   221675   221936   222196   222456   261 7 2716   2976   2336   2496   3705   4015   4274   4538   4792   5051   229 8   5389   5508   5526   6084   6342   6600   8555   7115   7372   7639   258 9   7857   6144   8400   8657   8913   9170   9426   9652   9938   230193   256 17   22049   230704   230909   231215   231470   221742   231979   232944   23452   232742   2355   23234   23245   2351   2296   2350   8504   8757   4011   4244   44517   4770   5698   5277   252   2528   245148   249709   241048   241799   241948	160	20412	204391	204663	204934	205204	205475	205746	206016	206286	206556	271
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4 4444 5109 5373 5698 5912 6166 6430 6694 6957 7221 264 5 7484 7747 8010 8378 8586 8799 9060 9329 9555 946 2262 6 220103 221370 220631 220892 221163 221414 221675 221936 222166 2616 7 2716 2976 8236 8496 8755 4015 4274 4533 4792 5051 259 7 7857 8144 8400 8657 8913 9170 9426 9652 9938 220193 2256 9 7857 8144 8400 8657 8913 9170 9426 9652 9938 220193 256 170 230409 230704 230909 231151 231470 231742 231970 232294 223485 223192 256 171 230409 230704 230909 231151 231470 231742 231970 232294 223485 223192 256 182 5598 5781 6033 6255 6537 6789 7741 7292 7344 7793 252 2 5598 5781 6033 6255 6537 6789 7741 7292 7344 7793 252 2 40549 240709 241045 241297 241546 241795 242243 224293 2541 2799 249 5 8 25459 240709 241045 241297 241546 241795 242244 242293 2541 2799 249 5 8 254420 250646 250908 251151 251395 251688 2513851 252125 222368 25167 245 8 254420 250646 250908 251151 251395 251688 2513851 252125 222368 25167 245 8 255429 250646 250908 251151 251395 251688 2513851 252125 222368 25161 2438 130 255273 255514 225755 255999 256287 256477 256718 250985 257109 257489 241 1 7679 7918 1515 83898 8687 8377 9116 9355 9594 9338 229 2 80071 240810 260548 260757 261025 261298 261501 261739 261076 262214 288 3 2451 2688 2923 3162 3899 8636 8873 4109 4346 4592 2877 2 71742 160810 260548 260757 261025 261298 261501 261739 261076 262214 288 3 2451 2688 2923 3162 3899 8636 8873 4109 4346 4582 2877 2 71742 27074 272396 2558 2770 80018 2838 3446 8096 89214 283 8 2451 2688 2923 3162 3899 8636 8873 4109 4346 4582 2877 2 71742 22074 272396 2558 2770 80018 2838 8464 8096 89214 283 8 2451 2688 2923 31618 3899 8636 8873 4109 4346 4596 26214 2486 9 6462 6692 6921 7151 7389 7669 7799 8198 8416 8936 9921 2238 9 6466 6692 6691 7151 7389 7669 7799 8198 8416 8686 8997 2999 2999 8999 8999 8999 8999 8999												
6         2010   829370   220461   220492   221148   221444   221475   221436   221444   221475   221436   221444   221475   221436   221444   221475   221438   24142   21475   221436   221444   221475   221436   22144   221475   221444   231476   231744   231476   231744   231476   231744   231476   231744   231476   231744   231476   231445   231476   231445   231476   231445   231476   231445   231476   231445   231476   231445   231476   231445   231476   23												
6         223/105         223/130         220/631         220/632         221/136         221/147         271/14         221/15         287/15         275/25         287/25												
8   5349   5568   5826   6084   6342   6600   6858   7115   7372   7630   258   7687   8144   8400   6657   8913   9470   9426   9682   9382   89193   2516												
9				3236								
170   293449   230704   230960   231215   231470   231724   231979   232234   232485   232742   255   258							6600	6858	7115			
1   2996							9110	9420	9002			
2         5598         5781         6938         6225         6537         6789         7049         9299         9550         9800         240050         240050         2500         250         9800         240050         2500         250         250         240050         240050         2500         2600								231979				
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5         299085         299287         290480         290702         290495         291417         291369         291591         291818         29264         292         292         3141         3363         3584         3804         4625         4246         221         74466         4667         4907         5127         5347         5567         5787         6007         6226         6446         220           8         6665         6884         7104         7323         7542         7761         7979         8198         8416         8635         219           9         8853         9071         9289         9507         9725         9943         30161         306378         306595         300813         218           200         301093         301247         301464         301681         301898         30214         302547         302764         302769         29209         217           1         3196         3412         3028         3844         4059         4275         4491         4706         4921         5136         216         225         6689         6854         7068         7282         213         4349         4710         4716												
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8         6665         6884         7104         7328         7542         7741         7979         8198         8416         8435         219           9         8853         9071         9289         9507         9725         9943         306161         300378         30555         300818         218           200         301030         301247         301464         301681         30189         302114         30231         302547         302764         302980         217           1         3196         3412         3028         3844         4059         4275         4491         4706         4921         5136         216           2         5351         5566         5781         5996         6211         6425         6689         6854         7068         7282         213           4         9630         9843         310056         310268         310481         310693         316906         311118         311330         31142         212           5         311754         311966         2177         2389         2600         2512         3023         32445         3455         3656         7761         77972         3173	6				2920							
9 8538 9071 9299 9507 9725 9943 301016 300878 300595 300818 218 200 301030 301247 301464 301681 301598 302114 302331 362547 362764 362980 21 1 3196 3412 3628 3844 4059 4275 4491 4706 4921 5136 216 2 5351 5566 5781 5996 6211 6425 6689 6854 7068 7282 218 8 7496 7710 7924 8137 8351 8564 8778 8991 9204 9417 213 4 9630 9843 310056 310268 310481 310693 316906 311118 311330 311542 212 5 311754 311966 2177 2389 2600 2812 8623 8284 2445 8556 5760 210 6 3867 4078 4289 4499 4710 4920 5130 5840 5551 5760 210 7 5970 6180 6390 6599 6809 7018 7227 7436 7646 7854 209 8 8063 8272 8481 8689 8898 9106 9314 9522 9730 9938 208 9 820146 320552 320562 32069 320977 321184 321391 321598 321805 322012 207 210 322219 322426 322633 322839 823046 82352 323488 323665 323871 324077 206 1 4232 4488 4694 4899 5165 5310 5516 5721 5926 6131 205 2 6336 6541 6745 6950 7155 7359 7563 7767 7772 8176 205 4 330414 330617 330819 331022 331225 331427 331630 231832 2684 2236 202 5 2438 2640 2842 8444 324 3447 3368 3476 3477 206 6 4454 4655 4856 5057 0257 5458 5658 5859 6059 6260 201 7 6460 6660 6860 7060 7260 7459 7659 7858 8088 8257 200 8 8156 8656 8855 9054 9259 345183 341632 341830 2028 2225 193					5127							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					7323		7761					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			3011	9438	9301	9120	G#66	000001	000013	000000	900919	210
2         5381         5566         5781         5996         6211         6425         6689         6854         7068         7282         215           8         7490         7710         7924         8187         8351         8564         8778         8991         9294         9417         218           4         9630         9843         310656         310468         310406         311118         311330         311542         212           5         311754         31196         2177         2389         2600         2312         8028         3234         2445         3656         211           7         5970         6180         6390         6599         6809         7018         7227         7436         7646         7854         209           8         8063         8272         8481         8689         8989         9106         9314         9522         9730         9932         9932           9         320146         232562         322893         828046         83252         23348         82865         32871         324077         206           1         4232         4488         4694         4899 <th< td=""><td>200</td><td>2108</td><td>301247</td><td>201464</td><td>301681</td><td>301898</td><td>302114</td><td>302331</td><td>4706</td><td>4001</td><td>302980</td><td>217</td></th<>	200	2108	301247	201464	301681	301898	302114	302331	4706	4001	302980	217
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					5996							
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3				8137							
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8	8068	2279	8491	9690	9909	0106	0214	0599	0720	0038	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9	320146	320354	320562	320769	320977	321184	321391	321598	321805	322012	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	210	322219	322426	322633	322839	323046	323252	323458	323665	323871	324077	206
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1	4282	4488	4694	4899	5105	5310	5516	5721	5926	6131	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$								7563	7767			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								331630	9805			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$												
7   6460   6660   6860   7060   7260   7459   7659   7858   8058   8257   200   8   8456   8656   8855   9054   9253   9451   9650   9349 340047 340246   199   340444 340642 340844   341039 341237 341435 341632 341830   2028   2225   198	6	4454	4655	4856	5057	5257	5458	5658	5859	6059		
9 340444 340642 340841 341039 341237 341435 341632 341830 2028 2225 193			6660				7459					
10, 0   1   2   3   4   5   6   7   8   9   Diff.			04001Z							_		-
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No.	0	1	2	3	4	5	6	7	8	9	Diff
220			342817								197
1	4392			4981	5178	5374	5570	5766	5962		196
2	6358	6549	6744		7135				7915	8110	195
3	8305				9083		9472			350054	194
4	350248	350442	350636	350829	351023	351216	351410	351608	351796	1989	193
5 6 7 8	2183			2761	2954						193
6	4108			4685	4876						
7	6026			6599	6790						
8	7935		8316	8506	8696						190
9			360215							361539	189
230	361728	361917	362105						363236	363424	188
1	3612		3988	4176	4363	4551	4739	4926		5301	188
1 2	5488	5675	5862	6049	6236	6423	6610	6796	6983	7169	187
3	7356	7542	7729	7915	8101	8287	8473	8659	8845	9030	186
4	9216			9772	9958				370698		185
5	371068	371253	371437		371806	1991	2175	2360		2728	184
6	2912	3096	3280	3464	3647	3831	4015	4198	4382	4565	184
6 7	4748	4932	5115	5298	5481	5664	5846	6029	6212	6394	183
0	6577	6759	6942	7124	7306	7488	7670	7852	8034		182
8 9	8898	8580	8761	8943	9124	9306	9487	9668		380030	181
240	380211	380392	380573	380754	380934	381115	381296	381476	381656	381837	181
1	2017	2197	2377	2557	2737	2917	3097	3277	3456	3636	180
2	3815	3995	4174	4353	4533	4712	4891	5070	5249	5428	179
3	5606	5785	5964	6142	6321	6499	6677	6856	7034	7212	178
1	7390	7568	7746	7923	8101	8279	8456	8634	8811	8989	178
¥	9166	9343	9520	9698	0075	900051	200000		390582		177
0								2169	2345		
0			391288			1817	1998			2521	176
0	2697	2873	3048	3224	3400	3575	3751	3926	4101	4277	176
456789	4452 6199	4627 6374	4802 6548	4977 6722	5152 6896	5326 7071	5501 7245	5676 7419	5850 7592	6025 7766	175
100	100	2.0	398287	-							173
1	9674		400020							401228	173
2	401401		1745	1917	2089	2261	2483	2605	2777	2949	172
2	3121	3292	3464	3635	3807	3978	4149	4320	4492	4663	171
1	4834	5005	5176	5346	5517	5688	5858	6029	6199	6370	171
3 4 5					7221						170
6	6540	6710	6881	7051		7891	7561	7731	7901	8070	
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8	411620	1788	1956	2124	2293	2461	2629	2796	2964	3132	168
9	3300	3467	3635	3803	3970	4137	4305	4472	4639	4806	167
			415307						416308		167
1 2 3	6641	6807	6973	7139	7306	7472	7638	7804	7970	8135	166
4	8301	8467	8633	8798	8964	9129	9295	9460	9625	9791	165
3			420286							421439	165
4 5 6 7 8	421604	1768	1933	2097	2261	2426	2590	2754	2918	3082	164
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6	4882	5045	5208	5371	5534	5697	5860	6023	6186	6349	163
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8	8135	8297	8459	8621	8783	8944	9106	9268	9429	9591	162
9	9752	9914	430075			430559	430720	430881	431042	431203	161
			431685							432809	161
1	2969	3130	3290	3450	3610	3770	3930	4090	4249	4409	160
2	4569	4729	4888	5048	5207	5367	5526	5685	5844	6004	159
3	6163	6322	6481	6640	6799	6957	7116	7275	7438	7592	159
5	7751	7909	8067	8226	8384	8542	8701	8859	9017	9175	158
	9333	9491	9648	9306	9964				440594	440752	158
6	440909	441066	441224	141381	141538	1695	1852	2009	2166	2323	157
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8	4045	4201	4357	4513	4669	4825	4981	5137	5293	5449	156
9	5604	5760	5915	6071	6226	6882	6537	6692	6848	7003	155

				2300111		Or I	UMBER	1130			10.
No.	. 0	1	2	3	4	5	6	7	8	9	Diff.
280	447158	3 447318	447468	447623	447778	447938	3 448088	448242	44839	448552	155
1	8706			9170	9324	9478	9633	9787	994	450095	154
2		450408	450557								154
3	1786			2247	2400	2558					153
4	3318		3624	3777							153
5 6	4845			5302 6821							
7	6366 7882			8336	6978 8487						$152 \\ 151$
0	9392			9845		160116	466206		7 AG050'	460748	151
8 9			461198						2098	2248	150
1 000	1000	1	1					1	1		
290			462697							463744	150
1	3893		4191	4340	4490	4639					149
2 3	5383 6868		5680 7164	5829 7312	5977 7460	6126					149 148
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5	9322		470116							471145	147
6		471438	1585	1732	1878						146
6 7 8	2756	2903	3049	3195	3341	3487	3633				146
8	4216	4362	4508	4653	4799	4944					146
9	5671	5816	5962	6107	6252	6397	6542		6832		145
300	477121	477266		477555		477844	477980	1	478979	478422	145
1	8566	8711	8855	8999	9143	9287	9431	9575			144
2	480007	480151			480582	480725	480869		481156	481299	144
3	1443	1586	1729	1872	2016	2159	2302	2445			143
4	2874	3016	3159	3302	3445	3587	3730		4015		143
5	4300	4442	4585	4727	4869	5011	5153	5295	5437	5579	142
6	5721	5863	6005	6147	6289	6430	6572	6714	6855		142
7	7138	7280	7421	7563	7704	7845	7986	S127	8269	8410	141
8	8551	8692	8833	8974	9114	9255	9396	9537	9677	9818	141
9	9958	490099	490239	490380	490520	490661	490801	490941	491081	491222	140
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1 2 3	4155	4294	4433	4572	4711	4850	4989	5128	5267	5406	139
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4	6930	7068	7206	7344	7483	7621	7759	7897	8035	8173	138
4 5 6	8311	8448	8586	8724	8862	8999	9137	9275	9412	9550	138
6	9687	9824					509511				137
7 8	501059 3 2427	2564	2700	1470 2837	$\frac{1607}{2973}$	1744 3109	1880 3246	2017 3382	2154 3518	2291 3655	137 136
9	3791	3927	4063	4199	4335	4471	4607	4743	4878	5014	136
10.63	11000							1			
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1	6505	6640	6776	6911	7046	7181	7316	7451	7586	7721	135
2 3	7856	7991	8126	8260	8395	8530	8664	8799	8934	9068	135
4	9203 $510545$	9337	9471	9606	9740		5100(9 1349	1482	1616	1750	134 134
5	1883	2017	2151	2284	$\frac{2418}{2418}$	2551	2684	2818	2951	3084	133
6	3218	3351	3484	3617	$\frac{2418}{3750}$	3883	4016	4149	4282	4415	183
6	4548	4681	4813	4946	5079	5211	5844	5476	5609	5741	133
8	5874	6006	6139	6271	6403	6535	6668	6800	6932	7064	182
9	7196	7328	7460	7592	7724	7855	7987	8119	8251	8882	132
330	518514					510171					131
330	9828		520090 5	20991	500050	590494	519308	590745	500976	521007	131
2	521138		1400	1530	1661	1792	1922	2058	2183	2314	131
2 3	2444	2575	2705	2835	2966	3096	3226	3356	3486	3616	180
4	3746	3876	4006	4136	4266	4396	4526	4656	4785	4915	130
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6	6339	6469	6598	6727	6856	6985	7114	7243	7872	7501	129
7	7630	7759	7888	8016	8145	8274	8402	8531	8660	8788	129
8	8917	9045	9174	9302	9430	9559	9687	9815		530072	128
9	530200 5	30328	30456	80584	030712	530840	30968	531096	581228	1351	128
No.	0	1	2	3	4	5	6	7	8	9	Diff.

1				3	4	5	6	1	8	9	Diff.
1	531479	531617	531734								128
	2754			3136			3518 4787				127
2 3	4026 5294			4407 5674	4534 5800			4914 6180			127 126
4	6553	6685	6811	6937	7063						126
5	7319	7945	8)71	8197	8322	8448					126
6	9)73	9202	9327 $540530$	9452	9578					540204 1454	125 125
7 8	1579	1704		1953	2078	2203					125
9	2325	2950	3374	3199	3323	3417	3571				124
			544316		544564						124
$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$	53)7	5431	5555 6789	5678 6913	5892 7036	5925 7159					124 123
3	6543 7775	6666 7893	8)21	8144	8267	8389			8758		123
4	9113	9126	9249	9371	9494	9616	9739	9861	9984	550106	123
5			55 )473								122
6 7	145) 2668	1572 2793	1694 2911	1816 3033	1938 3155	$\frac{2060}{3276}$	2181 3398	2303 3519	$\frac{2425}{3640}$		$\frac{122}{121}$
8	3333	4004	4123	4247	4368	4489	4610				121
9	5)91	5215	5336	5457	5578	5699	5820				121
360			556544								120
1	75)7	7627	7748	7863	7988	8108	8228		8469		120
$\begin{bmatrix} 2 \\ 3 \end{bmatrix}$	8709	8829 560026	8948 <sup>1</sup> 55J146	9)68 560265	9188. 560885	9308 560504	9428 $560624$	9548 560743	9667	9787	120 119
4	5311 1	1221	134)	1459	1578	1698		1936	2055		119
5	2233	2412	2531	2650	2769	2887	3006	3125	3244		119
6 7	3481 4555	3630 4784	3718 4903	3837 5021	3955 5139	4074 5257	4192 5376	4311 5494	4429 5612		119 118
8	5848	5966	6.)84	6202	6320	6437	6555	6673	6791		118
9	7026	7144	7262	7379	7497	7614	7732	7849	7967		118
370	568202	568319	568436	568554							117
1	9374	9491		9725	9842		570076				117
2 3	570543 1709	570650 1825	570776 1942	2J5S	$\frac{2174}{2174}$	2291	$\frac{1243}{2407}$	1359 2523	$\frac{1476}{2639}$	1592 2755	117 116
4	2872	2933	3104	3220	3336	3452	3568	3684	3800	3915	116
5	4)31	4147	4263	4379	4494	4610	4726	4841	4957	5072	116
6	5188	5303 6457	5419 6572	5534 6687	5650 6802	5765 6917	5880 7032	5996 7147	$\frac{6111}{7262}$	$6226 \\ 7377$	115 115
7 8	6341 7492	7607	7722	7836	7951	8066	8181	8295	8410	8525	115
9	8639	8754	8868	8983	9097	9212	9326	9441	9555	9669	114
380	579781	579898	580012	580126		580353	<b>5</b> 30 <b>4</b> 69		580697	580811	114
1 2	53,1925		1153	1267	1381	1495	1668	1722	1836	1950	114
$\frac{2}{3}$	2J63 3199	2177 3312	$\frac{2291}{3426}$	2404 3539	$2518 \\ 3652$	2631 3765	$\frac{2745}{3879}$	2858 3992	2972 4105	3085 4218	114 113
4	4331	4444	4557	4670	4783	4896	5009	5122	5235	5348	113
5	5461	5574	5686	5799	5912	6024	6137	6250	6362	6475	113
6	6587	6700 7823	6812 7935	6925 8047	7037 8160	7149 8272	7262 8384	7374 8496	7486 8608	7599 8720	112 112
7 8	7711 8332	8911	9056	9167	9279	9391	9503	9615	9726	9838	112
9			590173				590619				112
390 5	591065	591176	591287	591399			591732				111
1	2177	2283	2399	2510	2621	2732	2843	2954	3064	3175	111
2 3	3286 4393	3397 4503	3508 4614	3618 4724	3729 4834	3840 4945	3950 5055	4061 5165	4171 5276	4282 5386	111
4	5495	56)6	5717	5827	5937	6047	6157	6267	6377	6487	110
5	6597	6707	6817	6927	7037	7146	7256	7366	7476	7586	110
6 7	7695	7805	7914	8024	8134	8243	8353	8462	8572	8681 9774	110 109
8	8791 9383	8900 9992	9009	9119	9228 600319	9337 600428	9446	9556 600646	9665		109
	600973		1191	1299	1408	1517	1625	1734	1843	1951	109
No.	U	1	2	3	4	5	6	7	8	9	Diff.

No.   O	LOGARITANS OF NUMBERS.													
1   3144   3253   3361   3469   3577   3686   3794   3902   4010   4118   168   3   5305   5413   5521   5628   5736   5544   5951   6059   6166   6274   108   4   6881   6489   6586   6704   6811   6919   7026   7138   7241   7348   107   6   526   6832   6833   7740   8347	No.	0	1	2	3	4	5	6	7	8	9	Diff.		
1   3144   3253   3361   3469   3577   3686   3794   3902   4010   4118   168   3   5305   5413   5521   5628   5736   5544   5951   6059   6166   6274   108   4   6881   6489   6586   6704   6811   6919   7026   7138   7241   7348   107   6   526   6832   6833   7740   8347	400	602060	602169	602277	602386	602494	602603	602711	602819	602928	603036	108		
8         5935         5613         5521         5628         5736         5844         5951         6059         6166         6274         108           5         7155         7562         7669         7777         7854         7991         8695         8925         8912         8419         107           6         8526         8633         8740         8847         8934         9611         91728         1829         1940         1166         1192         1298         1405         1511         1617         106         1967         9274         9813         1948         107         981723         1829         1936         2942         2148         2254         2360         2424         2452         2360         2424         2464         4370         4510         4686         4792         106           40         61274         612890         61293         5189         5244         5529         5634         6740         5845         105           3         5950         6055         6160         6265         6370         6476         6581         6866         6790         6895         165         58348         8153         8827         88	1		3253	3361	3469	3577	3686	3794	3902	4010	4118	168		
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5         7155         7662         7669         7777         7834         7901         9895         8914         9161         9167         9274         9813         9485         107           6         8962         8939         8740         8847         8841         914         101021         10128         610244         610447         61054         107         994         9701         9808         9914         610021         610284         610447         61045         1165         1611         1617         106           410         612784         612890         612996         613102         613207         61331         613419         613525         613630         613736         106           1         3842         9447         4063         4159         4264         4370         4470         4551         4686         4792         105           3         3505         6055         6160         6265         6370         6476         6581         6866         6790         6895         105           4         7000         7105         721         731         7420         7525         7629         7734         7831         7931         7931 </td <td></td>														
6         8526         8633         8740         8847         8954         9161         9167         9274         9381         9485         167           8         610660         610767         610873         610979         1068         1192         1298         1405         1511         1617         106           410         612784         612809         613102         618207         13131         613419         618322         613330         613330         61341         1617         106           1         3849         39471         4453         4199         4264         4870         4475         4581         4666         4792         106           2         4897         5003         5108         5213         5319         5424         5529         5634         5740         5841         555         6160         6255         6276         6476         6481         6686         6790         6893         9198         9302         9406         9511         9615         9719         9824         9288         6208         62034         62034         620448         62055         620656         62076         62086         6710         6891         104														
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## 1728   1829   1936   2942   2148   2254   2360   2466   2572   2678   106   ## 1842   3947   4053   4159   4264   4370   4475   4381   4686   4792   106		9594	9701	9808										
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2   4897   5008   5108   5213   5319   5424   5529   5684   5740   5845   105     4   7000   7105   7210   7315   7420   7525   7629   7734   7839   7943   105     5   8345   8153   8257   8362   8466   8571   8376   8780   8584   8989   105     6   9939   9198   9302   9406   9511   9615   9719   9524   9928 (20022   104     7   620136 620240 620344 620448 620552 620656 620760 620564 62056   1072   104     8   1176   1287   1384   1488   1552   2628   2732   2835   2989   3042   3146   104     420   623249 623385 623456 623559 623663 623756 623859 623873 624076 624179   103     1   4282   4385   4488   4591   4695   4798   4901   5004   5107   5210   103     2   5312   5415   5518   5621   5724   5827   5929   6032   6135   6238   103     3   6340   6443   6546   6648   6751   6853   6956   7058   7161   7263   103     4   7366   7468   7571   7673   7775   7787   7799   8682   8185   8287   102     5   8359   8491   8598   8695   8797   8900   9002   9104   9206   9388   102     6   9410   9512   9613   9715   9817   9919   630021   630123   630224   630326   102     8   1444   1545   1647   1748   1849   1951   2052   2153   2255   2356   101     430   633468   633569   638670   633771   633872   633973   634074   634175   634276   634376   101     4477   4578   4679   4779   4880   4981   5061   5182   5283   5383   101     4   4774   4578   4669   4779   4880   4981   5061   5182   5283   5383   101     4   4774   4578   4669   4779   4880   4981   5061   5182   5283   5383   101     2   5445   5544   5685   5685   6889   6889   7889   7189   7290   7390   100     4   4790   7590   7690   7790   7890   7890   8190   8290   8381   101     4   4774   4578   4679   4779   4880   4981   5061   5182   5283   5383   101     2   5445   5544   5685   5685   6689   6889   7889	410													
8         5950         6055         6160         6265         6370         6476         6881         6866         6790         6895         105           4         7000         7105         7210         7315         7420         7525         7629         7784         7839         7943         105           5         8348         8133         8257         8862         8466         8571         8876         8780         8861         8671         8576         8780         8981         1072         1072         104         9620         9030         906         901         961         9719         9903         2007         2110         104         90         2214         2318         4488         1592         1695         1799         1903         2007         2110         104         90         22242         2231         2525         2628         2732         2835         2899         3042         316         104         10														
4         T000         T105         7210         7315         7429         7525         7629         7784         7890         7048         105           5         8.348         8133         8257         8862         8460         8571         8676         8780         8884         8989         105           6         9.993         9188         9302         9406         9511         9615         9719         9824         9928         620032         104           8         1176         1281         1384         1488         1592         1695         1799         1993         2072         2110         104           420         623249         623358         623456         623559         623663         623766         623859         623973         624076         624179         103           1         4282         4855         488         4591         4695         4798         4901         5004         5107         5210         103           2         5312         5415         5518         5621         5727         7890         6022         6135         6238         163           3         6340         7443         8675														
6         834S         8153         8257         8862         8466         8571         8719         9824         9928 620032         104           7         620136 620240 620344 620448         620552         620650 620760         620846 620963         6172         104           8         1176         1281         1384         1488         1592         1695         1799         1903         2007         2110         104           9         2214         2318         2421         2325         6282         2782         2835         2989         3042         3146         104           420         628249 623353 623456 623559         623603         623766 623869         623973 624076 624179         103           1         4282         4385         4491         4095         4798         4901         5004         5107         5210         103           2         5515         5618         5621         5724         5897         5929         6032         6135         6238         103           3         6340         6443         6546         6648         6751         6833         6936         6758         71617         7273         7175         7878				7210										
6         99.93         9198         9302         9406         9511         9615         9719         9824         9928 620032         104           8         1176         128)         1384         1488         1592         1695         1799         1903         2007         2110         104           9         2214         2318         2421         2325         2628         2732         2835         2939         3642         3146         104           420         628249         623358         623456         623559         623663         623766         623869         623973         624076         624179         103           1         4282         4885         4483         4591         4094         4901         5004         5107         5210         103           2         5812         5415         5515         5621         5774         5887         5929         6032         6135         6238         103           3         6366         7468         7571         7677         7775         7878         7890         6082         8185         8287         102           4         7040         9512         9613 <td< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>														
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8         6340         6443         6546         664S         6751         6753         7658         7655         7161         7263         103           4         7366         7468         7571         7678         7775         7878         7990         8622         8185         8287         102           5         8889         8491         8598         8991         8910         9002         9104         9206         9368         102           6         9410         9512         9613         9715         9817         8910         9002         9104         9206         2808         102           6         94262         30428         102         981         9191         5081         1981         1241         1442         162           8         1444         1545         1647         1748         1849         1951         2052         2153         2255         2356         101           430         633465         633569         638771         63872         638973         634074         648175         634276         634776         101           4         4777         4578         6683         5785         5886	1													
4         7366         7468         7571         7673         7775         7878         7990         9022         9104         9206         93(8)         162           5         8389         8491         8593         8695         8797         8900         902         9104         9206         93(8)         102           6         9410         9512         9613         9715         9817         9919 630021 630123 630224 630326 102           7         630425 630530 630631 630738 630835 636936         1038         1139         1241         1441         1445         1444         1445         1647         1748         1849         1951         2052         2153         2255         2356         101           430         633468         633569         633670         638771         63872         633973         634074         684175         634276 634376         101           4         4477         4578         4579         4479         4480         4981         5061         5182         5283         5383         101           4         4584         5584         5688         6689         6889         6989         7689         7189         7290         7390														
5         8389         8491         8598         8695         8797         8900         9002         9104         9206         9818         102           7         683428         630530         630631         630738         630835         630936         1038         1139         1241         1342         102           8         1444         1545         1647         1748         1849         1951         2052         2153         2255         2356         101           430         633468         633569         638771         633872         633973         634074         634175         63476         601           430         633468         633569         638771         633872         633973         634074         634175         63476         101           430         633468         63585         6683         6787         4880         4931         5081         5122         5243         53487         6883         101           4         1344         5584         5685         5785         5886         5986         6087         6187         6287         6388         100           4         7490         7590         7690 <td< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>8287</td><td>102</td></td<>											8287	102		
6         9410         9512         9613         9715         9917         9919         630021         630128         630224         630320         61083         630733         630835         630936         1038         1139         1241         1342         102           8         1444         1545         1647         1748         1849         1951         2052         2153         2255         2356         101           430         633465         633569         63876         68871         63871         638771         638771         638787         638771         63476         63476         63476         6411         44777         4578         4679         4479         4880         4951         5081         5182         5283         5383         101           2         5484         5584         5685         5785         5886         5986         6087         6187         6287         6387         101           4         7490         7590         7690         7790         7890         4890         8190         8298         889         100           5         8489         5586         6889         8789         8988         8989         90	$\hat{5}$										93(8			
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2 5484 5584 5685 6785 6889 6989 7089 7189 7290 7390 100 4 7490 7590 7690 7790 7890 7990 8090 8190 8290 8889 100 5 8489 8589 8689 8789 8888 8985 9088 9189 9287 9387 100 6 9486 9586 9686 9785 9885 9984 640084 640188 640283 640882 99 7 640481 640581 649680 640779 640879 64078 1077 1177 1276 1375 99 8 1474 1573 1672 1771 1871 1970 2069 2168 2267 2366 99 9 2465 2563 2662 2761 2560 2959 3058 3156 3255 3354 99 440 643453 643551 648650 648749 643847 643946 644044 644143 644242 644340 98 1 4429 4537 4636 4734 4832 4931 5029 5127 5226 5824 93 2 5422 5521 5619 5717 5815 5913 6011 6110 6208 6306 98 3 6404 6502 6600 6698 6796 6894 6992 7089 7187 7285 98 4 7383 7481 7579 7676 77774 7872 7969 8067 8165 8262 98 5 8360 8458 8555 8653 8750 8848 8945 9043 9140 9237 97 6 9385 9432 9580 9627 9724 9821 9919 650016 650113 65210 97 7 650308 650405 650502 650599 650696 650793 650890 0987 1084 1181 97 9 2246 2343 2440 2336 2363 23730 2826 2923 3019 3116 97 450 653213 653309 653405 653502 658598 653695 653791 658888 65984 654080 96 1 4177 4273 4369 4465 4562 4658 4754 4850 4946 5042 96 2 5188 5235 5331 6427 5523 5619 5715 5510 5906 6609 699 696 7097 1084 1181 97 9 2246 2343 2440 2366 2638 2760 2828 293 3019 3116 97 8 1278 1375 1472 1569 1666 1762 1859 1956 2058 2150 97 7 650308 650405 650502 650599 650696 650793 650890 0987 1084 1181 97 9 2246 2343 2440 2366 2633 2730 2826 2923 3019 3116 97 8 1278 1375 1472 1569 1666 1762 1859 1956 2058 2150 97 7 650308 650405 650502 650599 650696 650793 650890 0987 1084 1181 97 9 2246 2343 2440 2366 660716 660716 660716 660716 660716 660716 660716 660716 660716 660717 95 8 1278 1375 1472 1569 1666 1762 1859 1956 2058 2150 97 9 2246 2343 2440 2368 2368 2475 2369 8989 9989 8989 8989 8989 8989 8989 8														
8         6488         6583         6688         6789         6689         7089         7189         7290         7390         7390         100           4         7490         7590         7690         7790         7890         7990         8090         8190         8290         8889         100           5         8489         8589         8689         8789         8888         8988         968         9188         9287         9387         100           6         9486         9586         9686         9785         9885         9984         640084         640188         640238         640882         99           7         640451         640581         640779         640879         644077         641771         1277         1277         1275         99           8         1474         1573         1672         1771         1871         1970         2069         2168         2267         2366         99           9         2445         2563         2662         2761         2860         24981         244444         644444         6444444         6444444         6444444         6444444         6444444         6444444         64444				4019										
4         7490         7590         7690         7790         7890         8990         8190         8290         8881         100           5         8489         8589         8689         8788         8888         8988         9088         9188         9287         9387         100           6         9486         9586         9686         9785         9885         9984         640084         640183         640283         640283         640283         64085         99         7640481         640681         649680         640779         640879         644078         1677         1177         1276         1375         99         2465         2563         2662         2761         2860         2959         3058         3156         3255         3354         99           440         643453         643551         643656         643749         643847         643946         644044         6444148         6443440         98           1         4429         4537         4636         4734         4832         4931         5029         5127         5226         5324         98           2         5422         5521         5619         5717 <t< td=""><td>2 2</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>	2 2													
5         8489         8589         8689         8789         8888         8988         9088         9188         9287         9387         100           6         9486         9586         9686         9785         9885         9984         40084         640183         640283         640444         6444444         644444         644444         644444 <td></td>														
8         1474         1573         1672         1771         1871         1970         2069         2168         2267         2366         99           9         2465         2563         2662         2761         2860         2959         3058         3156         3255         3354         99           440         643458         643551         643749         643847         643847         644944         644144         644144         644144         644242         644349         98           1         4429         4537         4686         4734         4832         4931         5029         5127         5226         5324         98           2         5422         5521         5619         5717         5815         5913         6011         6110         6268         6306         98           3         6404         6502         6609         6699         6699         7699         7160         7774         7872         7969         9067         8165         8262         98           5         8360         8458         8555         8653         8750         8848         8945         9043         9140         9227         7724	5			8689	8789	8888	8988	9088	9188	9287	9387			
8         1474         1573         1672         1771         1871         1970         2069         2168         2267         2366         99           9         2465         2563         2662         2761         2860         2959         3058         3156         3255         3354         99           440         643458         643551         643749         643847         643847         644944         644144         644144         644144         644242         644349         98           1         4429         4537         4686         4734         4832         4931         5029         5127         5226         5324         98           2         5422         5521         5619         5717         5815         5913         6011         6110         6268         6306         98           3         6404         6502         6609         6699         6699         7699         7160         7774         7872         7969         9067         8165         8262         98           5         8360         8458         8555         8653         8750         8848         8945         9043         9140         9227         7724	6				9785		9984	640084	640183	640283	640382			
9 2465 2568 2662 2761 2860 2959 3058 3156 3255 3354 99  440 613453 643551 643656 643749 643847 643946 644044 644148 644242 644340 98  1 4449 4537 4636 4734 4382 4981 5029 5127 5226 5324 98  2 5422 5521 5619 5717 5815 5913 6011 6110 6208 6300 98  3 6404 6502 6600 6698 6796 6894 6992 7089 7187 7285 98  4 7383 7481 7579 7676 7774 7872 7969 8067 8165 8262 98  5 8360 8458 8555 8658 8750 8848 8945 9043 9140 9287 97  6 9335 9432 9580 9627 9724 9821 9919 650016 650113 650210 97  7 650308 650405 650502 650599 6506793 650890 0987 1084 1181 97  8 1278 1375 1472 1569 1666 1762 1859 1956 2658 2150 97  9 2246 2343 2440 2336 2633 2730 2826 2923 3019 3110 97  450 653213 658309 653405 655502 658598 658695 683701 658888 65984 664689 96  1 4177 4273 4369 4465 4562 4658 6757 6678 6758 65984 664689 96  2 5138 5235 5331 5427 5523 5619 5715 5810 5906 6002 96  4 7056 7152 7247 7343 7438 7534 7629 7725 7820 7916 96  5 8901 8000 9155 9250 9346 9441 9368 60881 60881 60061 66011 660106 660201 660296 660391 660486 660881 660676 66071 95  9 1813 1907 2002 2696 2191 2286 2380 2475 2569 2663 95	-7									1276				
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8     660865     0960     1055     1150     1245     1389     1484     1529     1623     1718     95       9     1813     1907     2002     2096     2191     2286     2380     2475     2569     2663     95														
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No.	0	1	2	3	4	5	6	7	8	9	Diff.
460	662758	662852	662947	663041	668185	663230	663324	668418	662512	663607	94
1	3701	3795					4266	4360	4454		94
2	4642								5393	5487	94
3	5581	5675			5956				6331	6424	94
4	6518	6612			6892						94
5	7453				7826						93
6	8386				6759					9224	93
7 8	9317	9410	9503 670431							670153 1(80	93 93
9	1173		1358		1543				1913		98
	1	1		1		1		i	1		1 36
470			672283				672652		672836		92
1	3021	3113			2890						92
2 3	3942	4034			4310						92
	4861	4953			5228 6145						92
5	5778 6094	5870 6785		6053 6908	7059						92
6	7667	7698		7881	7972						91 91
7	8518	8609			8882			9155			91
8	9428			9700				680(63			91
9			680517					(970	1660		91
	1	1	681422								
480 1	2145	681332		081513	2506				2867		90
2	3047	3137		3317	3407				3767	2957 3857	90
3	8947	4037	4127	4217	4307	4896			4666		90
4	4845	4935		5114	5204				55€3	5652	90
5	5742	5831	5921	6010	6100			6368	6458	6547	89
6	6636	6726		6904	6994			7261	7351	7440	69
7	7529	7618		7796	7886				8242		89
8	8420	85(-9		8687	8776				9131	9220	63
9	9309	9398	9486	9575	9664	9753	9841	9930	696619	€90167	63
490	CONTOR	600285	690373	600469	690550	(90629	690728	690816	600905	€9(€98	69
1	1(81	1170		1347	1435	1524		1760	1789	1877	88
2	1965	2053		2230	2318	2406	2494	2583	2671	2759	88
3	2847	2985		3111	3199	3287			2551	SCE 9	88
4	3727	3815	3903	8991	4078	4166	4254	4342	4430	4517	83
5	4605	4693	4781	4868	4956	5044	5131	5219	5307	€ 294	88 88 87
6	5482	5569	5657	5744	5832	5919	6007	60.94	6182	C219	87
7	(356	6444	6531	6618	6706	6793		6968	7055	7142	87
8	7229	7317	7404	7491	7578	7665	7752	7889	7926		87
9	8101	8188	8275	8362	8449	8535	8622	8769	8796	8883	87
500	698970	699057	699144	699231	699317	699404	699491	€99578	699664	(99751	87
1	9838	9924	700011	7000.98	700184	706271	700358	700444	701531	791 617	87
2	700704			0963	1050		1222	13(9	1895	1482	86
3	1568	1654	1741	1827	1913	1999	20.86	2172	2258	2844	86
4	2431	2517	2603	2689	2775	2861	2947	8(.83	3119	32(5	86
5	3291	3377	3468	3549	3625	3721	8807 4665	8893	£979 4837	4065	86 86
6 7	4151 50(3	4236 5094	4322 5179	4468 5265	4494 5350	4579 5436		4751 5607	5698	5778	86
8	5864	5949	6085	6120	6206	6291	6376	6462	6547	6632	85
9	6718	6803	6888	6974	7059	7144		7315	7400	7485	85
200				1							100
510			707740							7(8336	85
$\frac{1}{2}$	8421 9270	8506 9355	8591 9440	8676 9524	8761 9609	8846 9694	8931 9779	9615 9863	9100 9948	9185 710083	85 85
3	710117			710371						(879	85
	(963	10202	1132	1217	1301	1385	1470	1554	1689	1723	84
5	1807	1892	1976	2060	2144	2229	2313	2397	2481	2566	84
6	2650	2734	2818	2902	2986	3070	3154	3238	3323	3407	84
4 5 6 7	3491	3575	3659	3742	3826	3910	3994	4078	4162	4246	84
8	4330	4414	4497	4581	4665	4749	4833	4916	5000	5(84	84
9	5167	5251	5835	5418	55(2	5586	5669	5753	5836	5920	84
No.	0	1	2	3	4	5	6	7	8		Diff.
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520	716008	716087	716170	716254	716887	716421	716504	716588	716671	716754	83
1	6838						7338		7504		83
$\tilde{2}$	7671										
3	8502				8834		9000				
4	9331				9663		9828	9911	9994	720077	83
5	720159	720242	720325	720407	720490	720573	720655	720738	720821	0003	83
67	0936	1068	1151	1233	1316		1481		1646		82
7	1811		1975	2058	2140		2305		2469	2552	82
8	2634	2716	2798	2881	2963		3127	3209	3291	3374	82
9	3456	3538	3620	3702	3784	3866	3948	4030	4112	4194	82
530	724276	724358	724440	724522	724604	724685	724767	724849	724931	725013	82
1	5095		5258	5340	5422	5503	5585	5667			82
2	5912	5993	6075	6156	6238		6401				82
3	6727	6809	6890		7053	7134	7216	7297	7879	7460	81
<b>4 5</b>	7541	7623	7704	7785	7866	7948	8029	8110	8191	8273	81
5	8354	8435	8516	8597	8678	8759	8841		9003	9084	81
6	9165	9246	9327		9489	9570	9651	9732		9893	81
7	9974					730378		730540		730762	81
8	730782	0863	0944	1024	1105	1186	1266	1347	1428	1508	81
9	1589	1669	1750	1830	1911	1991	2072	2152	2233	2313	81
540	732394	732474	732555	732635	732715	732796	732876	732956	733037	733117	80
1	3197	3278	3358	3438	3518	3598	3679	3759	3839	3919	80
2	3999	4079	4160	4240	4320	4400	4480	4560	4640	4720	80
3	4800	4880	4960	5049	5120	5200	5279	5359	5439	5519	80
4	5599	5679	5759	5838	5918	5998	6078	6157	6237	6317	80
4 5	6397	6476	6556	6635	6715	6795	6874	6954	7034	7113	80
6	7193	7272	7352	7431	7511	7590	7670	7749	7829	7908	79
7	7987	8067	8146	8225	8305	8384	8463	8543	8622	8701	79
8	8781	8860	8939	9 118	9097	9177	9256	9335	9414	9493	79
9	9572	9651	9731	9310	9339	9968	740047	740126	740205	740284	79
550	740363	740442	740521	740600	740678	740757	740836	740915	740994	741073	79
1	1152	1230	1309	1388	1467	1546	1624	1703	1782	1860	79
1 2	1939	2018	2096	2175	2254	2332	2411	2489	2568	2647	79
3	2725	2804	2882	2961	3039	3118	3196	3275	3358	3431	78
4	3510	3588	3667	3745	3823	3902	3980	4058	4136	4215	78
5	4293	4371	4419	4523	4606	4684	4762	4840	4919	4997	78
6 7	5075	5153	5231	5309	5387	5465	5543	5621	5699	5777	78
7	5855	5933	6011	6089	6167	6245	6323	6401	6479	6556	78
8	6634	6712	6790	6868	6945	7023	7101	7179	7256	7334	78
9	7412	7489	7567	-7645	7722	7800	7878	7955	8033	8110	78
560	748188	748266	748343	748421	748498	748576	748653	748731	748808	748835	77
1	8963	9040	9118	9195	9272	9350	9427	9504	9582	9659	77
2	9736	9814	9391	9968		750123	750200				77
3 4				750740	0817	0894	0971	1048	1125	1202,	77
4	1279	1356	1433	1510	1587	1664	1741	1818	1895	1972	77
5	2048	2125	2202	2279	2356	2433	2509	2586	2663	2740	77
6 7	2816	2893	2970	3947	3123	3200	- 3277	<b>3</b> 353	3430	3506	77
7	3583	3660	3736	3813	3889	3966	4042	4119	4195	4272	77
8	4348	4425	4501	4578	4654	4730	4807	4883	4960	5086	76
9	5112	5189	5265	5341	5417	5494	5570	5646	5722	5799	76
570	755875	755951	756027	756103	756180	756256	756332	756408	756484	756560	76
1	6636	6712	6788	6864	6940	7016	7092	7168	7244	7820	76
2	7396	7472	7548	7624	7700	7775	7851	7927	8008	8979	76
3	8155	8230	8306	8382	8458	8533	8609	8685	8761	8836	76
4	8912	8988	9063	9189	9214	9290	9366	9441	9517	9592	76
5	9668	9743	9819	9894	9970	760045				760347	75
6			760573	760649	760724	0799	0875	0959	1025	1101	75
7	1176	1251	1326	1402	1477	1552	1627	1702	1778	1853	75
8	1928	2003	2078	2153	2228	2803	2378	2453	2529	2604	75
9	2679	2754	2829	2904	2978	3053	3128	3203	8278	8353	75
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1 4176 4251 4926 4400 4475 75291 5296 5370 5445 5590 5594 75 8 5669 5743 5818 5892 5946 6041 6115 6190 6264 6338 74 4 6418 6437 6522 6866 6710 6785 6859 6933 7007 7082 74 5 7156 7230 7304 7379 7453 7527, 7601 7675 7749 7523 74 6 7898 7972 8046 5120 8194 8268 8342 8416 8490 8564 74 7 8683 8712 8786 8860 8934 9008 9082 9156 9230 9308 74 8 9377 9451 9525 9599 9678 9746 9250 8934 9968 770042 74 9 77015 77015 77028 77028 77038 770410 770484 77057 77082 77042 74 1 5567 77052 77028 77039 771078 771146 771290 771293 771867 770440 771514 74 1 5567 1661 1734 1808 1831 1955 9289 929 918 78 2 9392 2995 2448 8542 2615 2888 2762 2837 2908 2931 78 3 9057 3125 8921 2574 8348 3421 3494 3567, 3640 3718 73 8 8 7016 1830 4663 4736 4869 4852 4855 5028 15100 5133 78 6 5246 3819 5992 3465 5538 5610 5683 8756 5629 502 78 9 7427 7499 7572 7644 7717 7775 7562 7934 8006 8079 72 600 778151 778294 77896 778388 784441 78518 77855 77082 78042 78 4 1037 1109 1181 1253 1824 1897 1855 77852 7856 7859 902 73 8 8 6701 6774 6646 6919 9992 7064 7137 7209 7822 3854 382 42 18 18 18 18 18 18 18 18 18 18 18 18 18	No.	0	1	2	3	4	5	6	7	8	9	Diff.
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3     1404     1472     1541     1609     1678     1747     1515     1884     1952     2221     2221     68       4     2089     2158     2226     2295     2363     2432     2500     2568     2637     2705     68       5     2774     2842     2910     2979     3047     3116     3184     2522     3321     3389     68       6     3457     3525     3594     3662     3730     3798     3867     3935     4003     4071     68       7     4139     4208     4276     4344     4412     4480     4548     4616     4685     4753     68       8     4821     4889     4957     5025     5093     5161     5229     5297     5365     5433     68       9     5501     5569     5687     5705     5773     5841     5908     5976     6044     6112     68	2		0786					1129		1266	1335	
4         2089         2158         2226         2295         2363         2432         2500         2568         2687         2705         68           5         2774         2842         2910         2979         3047         3116         3184         3525         3821         3889         68           6         3457         3525         3594         3662         3730         3798         3867         3935         4003         4071         68           7         4139         4208         4276         4344         4412         4480         4548         4616         4685         4753         68           8         4821         4899         4957         5025         5093         5161         5229         5297         5865         5433         68           9         5501         5569         5687         5705         5773         5841         5908         5976         6044         6112         68	3		1472	1541						1952	2021	69
6         3457         3525         3594         3662         3730         3798         3867         3935         4004         4071         68           7         4139         4208         4276         4944         4412         4480         4548         4616         4685         4753         68           8         4821         4889         4957         5025         5093         3161         5229         5297         5865         5433         68           9         5501         5569         5687         5705         5773         5841         5908         5976         6044         6112         68	4	2089	2158	2226	2295	2363	2432	2500	2568			
7 4139 4208 4276 4344 4412 4480 4548 4616 4685 4753 68 8 4821 4889 4957 5025 5093 5161 5229 5297 5865 5433 68 9 5501 5569 5687 5705 5773 5841 5908 5976 6044 6112 68	5				2979							
8     4321     4389     4957     5025     5093     5161     5229     5297     5365     5483     68       9     5501     5569     5687     5705     5773     5841     5908     5976     6044     6112     68	6											
9 5501 5569 5687 5705 5773 5841 5908 5976 6044 6112 68												
	8											
No. 0 1 2 3 4 5 6 7 8 9 Diff.	9	5501	5569			5113						
	No.	0	1	2	3	4	. 5	6	7	8	9	Diff.

-	No.	0	1	2	3	4	5	6	7	8	9	Diff.
	640	906190	806248	806816	806384	806451	806519	806587	806655	806799	806700	68
	1	6858		6994	7061	7129	7197	7264	7332	7400	7467	68
1	2	7535		7670	77 8	7806	7873	7941	8008	8076	8143	68
1	3	8211	8279	8346	8414	8481	8549	8616	8684	8751	8818	67
ı	4	8886	8953	9021	9088	9156	9223	9290	9358	9425	9492	67
ı	5	9560	9627	9694	9762	9829	9896		810031	810098		67
1	6						810569		0703	0770	0837	67
l	7	0904	0971 1642	1039 1709	1106	1173	1240 1910	1307 1977	1374	1441	1508	67
ı	8	1575 2245	2312	2379	$\frac{1776}{2445}$	1843 2512	2579	2646	2044 2713	2111 2780	2178 2847	67 67
1		11000	1									
۱	650						813247				813514	67
ı	1	3581 4248	3648 4314	3714 4381	3781 4447	3S48 4514	3914 4581	3981 4647	4048 4714	4114 4780	4181 4847	67 67
ı	3	4913	4980	5046	5113	5179	5246	5312	5378	5445	5511	66
l	4	5578	5644	5711	5777	5843	5910	5976	6042	6109	6175	66
1	5 6 7	6241	6308	6374	6440	6506	6573	6639	6705	6771	6838	66
١	6	6904	6970	7036	7102	7169	7235	7301	7367	7433	7499	66
1	7	7565	7631	7698	7764	7830	7896	7962	8028	8094	8160	66
1	8	8226	8292	8358	8424	8490	8556	8622	8688	8754	8820	66
-	9	8885	8951	9017	9083	9149	9215	9281	_9346	9412	9478	66
1	660						819873		820004	820070	820136	66
ı	1	820201	820267	820333	820399		820530		0661	0727	0792	66
	2	0858	6924	0989	1055	1120	1186	1251	1317	1382	1448	66
l	3	1514	1579	1645	1710	1775	1841	1906	1972	2037	2103	65
	4	2168 2822	2233 2887	2299 2952	2364	2430 3(83	2495 3148	2560	2626	2691 3344	2756 34(9	65
	6	3474	3539	3605	3018 3670	3735	3800	3213 3865	3279 3930	3996	4061	65 65
l	7	4126	4191	4256	4321	4386	4451	4516	4581	4646	4711	65
	4 5 6 7 8	4776	4841	4906	4971	5036	5101	5166	5231	5296	5361	65
	9	5426	5491	5556	5621	5686	5751	5815	5880	5945	6010	65
1	670	826075	826140	826204	826269	82.6224	826299	S26464	896598	826593	898658	65
	1	6723	6787	6852	6917	6981	7046	7111	7175	7240	7305	65
	2	7369	7434	7499	7563	7628	7692	7757	7821	7886	7951	65
	2 3	8015	8080	8144	8209	8273	8338	84(2	8467	8531	8595	64
	4 5 6 7	8660	8724	8789	8853	8918	8982	9046	9111	9175	9239	64
	5	9304	9368	9432	9497	9561	9625	9690	9754	9818	9882	64
l	6						830268		830396 1037			64
۱	8	830589 1230	0653 1294	0717 1358	$0781 \\ 1422$	0845 1486	0909 1550	6973 1614	1678	1102 1742	1166 1806	64 64
۱	9	1870	1934	1998	2062	2126	2189	2258	2317	2381	2445	64
1									1		-	-
1	680						832828			3657	3721	64 64
-	1 2	3147 3784	3211 3848	3275 3912	3338 3975	3402 4039	3466 4103	3530 4166	3593 4230	4294	4357	64
1	3	4421	4484	4548	4611	4675	4739	4862	4866	4929	4993	64
1		5056	5120	5183	5247	5310	5373	5437	5500	5564	5627	63
1	5	5691	5754	5817	5881	5944	6007	6071	6134	6197	6261	63
1	6	6324	6387	6451	6514	6577	6641	6704	6767	6830	6894	63
1	7	6957	7020	7083	7146	7210	7273	7836	7899	7462	7525	63
1	8 9	7588	7652	7715	7778	7841	7904	7967		8093	8156	63
1		8219	8282	8345	8408	8471	8534	8597	8660	8723	8786	63
1	690			838975	839038		839164		839289	839352	889415	68
1	1	9478	9541	9604	9667	9729	9792	9855	9918		840043	63
1	2 8	840106 0733	840169 0796	840232 0859	840294 0921	840357	840420	840482 1109	840545 1172	840608 1234	0671 1297	63 63
1	4	1359	1422	1485	1547	1610	1046 1672	1785	1797	1860		63
1	5	1985	2047	2110	2172	2235	2297	2360	2422	2484		62
1	6	2609	2672	2734	2796	2859	2921	2983	3046	3108		62
	7	8233	3295	3357	3420	3482	3544	3606	3669	8731	3793	62
1	8	8855	3918	3980	4042	4104	4166	4229	4291	4353		62
-	9	4477	4539	4601	4664	4726	4788	4850	4912	4974	5036	62
1	No.	0	1	2	3	4	5	6	7	8	9	Diff.
	-	-	-	ASSESSMENT OF REAL PROPERTY.							water to be desired	-

494				LOGAR	HIIMS	OF IN	UMBER	.5.			
No.	0	1	2	3	4	5	6	7	8	9	Diff.
700	845098	845160	845222	845284	845346	845408	845470	845532	845594	845656	62
1	5713	5780	5842		5956		6090	6151	6213	6275	
2	6337	6399	6461	6523	6585	6646	6708	6770	6832	6894	
3	6955	7917	7079	7141	7202	7264	7326	7388	7449	7511	
4	7573	7634	7696	7758	7819	7881	7943	8004	8066	8128	
5 6	8189	8251	8312 8928	8374	8435	8497	8559	8620	8682	8743	
7	88)5 9419	8355 9431	9542	-8989 9604	951 9665	9112 9726	9174 9783	9235 9849	9297 9911	9358 9972	
8	85-1023	850095		850217							
9	0645	0707	0769	083)	0891	0952	1014	1075	1136	1197	
710			851381	851442		951564					
1	1370	1931	1992	2953	2114	2175	2236	2297	2358	2419	61
2	218)	2541	2602	2663	2721	2785	2846	2907	2938	3529	
3	3)9)	3150	3211	3272	3333	3394	3455	3516	3577	3637	61
4	3593	3759	3820	3331	3941	4002	4063	4124	4185	4245	
5 6	4356	4367	4423	4133	4549	4610	4670	4731	4792	4852	
6	4913	4974	5034	5095	5156	5216	5277	5337	5398	5459	
7 8	5519 6124	5580 6185	5649 6245	5701 6336	5761 6366	5822 6427	5882 6487	5943 6548	6003 660S	6064 6638	
9	6729	6789	6850	6910	6970	7031	7091	7152	7212	7272	
						- 1					1
720	357332 7935	897393 7995	S57453 S056	S57513 S116	857574 8176	8236 8236	857694 8297	857755	857815 8417	857875 8477	60
2	8537	8597	8357	8718	8773	8338	8898	8958	9018	9978	60
3	9138	9193	9258	9318	8778 9379	9439	9499	9559	9619	9679	60
4	9739	9799	9359	9918	9978	860038				860278	60
5				8605188		0637	0697	0757	0817	0877	60
6	0937	0996	1056	1116	1176	1236	1295	1355	1415	1475	60
7	1534	1594	1654	1714	1773	1833	1893	1952	2012	2072	60
5 6 7 8 9	2131 2728	2191 2787	2251 2847	2310 2906	2370 2966	2430 3025	2489 3085	2549 3144	2608 3204	2668 3263	60
			i			1	1			1	
730	3917	853332 3977	353442 4036	863501 8 4096	363551 8 4155	333527 8 4214	$\frac{353680}{4274}$	863739 8 <b>433</b> 3	$\frac{363799}{4392}$	863858 4452	59 59
2	4511	4570	4630	4689	4743	4808	4867	4925	4985	5045	59
3	5104	5163	5222	5232	5341	5400	5459	5519	5578	5637	59
4	5393	5755	5314	5874	5933	5992	6051	6110	6169	6228	59
5	6287	6346	6495	6465	6524	6593 7173	6642	6701	6760	6819	59
6	6378	6937	6993	7055	7114	7173	7232	7291	7350	7409	59
7	7467	7523	7585	7614	-7703	7762	7821	7880	7939	7998	59
4 5 6 7 8 9	8356	S115 8703	S174 8732	8233 8821	8292	8350 8938	8439 8997	8468 9056	8527 9114	8586 9173	59 59
	8644	1			8879					1	
749		9377	569349	369408	70070	559525 8	5095848	569642	569701	270045	59
9	9313 870404	370132	9935	99913 870570	0638	870111 8 0693	0755	0S13	0872	0930	59 58
3	0989	1047	1105	1164	1223	1281	1339	1398	1456	1515	58
4	1578	1631	1695	1748	1836	1865	1923	1981	2040	2098	58
5	2153	2215	2273	2331	2389	2448	2506	2564	2622	2681	58
6	2739	2797:	2855	2913	2972	3030	3088	3146	3204	3262	58 58
1 2 3 4 5 6 7 8	3321	\$379	3437	3495	3553	3611	3669	3727	3785	3844	58
9	3902, 4482	3960, 4540,	4018 4593	4976 4656	4134 4714	4192 4772	4250 4830	4308 4888	4366 4945	4424 5003	58 58
			1	1	1			. 1		1	
	875061	375119	5757	S75235 S	75293 8	50351 8		875466 8	6100	875582	58
$\frac{1}{2}$	5640 6218	5393 6276	5756 6333	5813 6391	5871 6449	5929 6507	59S7 6564	6045	6102 6680	6160. 6737	58 58
3	6795	6853	6910	6968	7026	7083	7141	7199	7256	7814	58
4	7371	7429	7487	7541	7602	7659	7717	7774	7832	7889	53
4 5 6 7	7947	8004	8062	8119	8177	8234	8292	8349	8407	8464	59 57 57 57
6	8522	8579	8637	8694	8752	8839	8366	8924	8981	9039	57
	9093	9153	9211	9268	9325	9383	9440	9497	9555	9612	57
8 9	9669 830242	9726 880299	9784	9841 880413	9893		880013 8 0585	880070 8 0642	0699	80185 0756.	57 57
							-				
No.	0	1	2	3	4	5	6	7	8	9	Diff.
											-

No.   O   1   2   3   4   5   6   7   8   9   Diff.					30 01111				-			
1	No.	. 0	1	2	3	4	5	6	7	8	9	Diff.
1	760	220214	990971	890099	880085	881049	881600	881156	221019	891971	881898	57
2												
8         2525         2581         2688         2695         2752         2569         2866         2933         38150         57           5         3661         3718         3775         3832         8888         3945         4402         4759         4115         4172         577           6         4299         42855         4342         4899         4455         4512         4602         4759         4115         4172         577           7         4795         4852         4919         4065         5022         5078         5135         5192         5248         5305         57           8         5861         5185         5414         5031         5557         5644         5700         5513         5512         5613         5670         577           70         4818         5418         5609         6026         6221         6373         5813         5870         5613         5613         5873         8629         8609         5711         56         5424         7898         7490         7497         7411         7417         7423         7802         7802         7802         8669         9121         9777												
4         8,03         8150         82,17         8264         8291         3877         3434         3491         3648         8065         57           6         4229         4295         4342         4399         4465         6522         5078         5185         5192         5248         5305         57           7         4795         4852         4919         4965         5622         5078         5185         5192         5248         5305         57           8         58011         5418         5474         5531         5557         5644         5700         5757         5644         5700         5757         5644         5700         5643         5700         56												57
6         4229         42854         43824         44855         6522         5578         5135         5192         5243         5365         577         68         5861         5415         5474         5581         5587         5644         5700         577         5813         5870         577           70         886491         886547         886044         886044         886046         886048         886066         88716         88773         885829         88849         886047         886049         896049         9750         9866         69         987149         9470         9866         96219         987149         9470		3093										
To   To   To   To   To   To   To   To												
8 5861 5418 5474 5581 5575 5644 5700 5757 5813 5570 57  9 5926 5983 6039 6096 6152 6209 6265 6321 6378 6434 57  770 886491 886547 886604 886666 886716 886773 886829 886855 886942 88699 56  1 7054 7111 7167 7223 7280 7396 7392 7449 7575 7561 56  8 8179 8236 8292 8348 8404 8460 8516 8573 6811 8067 8123 56  8 8179 8236 8292 8348 8404 8460 8516 8573 6292 8685 56  5 9302 9358 9414 9470 9526 9582 9638 9694 9750 9866 56  6 9802 9918 9974 890.30 89085 80.41 89197 89.235 898.39 930.85  8 0930 1035 10.91 1147 12.3 1259 1314 1370 1426 1482 56  8 1937 1593 1649 1705 1760 1161 1372 -1928 1938 2090 56  8 0930 1035 10.91 1147 12.3 1259 1314 1370 1426 1482 56  8 1930 1045 1494 1705 1760 1316 1372 -1928 1938 2090 56  780 892095 892150 892202 892317 892573 892429 892484 892540 892595 56  8 370 2862 3318 3373 3429 3434 8540 3595 3651 3706 56  8 370 2862 3318 3373 3429 3434 8540 3595 3651 3706 56  8 370 3862 3318 3373 3429 3434 8540 3595 3651 3706 55  6 5423 5478 5483 5588 5644 5690 5754 5819 5864 5920 55  6 5423 5478 5483 5588 5644 5690 5754 5819 5864 5920 55  7 5970 897627 897682 897787 897792 897847 897962 897957 898012 89867 898122 55  7 5970 897627 897682 897787 897792 897847 897962 897957 898012 89867 898122 55  5 4 9321 9375 9381 9383 9383 9384 9384 9494 9494 9494 9495 9494 9495 9494 9494 9495 9494 9494 9495 9494												
To   Sedel   Sedes   Seded   Sede   Glob   Glob   Geof												
Trop												
To   To   To   To   To   To   To   To			1				10.00					
2									886885			
8         8170         8292         8292         8348         8404         8460         8516         8573         8629         8655         56           5         9302         9358         9414         9470         9526         9582         9638         9594         9500         9866         56           6         9802         9918         9974         890308         890086         80081         9973         890308         99036         56           7         90421         89042         89038         56         66         700         6756         612         668         924         56           8         6930         1035         1091         1147         12.3         12.99         1341         1370         1426         1482         56           780         89205         892150         892206         892202         892317         89237         89244         892540         892259.5         56           780         89205         892150         89226         89232         89234         8923         8944         8930         8924         8925         89215         56           780         89250         8931         8	1											
4         8741         8797         8355         89.9         8965         9021         9170         9184         9190         9246         56           6         9802         9918         9974         89.030         890080         89042         89042         9918         9974         89.0430         890086         80041         890421         890477         890538         6589         6645         6700         6756         6612         6682         6924         56           8         6930         1055         1691         1147         123         1229         1314         1370         1426         1482         56           9         1537         1593         1649         1705         1760         1816         1872         1928         1983         2639         56           780         892905         892150         892206         892217         892813         892813         892813         892414         8934         89404         89244         89240         89244         89250         89250         566           1         2657         5215         3626         3691         5146         5201         5257         5812         586         5												
6         9932         99382         9914         974         99.08         95.09         95.09         95.09         95.09         95.09         56         7         890421         89.0441         89.0441         89.0441         89.0441										9190		
6   9862   9918   9974   890.80   890.86   89.141   890.197   890.253   890.865   56   8   930   1035   10.91   1147   12.3   12.9   1314   1370   1426   1482   56   9   1537   1593   1649   1705   1760   1816   1572   1928   1983   2029   56   780   892.905   892.105   892.206   892.262   892.317   892.373   892.492   892.484   892.540   892.595   56   1   2651   2767   2762   2818   2573   2929   295.5   3040   30.96   3151   56   2   3207   2926   3318   3373   3429   3434   3540   35.95   3651   3766   56   3   3762   3817   3873   3928   3984   40.89   44.94   41.50   42.05   42.61   56   4   4316   4371   4427   4482   4538   40.99   40.48   4704   47.59   4814   55   5   4370   492.5   498.0   50.66   50.91   51.46   52.01   52.57   5312   5367   55   7   5975   60.80   60.85   61.40   61.95   62.51   63.66   63.61   6416   6471   55   8   652.6   6581   663.6   660.2   6747   68.2   6857   6912   6967   70.22   55   7   5075   60.80   60.85   61.40   61.95   62.51   63.66   63.61   6416   6471   55   8   652.6   6581   63.66   60.92   6747   68.2   6857   6912   6967   70.22   55   7   5075   807682   89773   897792   897847   897902   897957   898067   898122   55   1   8176   8231   8286   8341   8396   8451   8506   8561   8615   8670   55   2   8725   8780   8335   8393   9437   9492   9544   96.2   96.56   9711   7060   55   3   9273   9323   9383   9437   9492   9547   96.2   96.56   9711   7060   55   4   9821   9875   9930   9985 90.039 90.049   90.64   91.09   91.64   9218   55   5   900.667   900.67												
8         (980)         1035         1649         1147         12.3         12.9         1314         1870         1426         1482         56           780         892205         892150         892206         892206         892217         892317         892313         89249         892484         892540         892505         56           1         2651         2707         2702         2318         2873         2929         2955         3040         3096         3151         56           2         3207         3262         3318         3373         3429         3444         3540         3595         3661         3706         56           3         3762         3817         3429         3444         3595         3661         3706         4261         56           4         4316         4371         4427         4482         4588         4593         4648         4704         4759         4814         55           5         4876         4925         4980         5036         5619         5146         5201         5257         5812         5807         5812         5807         7907         7975         6030         6085	6				890030		89:141	890197	89,253	8903(9	890365	
Total				890533								
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1	9				-	-				0.00	5.0.0	
2   3207   3262   3318   3373   3429   3444   3540   3595   3651   3766   564   4816   4371   4427   4482   4338   4039   4044   4150   4205   4261   55   4870   4925   4980   5036   5091   5146   5201   5257   5312   5367   55   576   5823   5478   5583   5588   5644   5699   5754   5869   5864   5920   55   7   5975   6630   6636   6692   6747   6862   6857   6912   6967   7022   55   7   7   7   7   7   7   7   7												
8         8762         8817         8878         8928         3984         4089         40.91         41.91         4215         4265         4261         55           5         4870         4925         4980         5086         5591         5146         5201         5257         5812         5867         55           6         5423         5478         5583         5588         5644         5699         5754         58.9         5864         5920         57           7         5975         6030         6085         6140         6195         6251         6316         6316         6416         6416         6471         55           8         6526         6581         6636         6692         6747         6862         6857         6912         6967         7022         55           70         87027         89783         89784         89792         89757         89012         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861         89861			2707									
4         4916         4871         4487         4482         4588         4593         4648         4704         4759         4814         55           5         4870         4925         4980         5636         5691         5146         5201         5277         5812         5367         556         5584         5593         5588         5644         5699         5754         58.9         5864         5920         55         7         5975         6030         6085         6140         6195         6221         6366         6361         6416         6471         58         6526         6581         6636         6692         6747         6862         6857         6912         6967         7622         55           9         7077         7132         7187         7242         7297         7352         7407         7462         7517         7512         55           700         897627         897682         89737         89836         8451         8993         8956         8451         8999         89567         8912         55           4         9821         9875         9838         9437         9492         9547         96.2			8262									
5         4870         4925         4980         5686         5691         5146         5201         5257         5812         5867         55           6         5423         5478         5588         5588         5644         5699         5754         58.9         5864         5920         55           7         5975         6080         6085         6140         6195         6251         63:6         63t1         6416         6471         55           8         6526         6581         6686         6092         6747         68.2         6857         6912         6967         7622         55           790         897627         897682         897737         897799         89784         8999         8951         89615         8670         55           1         8176         8231         8286         8941         8999         90.54         910         9164         9218         9567         655           2         8725         8780         9835         930039         9945         9999         90.54         910         9164         9218         9218         947         9921         9766         9566         9711												
6         5428         5478         5588         5684         5699         5754         58.9         5844         5920         55           7         5975         6630         6085         6140         6195         6251         6316         6416         6471         55           8         6526         6581         6636         6602         6747         68c2         6857         6912         6967         7622         55           9         7077         7182         7187         7242         7297         7352         74c7         7462         7517         7572         55           790         897627         897682         89773         897792         897847         8902         8951         8616         8611         8612         8676         55           2         8778         8335         8830         8944         8999         9054         910         9164         9218         955         2670         55           3         9273         9383         9487         9929         9544         8999         9054         910         9164         9218         957         9652         90565         9711         97662         <												
To   Fig.   F												
8         6526         6681         6686         6692         6747         6862         6857         6912         6967         7622         55           700         87627         897682         897737         8977392         897847         897937         89812         55           1         8176         8281         8286         8341         8395         8451         8506         85612         8615         8670         55           2         8725         8780         8835         8390         9944         8999         91.54         910         9104         9218         56           3         9273         9323         9343         9347         992         9547         96.2         9656         9711         9766         55           4         9821         9875         9930         9985         90.039         9040         94         8062         6676         9711         9766         55           5         900367         90422         90531         9857         90.039         9904         90139         9014         9012         9014         9014         9012         9014         855         5           6												
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	8		6581		6692	6747		6857	6912	6967	7622	
1         8176         8931         8286         8341         8296         8451         8506         8561         8615         8670         55           2         8725         8780         8335         8890         8944         8999         9054         9169         9164         9218         55           3         9273         9323         9383         9437         9922         9547         96.2         9656         9711         9766         55           4         9821         9875         9930         9985         90039         90404         90404         90149         9	9	7077	7132	7187	7242	7297	7352	7407	7462	7517	7572	55
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	790	897627	897682	897737	897792	897847	897962	897957	898012	898067	898122	55
8         9973         99828         9983         9437         9992         9547         96.2         9656         9711         9766         55           5         990367         99850         99830         9985         90039         990039         99004         9002028         900258         900258         90039         55           6         6913         6968         1622         1077         1131         1186         1240         1295         1349         1464         56           7         1458         1513         1567         1692         1676         1781         1785         1819         1948         54           8         2003         2057         2112         2166         2221         2275         2529         2384         2438         2492         54           9         2547         2601         2655         2710         2764         2818         2873         2927         2981         3036         54           800         930809         93144         903199         903253         903807         903810         903540         908524         908575         54           1         3683         3687		8176	8231	8286	8341	8396	8451	8506	8561	8615	8670	
4         9821         9875         9939         9985 9.00.39 90.00.4 9.00.14 9.00.12 50.00.00         55           5         900367         900422         900247         90.0231         .0586         .0640         .0095         .0749         .0804         .0859         .55           6         (913)         .0968         .1022         .1077         .1131         .1180         .1295         .1349         .1444         .55           7         .1458         .1513         .1567         .1622         .1676         .1731         .1785         .1840         .1944         .55           8         .2008         .2557         .2112         .2166         .2221         .2275         .2292         .2384         .2488         .2492         .54           800         .903609         .938144         .903149         .903853         .938307         .93861         .93416         .908470         .908524         .908578         .54           1         .3633         .3687         .3741         .3793         .8494         .3905         .4126         .4066         .4120         .54           2         .4174         .4229         .42834         .4378         .4982         .4986	2		8780									
5         900367         900422         900422         904367         900422         904367         90422         904367         904367         904367         904367         904367         904367         90442         90432         1077         1131         1186         1240         1295         1349         1404         55           7         1458         1513         1567         1622         1676         1731         1785         1840         1941         1948         54           8         2003         2957         2112         2166         2921         2275         2329         2384         2488         2492         54           800         903609         938149         9093525         903507         93861         93416         903470         908524         903575         54           1         3633         3687         3741         3755         8849         8904         3958         4012         4066         4120         54           2         4174         4229         4288         4337         4391         4445         4499         4553         4607         4601         54           4         5256         5810         564<												
6         6913         6968         1022         1077         1131         1186         1240         1295         1349         1404         55           7         1458         1513         1567         1622         1676         1731         1785         1840         1894         1948         54           8         2008         2057         2112         2166         2221         2275         2329         2384         2488         2492         54           800         903090         93144         903199         903259         903307         903861         93341         903524         903575         54           1         3633         3687         3741         3795         8849         3944         3058         4112         4666         4120         54           2         4174         4229         4283         4337         4391         4445         4499         4553         4607         4661         54           3         4716         4770         4824         4878         4932         4986         5640         594         5148         5202         54           4         5256         5300         5944         <												
7         1458         1513         1567         1692         1676         1731         1785         1849         1948         54           8         2008         2057         2112         2166         2221         2275         2829         2884         2488         2492         54           800         908090         938144         903199         908253         908307         908361         93416         903470         908524         903578         54           1         3633         3687         3741         3795         8849         3944         3058         4/12         4066         4120         54           2         4174         4229         4283         4337         4391         4445         4499         4553         4607         4661         54           2         4174         4229         4283         4337         4391         4445         4499         4553         4607         4661         54           4         5256         5810         5644         5418         5472         5526         5580         5645         5547         54           5         5796         5850         5944         5958												
8         9008         29077         2112         2166         2921         2275         2899         2384         2488         2492         54           800         903090         903144         903199         908253         903307         908361         903410         908524         903578         54           1         3633         3687         3741         3795         8849         3904         3058         4112         4666         4120         54           2         4174         4229         4283         4387         4391         4445         4499         4553         4607         4601         54           4         5256         5810         5864         5418         5472         5526         5580         5634         5688         5742         54           4         5256         5810         5864         5418         5472         5526         5580         5634         5688         5742         54           5         5796         5850         5904         5958         6012         6066         6119         6173         6227         6281         54           6         6335         6389         6448												
9         2547         2601         2655         2710         2764         2818         2873         2927         2981         3086         54           800         903809         938144         903199         902825         903807         93861         938410         903847         903857         54           1         3693         3687         2741         2795         8849         3944         3958         4012         4661         54           2         4174         4229         4283         4387         4391         4445         4499         4553         4607         4661         54           3         4716         4776         4824         4878         4982         4986         5640         5148         5472         54           5         5796         5850         5904         5918         6418         5472         5526         5580         5687         5742         54           6         6325         6889         6443         6497         (551         6604         6619         6173         6227         6221         54           6         6874         6927         6981         7037         7620												
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$			3687		3795		3904					
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5         1158         1211         1264         1317         1871         1424         1477         1530         1584         1687         58           6         1690         1749         1797         1850         1903         1956         2009         2068         2116         2169         53           7         2292         2275         2825         2381         2438         2488         2541         2594         2647         2700         58           8         2753         2806         2859         2918         2966         8019         3072         3125         8178         3231         58           9         3284         3337         3390         3443         3496         3549         8602         8655         3708         3761         58	3	910091 9	910144 9	910197 9	010251 9	10304 9	10358 9	10411 9		010518	0571	58
6         1699         17443         1797         1850         1903         1956         2009         2068         2116         2169         58           7         2922         2975         2382         2381         2435         2488         2541         2594         2647         2700         58           8         2758         2806         2859         2918         2966         3019         3072         8125         8178         2931         58           9         8284         9337         3390         8443         8496         3549         8602         8655         3708         8761         58	4	0624	0678	0781	0784	0888	0891	0944	0998	1051		
7         2922         2275.         2328         2381         2435         2488         2541         2594         2647         2700         58           8         2753         2806         2859         2913         2966         3019         3072         3125         3178         3231         58           9         3284         3337         3390         3443         3496         3549         3602         3655         3708         3761         58								1477				
8     2753     2806     2859     2918     2966     3019     3072     3125     8178     3231     58       9     8284     3337     3390     3443     3496     3549     8602     8655     3708     3761     58												
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1 4848 4896 4449 4502 4555 4608 4660 4718 4766 4519 58 2 4872 4925 4977 5030 5083 5136 5189 5214 5294 5247 5847 58 3 5400 5433 5505 5555 5611 5664 5716 5769 5892 5515 88 4 5597 5980 6083 6085 6185 6191 6248 6296 6340 6411 84 5 5947 5980 6838 6185 6185 6191 6248 6296 6340 6411 84 5 6444 6507 6559 6612 6664 6717 6770 6822 6875 6927 58 6 6980 7083 7083 7085 7118 7100 7243 7295 7348 41.0 7458 38 7 7506 7588 7611 7668 7110 7768 7890 7873 7925 7978 52 8 8080 8083 8185 8185 8185 8240 6298 845 8397 8456 8562 52 8 9 8555 8667 8869 8712 8764 8518 8569 8891 8946 8562 52 8 9 19078 919130 919183 919285 919287 919340 919892 919444 919469 918549 2 920123 991176 926223 992080 927832 920 84 924456 92648 91646 (198 2017) 926 92149 9167 926719 9267 916 926 914 9967 926719 926 914 9167 926 914 9167 916 916 916 916 916 916 916 916 916 916	820	913814	918867	918920	918978	914096	914079	914139	914194	91/997	91/900	5.2
2 4572 4925 4977 5030 5083 5136 5189 5241 5294 5847 58 4 5927 5980 6083 6085 5115 5611 5664 5716 5709 5822 5857 58 5 644 5507 5590 619 5664 6717 6770 6822 6830 6441 88 5 6444 5507 6559 6619 6664 6717 6770 6822 6857 697 58 8 8030 8083 8135 5188 5240 6298 8245 6897 825 7978 22 9 8555 8667 8659 8712 8760 7710 7708 7825 7838 7440 7348 38 7 7506 7538 7617 7608 7710 7708 7829 7838 7440 7348 38 8 8030 8083 8135 5188 5240 6298 8245 6891 8973 9026 52 8 9 8555 8667 8659 8712 8764 7898 8245 6891 8973 9026 52 9 8 95078 91930 919183 919239 91928 91924 491944 91946 9164 9207 9207 9207 9207 9208 9208 9208 9208 9208 9208 9208 9208		4343	4896	4449	4502	4555						
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6         6404         6507         6559         6612         6644         6717         6776         6822         6575         6927         58           7         7506         7558         7611         7668         7716         7768         7820         7878         740         7598         59           8         5030         8083         8185         8188         8240         8298         8845         8807         845         862         52           80         919078         919188         91928         91927         91740         919999         919444         91946         916169         952         920129         920129         920229         92029         82029         82024         92020         82029         82029         82029         82029         92020         82029         82029												
\$\begin{array}{c} \text{919078} \text{919180} \text{919183} \text{919285} \text{919287} \text{9194} \text{40} \text{91944} \text{91944} \text{91946} \text{967} \text{92017} \text{522} \text{92017} \text{920223} \text{920230} \text{920230} \text{920230} \text{920230} \text{920230} \text{920230} \text{520230} \text{920230} \text{920230} \text{520230} \text{520230} \text{920230} \text{520230} \text{5202300} \text{520230} \text{5202300} \text{52023000} \text{52023000} \text{52023000} \text{520230000} 520230000000000000000000000000000000000	5							6770	6822			
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\$\begin{array}{c} \text{919078} \text{919180} \text{919183} \text{919285} \text{919287} \text{9194} \text{40} \text{91944} \text{91944} \text{91946} \text{967} \text{92017} \text{522} \text{92017} \text{920223} \text{920230} \text{920230} \text{920230} \text{920230} \text{920230} \text{920230} \text{520230} \text{920230} \text{920230} \text{520230} \text{520230} \text{920230} \text{520230} \text{5202300} \text{520230} \text{5202300} \text{52023000} \text{52023000} \text{52023000} \text{520230000} 520230000000000000000000000000000000000	7		7558	7611	7663	7716	7768	7820				
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4         1166         1218         1270         1822         1874         1246         1478         1580         1582         1684         52           5         1686         1788         1790         1242         1894         1946         1988         2602         2112         2154         52           7         2725         2777         2829         2881         2985         2985         3878         3889         3411         3192         52           8         3244         3296         3348         8399         3451         5563         5677         3678         38710         522           840         924279         924331         924888         924438         924488         924488         924484         924498         9244744         52           2470         46848         4699         4951         5068         5675         5616         5757         522         5241         5241         5261         52         5212         5812         5844         5445         5467         6548         6684         6687         6888         6487         6684         6684         6699         7011         7062         7714         7165									000456	920019		
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1         5008         5654         5164         5154         5265         5255         5866         5856         5466         5467         50           3         6011         6061         6111         6162         6212         6262         6313         6868         6413         6468         50           4         6514         6564         6614         6665         6715         6765         6515         6665         C016         6966         50           5         7016         7066         7117         7177         7217         7267         7317         7867         7418         7468         50           6         7518         7568         7618         7668         7718         7769         7819         7869         7919         7969         50           7         8019         8069         8119         8169         8219         8219         8820         8870         8424         8470         50           8         8520         8570         5620         8670         8720         9270         9320         9869         9419         9469         50           870         939519         989569         989619 </td <td>860</td> <td>934498</td> <td>934549</td> <td>984599</td> <td>934650</td> <td>924700</td> <td>984751</td> <td>984801</td> <td>934859</td> <td>984902</td> <td>934953</td> <td>50</td>	860	934498	934549	984599	934650	924700	984751	984801	934859	984902	934953	50
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	010	030019	040060	046119	040169	040019	040967	046917	040367	046417	940467	
4     1511     1561     1611     1660     1710     1760     1819     1859     1919     1988     50       5     2008     2058     2107     2157     2207     2256     2306     2355     2465     2455     50       6     2504     2554     2603     2653     2702     2752     2801     2851     2901     2250     50       7     3000     3049     3099     3148     3198     3247     3297     3846     3896     8445     49       8     8495     3543     4868     4834     8692     3742     3791     8841     3890     3989     49       9     3989     4038     4088     4137     4186     4286     4285     4385     4384     4428     49		0516				0716	0765	6815		0915	0964	
4     1511     1561     1611     1660     1710     1760     1819     1859     1919     1988     50       5     2008     2058     2107     2157     2207     2256     2306     2355     2465     2455     50       6     2504     2554     2603     2653     2702     2752     2801     2851     2901     2250     50       7     3000     3049     3099     3148     3198     3247     3297     3846     3896     8445     49       8     8495     3543     4868     4834     8692     3742     3791     8841     3890     3989     49       9     3989     4038     4088     4137     4186     4286     4285     4385     4384     4428     49	2			1114		1919	1969	1313	1869			
5     2008     2058     2107     2157     2207     2256     2806     2855     2465     245     50       6     2504     2554     2603     2653     2702     2752     2801     2851     2901     2950     50       7     3000     3049     3699     3148     3198     8247     3297     3846     896     8445     49       8     8495     3544     3593     3643     3692     3742     3791     3841     3890     3989     49       9     3989     4038     4088     4187     4186     4236     4285     4335     4384     4488     49	4					1710	1760					
8 8495 8544 8598 8643 8692 8742 8791 8841 8890 8989 49 9 8989 4088 4088 4187 4186 4286 4285 4385 4384 4488 49	5					2207	2256	2306				
8 8495 8544 8598 8643 8692 8742 8791 8841 8890 8989 49 9 8989 4088 4088 4187 4186 4286 4285 4385 4384 4488 49	6					2702	2752					
8 8495 8544 8598 8643 8692 8742 8791 8841 8890 8989 49 9 8989 4088 4088 4187 4186 4286 4285 4385 4384 4488 49	7					3198	3247					
9 3989 4038 4088 4137 4186 4236 4285 4335 4384 4433 49	8			3593								
	9											
No. 1 0   1 2   3   4   5   6   7   8   9   Diff.												
	No.	0 1	1	2	3	4	5	6	1-1	8	9 1	DIII.

					1		111				
No.	0	1	2	3	4	5	6	7	8	9	Diff.
880	044429	014590	014591	944631	044690	011790	944779	0.14899	01/1977	044097	49
1	4976				5173	5222		5321			49
2	5469			5616	5665	5715	5764	5813			
3	5961			6108	6157	6207	6256	6305	6354		49
4	6452			6500	6649	6698	6747	6796			49
5	6943		7041	7090	7140	7189	7238	7287	7336		49
6	7434			7581	7630	7679	7728	7777	7826	7875	49
7	7924		8022	8970	8119	8168	8217 8706	8266	8315	8364	49
8	8413		8511	8560 9048	8609 9097	8557 9146	9195	8755 9244	\$804 9292	8853 9341	49 49
		!	1					-	0.00		
890			949488	949536	949585	949634	949683	949731	949780	949829	49
1	9878	9926		953024							49
2 3	950505	950414	0949	0511	0560 1046	0608 1695	0657 1143	0706 1192	$0754 \\ 1240$	0803 1289	49
4	1338	1386	1435	1483	1532	1580	1629	1677	1726	1775	49
5	1823	1872	1920	1969	2017	2066	2114	2163	2211	2260	48
6	2308	2356	2405	2453	2502	2550	2599	2647	2696	2744	48
7	2792	2841	2889	2938	2936	3034	3083	3131	3180	3228	48
8	3276	3325	3373	3421	3470	3518	3566	3615	3663	3711	48
9	3760	3808	3856	39,15	3933	4001	4049	<b>-4098</b>	4146	4194	48
930	954243	954291	954339	954387	954435	954484	954532	954580	954628	954677	48
1	4725	4773	4821	4869	4918	4966	5014	5062	5110	5158	48
2	5207	5255	5303	5351	5399	5447	5495	5543	5592	5640	48
3	5683	5736	5784	5332	5830	5928	5976	6024	6072	6120	48
4	6168	6216	6265	6313	6361	6409	6457	6505	6553	6601	48
5	6649	6697	6745	6793	6840	6888	6936	6984	7032	7080	48
6	7123 7607	7176	7224 7703	7272	7320 7799	7368 7847	7416 7894	7464 7942	7512 7990	7559 8038	48 48
8	8086	7655 8134	8181	8229	8277	8325	8373	8421	8468	8516	48
9	8564	8612	8659	8707	8755	8803	8850	8898	8946	8994	48
910				959185		1			959423		48
1	9518	9566	9814	9661	9709	9757	9304	9852	9900	9947	48
2				960138							48
3	960471	0518	0566	0613.	0661	0709.	0756	0804	0851	0899	48
4	0946	0994	1041	1089	1136	1184	1231	1279	1326	1374	48
5	1421	1469.	1516	1563	1611	1658	1706	1753	1801	1848	47
6	1895	1943	1993	2,338	2085	2132	2180	2227	2275	2322	47
7	2369	2417	2464	2511	2559	2606	2653	2701	2748	2795	47
8	2843 3316	2390 3363	2937 3410	2985 3457	3032 3504	3079 3552	3126 3599	3174 3646	3221 3693	3268 3741	47 47
				1	1	1					
920				963929					964165		47
1	4260	4307	4354	4401	4448	4495	4542	4590	4637	4684	47
2 3	4731 5202	4778 5249	4825 5296	4872 5343	4919 5390	4966	5013 5484	5061	5108	5155	47 47
4	5672	5719	5766	5813	5860	5437 5907	5954	5531 6001	5578 6048	5625 6095	47
5	6142	6189	6236	6283	6329	6376	6423	6470	6517	6564	47
	6611	6658	6705	6752	6799	6845	6892	6939	6986	7033	47
6	7080	7127:	7173	7220	7267	7314	7361	7408	7454	7501	47
8	7548	7595	7642	7688	7735	7782	7829	7875	7922	7969	47
9	8016	8062	8109	8156	8203	8249	8296	8343	8390	8436	47
930	968488	968530	938576	968623	963670	968716	968763	968810	968856	968903	47
	8950	8996	9043	90901	9136	9183	9229	9276	9323	9369	47
1 2	9416	9463	9509	9556	9802	9649	9695	9742	9789	9835	47
3	9382	9928	9975	970021	970068	970114	970161	970207	970254	970300	47
4	970347	970393	970440	0486	0533	0579	0626	0672	0719	0765	46
5	0812	0858	0904	0951	0997	1044	1090	1137	1183	1229	46
6	1276	1322	1369	1415	1461	1508	1554	1601	1647	1693	46
7 8	1740	1786	1832	1879	1925	1971	2018	2064	2110	2157	46
9	2203 2666	2249 2712	2295 2758	2342 2804	2388 2851	2434 2897	$\frac{2481}{2943}$	2527 2989	2573 3035	2619 3082	46 46
				-							-
No.	0	1	2	3	4	5	6	7	8	9	Diff.
	THE OWNER WHEN PERSON NAMED IN										

400	ACCIMITATION OF TROMBERON												
No.	0	1	2	3	4	5	6	7	8	9	Diff.		
940	973128	973174	973220	973266	978813	973359	978405	973451	973497	973543	46		
1	3590		3682	3728	3774	3820	3866		3959	4005	46		
2	4051	4097	4143	4189	4235	4281	4327	4374			46		
3	4512	4558	4604	465)	4693	4742	4788				46		
4	4972	5018	5064	5110	5156	$\frac{5202}{5662}$	5248		5340	5386	46		
5	5432 5891	5478 5937	5524 5983	5570 6029	5616 6075	6121	5707 6167	5753 6212	5799 6258	5845 6304	46 46		
7	6350	6396	6442	6488	6533	6579	6625	6671	6717	6763	46		
8	6808	6854	6900	6946	6992	7037	7088	7129	7175	7220	46		
9	7266	7312	7358	7403	7449	7495	7541	7586	7632	7678	46		
950	977724	977769	977815	977861	977906	977952	977998	978043	978089	978135	46		
1	8181	8226	8272	8317	8363	8409	8454	8500	8546	8591	46		
2	8637	8683	8728	8774	8819	8865	8911	8956	9002	9047	46		
3	9093	9138	9184	9230	9275	9321	9366	9412	9457	9503	46		
4	9548	9594	9639	9685	9730	9776	9821	9867	9912	9958	46		
5		980049		980140			980276	980322	980367		45		
6	0458 0912	0503 0957	0549 1003	0594 1048	0640 1093	0685 1139	0730 1184	0776 1229	0821 1275	0867 1320	45 45		
8	1366	1411	1456	1501	1547	1592	1637	1683	1728	1773	45		
9	1819	1864	1909	1954	2000	2045	2090	2135	2181	2226	45		
		- 1			1			100					
960	982271 2723	2769	982362 2814	2859	2914	2949	952543 2 <b>99</b> 4	982588	3085	3130	45 45		
2	3175	3220	3265	3310	3356	3401	3446	3491	3536	3581	45		
3	3626	3671	3716	3762	3807	3852	3897	3942	3987	4032	45		
4	4077	4122	4167	4212	4257	4302	4347	4392	4437	4482	45		
5	4527	4572	4617	4662	4707	4752	4797	4842	4887	4932	45		
6	4977	5022	5067	5112	5157	5202	5247	5292	5337	5382	45		
7	5426	5471	5516	5561	5606	5651	5696	5741	5786	5830	45		
8	5875	5920	5965	6010	6055	6100	0144	6189	6234	6279	45		
9	6324	6369	6413	6458	6503	6548	6593	6637	6682	6727	45		
	986772			986936							45		
1	7219	7264	7309	7858	7398	7443	7488	7532	7577	7622	45		
2 3	7666	7711	7756	7800	7845	7890	7934	7979	8024 8470	8068 8514	45 45		
4	8113 8559	8157 8604	8202 8648	8247 8693	8291 8737	8336 8782	8381 8826	8425 8871	8916	8960	45		
5	9305	9049	9094	9138	9183	9227	9272	9316	9361	9405	45		
5 6	9450	9494	9539	9583	9628	9672	9717	9761	9806	9850	44		
7	9895	9939	9983	990028	990072		990161				44		
	990339		990428	0472	0516	0561	0605	0650	0694	0738	44		
9	0783	0827	0871	6916	0960	1004	1049	1093	1137	1182	44		
980	991226	991270	991315	991359	991403	991448	991492	991536		991625	44		
1	1669	1713	1758	1802	1846	1890	1935	1979	2023	2067	44		
2	2111	2156	2200	2244	2288	2333	2377	2421	2465	2509	44		
3	2554 2995	2598 3039	2642 3083	2686 3127	2730 3172	$\frac{2774}{3216}$	2819 3260	2863 3304	2907 3348	2951 8392	44		
5	3436	3480	3524	3568	3613	3657	3701	3745	3789	3833	44		
6	3877	3921	3965	4009	4053	4097	4141	4185	4229	4273	44		
7	4317	4361	4405	4119	4493	4537	4581	4625	4669	4713	44		
8	4757	4801	4845	4889	4933	4977	5021	5065	5108	5152	44		
9	5196	5240	5284	5328	5372	5416	5460	5504	5547	5591	44		
990	995635	995679	995728	995767	995811	995854	995898	995942	995986	996030	44		
1	6074	6117	6161	6205	6249	6293	6337	6380	6424	6468	44		
2	6512	6555	6599	6643	6687	6731	6774	6818	6862	6906	44		
3	6949	6993	7037	7080	7124	7168	7212		7299	7843	44		
4	7386	7430	7474	7517	7561	7605	7648			7779	44		
5	7823 8259	7867 8303	7910 8347	7954 8390	7998 8434	8041			8172 8608	8216 8652	44		
7	8209	8739	8782	8826	8434 8869	8477 8913	8956				44		
8	9131	9174	9218	9261	9305		9392			9522	44		
9	9565		9652	9696	9739	9783	9826		9913		43		
No.		1	2	3		5	6	7	8	9	Diff.		
140.	0	1	l Z	1 3	4	1 5	1 0	1_ 1_	1 0	1 3	DIII.		

Table of the Lengths of Circular Arcs, radius being unity.

Sec	Length of arc	Mın.	Length of arc.	Deg.	Length of arc.	Deg.	Length of arc
1	0.0000048	1	0.0002909	1	0.0174533	61	1.0646509
2	.0000097	2	.0005818	2 2	·0349066	62	.0821042
. 3	0000145	3	.0008727	8	0523599	63	.0995575
4	*0000194	4	0011636	4	•0698132	64	1170108
5	0000242	5	*0014544	5	*0872665 *1047198	65	1344641
6	*0000291	6	0017453	6 7	1047198	66	1519174
7	*0000339	7 8	*0020362	8	1396263	67	1693707
8	*0000388 *0000436	9	*0023271 *0026181	9	1570796	68	·1868240 ·2042773
10	0000485	10	0020181	10	1745329	70	2042113
11	*0000533	11	0023003	11	1919862	71	2391839
12	.0000582	12	.0034907	12	2094395	72	2566372
13	.0000630	13	.0037816	13	-2268928	73	2740905
14	.0000679	14	.0040725	14	·2443461	74	2915438
15	*0000727	15	.0043634	15	2617994	75	*3089970
16	*0000776	16	.0046543	16	•2792527	76	3264502
17	*0000824	17	.0049452	17	2967060	77	•3439034
18	.0000873	18	*0052361	18	*3141593	78	3613567
19	*0000921	19	.0055270	19	*3316136	79	3788100
2)	*0000970	20	•0058178	20	•3490659	80	*3962634
21	*0001018	21	0061087	21	*8665192	81	4137167
22	0001067	22 23	0063996	22 23	·3839725 ·4014258	82	*4311700
23	0001115	24	*0066935 *0069814	24	4188791	83	*4486233
24 25	0001164	25	0009314	25	4363324	84 85	•4660766 •4835299
26	0001212	26	0075632	26	4537857	86	5009832
27	0001201	27	0078540	27	4712390	87	5184365
23	0001358	28	0013340	28	4886923	88	•5358898
29	0001406	29	*0084358	29	•5061456	89	*5533431
3)	0001454	30	0087266	30	-5235988	90	•5707963
31	.0001502	31	0090175	31	•5410521	91	5882496
32	.0001551	32	.0093084	32	•5585054	92	.6057029
33	•0001599	33	.0095993	33	•5759587	93	•6231562
34	*0001648	34	.0093902	34	•5934120	94	·6406095
35	*0001696	35	.0101811	35	6108653	95	6580628
36	'0001745	36	0104720	36	6283186	96	6755561
37	.0001793	37	0107629	37	6457719	97	6929694
38 39	*0001842	38 39	0110538	38	·6632252 ·6806785	98	•7104227
40	.0001890	40	·0113447 ·0116355	40	6981317	99 100	•7278760
41	*0001939 *0001987	41	0119264	41	·7155850	100	·7453293 ·7627826
42	0001331	42	0122173	42	•7330383	2	·7802359
43	0002030	43	0125082	43	-7504916	3	1802333
44	•0002133	44	0127991	44	7679449	4	·S154125
45	-0002181	45	0130900	45	·78539S2	5.	*8325958
46	-0002230	46	0133809	46	8028515	6	·S500491
47	0002278	47	0136718	47	8203048	7	8675024
48	.0002327	48	*0139627	48	·8377581	8	*8849557
49	.0002375	49	0142536	49	8552113	9	9024090
50	0002121	50	0145444	50	*8726646	110	9198622
51	.0002472	51	*0148353	51	8901179	11	9373155
52	*0002521	$\frac{52}{2}$	0151262	52	9075712	12	9547688
53	*0002569	53	0154171	53	9250245	13	9722221
54	-0002618	54	0157089	54	9424778	14	9896754
55 56	0002666	55	*0159989	55	9599311	15	2.0071287
57	*0002715	56	0162898	56	9773844	16	*0245820
58	*0002763 *0002812	57 58	·0165807 ·0168716	57 58	9948377	17 18	·0420353 ·0594886
59	0002812	59	0171625	59	1·0122910 ·0297443	19	0769419
60	0002300	60	0174533	60	0471976	120	0943951
30	0002000	00	0113000	00	0111010	120	TOTOTO

Table of the Lengths of Circular Arcs, radius being unity.

Deg.	Length of arc	Deg.	Length cfarc.	Deg	Length of arc.	Deg.	Length of arc.
121	2.1118484	181	3.1590460	241	4.2062435	301	5.2584411
2	1293017	2	1764993	2	2236968	2	2708944
3	1467550	3	1939526	3	•2411501	3	2883477
4	1642088	4	2114059	4	2586034	4	-3058010
$\bar{5}$	1816616	5	2288592	5	2760567	5	*3232542
6	1991149	6	2463125	6	2935100	6	*3407075
7	•2165682	7	2637658	7	-3109633	7	*3581608
8	2340215	1 8	2812191	8	-3284166	8	*3756141
9	2514748	9	2986724	9	-3458699	9	3930674
130	-2689280	190	*3161256	250	*3633231	310	4105207
1	•2863813	1	3335789	1	3807764	1	4279740
2	-3038346	$\frac{1}{2}$	3510322	2	3982297	2	*4454273
3	3212879	3	3684855	3	•4156830	3	4628806
4	-3387412	4	3859388	4	•4331363	4	*4803339
5	*3561945	5	4033921	5	4505896	5	4977872
6	3736478	6	*4208454	6	•4680429	6	•5152405
7	*3911011	7	·4382987	7	4854962	7	.5326938
8	•4085544	8	4557520	8	•5029495	8 -	5501471
9	4260077	9	4732053	9	5204028	9	•5676004
140	•4434609	200	4906585	260	•5378560	320	·5850536
1	•4609143	1	5081118	1	•5553093	100	6025069
3	4783676	2	5255651	2	5727626	2	6199202
3	4958209	3	•5430184	3	5902160	3	6374135
4	5132742	4	•5604717	4	-6076693	4	.6548668
4 5 6 7	5307274	5	.5779250	5	6251225	5	6723201
6	•5481807	6	*5953783	6	6425758	6	6897744
7	5656340	7	*6128316	7	6600291	7 -	7072267
8	5830873	8	•630.2849	8	6774824	8	7246800
9	6005406	9	•6477382	9	•6949357	9	7421332
150	*6179939	210	6651914	270	7123890	330	7595865
1	6354472	1	6826447	1	7298423	1	7770398
2	6529005	2	7000980	2 3	7472956	2	7944931
2 3 4 5 6 7	6703538	3	7175513	3	7647489	3	·S119464
4	6878071	4	7350046	4 5	7822022	4	8293997
5	7052604	5 6	7524579	6	•7996554	5	*8468530
6	*7227137	7	·7699112 ·7873645	7	*8171087 *8345620	6	*8643063 *8817596
8	7401670	8	8048178	8	8520153	8	8992129
8	7576203	9	8222711	9	8694686	9	9166661
9	7750736	220	8397243	280	-8869219	340	9341194
160	·7925268 ·8099801	1	8571776	1	9043752	1	9515727
$\frac{1}{2}$		2	8746309	2	9218285	2	9690260
2 2	*8274334 *8448867	3	8920842	3	9392818	3	9864793
3 4 5	·\$623400	4	9095375	4	9567351	4 11	6.0039326
5	8797933	5	9269908	5	9741883	5 11	0213859
6	8972466	5 6	9144441	6	9916416	6 1:	0388392
6 7	9146999	7	9618974	7	5.0090949	7	0562955
8	9321532	8	9793507	8	0264582	. 8	0737458
9	9496065	9	9968040	9	*0440015	9	-0911990
170	9670597	230	4.0142572	290	0614548	350	1086523
1	9845130	1	0317106	1	0789081	1//	1261056
	3.0019667	2	.0491639		0963614	. 2	1435589
$\frac{2}{3}$	0194196	3	-0666172	2 3	1138147	3	1610122
4	0368729	4	0840705	4	1312680	4	1784655
4 5	0543262	5	1015237	5	1487213	5	•1959188
6	0707795	6	1189770	6	1661746	6 -	2133721
7	0892328	7	1364303	7	1836279	7	-2308254
8	1066861	8	1538836	8	2010812	. 8	-2482787
9	•1241394	9	1713369	9	2185345	9	2657320
180	•1415927	240	1887902	300	2359878	360	2831853
			1	ii		11114	

# EXPLANATION OF THE USES AND APPLICATIONS OF THE TABLE OF LONG CHORDS.

#### PROBLEM.

Required to find the distances or abscissas on the chord from which, if ordinates or perpendiculars be drawn, they will pass through the station points on the curve.

Example.—Let the given curve be 1000 ft. long of 5° curvature,

or 1146 ft. radius.

For the first station from the beginning we have

chord for 1000 ft. — chord for 800 ft. 
$$\frac{\text{chord for 1000 ft.}}{2}$$
 = 1st distance,

$$\frac{\text{chord } 800 - \text{chord } 600}{2} = 2\text{nd distance, etc.}$$

Then by table we have,

$$\frac{968 \cdot 87 - 784 \cdot 10}{2} = 92 \cdot 385$$

$$\frac{784 \cdot 10 - 593 \cdot 36}{2} = 95 \cdot 370$$

$$\frac{593 \cdot 36 - 398 \cdot 10}{2} = 97 \cdot 630$$

$$\frac{398 \cdot 10 - 198 \cdot 81}{2} = 99 \cdot 645$$

$$\frac{198 \cdot 81 - 0000}{2} = 99 \cdot 405$$

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$$\frac{198 \cdot 81 - 0000}{2} = 99 \cdot 405$$

Thus for any given station we take from the length of the whole chord the length of a chord of twice as many stations less than the one under consideration; that is, 1st station from beginning 2 less; 2 from beginning, 4 less, etc., and take half the difference.

If the chord had been for 900 ft. of curve, we should have,

$$\frac{877 \cdot 32 - 689 \cdot 39}{2} = 93 \cdot 965 = 1 \text{st distance.}$$

$$\frac{689 \cdot 39 - 496 \cdot 20}{2} = 96 \cdot 595 = 2 \text{nd} \qquad \text{``}$$

$$\frac{496 \cdot 20 - 299 \cdot 24}{2} = 98 \cdot 480 = 3 \text{rd} \qquad \text{``}$$

$$\frac{299 \cdot 24 - 100}{2} = \frac{99 \cdot 620}{2} = 4 \text{th} \qquad \text{``}$$

$$\frac{388 \cdot 660}{4 \text{dd}} = \frac{877 \cdot 32}{2} = \text{half length of chord.}$$

In like manner we may find the ordinates connecting these abscissas with their points on the curve.

Let the length of chord and radius be as already given. Then

we have,

Mid. ordinate 1000 ft. — mid. ordinate 800 ft. curve = ordinate at 1st station.

Mid. ordinate 1000 ft. — mid. ordinate 600 ft. = ordinate at

2nd station.

For this purpose we have calculated a table of middle ordinates corresponding to that of long chords. From this we have,

```
107:39 — 69:13 = 38:62 = 1st ordinate.

107:39 — 39:06 = 68:33 = 2nd "

107:39 — 17:41 = 89:98 = 3rd "

107:39 — 4:36 = 103:03 = 4th "

107:39 — 0:00 = 107:39 = 5th or middle ordinate.
```

Were the chord for 900 ft. of curve we should have by tables,

```
87·25 — 53·05 = 34·20 = 1st ordinate.

87·25 — 27·17 = 60·08 = 2nd "

87·25 — 9·81 = 77·44 = 3rd "

87·25 — 1·09 = 86·16 = 4th "

87·25 — 0·00 = 87·25 = middle "
```

This will sufficiently demonstrate how the ordinates can be obtained for any other length of chord or curve. The same principle obtains in regard to any other rate of curvature. After passing the middle ordinate, their lengths will be repeated inversely; as will also be the intermediate lengths of abscissas. Then from end of first abscissa erect first ordinate, and so on in regular rotation.

TABLE

Of Middle Ordinates from Chords subtending Curves of from 100 to 1000 feet in length; calculated to every 15' of Curvature from 15' to 8°. Radius of 1° being 5730 feet.

			LE	NGTHS	OF A	RCS.				
	100	200	300	400	500	600	700	800	900	1000
	1/-		M	IDDLE	ORDINA	res.				
Curvature.		1	1	1	1	1	1	1	1	1
Curvature.	.]								-	
0° 15′	0.06	0:22	0.49	0.87	1.36	1.96	2.67	3.49	4.42	5.45
30	0.11	0.44	0.98	1.75	2.73	3.93	5.84	6.98	8.83	10.90
45	0.16	0.65	1.47	2.62	4.09	5.89	8.01	10.47	13.25	16.35
1° 00'	0.22	0.87	1.96	3.49	5.45	7.85_	10.69	13.96	17.67	21.80
15	0.27	1.09	2.45	4.36	6.82	9.81	13.36	17.44	22.67	27.24
30	0.33	1.31	2.94	5.23	8.18	11.77	16.03	20.93	26.48	32.68
45	0.38	1.53	3.43	6.11	9.54	13.73	18.70	24.41	30.88	38.11
2° 00'	0.44	1.75	3.92	6.98	10.90	15.68	21.35	27.88	35.27	43.52
15	0.49	1.96	4.41	7.85	12.26	17.64	24.02	31.35	39.66	48.93
30	0.55	2.18	4.91	8.72	13.62	19.60	26.68	34.82	44.04	54.33
45	0.60	2.40	5.40	9.59	14.98	21.56	29.33	38.29	48.41	59.71
3° 00'	0.65	2.62	5.89	10.46	16.34	23.52	31.98	41.74	52.78	65.68
15	0.71	2.84	6.33	11.33	17.70	25.47	34.63	45.19	57.13	70.44
30	0.76	3.05	6.87	12.20	19.06	27.42	37.28	48.63	61.47	75.78
45	0.82	3.27	7.36	13.67	20.41	29.36	39.92	52.07	65.80	81.10
4° 00'	0.87	3.49	7.85	13.94	21.77	31.31	42.56	55.50	70.12	86.40
15	0.93	3.71	8.34	14.81	23.12	33.25	45.19	58.92	74.48	91.68
30	0.98	3.93	8.82	15.68	24.47	35.19	47.82	62.34	78.72	96.94
45	1.04	4.14	9.32	16.55	25.82	37.13	50.44	65.74	82.99	1(2.18
5° 00'	1.09	4.36	9.81	17.41	27.17	39.06	53.05	69.13	87.25	107:39
15	1.15	4.58	10.30	18.28	28.52	40.99	55.67	72.51	90.50	112.58
30	1.20	4.80	10.79	19.15	29.87	42.92	58.27	75.88	95 73	117.75
45	1.25	5.01	11.27	20.01	31.21	44.84	60.86	79.25	99.94	122.89
6, 00,	1.31	5.23	11.76	20.88	32.55	46.76	63.45	82.60	104.13	127.99
15	1.36	5.45	12.25	21.74	33.89	48.67	66.04	85.93	1(8:30	133.07
30	1.42	5.67	12.74	22.60	35.23	50.59	68.62	89.26	112.45	138-12
45	1.47	5.89	13.23	23.47	36.57	52.50	71.18	92.57	116.58	
7° 00'	1.53	6.10	13.71	24.33	37.91	54.40	73.74	95.87		148.12
15	1.58	6.32	14.20	25.19	39.24	56.30	76.30	99.15	124.78	173 07
30	1.64	6:54	14.69	26.05	40.57	58.19	78.84	162.42	128.84	157.98
45	1.69	6.76	15.18	26.91	41.90	60.08	81.37	105.68		162.86
8° 00'	1.75	6.98	15.66	27.77	43.23	61.97	83.90	108.92		167.70
NAME AND										-
	1/		1	-						

On the principles by which the following tables are calculated.

Let m = linear opening of switch rail, s = angular opening of

rail, f = angle of frog, g = gauge of track. Let x = length of ehord from opening of switch rail to point offrog. Then will the amount of curvature between the opening of rail where curve commences and point of frog = f--s; therefore the instrument setting over the open end of switch rail with a backsight on the fixed end of it, the instrumental deflection to the point of frog will be  $=\frac{f-s}{2}$ . But if the backsight be taken on a point (say 5 inches distant) parallel with the main track, the deflection will then be  $=\frac{f-s}{2}+s=\frac{f+s}{2}$ . Making the value of x, radius, g-m will be homologous to the sine of  $\frac{f+s}{2}$ . Then we have,

$$\operatorname{Sin}\left(\frac{f+s}{2}\right):R::g-m:x=\frac{R(g-m)}{\sin\left(\frac{f\div s}{2}\right)}$$

EXAMPLE:

Calling  $s=1^{\circ}$  15',  $f=6^{\circ}$  45', g=4.70, m=0.42, and g-m=4.28, we have sin.  $4^{\circ}:R:4.28:x=61.36$ ft.

When a double opening of a switch rail for a double turnout occurs, we have,

sin. 
$$\left(\frac{f+2s}{2}\right)$$
:  $R:: g-2\times 0: x = \text{distance to nearest frog.}$ 

The linear and angular opening of rail being the same, this table may be adapted to any other gauge by increasing the value of x as given in this table, and the length of radius of turnout 2 per cent. for every additional inch in the gauge. This is a little too much; the correction for a 6 ft. gauge being about 30 per cent. Thus 100 ft. chord of turnout on this track will give 130 ft. on 6 ft. gauge, and 1000 ft. radius will give 1300 ft. This is for a straight line. When on a curve going the same way as turnout, it is sufficiently accurate for practice to add rate of curve of main track to that of the table; but when going in opposite direction, subtract it; thus making relative departure from main track the same as on a straight line.

#### EXAMPLE:

Thus a 5° frog for a 4ft.  $8\frac{1}{2}$  inch gauge gives a distance of 78.5 ft. curvature 4° 46′. If the main track were a 4° curve and going the same way, distance being the same, the rate of curvature would be 4° 46' + 4° = 8° 46', radius 653 ft.; but going the other way 4° 46' - 4° = 0° 46', radius 7473 ft.

#### TABLE

Of distances on chord from opening of switch rail where the curve commences, to point of frog, radius of curvature and rate per 100 ft., calculated to every 15 minutes of frog angle, from 3° to 15°. Constant data: opening of switch rail 5 inches = 42 ft., average angular opening say 1° 15', rails being from 18 to 20 ft. long. Variable data gauges of road.

Gauge 4ft.  $8\frac{1}{2}$  inches = 4.70 ft.

An f	gle of rog.	Distances.	Length of radius.	cur	te of ve per 00 ft.		le of	Distances.	Length of radius.	Rate of curve per 100 ft.	
3°	0	115.43	3779.3	1°	31'	9°		47 99	355.0	16°	09
	15'	109.02	3023.3	1	50		15'	46.78	335.3	17	07
	30'	103.28	2613.2	2	11		30'	45.69	317.6	18	04
	45'	98.12	2249.0	2	33		45'	44.66	301.3	19	02
1°	80	93.45	1947.2	2	$56\frac{1}{2}$	10°		43.67	286.2	20	03
	15'	89.21	1704.0	3	22		15'	42.72	272.2	21	05
	30'	85.33	1508.0	3	48		30'	41.80	259.3	22	08
	45'	81.78	1339.0	4	17	1	45'	40.95	247.2	23	13
5°	W	78:51	1199.8	4	463	11°		40.11	236.0	24	20
	15'	75.50	1081.6	5	18		15'	39.36	225.4	25	28
	30'	72.70	980.3	5	51		30'	38.55	215.8	26	37
	45'	70.01	892.9	6	25		45'	37.81	206.6	27	48
30		67.69	816.8	7	01	12°		37.10	198.0	29°	_
	15'	65.44	715.1	7	39		15	36.41	189.5	30	13
	30'	63.33	690.4	8	18		30'	35.75	182.4	31	27
	45'	61.36	639.4	8	58		45"	35.12	175.3	32	43
ď	11	59.50	593.0	9	40	13°		34.51	168.6	34	02
	15'	57.75	550.8	10	24		15'	33.91	162.2	35	23
	30'	56.01	514.6	11	09		30'	33:34	156.3	36	45
	45'	54.55	481.1	11	56		45'	32.79	150.6	38	08
0	6	53.08	415.8	12	44	14°		32.26	145.3	39	32
	15'	51.69	423.3	13	35		15'	31.74	140.2	40	58
	30'	50.36	398.3	14	$25\frac{1}{2}$	1.64	30'	31.24	135.4	42	26
	45'	49.11	375.4	15	17		45'	30.75	130.8	43	56
	11	201	P-1			$15^{\circ}$		30.28	126.5	45	26

#### TABLE

Of distances on chord from opening of switch rail to point of frog, radius of curvature and rate per 100 ft.

Gauge 4ft. 10 inches.

Angle of frog.	Distances.	Length of radius.	cur	te of ve per 00 ft.	Ang fro	le of	Distances.	Length of radius	Rate of curve pe 100 ft.	
3°	118.89	3892	1°	28'	90		49.42	365.7	15°	41
15'	112.29	3217.0	1	47		15	48 18	345 3	16	36
30'	106.37	2709	2	-07		30'	47 06	327.1	17	32
45'	101.06	2316	2	$28\frac{1}{2}$		45'	46.00	310 3	18	29
4°	96.25	2006	2	51 <del>1</del>	10°		44.98	294.7	19	28
15'	91 88	1755	3	16		15'	44.00	280.3	20	27
30'	87.88	1553	3	411/2		30'	43:06	267	21	$28\frac{1}{2}$
45'	84:23	1379	4	091		45'	42 17	254 6	22	$31\frac{1}{2}$
5°	80 86	1235	4	381	11°		41 31	243	23	36
15'	77.76	1134	5	03		15	40 48	2323	24	42
30'	74.88	1009	5	401		30'	39.70	222.2	25	49
45'	72.21	919	6	14		45'	38.94	212.7	26	58
6°	69.72	841.	6	49	12°	-	38.21	203.9	28	09
15'	67.40	772	7	$25\frac{1}{2}$		15'	37.50	195.5	29	21
30'	65.22	712.	8	03		30'	36 82	187 8	30	33
45'	63.20	658	8	$42\frac{1}{2}$	7	45'	36.17	180 5	31	46
7°	61.28	610	9	$23\frac{1}{2}$	13°		35.54	173 6	33	00
15'	59.48	568.	10	06		15'	34:92	167	34	18
30'	57.79	530	10	50		30"	34.34	160.9	35	39
45'	56.18	495.5	11	35	1, 1	45'	33.77	155.	37	00
8°	54.67	464.3	12	21	14°		33.22	149.6	38	20
15'	53.24	436	13	09	11 8	15'	32.69	144.4	39	44
30'	51.87	410.2	13	59	7	30'	32.17	139.4	41	10
45'	50.58	386 6	14	50	1	45'	31.67	134.7	42	36
AT I		1 121		- 0	15°		31.18	130.2	44	04

TABLE

Of distances on chord from opening of switch rail to point of frog,

Of di		n chord fr udius of co					of frog,
			Gauge	5 feet.			
Angle of frog.	Distances.	Length of radius.	Rate of curve per 100 ft.	Angle of	Distances.	Length of radius.	Rate of curve per 100 ft.
3°	123.51	4036	$1^{\circ}25\frac{1}{2}'$	9°	51.24	379 9	15° 05′
15'	116.65	3436	1 40	15'	50.00	358.7	15 58
30′	110.50	2810	2 02	30	48.88	339.8	16 52
45'	104.98	2403	2 23	45'	47.78	322.3	17 48
4°	100.00	2080	2 45	10°-	46.72	306.2	18 44
15'	95.45	1820	$3 08\frac{2}{8}$	15'	45 71	291.2	19 42
30'	91 30	1611.	3 33	30'	44.73	277.4	20 40
45'	87.50	1430	4 00	45'	43.81	264.5	21 40
5°	84.	1281	4 28	11°	42.91	252.5	22 42
15'	80.78	1156.	4 57	15'	42.00	241.2	23 46
30'	77.78	1047	5 27	30'	41.24	230.9	24 52
45'	75.00	965.	5 58	45'	40.45	221.0	26 01
6°	72.32	873	6 331	12°	39.69	211.8	27 10
15'	70.00	802	7 09	15'	38.95	202.7	28 20
30'	67.76	739	7 45	30'	38.25	195.1	29 30
45'	65.65	684	8 23	45'	37.57	187.5	30 40
7°	63.66	634	9 02	13°	36.92	180-2	31 50
15'	61.78	590.	9 43	15'	36.28	173.5	33 02
30'	60.00	550	10 25	30'	35 67	167.2	34 17
45	58.36	514.	11 09	45'	35.08	1611	35 35
8°	56.79	482	11 54	14°	34 51	155.4	36 55
15'	55.30	452	12 40	15	33.96	150.0	38 16
30'	53.88	426	13   27	30'	33.42	144.8	39 38
45'	52.54	401.	14 17	45'	32.90	139 9	41 00
				1			

32.39 | 135.3

Of distances on chord from opening of switch rail to point of frog, radius of curvature and rate per 100 feet.

Gauge 5 feet 6 inches.

Angle of frog.	Distances.	Length of radius.	Rate of curve per 100 ft.	Angle of frog.	Distances.	Length of radius.	Rate of curve per 100 ft.
3°	136.78	4478	1° 17′	9°	56.87	420.7	13° 39′
15'	129.19	3750	1 32	15'	55.40	397.4	14 27
30'	122.38	3116.	1 50	30'	54.14	376.4	15 14
45'	116.27	2664	2 09	45'	52.92	357.0	16 04
4°.	110.75	2307	2 29	10°	51 74	339.1	16 55
15'	105.71	2019	2 50	15'	50.62	322.5	17 47
30′	101.11	1786	3 12	30'	49.54	307.2	18 40
45'	96 90	1586	3 37	45'	48:52	292.9	19 35
5°	93.03	1421.0	4 02	11°	47.52	280.0	20 30
15'	89.46	1281	4 28	15'	46.52	267.2	21 28
30'	86.14	1161	4 56	30'	45.68	255.7	22 26
45'	83.15	1062	5 24	45'	44.80	244 8	23 26
6°	80.16	967	5 56	12°	43.96	234.2	24 30
15′	77.53	888.8	6 27	15'	43.14	224.7	25 33
30'	75.04	819.	7 00	30'	42.36	215.9	26   36
45'	72.71	757.6	7 34	45'	41.61	207.7	27 40
7°	70.50	702.8	8 10	13°	40.89	199.7	28 46
15'	68 43	653.8	8 46	15'	40.18	192.2	29 54
30'	66 47	609 8	9 24	30'	39.50	185.2	31 02
45'	64 64	5700	10 04	45'	38.85	178.4	32 11
8°	62 89	534	10 45	14°	38.22	172:1	33 21
15'	61.25	501.6	11 27	15'	37.61	166.1	34 33
30'	59 67	471.9	12 10	30'	37.01	160.4	35 47
45'	58.19	444.8	$12 \ 54\frac{1}{2}$	45'	36.44	154.9	37 03
N M		10-51		15°	31.87	150.0	38 18

TABLE
Of distances on chord from opening of switch rail to point of frog,
radius of curvature and rate per 100 ft.

-			1211	Gauge	6 feet.	7.2	nid mo		01000
Angle of frog.	Distances.	Length of radius.	R cur 10	ate of ve per 0 ft.	Angle of frog.	Distances.	Length of radius.	curv	e of ve per ) ft.
3°	150.06	4913.1	1	10'	9°	62.40	461 6	12	26'
15'	141.73	4060.3	1	$24\frac{2}{3}$	15'	60.81	435 9	13	10
30′	134.26	3419.3	1	$40\frac{1}{2}$	30'	59 40	412.9	13	55
45'	127.56	2923.7	1	57½	45'	58.06	391.7	14	40
4°	121.50	2531.4	2	16	10°	56.77	372-1	15	25
15'	115.97	2215.2	2	35	15'	55.54	353 9	16	12.
30'	110.93	19604	2	$55\frac{1}{2}$	30'	54.35	337 1	17	00
45'	106.31	1740.7	3	$17\frac{1}{2}$	45'	53.24	321.4	17	50
5°	102.06	1560.0	3	$40\frac{1}{2}$	11°	52.14	306.8	18	42
15'	98.15	1406.1	4	$04\frac{1}{2}$	15'	51.04	293.2	19	34
30'	94.51	1274.4	4	30	30'	50.12	280.5	20	27
45'	91.14	1160.8	4	56	45'	49.15	268.6	21	22
6°	88.00	1061.8	5	24	12°	48.23	257.4	22	18
15'	85.07	975.0	5	53	15'	47:33	246:0	23	15.
30'	82.33	898.8	6	23	30'	46.47	237:1	24	12
45'	79.77	831.2	6	54	45'	45.66	227.9	25	12
7°	77.35	771.0	7	26	13°	44.86	219.2	26	12
15'	75.08	717.3	8	00	15'	44.08	210.9	27	14
30'	72.94	669.0	8	34	30'	43.34	203.2	28	17
45	70.92	625.4	9	10	45'	42.63	195.8	29	20
8°	69.00	586.0	9	$47\frac{1}{2}$	14°	41.94	188.9	30	23
15'	67.20	550.3	10	$25\frac{1}{2}$	15'	41.26	182.3	31	28
30'	65.47	517.8	11	05	30'	40 61	176.0	32	36
45'	63.84	488.0	11	46	45'	39.98	170.0	93	45
1 17					15° ·	39.36	164.5	33	54

### MISCELLANEOUS NOTES AND EXAMPLES.

Suppose a curve contain 57° 24' curvature, distance between centres of inner and outer track 5ft. Required difference between main and outside track. By table of circular arcs:

57° gives 0.9948377
24° " 0.0069814
1-0018191
Multiply 5
5-0090955

Ans. 5 ft.

To find the length of any circular arc, multiply tabular arc of given number of degrees by the radius. Half of this tabular length gives the tabular area of a section of some number of degrees, and this tabular area multiplied by the square of radius, gives the required area of sector; or this tabular area, multiplied by the required area of the squares of the two radii, gives the area of a ring. Thus if inner radius = 3 ft., outer = 4, thickness being 1, we have  $4^2-3^2=7$ , which multiplied by tabular area gives area required. Suppose the radius of the intrados of an arch containing  $134^\circ$  46' is 6'3 ft., the thickness of voussoirs = 1.5.

Then  $8^2 - 6.5^2 = 21.75$ .  $134^\circ \text{ gives } 2.3387412$  46' 0.0133809  $134^\circ 46'$   $2.3521221 \times 21.75 = 51.16$  nearly,

and  $\frac{51.16}{2} = 25.08 =$ area.

When the span and rise are given to find the curvature of arc, make  $\frac{\text{rise}}{\text{half span}} = \text{nat. tang. } \frac{1}{4}$  curvature.

Example.—Suppose span = 18 ft., rise = 6 ft., then  $\frac{6}{9}$  = 0.666667 = nat. tang. 33° 41½′, and 33° 41½′ × 4 = 134° 46′ of curvature. Let it be required to find radius, we would then have,

 $\frac{(\frac{1}{2} \operatorname{span})^2 + (\operatorname{rise})^2}{2 \times \operatorname{rise}} = \operatorname{radius}. \text{ Thus } \frac{9^2 + 6^2}{2 \times 6} = 9.75 = \operatorname{radius} \text{ of arc.}$ 

Had it been a 12 ft. span and 4 ft. rise, radius would have been 6.5 feet.

Analogous to this last example, and derived from the same proposition of geometry, is an easy method of determining the distance across a river or ravine.

Let the instrument be at B with a foresight upon C across river; from B lay off a right angle to D. Set the instrument over D and

lay off from DC a right angle DA meeting CB produced in A. Then by similar triangles,

AB: BD:: BD: BC; or  $\frac{BD^2}{AB}$  = BC. Suppose that BD = 50 ft. and AB = 3 ft., then  $\frac{2500}{3}$  = 833·3 ft.

To Triangulate round an Obstruction on a Curve.

Example.—Suppose in running a 3° curve, I find the point for sta. 2645 to be occupied by a house; I find, however, that 2644 + 75 and 2645 + 25 are clear of the house; also, that I have sufficient room for an equilateral triangle whose sides are 50 ft. each. tablish 2644 + 75 and set the instrument over it. Now suppose the last reliable point on curve to be at sta. 2640. The instrumental deflection from 2640 to 2645 + 25 = 525 ft. is  $7^{\circ}$  52\frac{1}{2}'. Set the vernier to this reading, and clamp the instrument with a backsight on 2640, so that, when the vernier is at 0, the telescope may point towards 2645 + 25. Unclamp vernier, set the reading at 60°, and measure 50 ft. in line of telescope. Set instrument over this point, and turn the interior angle =  $60^{\circ}$ , measuring 50 ft. as before. the transit over this last point, sta. 2645 + 25, with the vernier at 60° so that the zero line shall coincide with the chord from 2644 + 75 to 2045 + 25. Clamp the instrument with a sight on the second point or vertex of triangle. Then set the vernier at 1° 52½, the instrumental deflection for 125 ft., and the telescope will point in direction of sta. 2646, from whence continue the curve, if required, as before.

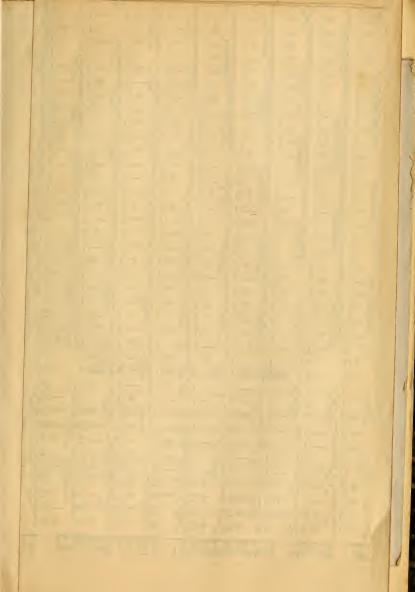
This was an expedient applied to advantage by a former associate in making the final location of the Ohio and Mississippi R. R.,

Ripley County, Indiana.

Similar examples and corollaries to previous propositions might be added indefinitely, but this would transcend the proper limits of the work. To an adept practitioner possessing ordinary faculties of generalization, it is believed the rules and formulas already given will be suggestive of the means of solving most of the other problems which may occur in practice.

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# TABLE FOR CURVING RAILROAD IRON.

BY CHARLES HASLETT, CIVIL ENGINEER.

GIVEN to the nearest sixteenth of an inch, the spring of a 10 feet rail being one inches, and 1½ inches. The spring will be tested at each point by a suitable straight edge fourth that of a 20 feet rail; the spring of a 9 feet rail being one fourth that of an 18 feet rail. When the rail is properly curved, the spring at one fourth the length from little less. the end of the rail, will be three-fourths that at the middle. At 5, 10, and 15 feet of a 20 feet rail, the spring for a 19 degree curve (301 feet radius) would be 1½ inches, 2 quired spring, in inches and parts of an inch.

Where the sign + occurs, curve a little more; and where the sign - occurs, curve a

Opposite the rate of curvature and under the length of rail, will be found the re-

tion per 100 ft.	t.							3700==	0.		T37									s n	De-
100 ft.	Radius feet.					10		NGTH			IN F			07 1	20 1	0 = 1				Radius feet.	flect'n per 100 ft.
	-	10 11 1	$\begin{bmatrix} 2 & 13 \\ - & \end{bmatrix}$	14	15	16   17	18	$\left  \begin{array}{c} 19 \\ - \end{array} \right $	20	21	22	23 	24	25	$-\frac{26}{}$	27			30		100 lt.
1°00′	5730	$\begin{bmatrix} \frac{1}{3} \frac{1}{2} - \frac{1}{3} \frac{1}{2} \\ \frac{1}{3} \frac{1}{2} \end{bmatrix}$	+ 32+	1 16	$\begin{array}{c c} 1 \\ \hline 16 \\ 1 \end{array}$	$\frac{1}{\frac{1}{6}} + \frac{1}{\frac{1}{6}} \cdot \frac{1}{\frac{1}{6}}$	$+ \frac{1}{16} +$	1 -	<u> </u>	18 -	1 8 3	1/8, +	$\frac{\frac{1}{8}}{\frac{3}{16}}$	$\frac{3}{16} + \frac{3}{16} + \frac{3}{16}$	$\frac{3}{16}$	$\begin{bmatrix} \frac{3}{16} \end{bmatrix}$	$\frac{3}{\frac{1}{1}6} + $	$\frac{3}{16} + \frac{1}{4} + \frac{1}{16} +$	1	5730	1000
15 30	4584 3820	$\begin{vmatrix} \frac{3}{2} & \frac{3}{2} \\ \frac{1}{3} & \frac{1}{2} \\ \frac{1}{3} & \frac{1}{2} + \frac{1}{16} \\ \frac{1}{3} & \frac{1}{2} + \frac{1}{16} \\ \frac{1}{3} & \frac{1}{2} + \frac{1}{16} \\ \end{vmatrix}$	- 16- - 16+	16 16 16 16 16		$\frac{1}{6} + \frac{1}{16}$	+		8 3	$\frac{1}{8}$ + $\frac{1}{3}$ $\frac{3}{6}$ +	$\begin{bmatrix} \frac{1}{6} \\ \frac{3}{16} \end{bmatrix}$	$\frac{\frac{1}{8}}{\frac{3}{16}}$	$\frac{16}{16}$	16	1 +	15 16	$\begin{bmatrix} \frac{\widehat{4}}{5} \\ \frac{1}{6} \end{bmatrix}$	· <del>*</del> 十	3 -	$\frac{4584}{3820}$	15
45	3274	$\frac{32}{32} + \frac{10}{16} - \frac{10}{16}$	$\begin{bmatrix} \frac{16}{16} + \end{bmatrix}$	$\frac{1}{16} +$	$\left  \frac{1}{8} \right  = \left  \frac{1}{8} \right $		$\frac{1}{8}$ +	$\frac{8}{1.6}$	$\frac{\overline{16}}{\overline{36}}$	$\frac{\frac{1}{3}^{6}}{\frac{1}{6}}$	10-	$\frac{1}{4}^{6}$	1 +	$\frac{\overline{5}}{16}$	$\frac{3}{1}\frac{5}{6}$	$\frac{\frac{5}{16}}{\frac{3}{8}}$	3/8,	$\frac{3}{8}$ +	$\frac{{}^{5}7}{\frac{1}{1}6}$	3274	45
2°00 15	2865 2546	$\begin{vmatrix} \frac{1}{16} - \frac{1}{16} \\ \frac{1}{16} - \frac{1}{16} + \frac{1}{16} \\ \frac{1}{16} - \frac{1}{16} + \frac{1}{16} \\ \frac{1}{16} + \frac{1}{16} + \frac{1}{8} \\ \frac{1}{16} + \frac{1}{16} + \frac{1}{8} \end{vmatrix}$	+   1	18 -		+ <del> </del> <del> </del> 8	$+ \frac{3}{16} -$	$\begin{bmatrix} \frac{3}{16} \\ \frac{3}{16} \\ \frac{3}{16} \end{bmatrix} + \begin{bmatrix} \frac{3}{16} \\ \frac{3}{16} \end{bmatrix}$	16	1 +	$\frac{1}{4}$	<u>-</u> +	1 6 5 +	3 -	3 +	$\frac{\frac{3}{8}}{\frac{7}{16}}$	$\frac{\frac{1}{16}}{\frac{7}{16}} +$	16	· · ·   · · · · · · · · · · · · · · ·	$\begin{array}{c} 2865 \\ 2546 \end{array}$	2°00 15
30	2292	$\begin{vmatrix} 1 & 6 \\ 1 & 6 \end{vmatrix} = \begin{vmatrix} 1 & 6 \\ 1 & 6 \end{vmatrix} + \begin{vmatrix} 1 & 6 \\ 1 & 8 \end{vmatrix}$ .		80 8		$ \frac{\frac{1}{3}}{\frac{3}{6}} + \frac{\frac{3}{16}}{\frac{3}{16}} = \frac{\frac{3}{16}}{\frac{3}{16}} $	$\begin{bmatrix} \frac{1}{16} \\ \frac{3}{16} \\ \frac{3}{16} \end{bmatrix} +$	$\begin{vmatrix} \frac{1}{6} \\ \frac{1}{4} \end{vmatrix}$	1/4_+	$\frac{\frac{4}{5}}{\frac{16}{16}}$	$\begin{bmatrix} \overline{16} \\ \overline{5} \\ \overline{16} \end{bmatrix}$	$ \begin{array}{c c}  & 5 \\ \hline  & 3 \\ \hline  & 8 \\ \hline  & 3 \\ \hline  & 7 \\  & 7 \\ \hline  & 7 \\ \hline  & 7 \\  & 7 \\ \hline  & 7 \\  & 7 \\ \hline  & 7 \\  & $	$\frac{16}{16} + \frac{5}{16} + \frac{3}{16} + \frac{7}{16}	$\frac{87}{126}$	$\frac{8}{16}$	$\frac{\frac{1}{1}}{2}^{6}$	$\frac{1}{2}$ $\frac{1}{9}$ $\frac{9}{16}$	$\frac{2}{16}$	$\frac{2}{16} +$	2292	30
45 3°00	2083 1910		-분 -분+	<del>                                    </del>	$\frac{3}{136}$	9 <del></del>	+	4 +	$\frac{5}{1_{5}^{6}}$	$\frac{5}{16}$	3 -	3 8	16 <del>1</del> +	16	\frac{1}{2} - \rightarrow \frac{1}{2} + \rightarrow \frac{1}{2}	<u>+</u> +	$\frac{9}{16}$	58 <del>-</del> +	$\begin{vmatrix} \frac{5}{8} + \\ \frac{11}{16} + \end{vmatrix}$	$\frac{2083}{1910}$	3°00
15	1763	$\begin{vmatrix} \frac{1}{16} + \frac{1}{8} & -\frac{1}{8} \\ \frac{1}{16} + \frac{1}{8} & -\frac{1}{8} \end{vmatrix}$		$\frac{3}{16}$	:3	3 + 4 -	- 4 +	1.6 5 1.6	$\frac{\frac{16}{16}}{\frac{5}{16}} +$	838	38 +	$\frac{16}{76} +$	$\frac{\overline{1}^{6}}{2}$	$\frac{1}{2}$ +	$\frac{29}{16} +$	$\frac{\frac{5}{8}}{6}$	$\frac{8}{11}$	116+	3 +	1763	15
30	1637	16+ 5 - 5	. 10 1	$\frac{1}{1}\frac{3}{6}$	$\frac{3}{16} + \frac{1}{1}$	$- \frac{1}{4}$	$+ \frac{5}{156} -$	1 3 +1	<del>š</del>	$\frac{3}{8}$ +	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{\frac{1}{2}}{\frac{1}{16}}$	$\frac{9}{\frac{1}{5}6}$	$\frac{5}{8}$	11 +	$\frac{11}{16}$ $\frac{1}{16}$ $\frac{3}{4}$ +	$\frac{3}{4} + \frac{1}{13} + \frac{1}{13}$	$\frac{13}{16} + \frac{7}{2}$	$\frac{1637}{1528}$	30 45
45 4°00	$\begin{array}{c c} 1528 \\ 1432 \end{array}$		$+ \begin{vmatrix} \frac{3}{16} - \end{vmatrix} + \begin{vmatrix} \frac{3}{16} - \end{vmatrix}$	$     \begin{array}{c}             \hline             16 \\             \hline             3 \\           $	1 1	$+\frac{16}{16}$	$\begin{array}{c c} + & \frac{5}{16} - \\ - & \frac{5}{16} + \\ - & \frac{5}{16} + \end{array}$	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\frac{\frac{3}{8}}{\frac{7}{1.6}}$	$\frac{16}{76}$	$\frac{\overline{2}}{\frac{1}{2}}$	$\frac{\frac{1}{2}}{\frac{9}{16}} +$	$\frac{5}{8}$ —	5 +	$\frac{\frac{1}{1}\frac{6}{6}}{\frac{1}{6}}+$	116+	$\frac{\frac{1}{1}3}{\frac{1}{6}6}+$	$\frac{13}{16} + \frac{1}{8}$	$\begin{bmatrix} 8 & 1 \\ 15 & 16 \end{bmatrix}$	1432	4°00
15	1348	$\begin{vmatrix} 1 & - & 1 & 1 & 3 \\ 1 & 1 & 1 & 3 & 3 \end{vmatrix}$	$+\left  \frac{\frac{3}{16}}{\frac{3}{16}} - \right $	$\frac{3}{16} + \frac{3}{16}$	1 1	$\frac{5}{56}$ $\frac{7}{156}$	$\frac{1}{8}$ —	§ +	76	$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{3} \end{bmatrix} + \begin{bmatrix} \frac{1}{2} \\ \frac{1}{3} \end{bmatrix}$	1 6 -	$\frac{^{29}}{^{16}}$ +	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	$\frac{11}{16}$	$\frac{3}{4}$ $13$	$\frac{13}{16}$	$\begin{bmatrix} \frac{7}{8} \\ 15 \end{bmatrix}$	$\frac{15}{16}$	1 1.1	$\frac{1348}{1273}$	$\begin{array}{ c c c }\hline & 15\\ 30 \\ \end{array}$
$\begin{bmatrix} 30 \\ 45 \end{bmatrix}$	$1273 \\ 1206$	S   T   16   16   16   16   16   16   16	$-\frac{3}{16}+$	4 -	$\frac{\frac{1}{4}}{\frac{5}{156}} + \frac{7}{1}$	$\frac{6}{\frac{5}{6}}$ $\frac{1}{\frac{3}{8}}$ $\frac{5}{3}$ $+$ $\frac{3}{3}$	$\frac{1}{8}$	$\left \begin{array}{c} \overline{16} \\ \overline{16} \end{array}\right $	÷	3)	$\frac{\overline{1} \ \overline{6}}{\underline{5}}$	1 1	11 + 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 =	¥ +	$\frac{1}{1}\frac{6}{3} +$	87 十	$1^{\overline{1}\overline{6}}$	$1_{\frac{1}{16}}$	$1\frac{1}{8}$	1206	45
5°00	1146	$\begin{vmatrix} \frac{7}{8} & \frac{1}{36} \\ -\frac{1}{36} \end{vmatrix} = \begin{vmatrix} \frac{3}{36} \\ \frac{1}{36} \end{vmatrix}$	1 4 -	1 1	$\frac{1}{1}\frac{5}{6}$	$\frac{5''}{6} + \frac{3}{8}$	16 7 16 1 7 +	$\left  \frac{1}{2} - \right $	129	$\frac{\frac{1}{9}^{6}}{\frac{1}{6}}+$	5 8	$\frac{\frac{5}{8}}{\frac{11}{16}}$	34	$\frac{1}{1}\frac{3}{6}$	8	$\frac{15}{16}$	1 +		$1\frac{3}{16}$	$\frac{1146}{1092}$	5°00 15
15 30	$\begin{array}{c} 1092 \\ 1041 \end{array}$	$\begin{vmatrix} \frac{1}{3} + \frac{1}{16} - \frac{3}{16} \\ \frac{1}{3} + \frac{3}{16} - \frac{3}{3} - \frac{3}{3} - \frac{3}{3} \end{vmatrix}$		$\frac{1}{4}$ +	$\begin{array}{c c} \overline{16} & \overline{136} \\ 5 \overline{16} & \overline{38} \\ 5 \overline{16} & \overline{38} \\ 5 & \overline{38} \end{array}$	- 7	$\frac{1}{16} + \frac{7}{16} $	$\frac{\frac{1}{2}}{\frac{1}{2}}$ +	$\frac{\frac{9}{16}}{\frac{9}{16}}$	* -   \$ +	16 16 16 +	을 <u>+</u>	$\frac{\hat{1}\frac{3}{16}}{\frac{1}{16}}$	\frac{1}{8} + \frac{1}{8}	$\begin{bmatrix} \frac{1}{1} \frac{5}{6} \\ 1 \end{bmatrix}$	1 -	$1\frac{1}{16}$ + $1\frac{1}{8}$	$1\frac{3}{16} +$	$1\frac{1}{4}$ $1\frac{5}{16}$ —	1041	30
45	996	$\begin{vmatrix} \frac{1}{8} & + \begin{vmatrix} \frac{3}{16} - & \frac{3}{16} \\ \frac{1}{8} & + \begin{vmatrix} \frac{3}{16} - & \frac{3}{16} \end{vmatrix} \end{vmatrix}$	-   <del>1</del>	$\frac{\overline{1}_{5}\overline{6}}{\overline{1}_{5}\overline{6}}$	$\frac{\frac{1}{5}}{\frac{1}{6}}$ $\frac{\frac{3}{8}}{\frac{1}{8}}$	$+ \frac{1}{1} \frac{7}{6}$	$\frac{1}{2}^{6}$	49	8	$\frac{1}{1}\frac{1}{6}$	₹ <del></del>	13	$\frac{7}{8}$	$\begin{bmatrix} \frac{1}{1}\frac{5}{6} \end{bmatrix}$	1 + 1	$\frac{1}{8}$	$1\frac{3}{16}$	$1\frac{1}{4}$ +	$1\frac{3}{8}$	$\frac{996}{955}$	6°00
6°00 15	$\frac{955}{918}$	$\begin{vmatrix} \frac{3}{16} - \\ \frac{3}{16} - \\ \frac{3}{16} + \end{vmatrix} = \begin{vmatrix} \frac{1}{4} - \\ \frac{3}{4} - \\ \frac{3}{16} - \end{vmatrix}$	-  <del> </del> +	$\frac{5}{1.6} + \frac{5}{1.6} + \frac{5}$	383 - 8	$+ \begin{vmatrix} \frac{170}{6} - \\ \frac{1}{6} - \end{vmatrix}$	H		多 十	16	$\frac{3}{4} + \frac{1}{13}$	$\frac{\frac{1}{3}}{\frac{1}{6}} +$	$\frac{15}{16}$	1 + ]	$\begin{bmatrix} \frac{1}{1} & 6 \\ \frac{1}{8} & \end{bmatrix}$	3 3	$1\frac{1}{4}$	1元十 13	116 -	$\frac{903}{918}$	15
30	881	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$-\frac{\frac{4}{5}}{\frac{1}{5}6}$	$\frac{1.6}{1.6}$	$\frac{8}{3}$ + $\frac{1}{1}$	$\begin{bmatrix} \frac{6}{76} \\ \frac{7}{6} \end{bmatrix} = \begin{bmatrix} \frac{2}{12} \\ \frac{1}{2} \end{bmatrix} = \begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$	<sup>2</sup> 9		$\frac{\frac{8}{1}}{\frac{1}{6}}\frac{1}{6}$	3 4	$\frac{\frac{13}{16}}{\frac{13}{16}}$	5 15 16	1"	$\begin{bmatrix} \frac{1}{16} \end{bmatrix}$	$ \frac{1}{8}  +  1 $	10-	$1\frac{\frac{1}{5}}{\frac{1}{6}} +$	$1\frac{^{\circ}7}{^{1}6}$	$1\frac{1}{2} + \frac{1}{2}$	881	30
7°00	818 818	$\begin{vmatrix} \frac{3}{16} - & \frac{3}{16} + \frac{1}{4} \\ \frac{3}{16} & \frac{1}{4} - \frac{1}{4} \end{vmatrix}$	$+\left \frac{\frac{5}{1}6}{\frac{5}{1}6}\right $	3 (23)	/ 1	· 7	1 1 6 + 9 + 1 9 + 1 9 + 1 1 6 + 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	\$ + 11	116+	章 十 13 13 13	\$ - \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	16	] +  -  -  -  -  -  -  -  -  -  -  -  -  -	<del>                                    </del>	$\frac{1}{1} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\frac{3^26}{3^26} + 1$	$1\frac{3}{16}$	1 2	156+	848 818	7°00
15	792	$\begin{bmatrix} \overline{16} \\ \overline{3} \\ \overline{16} \end{bmatrix} \begin{bmatrix} \frac{1}{4} \\ \overline{4} \end{bmatrix} = \begin{bmatrix} \frac{4}{1} \\ \overline{4} \end{bmatrix}$	$+ \begin{vmatrix} \frac{1}{5} & 6 \\ \frac{5}{1} & 6 \end{vmatrix}$	$\frac{8}{3}$	$\begin{array}{c c} \overline{1} \overline{6} & \overline{1} \\ \overline{7} \overline{1} \overline{6} & \overline{1} \\ \end{array}$	$\frac{1}{1} - \frac{1}{2} \frac{1}{3} - \frac{1}{1} \frac{1}{6} - \frac{1}{1}$	$-\frac{1}{8}\frac{1}{8}$	$ \begin{array}{c c} 11 \\ 16 \\ 11 \\ 16 \end{array} $	* +	$\frac{13}{16}$ +	$\frac{1}{1}\frac{5}{6}$	i	$1\frac{1}{16} + 1$	$1\frac{3}{16}$ - 1	$\frac{2}{1}\frac{5}{1}$ 1	$\frac{1}{8}$ +	$\left  \frac{1}{2} \right ^{0}$	$1\frac{19^{6}}{16}$		792 $764$	15
30	$\begin{array}{c} 764 \\ 739 \end{array}$	$\frac{3}{16} + \frac{1}{16} - \frac{5}{16} $	$-\begin{vmatrix} \frac{5}{1} & + \\ \frac{5}{5} & + \end{vmatrix}$	388 +	$\frac{7}{16} + \frac{1}{2}$	$\frac{1}{16}$	5 + 5 +	116	$\frac{1}{1}\frac{3}{6}$	· 등 -	16十二	$1\frac{1}{16}$	$\begin{bmatrix} 1\frac{1}{8} \\ 1\frac{3}{2} \end{bmatrix}$	축  1  추 +  ]	$\frac{3}{16} + 1$	ディー   ま 十月	$\begin{bmatrix} \frac{1}{1} \frac{9}{6} \\ \frac{9}{1} \end{bmatrix} + \begin{bmatrix} \frac{9}{1} \\ \frac{9}{1} $	1章 十 144 十	14 + 1 143 +	70± 739	$\begin{array}{c c} & 30 \\ & 45 \end{array}$
8°00	716	$\frac{16}{3} + \frac{1}{4}$ $\frac{16}{16}$	$-\frac{1}{3}\frac{6}{8}$	8 16	$\left. rac{\overline{1}}{\overline{2}} \stackrel{6}{-} \right  \left. rac{\overline{2}}{\overline{1}} \right $	$\frac{1}{6}$ $\frac{1}{8}$ $\frac{1}{8}$ $\frac{1}{8}$	$-\begin{bmatrix} \frac{8}{11} \\ \frac{1}{16} \end{bmatrix}$	3	$\frac{1}{1}\frac{6}{6}$ +	$\frac{1}{1}\frac{5}{6}$	+	$1\frac{1}{8}^{6}$	$1\frac{1}{1}\frac{3}{1}\frac{6}{6}+$	$\begin{bmatrix} \frac{4}{5} \\ \frac{1}{6} \end{bmatrix}$	$\frac{8}{1.6}$ - $1$	$\frac{2}{2}$ +	1 1 5 +	1章 十	$1\frac{7}{8}$ +	716	8°00
15	694	$\frac{13^{\circ}}{16} + \left  \frac{1}{1} + \right  \frac{15^{\circ}}{16^{\circ}}$	3 -	$\frac{77}{1}\frac{7}{6}$	$\frac{1}{2}$ $-$	$\frac{9}{6} - \frac{5}{8} = \frac{5}{8}$	$\begin{bmatrix} \frac{11}{16} + \frac{1}{3} \end{bmatrix}$	学 十   13	$\begin{bmatrix} \frac{7}{8} & - \\ \frac{7}{4} & + \end{bmatrix}$	$\frac{15}{16} +  $	$\begin{bmatrix} \frac{1}{16} & - \\ \frac{1}{16} & + \end{bmatrix}$	$1\frac{1}{8} + \frac{1}{1}$		$\begin{bmatrix} \frac{3}{8} & \end{bmatrix} 1$	$\frac{1}{1}$ $\frac{1}{6}$ $\frac{1}{1}$	$\frac{9}{16}$	l 뉴 등 l 후	1수중 1구	$\begin{bmatrix} 1\frac{13}{16} \\ 2 \end{bmatrix}$	$\begin{array}{c} 694 \\ 674 \end{array}$	$\begin{vmatrix} 15\\ 30 \end{vmatrix}$
10 45	$\begin{array}{c} 674 \\ 654 \end{array}$	\$ - \frac{1}{5} + \frac{1}{5} = \frac{1}{5}	+ 3 +	$\frac{16}{7}$	豆 十 ~	$\frac{1}{9}\frac{1}{6} + \frac{1}{1}\frac{1}{6}$	\ \frac{1}{2} \frac{1}{2} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	$\frac{16}{16} +$	$\frac{1}{1}\frac{5}{6}$	1	$\left[\frac{\frac{1}{8}}{\frac{1}{8}}\right]^{6}$	$1\frac{16}{16} +$	$1\frac{4}{1\frac{5}{16}}$	$\left[\frac{8}{1}, \frac{7}{6}, \dots\right]$	$\frac{2}{1.6}$ - 1	$\frac{8}{1}\frac{1}{6}$	$\begin{bmatrix} \frac{1}{1} & 3 \\ \frac{1}{1} & 6 \end{bmatrix}$	$1\frac{15}{16}$	$2\frac{1}{16}$	654	45
9°00	636	$\frac{1}{4} + \left  \frac{15}{156} - \left  \frac{150}{156} \right  \right $	$\left  - \left  \frac{3}{8} \right  + \right $	$\frac{7}{16} + $	$\frac{1}{2}$ + $\frac{3}{8}$	- 11 16	- 皇十	$\left \begin{array}{c} \frac{\hat{7}}{8} \\ \frac{\hat{7}}{8} \end{array}\right $	$\begin{bmatrix} \frac{1}{1}\frac{5}{6} \\ \frac{1}{1}\frac{5}{6} \end{bmatrix}$	1 +	[블 +년 대3년	1 -	$\begin{bmatrix} \frac{3}{8} \\ 1 \end{bmatrix}$	[를[] [보 +-]]	$\frac{9}{16} + 1$	$\frac{11}{16} + \frac{1}{3}$		2 — 9——	$2\frac{1}{8}$ - $2\frac{3}{8}$ - $2\frac{3}{8}$ - $2\frac{3}{8}$	$\frac{636}{619}$	9°00
$\frac{15}{30}$	$\begin{array}{c c} 619 \\ 603 \end{array}$	$\frac{1}{4}$ - $\frac{1}{16}$ - $\frac{3}{8}$ - $\frac{1}{4}$ - $\frac{3}{8}$ - $\frac{3}{8}$ -	16	½ —	$\begin{bmatrix} \frac{3}{16} \\ \frac{9}{16} \end{bmatrix}$	+ 11 -		\$ +	1 5 7	1万百 1克 ————————————————————————————————————	$\left[\frac{16}{16} + \right]$	$1\frac{1}{4}$ $1\frac{5}{16}$	$\begin{bmatrix} \frac{1}{8} & \frac{1}{6} \\ \frac{7}{16} & \frac{1}{6} \end{bmatrix}$	$\begin{bmatrix} \frac{2}{9} & 1 \\ \frac{1}{16} & 6 \end{bmatrix}$	$\frac{8}{116}$ 1	$\frac{1}{1}\frac{3}{6}$	$1\frac{1}{1}\frac{5}{6}$	$2\frac{16}{16} +$	$2\frac{1}{4}^{6}$	603	30
45	587	$\begin{bmatrix} \frac{1}{5} \\ \frac{1}{1} \end{bmatrix} \begin{bmatrix} \frac{1}{5} \\ \frac{3}{5} \end{bmatrix} = \begin{bmatrix} \frac{3}{5} \\ \frac{3}{5} \end{bmatrix} = \begin{bmatrix} \frac{3}$	$-\left \frac{\frac{1}{7}^{6}}{\frac{1}{6}}-\right $	$\frac{1}{2}$	$\frac{19^{\circ}}{16} + \frac{3}{5}$	+ 3"-	$-\frac{1}{2}\frac{3}{6}$ +	$\begin{bmatrix} \frac{1}{1} \frac{5}{6} \end{bmatrix}$		$\begin{bmatrix} \frac{1}{8} \\ \frac{1}{8} \end{bmatrix}$		$1\frac{3}{8}$	$[\frac{1}{2}]$	$\lfloor \frac{9}{16} + 1 \rfloor$	축 <del>-</del> 11	787	2	24 十	$2\frac{5}{16}$	587 573	45 10°00
10°00 15	573 559	$\frac{1}{4} + \begin{vmatrix} 3 \\ 16 \end{vmatrix} = \begin{vmatrix} 3 \\ 8 \end{vmatrix}$	1 <sup>7</sup> 6 +	1 + 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 =	16 + 1 5 - 1	3 1 1 3 -	H + —	16 1	$\frac{1}{16} \frac{1}{6} + \frac{1}{12} + \frac{1}{12} \frac{1}{6} + $	$1\frac{2}{8}$ $1\frac{3}{4}$	$\lfloor \frac{5}{16} -                                   $	1 = +	$1\frac{9}{16}$	$\begin{bmatrix} \frac{1}{8} & -1 \\ \frac{1}{16} & -1 \end{bmatrix}$	$\frac{1}{\frac{13}{6}}$	$\frac{8}{15} + \frac{1}{16}$	$2\frac{1}{8}$	$\frac{216}{24}$	$2\frac{7}{16}$	559	15
30	545	$\frac{1}{4} + \frac{1}{5} + \frac{8}{8} +$	$-\frac{16}{16}+$	$\frac{\frac{2}{9}}{\frac{1}{6}}$	8 - 1	$\left  \frac{1}{6} + \right  \frac{1}{16} = $	\ \frac{1}{5} +	1 6	$1\frac{1}{8}^{6}$	$1\frac{\frac{1}{3}}{\frac{1}{1}} + 1$	$\lfloor \frac{\frac{1}{3}}{\frac{3}{6}} + \rfloor$	$1\frac{\frac{1}{7}^{6}}{\frac{1}{6}}+$	$1^{\frac{1}{9}^{0}}_{\frac{1}{6}}+1$	$\left[\frac{\frac{1}{1}}{\frac{1}{6}} + \right]$	$\frac{7}{8}$ — 2	1	2美十	$\frac{2.5}{1.6}$	21 —	$\begin{array}{c} 545 \\ 533 \end{array}$	30 45
45	533	$\frac{1}{4} + \left  \frac{5}{16} + \left  \frac{3}{8} \right  \right $		$\frac{9}{196}$	5 + State	$\begin{array}{c c} - & \frac{13}{16} \\ \hline & \frac{13}{13} \end{array}$	$\begin{bmatrix} \frac{15}{16} - \\ \frac{13}{13} \end{bmatrix}$	1 +		l축 ㅡ  1분 +	1章 十	l층 —	1층 년 1층 부분	$1\frac{1}{1}\frac{3}{1}$	$\frac{15}{16}$ 2	흥   	2 <del>1 6</del> 十   2 十	$2\frac{7}{8}$ $2\frac{7}{8}$	$\begin{bmatrix} 2\frac{1}{2} \\ 2\frac{1}{16} \end{bmatrix} + \begin{bmatrix} 2\frac{1}{2} \\ 1 \end{bmatrix}$	521	11°00
11°00   15	521 509	$\frac{16}{5} - \frac{8}{3} - \frac{16}{5} - \frac{7}{6}$		$\frac{16}{9}+$	$\frac{8}{16} - \frac{3}{4}$	$\frac{16}{78}$	$\frac{16}{15}$	$1\frac{1}{1}\frac{6}{6}$	$1\frac{\frac{8}{3}}{\frac{1}{6}}$	$1\frac{5}{1.6}$	$1\frac{87}{1.6}$	$1\frac{\frac{2}{9}}{\frac{1}{6}}$	$[\frac{1}{1},\frac{1}{6},\frac{1}{6}]$	$1\frac{1}{1}\frac{3}{6}+ 2$	-2		$2\frac{1}{16}$	25 —	25 +	$\frac{509}{498}$	15
30	498	$\frac{1}{5}\frac{5}{1}\frac{6}{6}$ $\frac{3}{8}$ $-\frac{170}{126}$		$\frac{9}{16} + \frac{9}{16}$		$\frac{1}{3} + \frac{7}{8}$	1 —	$\left  \frac{1}{1} \frac{1}{6} + \right $	$1\frac{3}{16} +  $	$\left \frac{1\frac{5}{16}+1}{1\frac{3}{16}-1}\right $	$ \frac{1}{16} +  $	$\frac{1\frac{9}{16}}{12}$	1章 一月 1季 十月	$1\frac{1}{8} - \frac{1}{2}$ $1\frac{1}{2}\frac{5}{8} - \frac{1}{2}$	: 十2 ミューナー2:	16 1 —	2 <del>g</del> — 7 2 - 7 — 1	25 工	2年十	487	45
45 12°00	$\begin{array}{c c} 487 \\ 477 \end{array}$	$\begin{bmatrix} \overline{16} \\ \overline{5} \\ \overline{3} \end{bmatrix} \begin{bmatrix} \overline{16} \\ \overline{5} \\ \overline{3} \end{bmatrix} = \begin{bmatrix} \overline{16} \\ \overline{5} \\ \overline{5} \end{bmatrix}$	-   <del>                                  </del>	5	16 16 16	<del>6</del> <del>8</del> -	+ 1 +	$1\frac{1}{8}$ +	$1\frac{1}{4}$	$1\frac{3}{8} + 1$	$1\frac{1}{2}$ +	$1\frac{1}{16}$	$1\frac{1}{1}\frac{3}{6}$	$1\frac{1}{1}\frac{3}{6} + 2$	$\frac{1}{8}$ 2	$\frac{1}{1.6}$	$2\frac{170}{16} + \frac{1}{16}$	$2\frac{5}{8}$ +	$2\frac{13}{16} +$	477 468	12°00 15
15	468	$\frac{156}{16} + \frac{3}{3} + \frac{176}{16} + \frac{1}{16}$	$-\frac{29}{1.6}$	9 <u>5</u>  8	$\frac{3}{4}$ $\longrightarrow$ $\frac{1}{3}$	$\begin{bmatrix} \frac{3}{6} \\ \frac{1}{3} \end{bmatrix} = \begin{bmatrix} \frac{1}{1} \frac{5}{6} - \\ \frac{1}{1} \frac{5}{5} \end{bmatrix}$	$-\left[1\frac{1}{1}\frac{1}{6}\right]$	$1\frac{1}{8} + 1$	$\frac{11}{15} + \frac{1}{15}$	$\frac{1}{176} = $	$\frac{1}{1}\frac{9}{6}$	$1\frac{11}{16}$	$1\frac{7}{8}$ $\frac{4}{17}$	$\frac{2}{2}$	$\begin{bmatrix} \frac{3}{16} - 2 \\ \frac{3}{16} + 2 \end{bmatrix}$	$\frac{3}{16} + \frac{1}{16}$	2步 十 <sub>2</sub> 2 <u>9</u>	<sup>2</sup> 16 2후	$2\frac{1}{8}$ $2\frac{1}{15}$	458	30
30 35	$\begin{array}{c c} 458 \\ \hline 449 \end{array}$	<u> </u>	$-\frac{9}{16}$	1 + +			$+1\frac{1}{16}$	$1\frac{1}{16}$ +	$1\frac{1}{16}$ $1\frac{5}{16}$ $+$	$1\frac{1}{9}\frac{1}{9}$	$\left\lfloor \frac{16}{8} \right\rfloor$	1를 +	$1\frac{1}{1}\frac{5}{6}$ $\longrightarrow$ $ 2$	$2\frac{16}{16} + 2$	$\frac{1}{4}^{6}$ 2.	$\frac{8}{16}$	$2\frac{1}{8}^{6}$	$2\frac{1}{1}\frac{3}{6}$	3	449	45 13°00
13°00	441	$\frac{16}{5} + \begin{vmatrix} 87\\ 16 \end{vmatrix} = \begin{vmatrix} 21\\ 16 \end{vmatrix} = -\begin{vmatrix} 21\\ 12 \end{vmatrix}$	$-\left \frac{\frac{1}{9}^{6}}{\frac{1}{6}}+\right $	$\frac{\frac{8}{1}}{\frac{1}{6}}$	3 + 3	1 16-	-11 1 °	$1\frac{1}{4}^{\circ}$	$1\frac{\frac{3}{8}}{\frac{8}{8}}$	1 = 1	$\lfloor \frac{5}{8} \rfloor + \lfloor \frac{5}{8} \rfloor$	$1\frac{13}{16}$	$1\frac{15}{16} + \frac{1}{2}$	2   2   2   2   2   3   3   3   3   3	$\begin{bmatrix} \frac{5}{16} - 2 \\ \frac{5}{16} + 2 \end{bmatrix}$	$\frac{1}{2} - \frac{1}{2}$	$\frac{211}{16}$	$2\frac{1}{8}$	316	$\begin{array}{c} 441 \\ 432 \end{array}$	15 00
$\begin{bmatrix} 15 \\ 30 \end{bmatrix}$	432 424	$\frac{3}{8} - \begin{vmatrix} \frac{7}{6} - \end{vmatrix} \frac{1}{2}$	$\begin{bmatrix} \frac{9}{16} + \\ \frac{1}{5} \end{bmatrix}$	11 11	3 + 3 13 - 2	+1 -	- 1  <del>  </del>	14 +	$1\frac{8}{8} + 1\frac{7}{1}$			1音音 —	$\frac{2}{2} + \frac{1}{2}$	$2\frac{16}{16} + 2$	$\frac{1}{3}\frac{6}{8} + 2$	$\frac{2}{9} + \frac{2}{2}$	16 十	$2\frac{16}{16}+$	$3\frac{3}{16}$	424	30
45	416	$\frac{1}{8}$ $\frac{1}{6}$ $\frac{1}{6}$ $\frac{1}{3}$ $\frac{1}{6}$	-	$\frac{16}{16} +  $	$\frac{\frac{1}{1}\frac{6}{3}}{\frac{1}{6}}$	$\frac{1}{6}$ $\frac{1}{1.6}$	$-1\frac{8}{1.6}$	$1\frac{4}{1.6}$	$1\frac{1.6}{1.6}$	$1\frac{1}{16}^{6} + 1$	[基 	$1\frac{2}{8} + \frac{2}{8}$	$2\frac{1}{16}$	$2\frac{1}{4}$ 2	$\frac{7}{16}$ - 2	5 8	$\frac{13}{16}$	3 +	34 -	$\begin{array}{c} 416 \\ 409 \end{array}$	$\begin{vmatrix} 45 \\ 14^{\circ}00 \end{vmatrix}$
14°00	409	$\frac{3}{8} - \begin{vmatrix} \frac{7}{16} \\ \frac{1}{7} \end{vmatrix} = \begin{vmatrix} \frac{1}{2} \\ \frac{1}{2} \end{vmatrix} = \frac{1}{2}$	- \frac{5}{8} -	$\frac{11}{16}$ +	$\frac{13}{16} + \frac{1}{13} + \frac{1}{13}$	$\frac{1}{16}$	$\frac{1\frac{3}{16}}{1\frac{3}{6}}$	$\frac{1\frac{5}{16}+}{1\frac{5}{6}+}$	176+		発 十     <mark>計3</mark> —		2章 <del>-</del>  2 2章 十2	$\frac{16}{25} + 2$	$\frac{1}{2}$ + 2	$\frac{1}{1}\frac{1}{6}+2$	$\frac{1}{1}\frac{5}{6}$	316   318	$3\frac{3}{8}^{6}$	402	15
15 30	$\begin{array}{c} 402 \\ 395 \end{array}$	$\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$	5 +	3 -	$\frac{\frac{1}{7}6}{8}$ — 1	$-1\frac{1}{8}$		$ 1\frac{3}{8}^{6} $	$1\frac{1}{2} + $	$\left \frac{1}{1}\frac{1}{6}\right $	$\frac{13}{16} + 2$	2 6	$2\frac{3}{1.6} - 2$	$\frac{1}{8}$ - 2	$\frac{9}{16}$ 2	$\frac{3}{4}$ + 3		$\frac{3-3}{16}$	$3\frac{7}{16}$	395 388	30 45
45	388	$\frac{3}{8} + \frac{7}{16} + \frac{9}{16}$	$-\frac{5}{8}$ +	3 4 1	$\frac{7}{8}$ - 1	$-\frac{1\frac{1}{8}}{1\frac{1}{1}}$	$-\frac{1}{4}$	13 +	$\frac{1}{1}\frac{9}{1}$	$(\frac{1}{1},\frac{1}{6},+)$	13 - 2	$\frac{1}{16}$	2 1 6 7 2	$\frac{16}{16} + 2$	+ 2-	$\frac{3}{16}$ $\frac{3}{3}$ $\frac{7}{3}$ $\frac{3}{3}$		3.5	31/3 +	382	15°00
15°00 16°00	382 358			$\frac{3}{13} + \frac{1}{16} + \frac{1}{16}$	$\begin{array}{c c} \frac{1}{8} & 1 \\ \frac{1}{16} & 1 \\ \end{array}$	$\frac{1}{6}  \begin{bmatrix} 1 & 8 \\ 1 & 3 \end{bmatrix} = \frac{1}{16}$	+ 13	$\begin{vmatrix} 1 \overline{16} \\ 1 \overline{2} \end{vmatrix}$	$1\frac{16}{16}$		2 + 2	$2\frac{16}{16} + 3$	$2\frac{1}{16}$	$\frac{1}{2} \frac{5}{8} - 2$ $\frac{1}{2} \frac{5}{8} + 3$	$\frac{13}{16} + 3$	$\frac{1}{16} - 3$	$\frac{1}{4}^{6} + \frac{1}{2}$	3 1 4	3事 十	$\begin{array}{c} 358 \\ 337 \end{array}$	16°00 17°00
17°00	337		$+ \left  \frac{\frac{1}{3}}{\frac{4}{3}} \right ^{6}$	$\frac{7}{8}$  1	$\begin{bmatrix} \frac{1}{1} \frac{3}{6} \\ 1 \end{bmatrix} \begin{bmatrix} 1 \frac{1}{6} \\ 1 \end{bmatrix}$	$\begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 3 \end{pmatrix} + \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 3 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 3 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 6 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\$	$-1\frac{7}{16}$		1 <del>1 6</del> 1 <del>1 7</del> <del>1 1 7</del> <del>1 1 7</del> <del>1 /del> <del>1 7</del> <del>1 7</del> <del>1 7</del> <del>1</del>	$1\frac{15}{16} + 9$	$\frac{21}{8} + \frac{1}{2}$	$\frac{23}{8}$	sîĭ⊥do	隆 十3	3 3	$\frac{1}{7} - \frac{3}{3}$	$\frac{1}{2}$ - 3	315 十	41	318	18°00
18°00 19°00	318 301	2 16 16	$-\frac{13}{16} - \frac{13}{16} + \frac{13}{16} + \frac{7}{16} + \frac{1}{16}$	$\frac{\frac{3}{1}\frac{5}{6}}{1} - \frac{1}{1}$	$\begin{bmatrix} \frac{1}{16} \\ \frac{1}{6} \end{bmatrix} - \begin{bmatrix} 1 \\ \frac{1}{2} \end{bmatrix}$	$\frac{26}{6} + 1\frac{2}{6} - 1\frac{7}{16}$	- 1½ 十  1½	1 - 1 9 1	a la	$ \begin{array}{c} 1\frac{1}{16} + 5 \\ 2\frac{1}{16} + 5 \\ 2\frac{3}{16} \\ 2\frac{5}{16} \end{array} $	$2\frac{1}{4} + 2$ $2\frac{1}{8} + 2$ $2\frac{1}{7} + 2$	25	$2\frac{1}{8}$ — 3	$\frac{1}{8}$ $\frac{1}{8}$ $\frac{1}{8}$ $\frac{3}{8}$	$\frac{1}{8}$ - $3\frac{1}{8}$	3	1 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 +	$1\frac{15}{16} + 1\frac{3}{16} + 1\frac{3}{8} + 1$	$4\frac{1}{2}$ - $4\frac{9}{16}$ +	301	19°00 20°00
20°00	286	$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \end{bmatrix} + \begin{bmatrix} \frac{1}{8} \\ \frac{1}{8} \\ \frac{1}{8} \end{bmatrix} + \begin{bmatrix} \frac{1}{16} \\ \frac{3}{4} \end{bmatrix}$	76+	1 +1	$\lfloor \frac{8}{16} - \rfloor \lfloor \frac{7}{3} \rfloor$	$\frac{5}{16} + 1\frac{1}{2}$	$+\left 1\frac{\frac{8}{11}}{16}\right $	1章 十	$2\frac{1}{16} + 2$	$2\frac{\overline{16}}{\overline{16}}$	$2\frac{1}{2} + 2$	隆 十	3 + 3	1 + 3	$\frac{9}{16}$ $-3\frac{1}{9}$	1 3 4	8 -	13 +	176 7	286	20 00
			$-\begin{vmatrix} \frac{\circ}{13} \end{vmatrix}$	14	15	16 17	18	19	20	21	22	${23}$	24	25	26	27	28	29	30		



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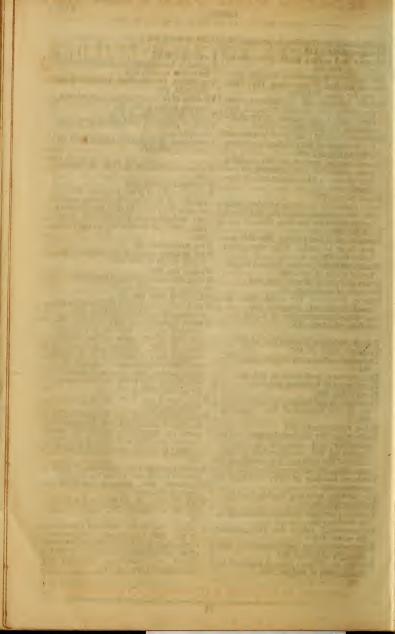
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No. on Wire Gauge 1 2 3 4 5 6 7 8 9 10 11												
Pounds Avoir 12.5 12 11 10 9 8 7.5 7 6 5.68 5												
No. on Wire Gauge 12	13	14	15	16	17	18	19	20	21	22		
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Of the Weight of a Square Foot of Boiler Plate Iron, from 1-8 to 1 inch thick, in pounds avoirdupois.

1	18	$\frac{3}{16}$	$\frac{1}{4}$	$\frac{5}{16}$	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{9}{16}$	<u>5</u> 8	$\frac{11}{16}$	$\frac{3}{4}$	$\frac{13}{16}$	$\frac{7}{8}$	$\frac{15}{16}$	1 In.
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1st in the triangle of BC, to find

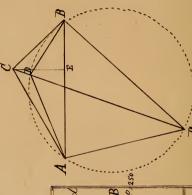
i.e. 810 : 1000 ::: 200 : 200 x 200 250 AB: AC+CB:: AC-CB: AE-EB then 800+250 = 325 = A.E.

800-250 = 275 = IB.

In AEC, to find the angle ACE. AC 600 (Ar.C.) 5.25 :: Sin E 90°

: Sin ACE

In CEB, to Find the angle ECB. CB 400 Ar. Comp.



SinAPC 3345 an. com. Sin ACP

dy pury IL

: sin CAP :: Ac 600 : CP To hind BP ACB-ACP=PCB or	Sin CPB 22°30' an.e. Sin PcB CB 400 PB				Эниншинининининининкаванинининининининин
### ### #### #### ####################	2114 in the triangle ADB, to find AD&BD.  DAB = CPB or $22^{\circ}30'$ DBA = APC or $33^{\circ}48'$ ADB = $180^{\circ}-22^{\circ}30'+33^{\circ}45' = 123^{\circ}48'$	Sin D 123045' an comp. Sin B 33° 45' .: AB 800	Tr find BD.  Sin D 125'48' an comp,  Sin A 22'30'  AB 800	CAB - DAB = CAD or AC + AC + AC + AC + AC + AD AC + AC +	: $tan_{\frac{1}{2}}(D-C)$ = $\frac{1}{2}(D-C)$ = $ACP$ or $Then_{\frac{1}{2}}(C+D)$ - $\frac{1}{2}(D-C)$ = $ACP$ or $Then_{\frac{1}{2}}(C+D)$ - $\frac{1}{2}(D-C)$ = $ACP$ or $Then_{\frac{1}{2}}(D-C)$ = $ACP$ or $Then_{\frac{1}{2$

EEH.

#### Of the Weight of Flat Bar Iron, 12 inches long, in pounds avoirdupois.

$ \begin{array}{ c c c c c c c c c } \hline & \frac{1}{2} & 21 & 31 & 42 & 63 & \\ \hline & \frac{1}{3} & 32 & 48 & 63 & 95 & 1 \cdot 27 & 1 \cdot 58 \\ \hline & 1 & 42 & 63 & 84 & 1 \cdot 26 & 1 \cdot 69 & 2 \cdot 11 & 2 \cdot 53 & 2 \cdot 96 \\ \hline & 1 & 42 & 63 & 84 & 1 \cdot 26 & 1 \cdot 69 & 2 \cdot 11 & 2 \cdot 64 & 3 \cdot 16 & 3 \cdot 70 & 4 \cdot 22 \\ \hline & 1 & 52 & 79 & 1 \cdot 05 & 1 \cdot 58 & 2 \cdot 11 & 2 \cdot 64 & 3 \cdot 16 & 3 \cdot 70 & 4 \cdot 22 \\ \hline & 1 & 58 & 58 & 87 & 1 \cdot 16 & 1 \cdot 74 & 2 \cdot 32 & 2 \cdot 90 & 3 \cdot 48 & 4 \cdot 06 & 4 \cdot 64 \\ \hline & 1 & 74 & 1 \cdot 11 & 1 \cdot 48 & 2 \cdot 21 & 2 \cdot 95 & 3 \cdot 70 & 4 \cdot 43 & 5 \cdot 43 & 5 \cdot 91 \\ \hline & 2 & 84 & 1 \cdot 27 & 1 \cdot 69 & 2 \cdot 53 & 3 \cdot 38 & 4 \cdot 22 & 5 \cdot 07 & 5 \cdot 92 & 6 \cdot 76 \\ \hline & 2 & 1 \cdot 06 & 1 \cdot 58 & 2 \cdot 11 & 3 \cdot 17 & 4 \cdot 22 & 5 \cdot 28 & 6 \cdot 33 & 7 \cdot 40 & 8 \cdot 45 \\ \hline & 2 & 1 \cdot 06 & 1 \cdot 58 & 2 \cdot 11 & 3 \cdot 17 & 4 \cdot 22 & 5 \cdot 28 & 6 \cdot 33 & 7 \cdot 40 & 8 \cdot 45 \\ \hline & 2 & 1 \cdot 106 & 1 \cdot 58 & 2 \cdot 11 & 3 \cdot 17 & 4 \cdot 22 & 5 \cdot 28 & 6 \cdot 33 & 7 \cdot 40 & 8 \cdot 45 \\ \hline & 3 & 1 \cdot 27 & 1 \cdot 90 & 2 \cdot 53 & 3 \cdot 80 & 5 \cdot 07 & 6 \cdot 34 & 7 \cdot 60 & 8 \cdot 87 & 10 \cdot 14 \\ \hline & 3 & 1 \cdot 137 & 2 \cdot 06 & 2 \cdot 74 & 4 \cdot 12 & 5 \cdot 49 & 6 \cdot 86 & 8 \cdot 24 & 10 \cdot 09 & 10 \cdot 98 \\ \hline & 3 & 1 \cdot 148 & 2 \cdot 22 & 2 \cdot 95 & 4 \cdot 43 & 5 \cdot 91 & 7 \cdot 39 & 8 \cdot 87 & 10 \cdot 87 & 11 \cdot 83 \\ \hline & 3 & 1 \cdot 188 & 2 \cdot 38 & 3 \cdot 17 & 4 \cdot 75 & 6 \cdot 34 & 7 \cdot 92 & 9 \cdot 51 & 11 \cdot 65 & 12 \cdot 68 \\ \hline & 4 & 1 \cdot 69 & 2 \cdot 53 & 3 \cdot 80 & 5 \cdot 07 & 6 \cdot 60 & 8 \cdot 45 & 10 \cdot 14 & 11 \cdot 83 & 13 \cdot 52 \\ \hline & 4 & 1 \cdot 109 & 2 \cdot 85 & 3 \cdot 80 & 5 \cdot 07 & 7 \cdot 60 & 9 \cdot 50 & 11 \cdot 44 & 11 \cdot 83 & 13 \cdot 52 \\ \hline & 4 & 1 \cdot 190 & 2 \cdot 85 & 3 \cdot 80 & 5 \cdot 70 & 7 \cdot 60 & 9 \cdot 50 & 11 \cdot 44 & 11 \cdot 83 & 15 \cdot 21 \\ \hline \end{array}$	Thic	kness.	1/8	$\frac{3}{16}$	$\frac{1}{4}$	3/8	$\frac{1}{2}$	<u>5</u> 8	$\frac{3}{4}$	7 8	1 Inch.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	IN INCHES.	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{4} & $	21 32 42 52 58 63 74 84 95 1:06 1:27 1:37 1:48 1:58 1:69 1:90	*31 *48 *63 *79 *87 *95 1·11 1·27 1·42 1·58 1·74 1·90 2·06 2·22 2·38 2·53 2·85	*42 *63 *84 1.05 1.16 1.27 1.48 1.69 1.90 2.11 2.32 2.53 2.74 2.95 3.17 3.38 3.80	63 ·95 1·26 1·58 1·74 1·90 2·21 2·53 2·85 3·17 3·49 4·12 4·43 4·75 5·07 5·70	1·27 1·69 2·11 2·32 2·53 2·95 3·38 3·80 4·22 4·64 5·07 5·49 5·91 6·34 6·76 7·60	1·58 2·11 2·64 2·90- 3·17 3·70 4·22 4·75 5·28 5·81 6·34 6·86 7·39 8·45 9·50	2·53 3·16 3·48 3·80 4·43 5·07 5·70 6·33 6·97 7·60 8·24 8·87 9·51 10·14 11·41	2:96 3:70 4:06 4:44 5:43 5:92 6:65 7:40 8:13 8:87 10:09 10:87 11:65 11:83 13:31	4·22 4·64 5·07 5·91 6·76 7·60 8·45 9·29 10·14 10·98 11·88 12·68 13·52 15·21

SCOVIL'S PATENT IS THE ONLY COMPLETE SYSTEM OF BOX PILING EVER INVENTED. ITS VALUE HAS BEEN PROVED BY 4 YEARS' CONSTANT USE IN THE "KENSINGTON NAIL AND ROLLING MILLS OF MESSRS. JAS. ROWLAND & CO., NO. 920 NORTH DELAWARE AV., PHILADELPHIA," PRODUCING CHEAPER PLATES AND BETTER EDGES THAN BAR PILES. REQUIRES NO BINDERS OR TIES. WORKMEN LIKE IT, AS IT DOES NOT SPREAD AND IS EASILY HANDLED.

ADDRESS E. G. SCOVIL, Mill Manager,

COLDBROOK P. O., SAINT JOHN, N. B.

Containing the Weight of Wrought Iron Bars, 12 inches long, in pounds avoirdupois.

Inch.	Round.	Square.	Inch.	Round.	Square.	Inch.	Round.	Square.
1	1.66	.211	$1\frac{3}{4}$	8.13	10.35	$3\frac{1}{2}$	32.52	41.41
38	.373	.475	$1\frac{2}{8}$	9.33	11.88	$3\frac{3}{4}$	37.34	47.53
$\frac{1}{2}$	.664	.845	2	10 62	13.52	4	42.48	54.08
58	1.04	1.32	$2\frac{1}{8}$	11.99	15.26	41	47.96	61:05
3	1.20	1.90	$2\frac{1}{4}$	13.44	17:11	4 4 5	53.77	68.45
니 + 0일(00 ~ (C 115)(00 c5)(작1 ~ (c	2.03	2.59	$2\frac{3}{8}$	14.98	19.07	$4\frac{3}{4}$	59.91	76.27
1	2.65	3.38	$2\frac{1}{2}$	16.59	21.13	5	66.38	84.51
$1\frac{1}{8}$	3.36	4.28	25	18.30	23.29	$5\frac{1}{4}$	73.18	93.17
11	4.15	5.28	21000000000000000000000000000000000000	20.08	25.56	51	80.35	102.25
$1\frac{3}{8}$	5.05	6.39	$2\frac{7}{8}$	21.94	27.94	$5\frac{3}{4}$	87.78	111 76
15	5.99	7.60	3	23.96	30.42	6	95.58	121.69
1½ 1½	7.01	8.92	$3\frac{1}{4}$	28.04	35.70	7	130.10	165.63

AVING had 20 years' experience in Rolling Mill and Nail Business, can be consulted on Building, Repairing, Foundations, &c., &c.

Estimates on Manufacturing. Prime Costs taken. References when required.

E. G. SCOVIL, Coldbrook Post Office, St. John, N. B.







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